

**Vivian Joseph**

**(20BCE0777)**

# **Machine Learning**

**Lab Da-3**

**Single Layer Perceptron**

**and KNN Classifier**

## Dataset:

|    | Year | Model | Price | buy |
|----|------|-------|-------|-----|
| 0  | 2010 | 1.10  | 120   | no  |
| 1  | 2011 | 1.20  | 150   | no  |
| 2  | 2011 | 1.80  | 160   | no  |
| 3  | 2012 | 2.00  | 145   | no  |
| 4  | 2012 | 2.10  | 150   | no  |
| 5  | 2012 | 2.40  | 160   | no  |
| 6  | 2013 | 2.60  | 190   | no  |
| 7  | 2013 | 2.80  | 210   | no  |
| 8  | 2014 | 2.90  | 220   | no  |
| 9  | 2014 | 3.00  | 200   | no  |
| 10 | 2015 | 3.10  | 210   | no  |
| 11 | 2015 | 3.20  | 215   | yes |
| 12 | 2016 | 3.30  | 220   | yes |
| 13 | 2016 | 3.40  | 260   | no  |
| 14 | 2017 | 3.50  | 270   | no  |
| 15 | 2017 | 3.70  | 280   | no  |
| 16 | 2018 | 4.00  | 250   | yes |
| 17 | 2018 | 4.20  | 264   | yes |
| 18 | 2018 | 4.40  | 270   | yes |
| 19 | 2019 | 4.60  | 282   | no  |
| 20 | 2019 | 4.70  | 295   | no  |
| 21 | 2020 | 4.80  | 303   | no  |
| 22 | 2020 | 4.82  | 312   | no  |
| 23 | 2020 | 4.90  | 323   | yes |
| 24 | 2021 | 4.95  | 337   | yes |
| 25 | 2021 | 5.00  | 300   | yes |
| 26 | 2022 | 5.10  | 315   | yes |
| 27 | 2022 | 5.20  | 340   | yes |
| 28 | 2022 | 5.40  | 360   | no  |
| 29 | 2023 | 5.80  | 399   | yes |

## Q1) Apply KNN classification on the dataset and visualize the same

Making a function to check the distances of an input point from all points in the dataset

```
def knn(year,price):  
    df['diff1']=df['Year']-year  
    df['diff2']=df['Price']-price  
    df['d1sqr']=df['diff1']**2  
    df['d2sqr']=df['diff2']**2  
    df['dist']=np.sqrt(df['d2sqr']+df['d1sqr'])  
    print(df)
```

