

EXERCISE 19.1

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1. Construct line segments whose lengths are:

(i) 4.8 cm

(ii) 12 cm 5 mm

(iii) 7.6 cm

Solution:

(i) 4.8 cm

Construct a line L on a paper and mark A on it.

Now place the metal point of the compass at zero mark of the ruler.

Make adjustments in the compass such that the pencil point is at 4.8 cm mark on the ruler.

Take compass on L such that its metal point is on A.

Now mark a small mark as B on L which is corresponding to the pencil point of the compass.

Here, AB is the required line segment of length 4.8 cm.



(ii) 12 cm 5 mm

Construct a line L on a paper and mark A on it.

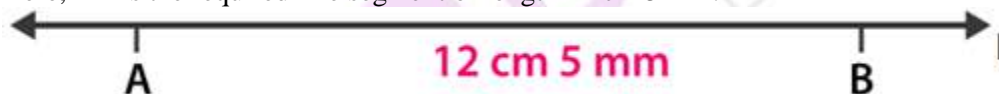
Now place the metal point of the compass at zero mark of the ruler.

Make adjustments in the compass such that the pencil point is at 5 small points from the mark of 12 cm to 13 cm on the ruler.

Take compass on L such that its metal point is on A.

Now mark a small mark as B on L which is corresponding to the pencil point of the compass.

Here, AB is the required line segment of length 12 cm 5 mm.



(iii) 7.6 cm

Construct a line L on a paper and mark A on it.

Now place the metal point of the compass at zero mark of the ruler.

Make adjustments in the compass such that the pencil point is at 6 small points from the mark of 7 cm to 8 cm of the ruler.

Take compass on L such that its metal point is on A.

Now mark a small mark as B on L which is corresponding to the pencil point of the compass.

Here, AB is the required line segment of length 7.6 cm.



2. Construct two segments of length 4.3 cm and 3.2 cm. Construct a segment whose length is equal to the sum of the lengths of these segments.

Solution:

With the help of compass and ruler, construct AB and CD of lengths 4.3 cm and 3.2 cm.

Construct a line L and mark P on it.

Now place the metal point of the compass at zero mark of the ruler.

Make adjustments in the compass such that the pencil point reaches the point B.

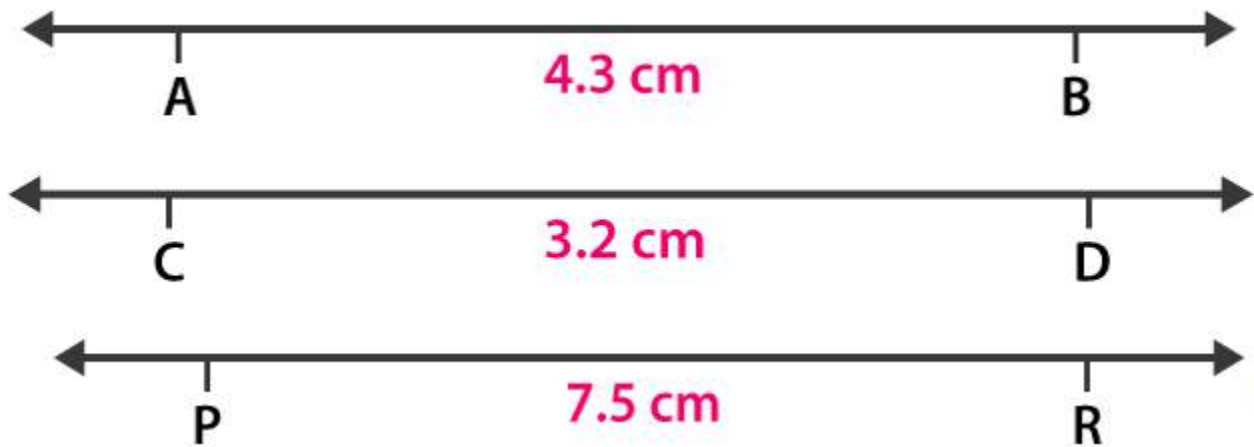
Take compass on L such that its metal point is on P.

Now mark a small mark as Q on the line L corresponding to the pencil point of the compass.

Reset the compass so that its metal and pencil points are on C and D.

Take compass on L such that its metal point is on Q and the pencil point makes a small mark as R which is opposite to P on L.

Here, PR is the required segment whose length is equal to the sum of the lengths of these segments.



EXERCISE 19.2

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1. How many lines can be drawn which are perpendicular to a given line and pass through a given point lying

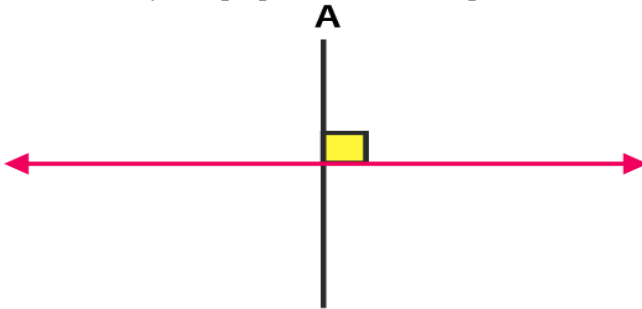
(i) outside it?

(ii) on it?

Solution:

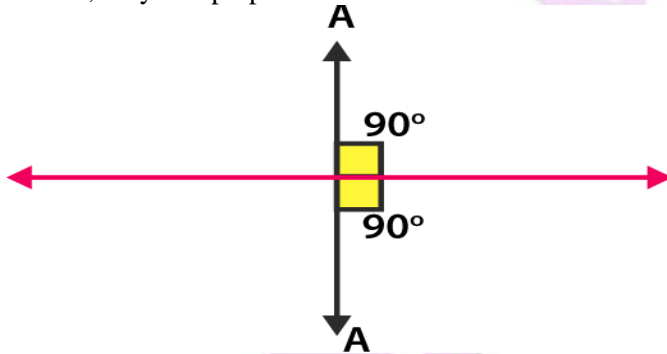
(i) We know that a line perpendicular from a given point to a given line is the shortest distance between them. Here only one shortest distance is possible.

Therefore, only one perpendicular line is possible from a given point lying outside it.



(ii) We can draw only one perpendicular line from any point on the line.

Therefore, only one perpendicular line can be drawn from a given point lying on it.



2. Draw a line PQ. Take a point R on it. Draw a line perpendicular to PQ and passing through R. (Using (i) ruler and a set-square (ii) ruler and compasses)

Solution:

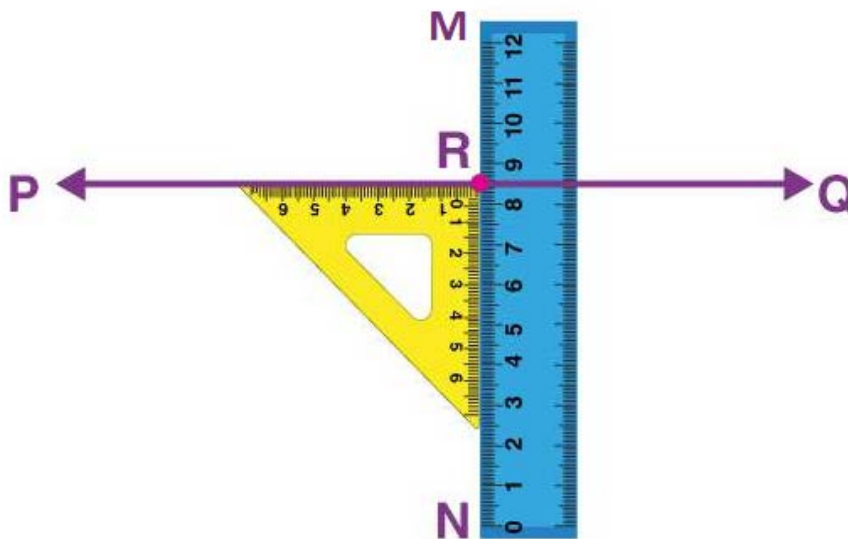
(i) Construct a line PQ and mark a point R on it.

Now place the set square with its one arm of the right angle along the line PQ.

Place the ruler along its edge without disturbing the position of set square.

Remove the set square without disturbing the position of the ruler and construct a line MN through R.

Here, MN is the required line which is perpendicular to PQ through the point R.



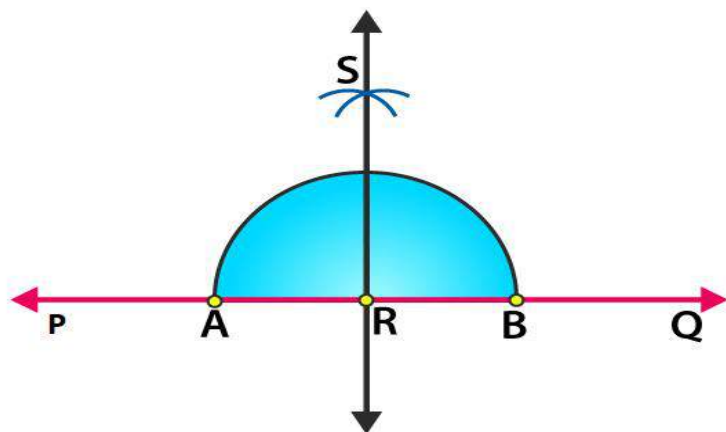
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(ii) Construct a line PQ and mark R on it.

