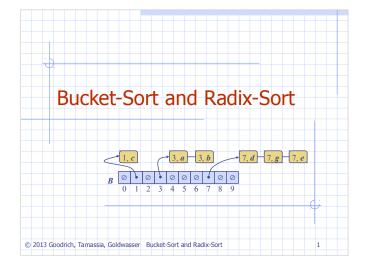
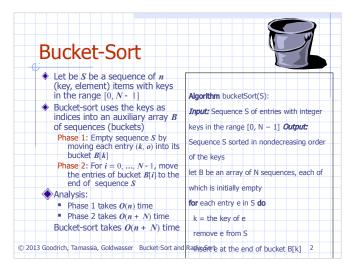
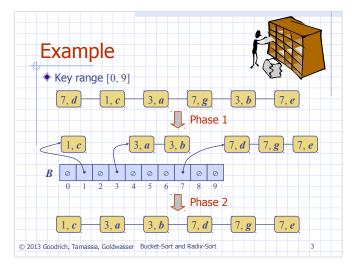
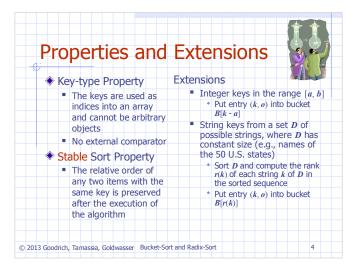
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Lexicographic Order



- A *d*-tuple is a sequence of *d* keys $(k_1, k_2, ..., k_d)$, where key k_i is said to be the *i*-th dimension of the tuple
- Example:
- The Cartesian coordinates of a point in space are a 3-tuple
- The lexicographic order of two d-tuples is recursively defined as follows

$$(x_1, x_2, ..., x_d) < (y_1, y_2, ..., y_d)$$
 \Leftrightarrow
 $x_1 < y_1$
 $\xrightarrow{\vee} x_1 = y_1 \xrightarrow{\wedge} (x_2, ..., x_d) < (y_2, ..., y_d)$

I.e., the tuples are compared by the first dimension, then by the second dimension, etc.

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Lexicographic-Sort

- Let C_i be the comparator that compares two tuples by their *i*-th dimension
- Let stableSort(S, C) be a stable sorting algorithm that uses comparator C
- Lexicographic-sort sorts a sequence of d-tuples in lexicographic order by executing d times algorithm stableSort, one per dimension
- Lexicographic-sort runs in O(dT(n)) time, where T(n) is the running time of stableSort

Algorithm lexicographicSort(S)

Input sequence *S* of *d*-tuples **Output** sequence *S* sorted in lexicographic order

for $i \leftarrow d$ downto

stableSort(S, C,)

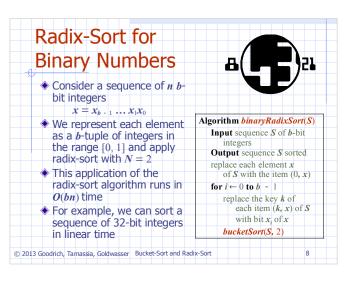
Example:

(7,4,6) (5,1,5) (2,4,6) (2, 1, 4) (3, 2, 4) (2, 1, 4) (3, 2, 4) (5,1,5) (7,4,6) (2,4,6)

(2, 1, 4) (5,1,5) (3, 2, 4) (7,4,6) (2,4,6) (2, 1, 4) (2,4,6) (3, 2, 4) (5,1,5) (7,4,6)

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Radix-Sort Radix-sort is a specialization of lexicographic-sort that uses bucket-sort as the stable sorting algorithm Algorithm radixSort(S, N) in each dimension Input sequence S of d-tuples such Radix-sort is applicable to tuples where the that $(0, ..., 0) \le (x_1, ..., x_d)$ and keys in each dimension $(x_1, ..., x_d) \leq (N - 1, ..., N)$ i are integers in the range [0, N - 1] for each tuple $(x_1, ..., x_d)$ in SOutput sequence S sorted in Radix-sort runs in time exicographic order O(d(n+N))for $i \leftarrow d$ downto 1 bucketSort(S, N) © 2013 Goodrich, Tamassia, Goldwasser Bucket-Sort and Radix-Sort



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