eg:

```
knn(2017,340)
```

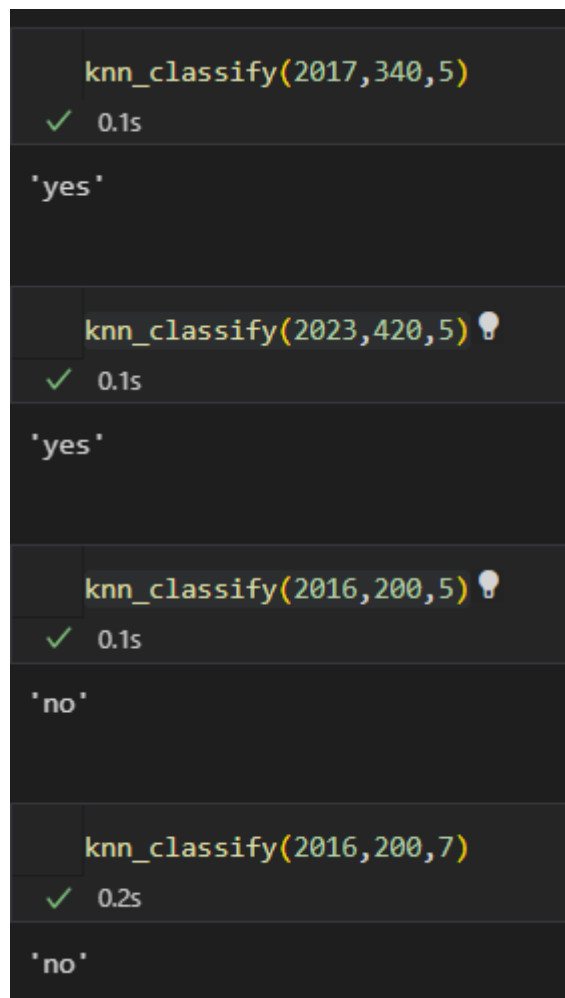
|    | Year | Model | Price | buy | diff1 | diff2 | d1sqr | d2sqr | dist       |
|----|------|-------|-------|-----|-------|-------|-------|-------|------------|
| 0  | 2010 | 1.10  | 120   | no  | -7    | -220  | 49    | 48400 | 220.111335 |
| 1  | 2011 | 1.20  | 150   | no  | -6    | -190  | 36    | 36100 | 190.094713 |
| 2  | 2011 | 1.80  | 160   | no  | -6    | -180  | 36    | 32400 | 180.099972 |
| 3  | 2012 | 2.00  | 145   | no  | -5    | -195  | 25    | 38025 | 195.064092 |
| 4  | 2012 | 2.10  | 150   | no  | -5    | -190  | 25    | 36100 | 190.065778 |
| 5  | 2012 | 2.40  | 160   | no  | -5    | -180  | 25    | 32400 | 180.069431 |
| 6  | 2013 | 2.60  | 190   | no  | -4    | -150  | 16    | 22500 | 150.053324 |
| 7  | 2013 | 2.80  | 210   | no  | -4    | -130  | 16    | 16900 | 130.061524 |
| 8  | 2014 | 2.90  | 220   | no  | -3    | -120  | 9     | 14400 | 120.037494 |
| 9  | 2014 | 3.00  | 200   | no  | -3    | -140  | 9     | 19600 | 140.032139 |
| 10 | 2015 | 3.10  | 210   | no  | -2    | -130  | 4     | 16900 | 130.015384 |
| 11 | 2015 | 3.20  | 215   | yes | -2    | -125  | 4     | 15625 | 125.015999 |
| 12 | 2016 | 3.30  | 220   | yes | -1    | -120  | 1     | 14400 | 120.004167 |
| 13 | 2016 | 3.40  | 260   | no  | -1    | -80   | 1     | 6400  | 80.006250  |
| 14 | 2017 | 3.50  | 270   | no  | 0     | -70   | 0     | 4900  | 70.000000  |
| 15 | 2017 | 3.70  | 280   | no  | 0     | -60   | 0     | 3600  | 60.000000  |
| 16 | 2018 | 4.00  | 250   | yes | 1     | -90   | 1     | 8100  | 90.005555  |
| 17 | 2018 | 4.20  | 264   | yes | 1     | -76   | 1     | 5776  | 76.006579  |
| 18 | 2018 | 4.40  | 270   | yes | 1     | -70   | 1     | 4900  | 70.007142  |
| 19 | 2019 | 4.60  | 282   | no  | 2     | -58   | 4     | 3364  | 58.034473  |
| 20 | 2019 | 4.70  | 295   | no  | 2     | -45   | 4     | 2025  | 45.044423  |
| 21 | 2020 | 4.80  | 303   | no  | 3     | -37   | 9     | 1369  | 37.121422  |
| 22 | 2020 | 4.82  | 312   | no  | 3     | -28   | 9     | 784   | 28.160256  |
| 23 | 2020 | 4.90  | 323   | yes | 3     | -17   | 9     | 289   | 17.262677  |
| 24 | 2021 | 4.95  | 337   | yes | 4     | -3    | 16    | 9     | 5.000000   |
| 25 | 2021 | 5.00  | 300   | yes | 4     | -40   | 16    | 1600  | 40.199502  |
| 26 | 2022 | 5.10  | 315   | yes | 5     | -25   | 25    | 625   | 25.495098  |
| 27 | 2022 | 5.20  | 340   | yes | 5     | 0     | 25    | 0     | 5.000000   |
| 28 | 2022 | 5.40  | 360   | no  | 5     | 20    | 25    | 400   | 20.615528  |
| 29 | 2023 | 5.80  | 399   | yes | 6     | 59    | 36    | 3481  | 59.304300  |

**Make function that take input values and k value and gives the classification of that point according to k nearest neighbours**

```
def knn_classify(year,price,k):  
    df['diff1']=df['Year']-year  
    df['diff2']=df['Price']-price  
    df['d1sqr']=df['diff1']**2  
    df['d2sqr']=df['diff2']**2  
    df['distance']=np.sqrt(df['d2sqr']+df['d1sqr'])  
    top_k = df.nsmallest(k, 'distance')  
    prediction = top_k['buy'].value_counts().head(1).index[0]  
    return prediction
```

**returns yes/no**

```
knn_classify(2017,340,5)
```



```
knn_classify(2017,340,5)  
✓ 0.1s  
'yes'  
  
knn_classify(2023,420,5)💡  
✓ 0.1s  
'yes'  
  
knn_classify(2016,200,5)💡  
✓ 0.1s  
'no'  
  
knn_classify(2016,200,7)  
✓ 0.2s  
'no'
```