Considering R as the centre and measuring convenient radius, draw an arc which touches the line PQ at A and B. Considering A and B as centres and radius which is greater than AR, draw two arcs which cut each other at the point S.

Now join the points RS and extend in both directions.

Here, RS is the required line which is perpendicular to PQ through the point R.



3. Draw a line l. Take a point A, not lying on l. Draw a line m such that $m \perp l$ and passing through A. (Using (i) ruler and a set-square (ii) ruler and compasses)

Solution:

(i) Construct a line L and mark a point A outside it.

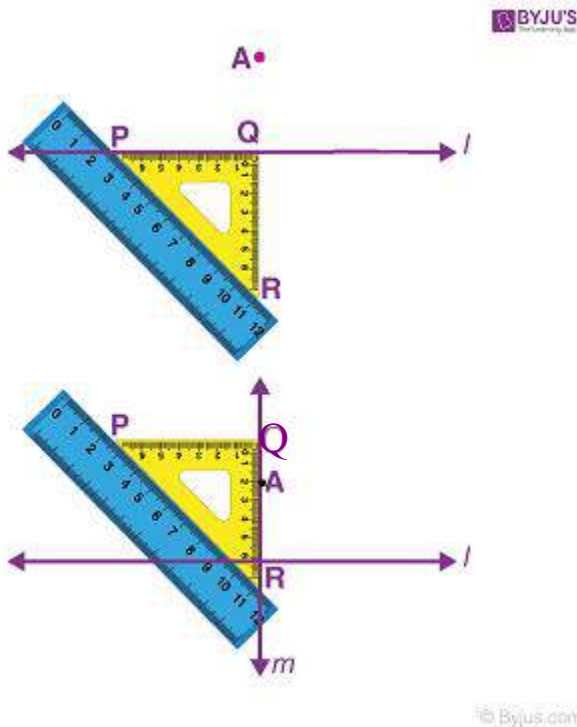
Now place the set square PQR with its one arm PQ of the right angle along the line L.

Place the ruler along the edge PR without disturbing the position of set square.

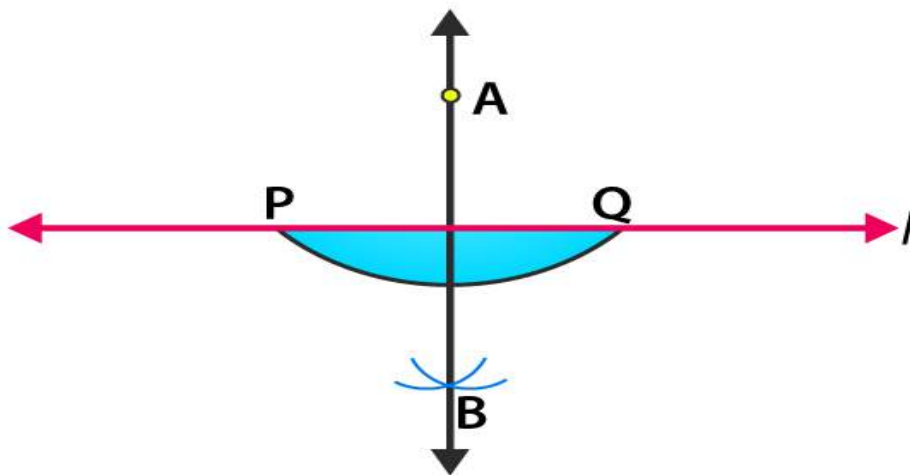
Slide the set square along the ruler until its arm QR reaches A without disturbing the position of the ruler.

Draw a line m.

Here, line m is the required line which is perpendicular to the line L .



(ii) Considering A as centre, construct an arc PQ which intersects the line L at P and Q .
By taking P and Q as centres, draw two arcs which intersect each other at the point B .
Now join the points A and B and extend in both the directions.
Here, AB is the required line.



4. Draw a line AB and take two points C and E on opposite sides of AB . Through C , draw $CD \perp AB$ and through E draw $EF \perp AB$.

(Using (i) ruler and a set-square (ii) ruler and compasses)

Solution:

(i) Construct a line AB and mark two points C and E on the opposite sides of AB.

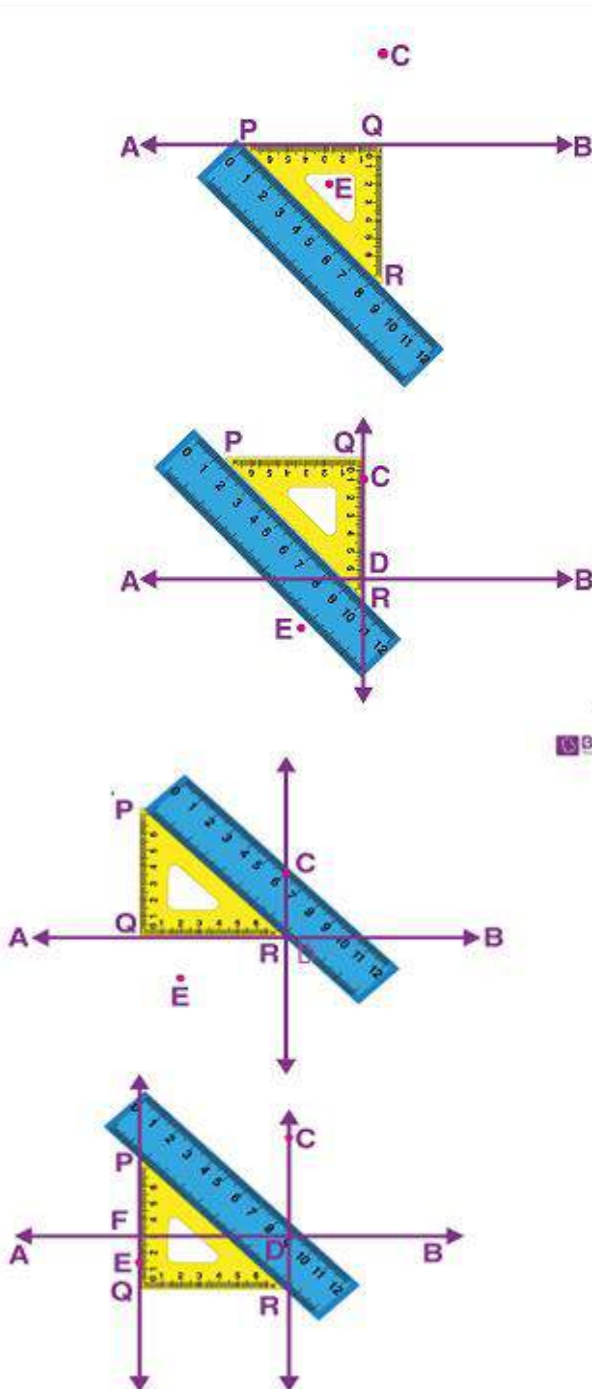
Place the set square PQR on the side E with its one arm PQ of the right angle along the line AB. Place the ruler along the edge PR.

Slide the set square along the ruler until the arm QR reaches C.

Construct a line CD where D is a point on the line AB.

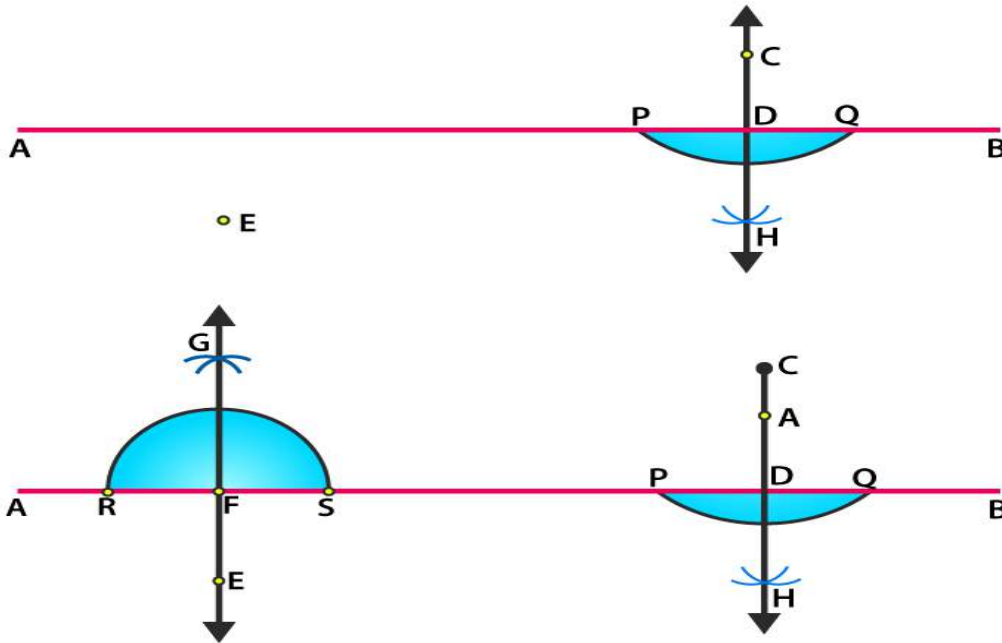
Here CD is the required line where $CD \perp AB$

Now follow the same steps using a set square on the side E, we construct a line $EF \perp AB$.



