

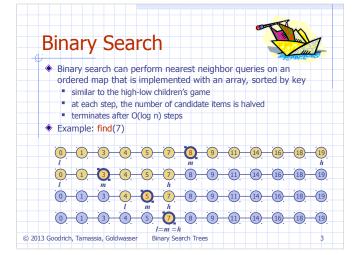
## **Ordered Maps**



- •Keys are assumed to come from a total order.
- ◆Items are stored in order by their keys
- This allows us to support nearest neighbor queries:
  - ◆ Item with largest key less than or equal to k
  - Item with smallest key greater than or equal to k

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Binary Search Trees



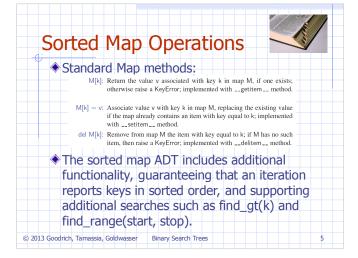
## Search Tables

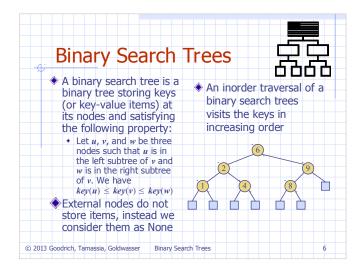


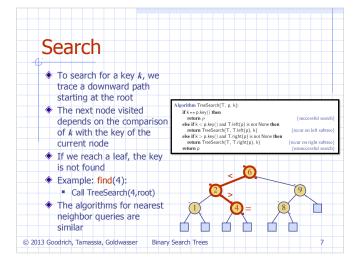
- A search table is an ordered map implemented by means of a sorted sequence
  - We store the items in an array-based sequence, sorted by key
  - We use an external comparator for the keys
- Performance:
  - Searches take  $O(\log n)$  time, using binary search
  - Inserting a new item takes O(n) time, since in the worst case we have to shift n/2 items to make room for the new item
- Removing an item takes O(n) time, since in the worst case we have to shift n/2 items to compact the items after the removal
- The lookup table is effective only for ordered maps of small size or for maps on which searches are the most common operations, while insertions and removals are rarely performed (e.g., credit card authorizations)

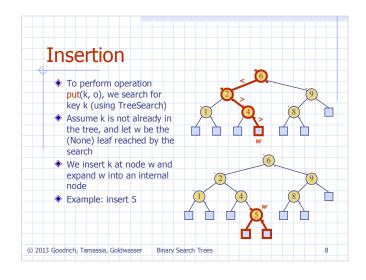
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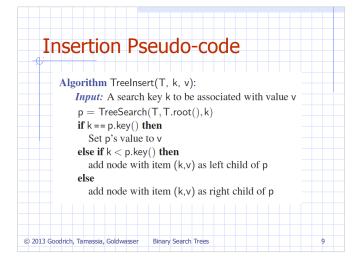
Binary Search Trees

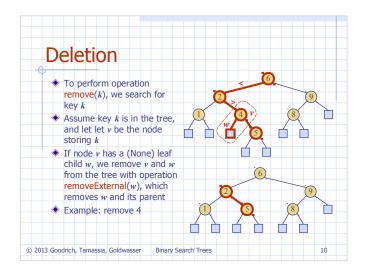


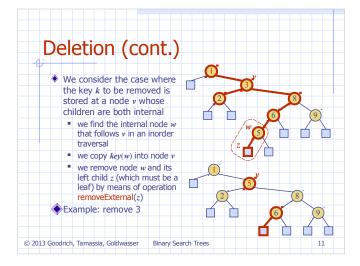


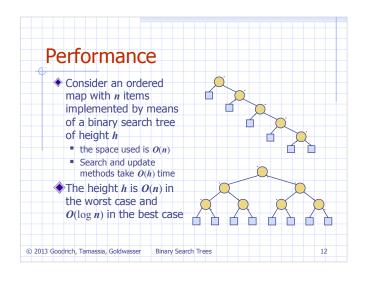


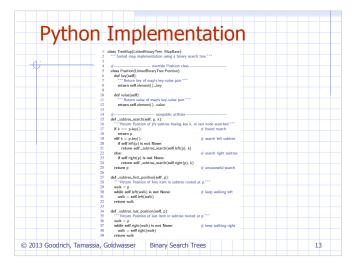


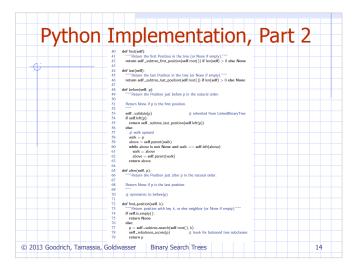


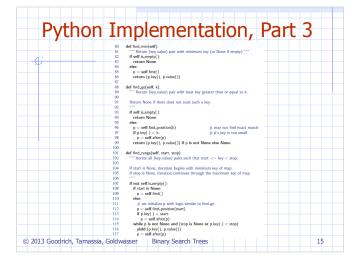


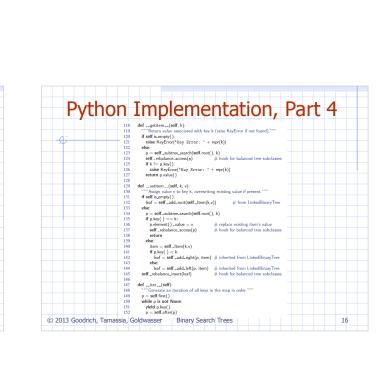












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Python Implementation, end

def delete(self, p):
""Remove the item at given Position."""
self_validate(p)  # inherited from LinkedBinaryTree
if self_left(p) and self_right(p):  # p has two children
replacement = self_subtree_last_position(self_left(p))
self_veplace(p, replacement_element())  # from LinkedBinaryTree
p= replacement
# now p has at most one child
parent = self_parent(p)
self_delete(p)  # inherited from LinkedBinaryTree
self_delete(p)  # inherited from LinkedBinaryTree
self_delete(p)  # if root deleted, parent is None

def_delete(p)  # if root deleted, parent is None

def_delitem__(self, k):
""Remove item associated with key k (raise KeyError if not found).""
if not self_is_empty():
    p = self_subtree_search(self_root(), k)
if self_delete(p)  # rely on positional version
return  # successful deletion complete
self_rebalance_access(p)  # hook for balanced tree subclasses
raise KeyError('Key Error: ' + repr(k))

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