## Plotting the dataset and plotting regions according to what classification they would give

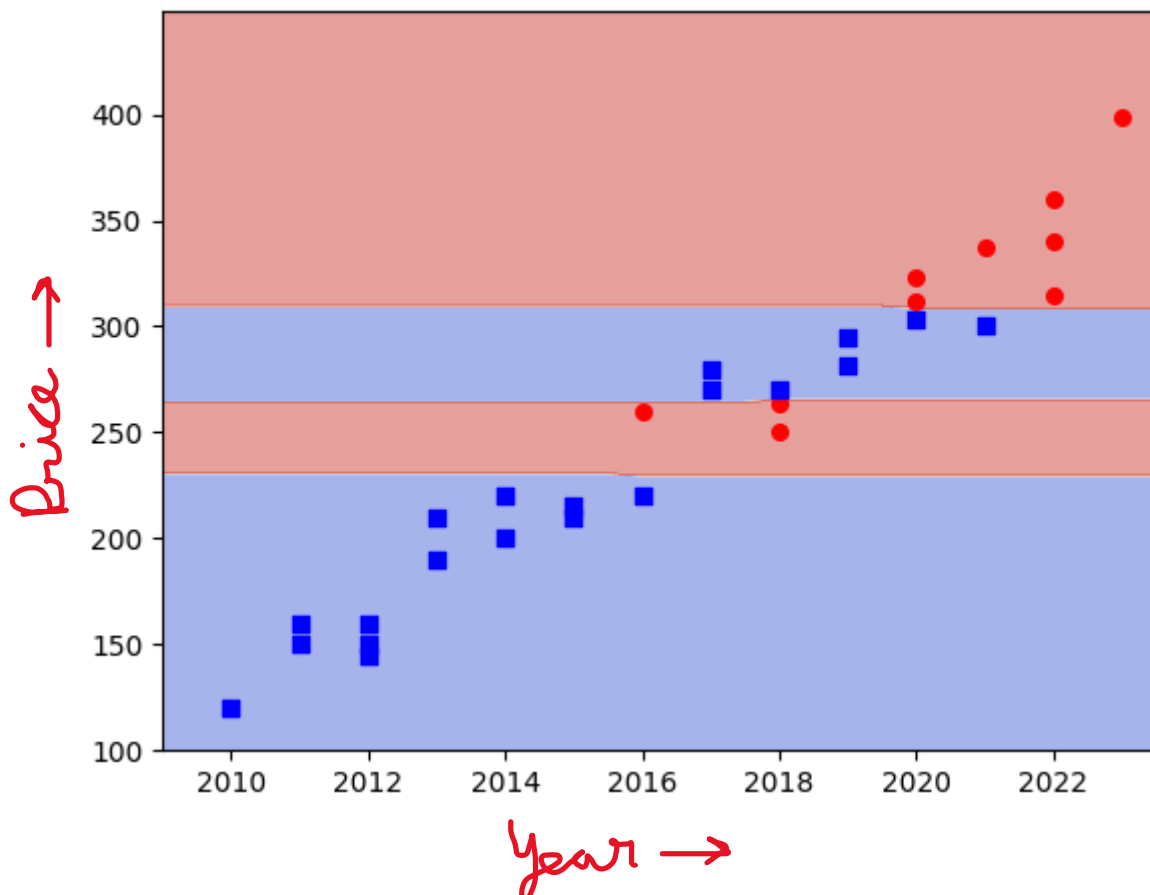
```
k=5
xx, yy = np.meshgrid(np.arange(2009, 2024, 0.5), np.arange(100, 450, 1))
zz = np.array([knn_classify(x, y, k)=='yes' for x, y in zip(xx.ravel(), yy.ravel())])
zz = zz.reshape(xx.shape)
# print(zz)
fig, ax = plt.subplots()
ax.contourf(xx, yy, zz, cmap='coolwarm', alpha=0.5)

colors = {'yes': 'red', 'no': 'blue'}
markers = {'yes': 'o', 'no': 's'}
for i, row in df.iterrows():
    ax.scatter(row['Year'], row['Price'], c=colors[knn_classify(row['Year'],
row['Price'], k)], marker=markers[knn_classify(row['Year'], row['Price'], k)], s=30)
plt.show()
```

plot the contour

Make contours according to  
classification and color them  
accordingly

Red="Yes" Blue="No"