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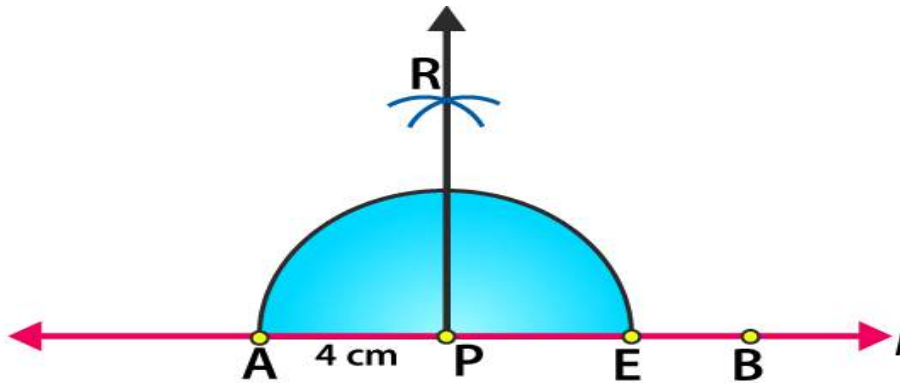
(ii) Construct a line AB and mark two points C and E on the opposite sides.
Considering C as centre, construct an arc PQ which intersects AB at P and Q.
Considering P and Q as centres, draw two arcs which intersect each other at the point H.
Now join the points H and C where HC crosses the line AB at the point D.
We know that $CD \perp AB$
In the same way, consider E as centre and construct an arc RS.
Considering R and S as centres, construct two arcs which intersect each other at the point G.
Now join the point G and E such that GE crosses the line AB at the point F
We know that $EF \perp AB$.



5. Draw a line segment AB of length 10 cm. Mark a point P on AB such that $AP = 4$ cm. Draw a line through P perpendicular to AB.

Solution:

Construct a line L and mark a point A on it.
With the help of a ruler and a compass mark a point B which is at 10 cm from the point A on the line L.
Here, AB is the required line segment of length 10 cm.
Now, mark a point P which is 4 cm from the point A in the direction of B.
Taking P as centre and radius 4 cm draw an arc which intersects the line L at A and E.
Taking A and E as centres and radius 6 cm draw two arcs which intersect each other at the point R.
Now join P and R and extend it.
Here, PR is the required line which is perpendicular to the line AB.



6. Draw a line segment PQ of length 12 cm. Mark a point O outside this segment. Draw a line through O perpendicular to PQ.

Solution:

Construct a line L and mark a point P on it.

With the help of a ruler and a compass mark a point Q on the line L having a length $PQ = 12$ cm

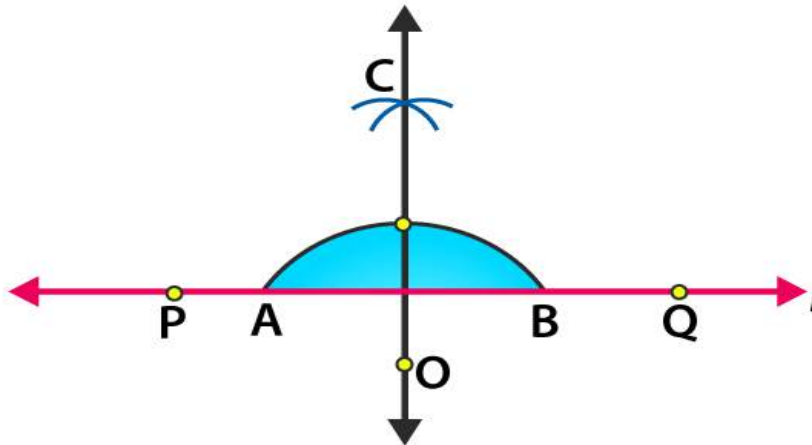
Now mark a point O outside the line PQ.

Taking O as centre, construct an arc having appropriate radius such that the arc cuts the line at A and B.

Considering A and B as centres, draw two arcs such that they intersect each other at the point C.

Join the points OC.

Here, OC is the required line which is perpendicular to the line PQ.



7. Using a protractor, draw $\angle BAC$ of measure 70° . On side AC, take a point P, such that $AP = 2$ cm. From P draw a line perpendicular to AB.

Solution:

Construct a line segment AC on the line L

(i) Place a protractor on the line segment AC such that it coincides with the line of diameter of protractor and the middle of the line coincides with A.

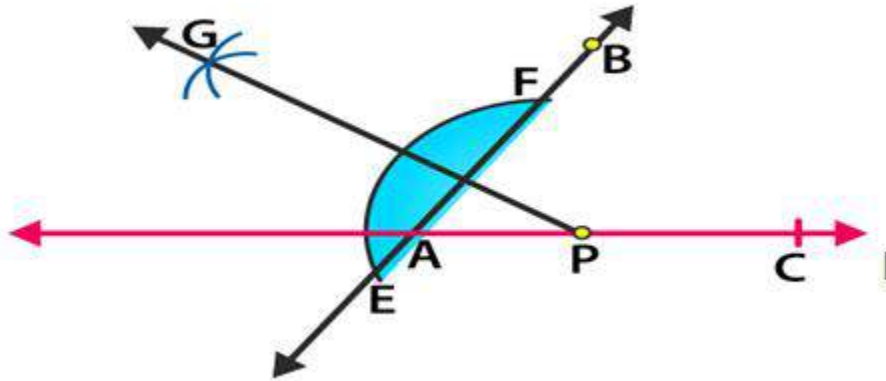
(ii) Now by counting from the right side, mark B as the point of 70° of the protractor and construct AB.

(iii) Measure 2 cm from the point A on the line segment AC and mark P.

(iv) Considering P as centre, construct an arc which intersects the line l at E and F.

(v) Considering the same radius and the points E and F as centres, draw two arcs which intersect G on the other side.

(vi) Join the points P and G.



8. Draw a line segment AB of length 8 cm. At each end of this line segment, draw a line perpendicular to AB. Are these two lines parallel?

Solution:

(i) By taking a convenient radius with A as centre construct an arc which intersects the line at W and X.

(ii) Taking W and X as centres and radius which is greater than AW, draw two arcs which intersect each other at the point M.

(iii) Now join the points AM and extend in both directions to P and Q.

(iv) With B as centre and convenient radius construct an arc which intersects the line at Y and Z.

(v) Considering Y and Z as centres and radius which is greater than YB, draw two arcs which intersect each other at the point N.

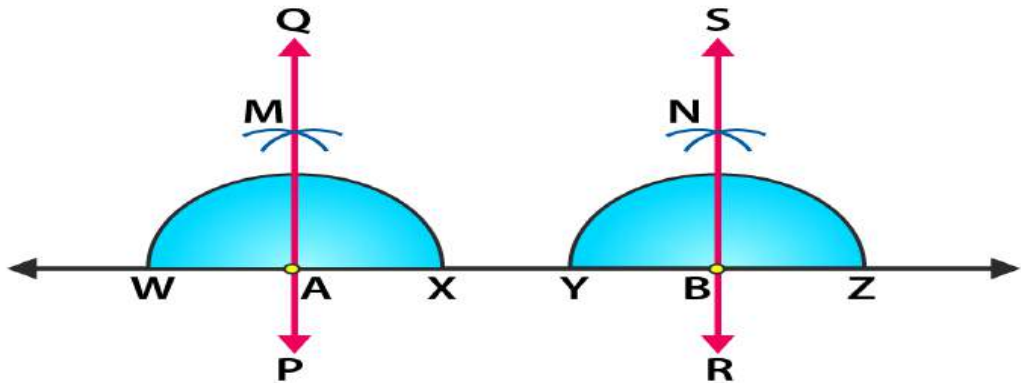
(vi) Now join the points BN and extend in both directions at the point S and R.

Consider the lines perpendicular to the points A and B be PQ and RS

We know that $\angle QAB = \angle ABR = 90^\circ$

Two alternate interior angles are equal when the two parallel lines are intersected by a third line.

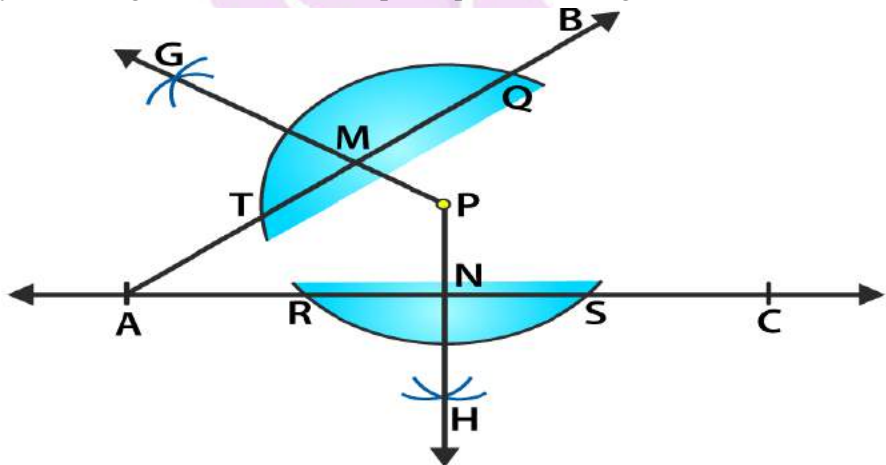
Hence, PQ and RS are parallel.



9. Using a protractor, draw $\angle BAC$ of measure 45° . Take a point P in the interior of $\angle BAC$. From P draw line segments PM and PN such that $PM \perp AB$ and $PN \perp AC$, Measure $\angle MPN$.

