

1)

$$\frac{1-\phi c_t}{\phi} \frac{y_t}{l_t} = (1-\alpha) \frac{y_t}{n_t}$$

$$E_{t-1} \left[\beta \frac{u(l_t, l_t)}{c_t} \left(\alpha \frac{y_t}{k_t} + 1 - \delta \right) \right] = u(l_{t-1}, l_{t-1}) \frac{c_{t-1}}{c_t}$$

$$y_t = z_t k_t^\alpha n_t^{1-\alpha}$$

$$1 = n_t + l_t$$

$$y_t = c_t + i_t$$

$$k_t = i_{t-1} + (1-\delta) k_{t-1}$$

$$u(c, l) = \frac{(c^\phi l^{1-\phi})^{1-\psi}}{1-\psi}$$

$$\ln z_t = (1-\rho) \ln \bar{z} + \rho \ln z_{t-1} + e_t$$

$$\frac{\bar{y}}{\bar{n}} = \eta \quad \frac{\bar{c}}{\bar{n}} = \eta - \delta \theta \quad \frac{\bar{l}}{\bar{n}} = \delta \theta$$

$$\bar{n} = \frac{1}{1 + \left(\frac{1}{1-\alpha} \right) \left(\frac{1-\phi}{\phi} \right) [1 - \delta \theta^{1-\alpha}]}$$

$$\bar{l} = 1 - \bar{n}$$

$$\frac{\bar{k}}{\bar{n}} = \theta$$

$$\theta = \left(\frac{\alpha}{\frac{1}{\beta} - 1 + \delta} \right)^{\frac{1}{1-\alpha}}$$

$$\eta = \theta^\alpha$$

$$z_t = z_0 (1+g)^t e^{\omega t}$$

$$\omega_t = \rho \omega_{t-1} + \varepsilon_t$$

$$\left(1 + \frac{g}{1-\alpha} \right) k_{t+1} = i_t + (1-\delta) k_t$$

$$k = \phi(1-\phi) - 1$$

Residual factor is given by $(1 + \frac{g}{1-d})^k$.

$$c_t^k l_t^A = \beta E_t \left\{ \left(1 + \frac{g}{1-d}\right)^k c_{t+1}^k l_{t+1}^A \left[\alpha z_{t+1} \left(\frac{n_{t+1}}{k_{t+1}}\right)^{1-\alpha} + (1-\delta) \right] \right\}$$

$$A z_{t+1} = B x_t + C v_{t+1} + D \eta_{t+1}$$

$$0 = \log\left(\frac{1-\phi}{\phi}\right) + \log c' - \log l' - \log(1-d) - \log z' \\ - d \log k + d \log n'$$

$$0 = k \log c + \lambda \log t - \log \beta - k \log c' - \lambda \log l' \\ - \log \left[\alpha \exp(\log z') \frac{\exp[(1-\alpha) \log n']}{\exp[(1-\alpha) \log k']} + (1-\delta) \right]$$

$$0 = \log y' - \log z' - d \log k - (1-d) \log n'$$

$$0 = \log y' - \log [\exp[\log(c')]] + \exp[\log(c')]$$

$$0 = \log k' - \log [\exp[\log(l')]] + (1-\delta) \exp[\log(k')]$$

$$0 = -\log [\exp[\log(n')]] + \exp[\log(l')]$$

$$0 = \log z' - \rho \log z.$$