

























n vertices, m edges	Edge	Adjacency	Adjacenc
<ul><li>no parallel edges</li><li>no self-loops</li></ul>	List	List	Matrix
Space	n + m	n + m	<b>n</b> <sup>2</sup>
incidentEdges(v)	m	deg(v)	n
areAdjacent (v, w)	m	$\min(\deg(v), \deg(w))$	1
insertVertex(o)	1	1	<b>n</b> <sup>2</sup>
insertEdge(v, w, o)	1	1	1
removeVertex(v)	m	deg(v)	<b>n</b> <sup>2</sup>
removeEdge(e)	1	1	1

## Python Graph Implementation We use a variant of the adjacency map representation. For each vertex v, we use a Python dictionary to represent the secondary incidence map I(v). The list V is replaced by a top-level dictionary D that maps each vertex v to its incidence map I(v). Note that we can iterate through all vertices by generating the set of keys for dictionary D. A vertex does not need to explicitly maintain a reference to its position in D, because it can be determined in O(1) expected time. Running time bounds for the adjacency-list graph ADT operations, given above, become expected bounds.

```
Vertex Class
                                    nested Vertex class -
             class Vertex:
                """Lightweight vertex structure for a graph."""
__slots__ = '_element'
                def __init__(self, x):
                    "Do not call constructor directly. Use Graph's insert_vertex(x)."""
                  self._element = x
       10
                def element(self):
                    "Return element associated with this vertex."""
                  return self._element
       13
       14
                def __hash__(self):
                                              # will allow vertex to be a map/set key
                  return hash(id(self))
© 2013 Goodrich, Tamassia, Goldwasser
                                            Graphs
```