Solution:

- (i) Construct a line segment A on the line L.
 - (ii) Place the protractor on the line segment AC such that it coincides with the line of the diameter of the protractor and the middle point of the line coincides with A.
 - (iii) By counting from the right side, mark B as the point of 45° of protractor and construct AB.
 - (iv) Taking P as centre and convenient radius draw an arc which intersects the line segment AB at points T and Q and AC at points R and S.
 - (v) Taking T and Q as centres and same radius, draw two arcs which intersect at point G on the other side.
 - (vi) Taking R and S as centres and same radius, draw two arcs which intersect at point H on the other side.
 - (vii) Now join the points PG and PH which intersect the line segments AB and AC at points M and N.
- By measuring $\angle MPN$ with the help of a protractor we get $\angle MPN = 135^\circ$.



10. Draw an angle and label it as $\angle BAC$. Draw its bisector ray AX and take a point P on it. From P draw line segments PM and PN, such that $PM \perp AB$ and $PN \perp AC$, where M and N are respectively points on rays AB and AC. Measure PM and PN. Are the two lengths equal?

Solution:

- (i) Construct $\angle BAC$ on the line segment AC.

Considering A as centre with convenient radius, construct an arc from the line AB and AC.

(ii) Take both the points where the arc cuts the line segments AB and AC as centres, construct two small arcs which intersect at the point X and draw AX.

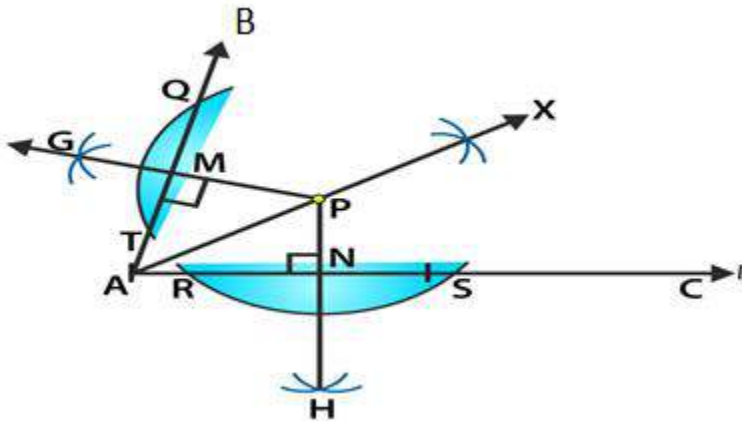
(iii) Now mark a point P on the ray AX.

(iv) Taking P as centre and convenient radius draw an arc which intersects AB at T and Q and AC at R and S.

(v) Taking T and Q as centres and same radius draw two arcs which intersect at point G on the other side.

(vi) Taking R and S as centres and same radius, draw two arcs which intersect at H on the other side.

(vii) Now join PG and PH which intersects the line segments AB and AC at the points M and N.
By measuring PM and PN with the help of a ruler, we get to know that both are equal.



EXERCISE 19.3

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1. Draw a line segment of length 8.6 cm. Bisect it and measure the length of each part.

Solution:

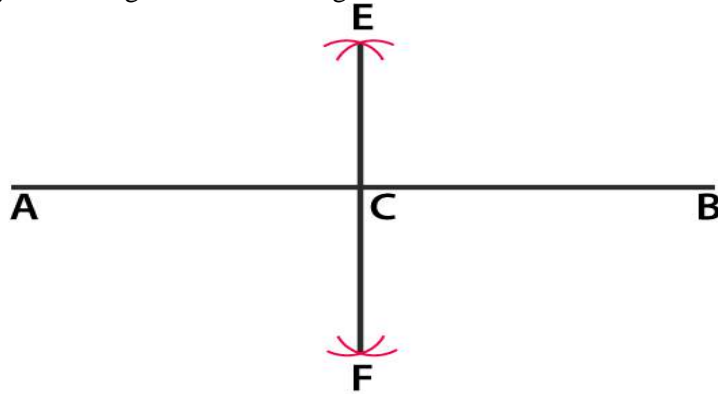
Construct a line segment AB of length 8.6 cm.

Taking A as centre and radius which is more than half of line segment AB, construct arcs on both sides of AB.

Taking B as centre and same radius, construct arcs on both sides of AB which cuts the previous arcs at the points E and F.

Construct a line segment from the points E and F which intersects AB at the point C.

By measuring AC and BC we get $AC = BC = 4.3$ cm.



2. Draw a line segment AB of length 5.8 cm. Draw the perpendicular bisector of this line segment.

Solution:

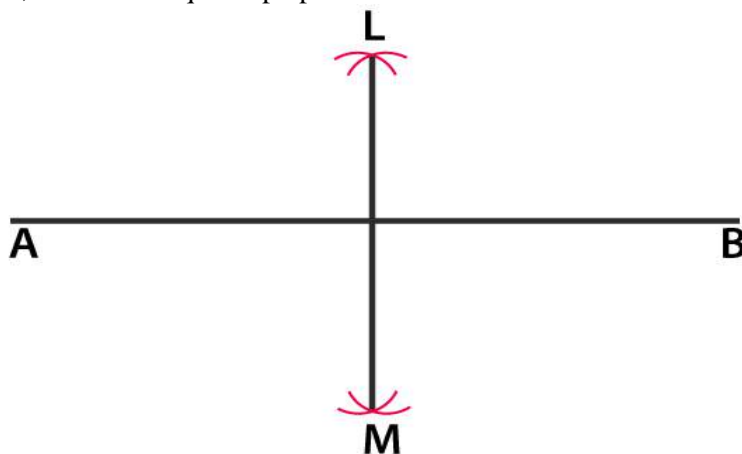
Construct a line segment AB of length 5.8 cm with the help of a ruler.

Taking A as centre and radius which is more than half of AB, construct arcs on both sides of the line segment AB.

Taking B as centre and same radius, construct arcs on both sides of AB which intersects the previous arcs at the points L and M.

Construct the line segment LM with L and M as the end points.

Here, LM is the required perpendicular bisector of AB.



3. Draw a circle with centre at point O and radius 5 cm. Draw its chord AB, draw the perpendicular bisector of line segment AB. Does it pass through the centre of the circle?

Solution:

Take a point O. By considering O as centre and radius which is equal to 5 cm construct a circle.

Now take points A and B on the circumference of the circle and construct a line segment with the points A and B as its end points.

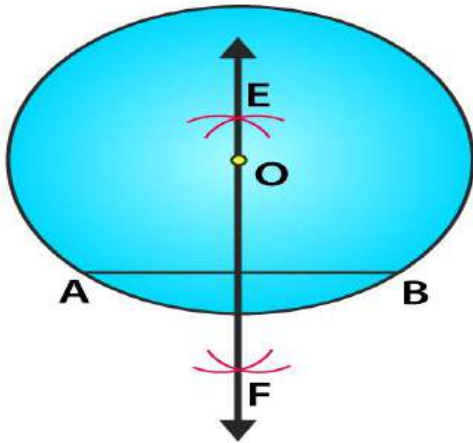
Here AB is the chord of the circle.

Taking A as centre and radius which is more than half of AB, construct arcs on both sides of AB.

Taking B as centre and same radius, construct arcs on both sides of AB which cuts the previous arcs at the points E and F.

Construct a line passing through the points E and F.

Here, the line EF passes through the centre O of the circle.



4. Draw a circle with centre at point O. Draw its two chords AB and CD such that AB is not parallel to CD. Draw the perpendicular bisectors of AB and CD. At what point do they intersect?

Solution:

Construct a circle with O as the centre. Construct two chords AB and CD.

(i) Taking A as centre and radius more than half of AB construct arcs on both sides of the line segment AB.

(ii) Taking B as centre and same radius, construct arcs which cuts the previous arcs at the points P and Q.

(iii) Now join the points P and Q.

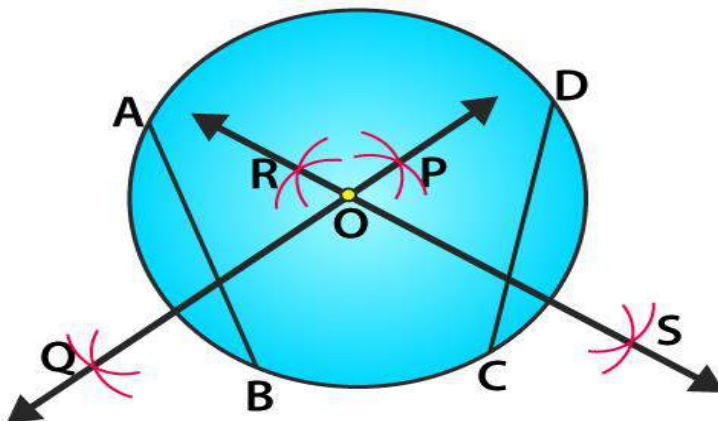
(iv) Taking C as centre and radius more than half of CD construct arcs on both sides of CD.

(v) Taking D as centre and same radius, construct arcs which cuts the previous arcs at the points R and S.

(vi) Now join the points R and S.

Construct the line segments of perpendicular bisector of AB and CD.

Here, the perpendicular bisector of line segments AB and CD meet at the point O which is the centre of the circle.



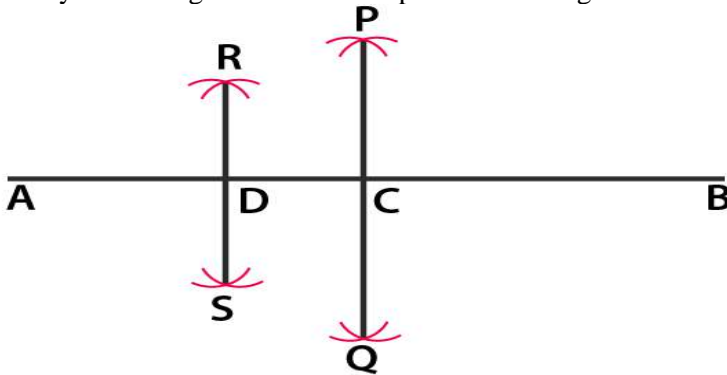
5. Draw a line segment of length 10 cm and bisect it. Further bisect one of the equal parts and measure its length.

Solution:

Construct a line segment AB of length 10 cm and bisect it.

- (i) Taking A as centre and radius which is more than half of AB, construct arcs on both sides of AB.
- (ii) Taking B as centre and same radius, construct arcs which cuts the previous arcs at the points P and Q.
- (iii) Now join the points P and Q which intersects the line AB at the point C.
- (iv) Taking A as centre and radius which is more than half of AC, construct arcs on both sides of AB
- (v) Taking C as centre and same radius, construct arcs which cuts the previous arcs at the points R and S.
- (vi) Join the points R and S such that the line intersects AC at the point D.

Now by measuring AD with the help of a ruler we get $AD = 2.5$ cm.



6. Draw a line segment AB and bisect it. Bisect one of the equal parts to obtain a line segment of length $1/2$ (AB).

Solution:

Construct a line segment AB.

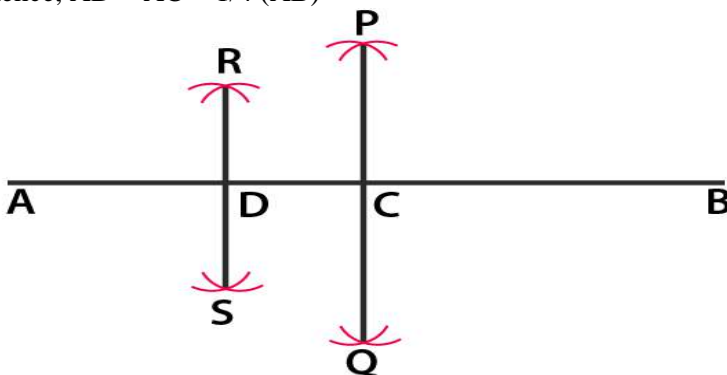
- (i) Taking A as centre and radius which is more than half of AB construct arcs on both sides of AB.
- (ii) Taking B as centre and same radius, construct arcs which cuts the previous arcs at the points P and Q.
- (iii) Now join the points P and Q such that the line PQ intersects AB at the point C.
- (iv) Taking A as centre and radius more than half of AC construct arcs on both sides of AC.
- (v) Taking C as centre and same radius construct arcs which cuts the previous arcs at the points R and S.
- (vi) Now join the points R and S such that the line intersects AB at the point D.

Here, $AC = CB = 1/2$ (AB)

By dividing AC at D

We know that AD and AC are of same length

Hence, $AD = AC = 1/4$ (AB)



7. Draw a line segment AB and by ruler and compasses, obtain a line segment of length $\frac{3}{4}$ (AB).

Solution:

Construct a line segment AB with the help of a ruler.

- (i) Taking A as centre and radius which is more than half of AB construct arcs on both sides of AB.
- (ii) Taking B as centre and same radius construct arcs which cuts the previous arcs at the points P and Q.
- (iii) Now join the points P and Q such that the line intersects AB at the point C.

- (i) Taking A as centre and radius which is more than half of AB construct arcs on both sides of AC.
- (ii) Taking C as centre and same radius construct arcs which cuts the previous arcs at the points R and S.
- (iii) Now join the points R and S such that the line intersects AB at the point D.

Bisect AC and mark D as the point of bisection.

We know that

$$AD = \frac{1}{4} (AB)$$

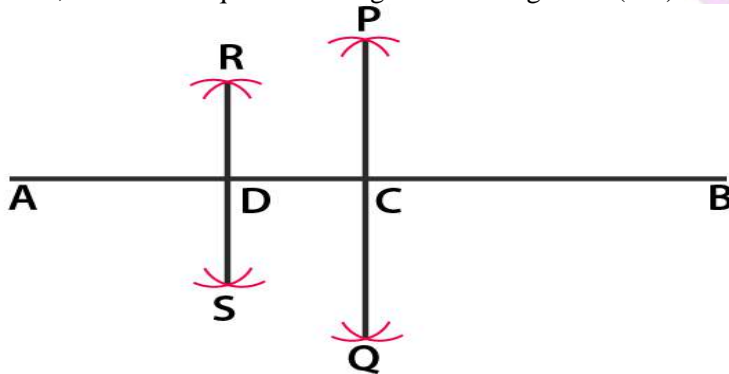
It can be written as

$$DC = \frac{1}{4} (AB) \text{ and } CB = \frac{1}{2} (AB)$$

So we get

$$DB = \frac{1}{4} (AB) + \frac{1}{2} (AB) = \frac{3}{4} (AB)$$

Hence, DB is the required line segment of length $\frac{3}{4}$ (AB).



EXERCISE 19.4

PAGE: 19.9

1. Construct the following angles with the help of a protractor:

45° , 67° , 38° , 110° , 179° , 98° , 84°

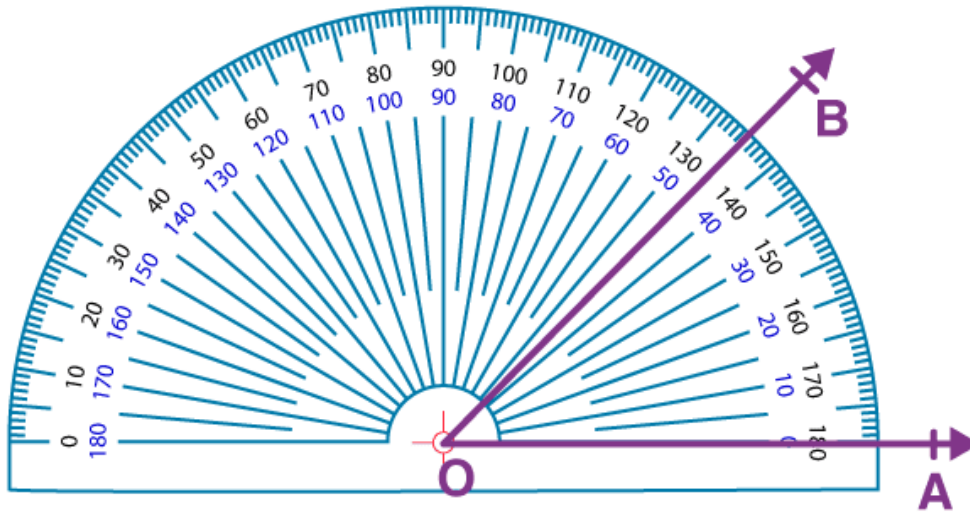
Solution:

Construct a ray OA.

Now place the protractor on the ray OA such that its centre coincides with point O and the diameter coincides with OA.

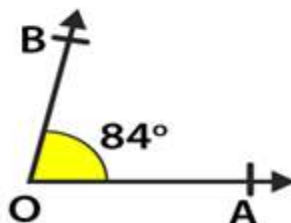
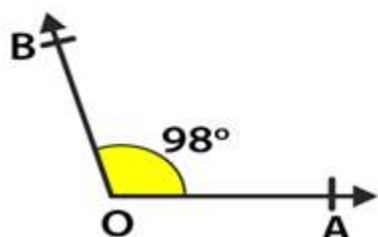
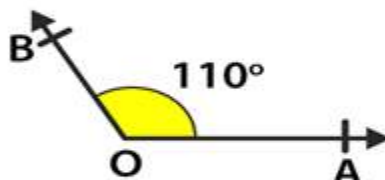
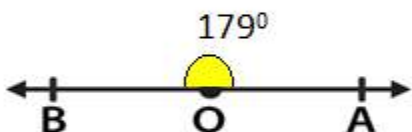
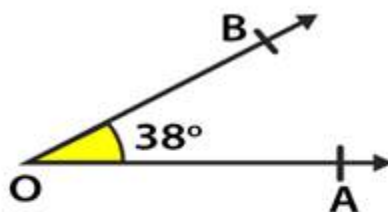
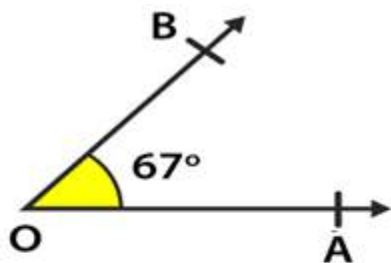
Mark a point B against the mark of 45° on the protractor.

Remove the protractor and construct the line OB where $\angle AOB$ is the required angle.

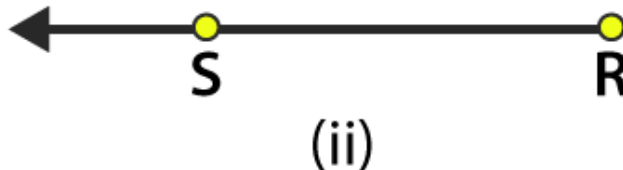
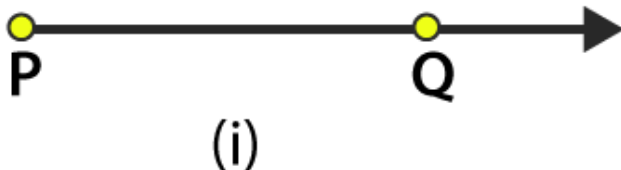


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In the same way draw the angles 67° , 38° , 110° , 179° , 98° and 84°



2. Draw two rays PQ and RS as shown in Fig. 19.14 (i) and (ii). Using protractor, construct angles of 15° and 138° with one arm PQ and RS respectively.



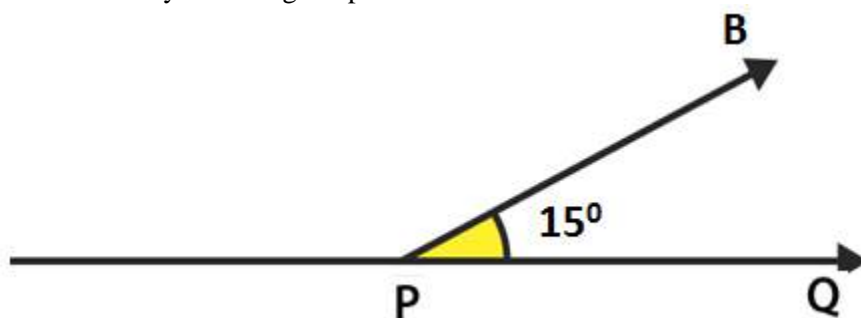
Solution:

(i) Construct a ray PQ as given in the question.

Now place the protractor on PQ such that its centre coincides with the point P and the diameter coincides with PQ.

Mark B against the mark of 15° on the protractor.

Construct PB by removing the protractor.



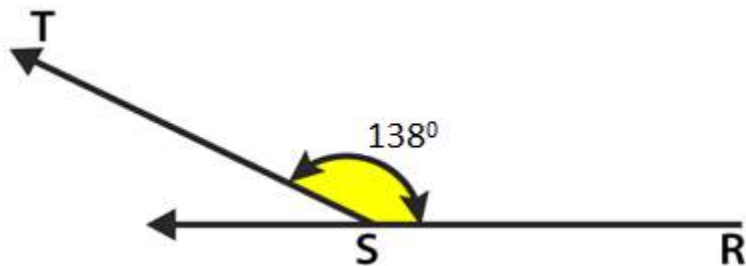
Here $\angle QPB$ is the required angle of 15° .

(ii) Construct a ray RS as given in the question.

Now place the protractor on RS such that its centre coincides with the point R and the diameter coincides with RS.

Mark T against the mark of 138° on the protractor.

Construct ST by removing the protractor.



Here $\angle RST$ is the required angle of 138° .

EXERCISE 19.5

PAGE: 19.13

1. Draw an angle and label it as $\angle BAC$. Construct another angle, equal to $\angle BAC$.

Solution:

Construct an angle $\angle BAC$ and draw a ray OP .

Taking A as centre and suitable radius, construct an arc which intersects AB and AC at points X and Y .

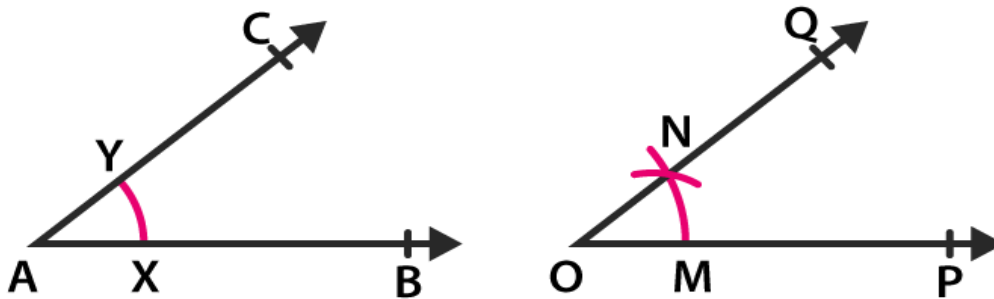
Taking O as centre and same radius, construct an arc which intersects the arc OP at the point M .

Now measure XY with the help of compass.

Taking M as centre and XY as radius construct an arc which intersects the arc which is drawn from O and name it as point N .

Now join the points O and N and extend it to the point Q .

Here, $\angle POQ$ is the required angle.



2. Draw an obtuse angle. Bisect it. Measure each of the angles so obtained.

Solution:

We know that obtuse angles are those which are greater than 90° and less than 180° .

Construct an obtuse angle $\angle BAC$.

Taking A as centre with appropriate radius construct an arc which intersects AB and AC at the points P and Q .

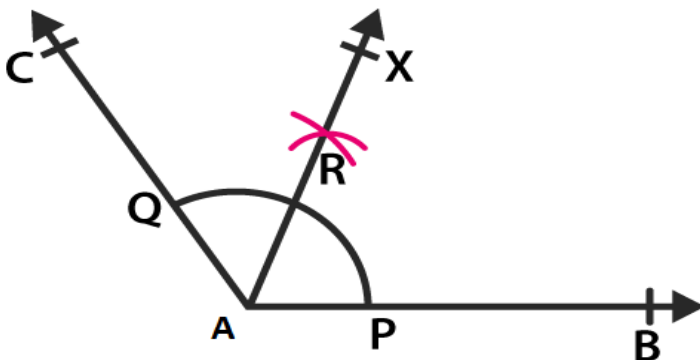
Taking P as centre and radius which is more than half of PQ construct an arc.

Taking Q as centre and same radius construct another arc which intersects the previous arc at the point R .

Now join A and R and extend it to the point X .

So the ray AX is the required bisector of $\angle BAC$.

By measuring $\angle BAR$ and $\angle CAR$ we get $\angle BAR = \angle CAR = 65^\circ$.



3. Using your protractor, draw an angle of measure 108° . With this angle as given, drawn an angle of 54° .

Solution:

Construct a ray OA.

Using protractor, draw an angle $\angle AOB$ of 108° where $108/2 = 54^\circ$

Hence, 54° is half of 108° .

In order to get angle 54° , we must bisect the angle of 108° .

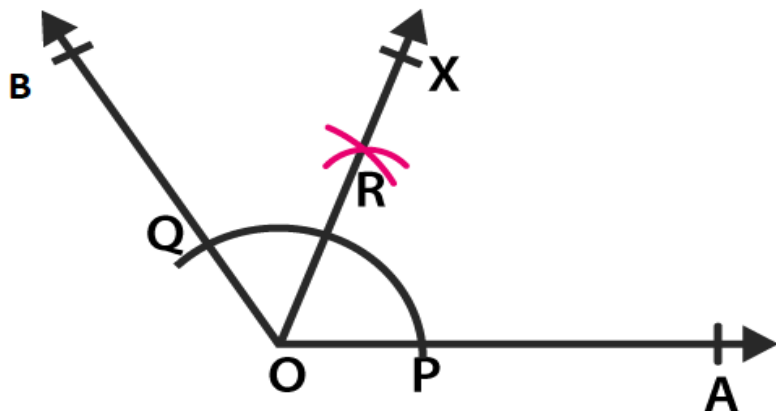
Taking O as centre and convenient radius, construct an arc which cuts the sides OA and OB at the points P and Q.

Taking P as centre and radius which is more than half of PQ construct an arc.

Taking Q as centre and same radius construct another arc which intersects the previous arc and name it as point R.

Now join the points O and R and extend it to the point X.

Here, $\angle AOX$ is the required angle of 54° .



4. Using protractor, draw a right angle. Bisect it to get an angle of measure 45° .

Solution:

Construct a ray OA.

Using a protractor construct $\angle AOB$ of 90° .

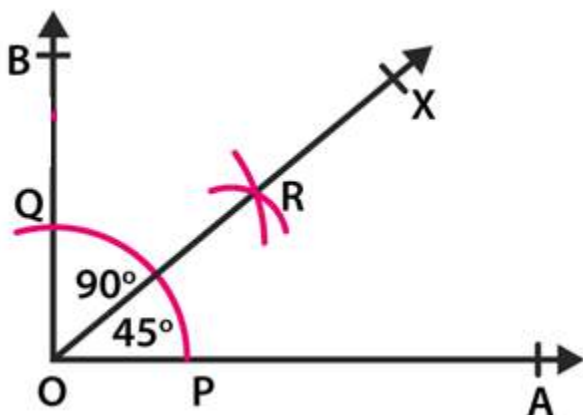
Taking O as centre and convenient radius, construct an arc which cuts the sides OA and OB at the points P and Q.

Taking P as centre and radius which is more than half of PQ, construct an arc.

Taking Q as centre and same radius, construct another arc which intersects the previous arc and name it as point R.

Now join the points O and R and extend it to the point X.

Here, $\angle AOX$ is the required angle of 45° where $\angle AOB = 90^\circ$ and $\angle AOX = 45^\circ$.



5. Draw a linear pair of angles. Bisect each of the two angles. Verify that the two bisecting rays are perpendicular to each other.

Solution:

We know that the two angles which are adjacent and supplementary are known as linear pair of angles.

Construct a line AB and mark a point O on it.

By constructing an angle $\angle AOC$ we get another angle $\angle BOC$.

Now bisect $\angle AOC$ using a compass and a ruler and get the ray OX.

In the same way bisect $\angle BOC$ and get the ray OY.

We know that

$$\angle XOY = \angle XOC + \angle COY$$

It can be written as

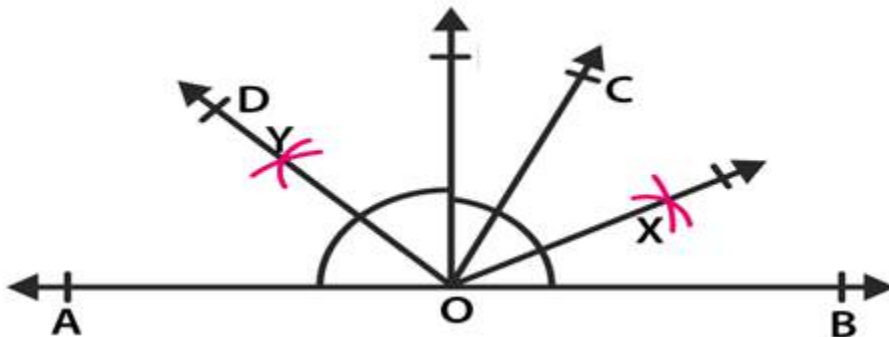
$$\angle XOY = \frac{1}{2} \angle AOC + \frac{1}{2} \angle BOC$$

So we get

$$\angle XOY = \frac{1}{2} (\angle AOC + \angle BOC)$$

We know that $\angle AOC$ and $\angle BOC$ are supplementary angles

$$\angle XOY = \frac{1}{2} (180^\circ) = 90^\circ$$



6. Draw a pair of vertically opposite angles. Bisect each of the two angles. Verify that the bisecting rays are in the same line.

Solution:

Construct two lines AB and CD which intersect each other at the point O

Since vertically opposite angles are equal we get

$$\angle BOC = \angle AOD \text{ and } \angle AOC = \angle BOD$$

Now bisect angle AOC and construct the bisecting ray as OX.

In the same way, we bisect $\angle BOD$ and construct bisecting ray OY.

We get

$$\angle XOY = \angle XOA + \angle AOD + \angle DOY = \frac{1}{2} \angle AOC + \angle AOD + \frac{1}{2} \angle BOD$$

We know that $\angle AOC = \angle BOD$

$$\angle XOY = \frac{1}{2} \angle BOD + \angle AOD + \frac{1}{2} \angle BOD$$

So we get

$$\angle XOY = \angle AOD + \angle BOD$$

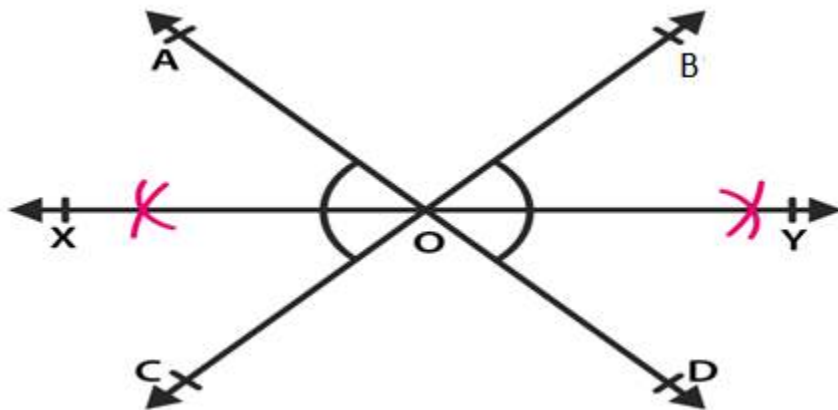
AB is a line

We know that $\angle AOD$ and $\angle BOD$ are supplementary angles whose sum is equal to 180° .

$$\angle XOY = 180^\circ$$

The angles on one side of a straight line is always 180° and also the sum of angles is 180°

Here, XY is a straight line where OX and OY are in the same line.



7. Using ruler and compasses only, draw a right angle.

Solution:

Construct a ray OA.

Taking O as centre and convenient radius construct an arc PQ using a compass intersecting the ray OA at the point Q.

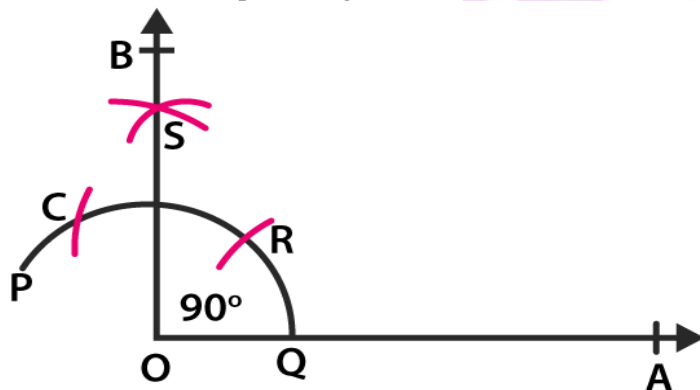
Taking P as centre and same radius construct another arc which intersects the arc PQ at the point R.

Taking R as centre and same radius, construct an arc which cuts the arc PQ at the point C opposite to P.

Using C and R as the centre construct two arcs of radius which is more than half of CR intersecting each other at the point S.

Now join the points O and S and extend it to the point B.

Here, $\angle AOB$ is the required angle of 90° .



8. Using ruler and compasses only, draw an angle of measure 135° .

Solution:

Construct a line AB and mark a point O on it.

Taking O as centre and convenient radius, construct an arc PQ using a compass which intersects the line AB at the point P and Q.

Taking P as centre and same radius, construct another arc which intersects the arc PQ at the point R.

Taking Q as centre and same radius, construct another arc which intersects the arc PQ at the point S which is opposite to P.

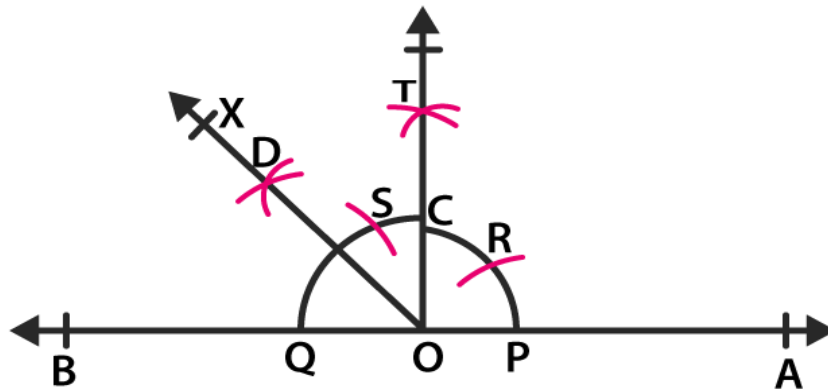
Considering S and R as centres and radius which is more than half of SR, construct two arcs which intersect each other at the point T.

Now join the points O and T which intersects the arc PQ at the point C.

Considering C and Q as centres and radius which is more than half of CQ, construct two arcs which intersect each other at the point D.

Now join the points O and D and extend it to point X to form the ray OX.

Here, $\angle AOX$ is the required angle of 135° .



9. Using a protractor, draw an angle of measure 72° . With this angle as given, draw angles of measure 36° and 54° .

Solution:

Construct a ray OA.

Using protractor construct $\angle AOB$ of 72°

Taking O as centre and convenient radius, construct an arc which cut sides OA and OB at the point P and Q.

Taking P and Q as centres and radius which is more than half of PQ, construct two arcs which cut each other at the point R.

Now join the points O and R and extend it to the point X.

Here, OR intersects the arc PQ at the point C.

Taking C and Q as centres and radius which is more than half of CQ, construct two arcs which cut each other at point T.

Now join the points O and T and extend it to the point Y.

OX bisects $\angle AOB$

It can be written as

$$\angle AOX = \angle BOX = 72/2 = 36^\circ$$

OY bisects $\angle BOX$

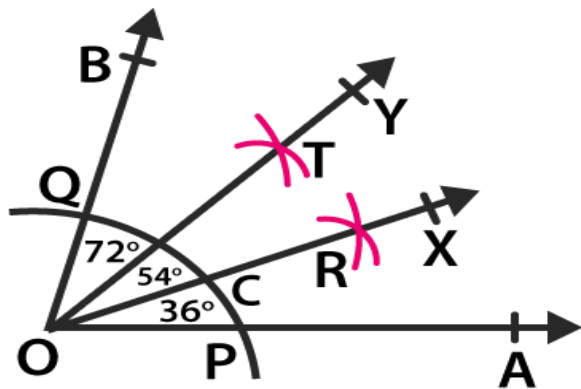
It can be written as

$$\angle XOY = \angle BOY = 36/2 = 18^\circ$$

We know that

$$\angle AOY = \angle AOX + \angle XOY = 36^\circ + 18^\circ = 54^\circ$$

Here, $\angle AOX$ is the required angle of 36° and $\angle AOY$ is the required angle of 54° .



EXERCISE 19.6

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1. Construct an angle of 60° with the help of compasses and bisect it by paper folding.

Solution:

Construct a ray OA

Taking O as centre and convenient radius, construct an arc which cuts the ray OA at the point P.

Taking P as centre and same radius, construct another arc which cuts the previous arc at the point Q.

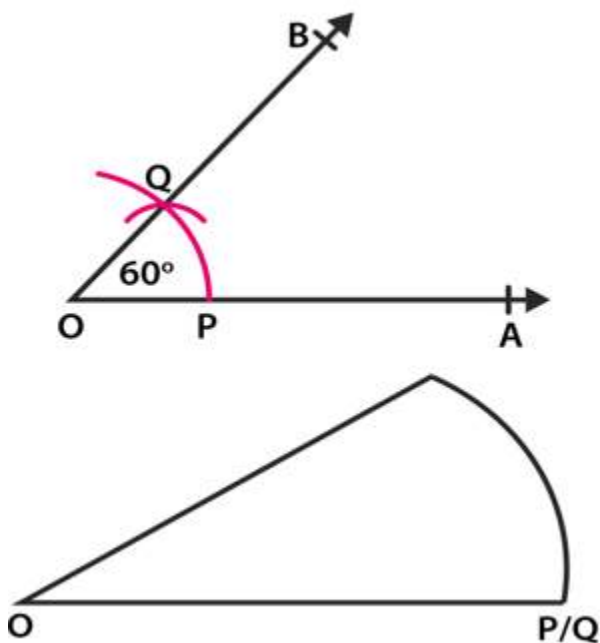
Construct OQ and extend it to the point B.

Here, $\angle AOB$ is the required angle of 60°

Now cut the part of paper as sector OPQ

Fold the part of paper such that the line segments OP and OQ coincides.

The angle which is made at point O is the required angle which is half of $\angle AOB$.



2. Construct the following angles with the help of ruler and compasses only:

(i) 30°

(ii) 90°

(iii) 45°

(iv) 135°

(v) 150°

(vi) 105°

Solution:

(i) 30°

Construct a ray OA.

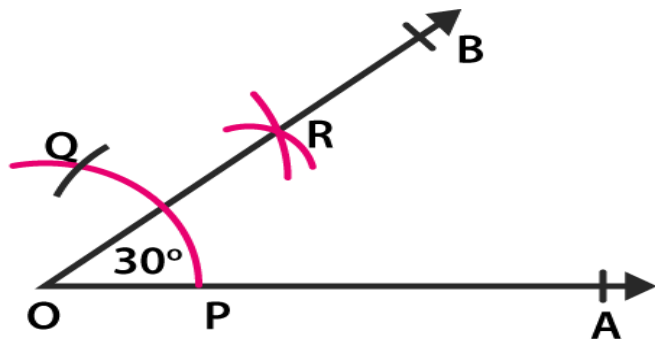
Taking O as centre and with convenient radius, construct an arc which cuts OA at the point P.

Taking P as centre and same radius, construct an arc which cuts the previous arc at the point Q.

Considering P and Q as centres and radius which is more than half of PQ construct two arcs which cuts each other and name it as point R.

Construct OR and extend it to the point B.

Here, $\angle AOB$ is the required angle of 30°



(ii) 90°

Construct a ray OA.

Taking O as centre and with convenient radius, construct an arc which cuts OA at the point P.

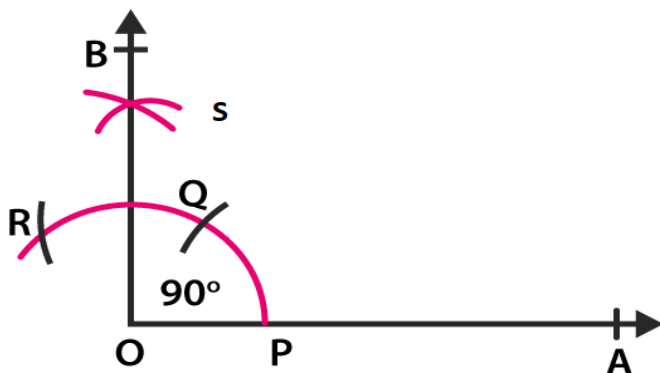
Taking P as centre and same radius, construct an arc which cuts the previous arc at the point Q.

Taking Q as centre and same radius, construct an arc which cuts the previous arc at the point R.

Considering Q and R as centres and radius which is more than half of QR construct two arcs which cuts each other and name it as point S.

Construct OS and extend it to the point B from the ray OB.

Here, $\angle AOB$ is the required angle of 90° .



(iii) 45°

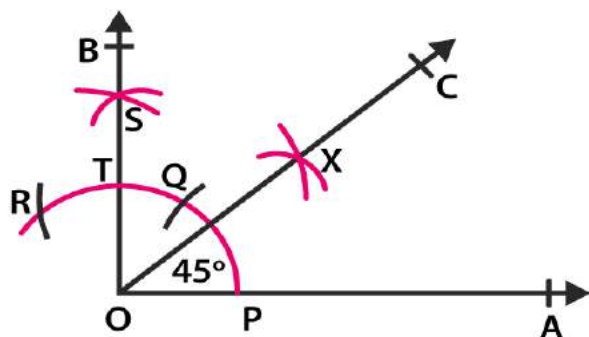
In order to draw an angle of 45° , construct an angle of 90° and bisect it.

Construct $\angle AOB = 90^\circ$ where OA and OB are the rays which intersect the arc at the points P and T

Taking P and T as centres and radius which is more than half of PT, construct two arcs which cuts each other and name it as point X

Construct OX and extend it to the point C to form the ray OC

Here, $\angle AOC$ is the required angle of 45° .



(iv) 135°

Construct a line AB and mark a point O in the middle of AB.

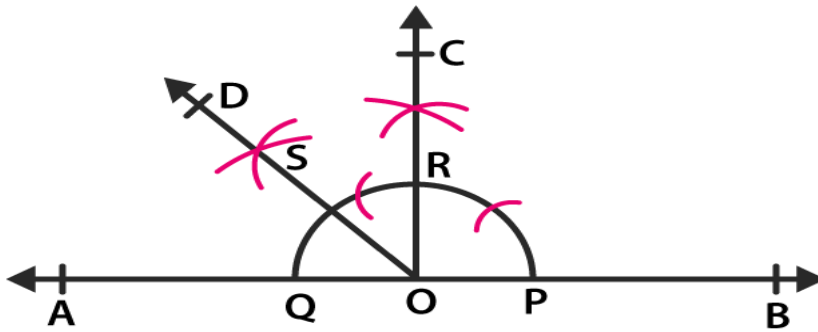
Taking O as centre and convenient radius, construct an arc which cuts the line AB at the points P and Q.

Construct an angle of 90° on the ray OB as $\angle BOC = 90^\circ$ where OC cuts the arc at the point R

Taking Q and R as centres and radius which is more than half of QR, construct two arcs which cuts each other and name it as point S.

Construct OS and extend it to the point D to form the ray OD.

Here, $\angle BOD$ is the required angle of 135° .



(v) 150°

Construct a line AB and mark a point O in the middle of AB.

Taking O as centre and convenient radius construct an arc which cuts the line AB at the points P and Q.

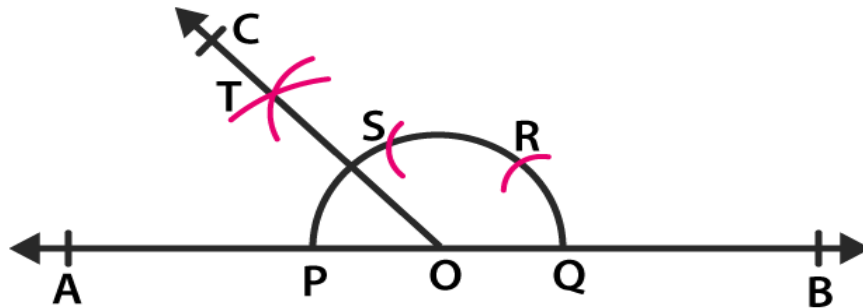
Taking Q as centre and same radius construct an arc which cuts the previous arc and name it as point R.

Taking R as centre and same radius construct an arc which cuts the previous arc and name it as point S.

Taking P and S as centres and radius which is more than half of PS, construct two arcs which cuts each other and name it as point T.

Construct OT and extend it to the point C to form the ray OC.

Here, $\angle BOC$ is the required angle of 150° .

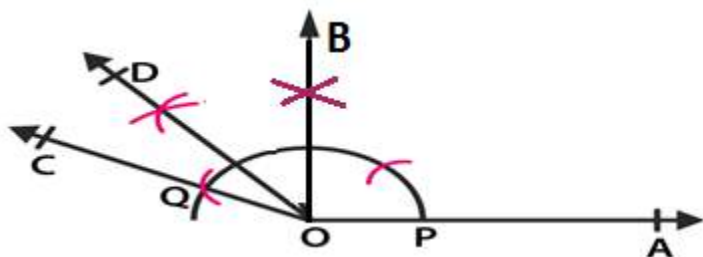


(vi) 105°

Construct a ray OA and make $\angle AOB = 90^\circ$ and $\angle AOC = 120^\circ$

Bisect $\angle BOC$ and get the ray OD.

Here, $\angle AOD$ is the required angle of 105° .



3. Construct a rectangle whose adjacent sides are 8 cm and 3 cm.

Solution:

Construct a line segment AB of length 8 cm.

Draw $\angle BAX = 90^\circ$ at A and $\angle ABY = 90^\circ$ at B

With the help of compass and ruler, mark a point D on the ray AX where AD = 3 cm

In the same way mark the point C on the ray BY where BC = 3 cm

Construct the line segment CD

Hence, ABCD is the required rectangle.