**Q2) Pass the dataset through a single layer perceptron to find the weights of each feature and the bias**

**Converting class labels “yes” and “no” to ordinal 0 and 1**

```
df['ifBuy']=(df['buy'].map({'yes':1,'no':0}))
```

|    | Year | Model | Price | buy | ifBuy |
|----|------|-------|-------|-----|-------|
| 0  | 2010 | 1.10  | 120   | no  | 0     |
| 1  | 2011 | 1.20  | 150   | no  | 0     |
| 2  | 2011 | 1.80  | 160   | no  | 0     |
| 3  | 2012 | 2.00  | 145   | no  | 0     |
| 4  | 2012 | 2.10  | 150   | no  | 0     |
| 5  | 2012 | 2.40  | 160   | no  | 0     |
| 6  | 2013 | 2.60  | 190   | no  | 0     |
| 7  | 2013 | 2.80  | 210   | no  | 0     |
| 8  | 2014 | 2.90  | 220   | no  | 0     |
| 9  | 2014 | 3.00  | 200   | no  | 0     |
| 10 | 2015 | 3.10  | 210   | no  | 0     |
| 11 | 2015 | 3.20  | 215   | yes | 1     |
| 12 | 2016 | 3.30  | 220   | yes | 1     |
| 13 | 2016 | 3.40  | 260   | no  | 0     |
| 14 | 2017 | 3.50  | 270   | no  | 0     |
| 15 | 2017 | 3.70  | 280   | no  | 0     |
| 16 | 2018 | 4.00  | 250   | yes | 1     |
| 17 | 2018 | 4.20  | 264   | yes | 1     |
| 18 | 2018 | 4.40  | 270   | yes | 1     |
| 19 | 2019 | 4.60  | 282   | no  | 0     |
| 20 | 2019 | 4.70  | 295   | no  | 0     |
| 21 | 2020 | 4.80  | 303   | no  | 0     |
| 22 | 2020 | 4.82  | 312   | no  | 0     |
| 23 | 2020 | 4.90  | 323   | yes | 1     |
| 24 | 2021 | 4.95  | 337   | yes | 1     |
| 25 | 2021 | 5.00  | 300   | yes | 1     |
| 26 | 2022 | 5.10  | 315   | yes | 1     |
| 27 | 2022 | 5.20  | 340   | yes | 1     |
| 28 | 2022 | 5.40  | 360   | no  | 0     |
| 29 | 2023 | 5.80  | 399   | yes | 1     |

## Running a single layer perceptron with all weights starting at 1, alpha as 0.005 and for 10000 epochs

```
w0=1
w1=1
w2=1
w3=1
alpha=0.005
epochs=10000

for i in range(0,epochs):
    for j in range(0,df.shape[0]):
        sum=w0*(-100)+w1*df['Year'][j]+w2*df['Model'][j]+w3*df['Price'][j]

        if sum>=0:
            pred=1
        else:
            pred=0
        delta=alpha*(df['ifBuy'][j]-pred)

        w0=w0-delta
        w1=w1+delta*df['Year'][j]
        w2=w2+delta*df['Model'][j]
        w3=w3+delta*df['Price'][j]

df['preds']=w0+w1*df['Year']+w2*df['Model']+w3*df['Price']
df['preds']=(df['preds'] >=0).astype(int)
print(df)
print(w0,w1,w2,w3)
```

*Handwritten annotations in red:*

- } initial weights* (next to w0, w1, w2, w3)
- } Activation function* (next to the if-else block)
- } update weights* (next to the weight update lines)

|   | Year | Model | Price | buy | ifBuy | preds |
|---|------|-------|-------|-----|-------|-------|
| 0   | 2010 | 1.10  | 120   | no  | 0     | 0     |
| 1   | 2011 | 1.20  | 150   | no  | 0     | 0     |
| 2   | 2011 | 1.80  | 160   | no  | 0     | 0     |
| 3   | 2012 | 2.00  | 145   | no  | 0     | 0     |
| 4   | 2012 | 2.10  | 150   | no  | 0     | 0     |
| 5   | 2012 | 2.40  | 160   | no  | 0     | 0     |
| 6   | 2013 | 2.60  | 190   | no  | 0     | 0     |
| 7   | 2013 | 2.80  | 210   | no  | 0     | 0     |
| 8   | 2014 | 2.90  | 220   | no  | 0     | 0     |
| 9   | 2014 | 3.00  | 200   | no  | 0     | 0     |
| 10  | 2015 | 3.10  | 210   | no  | 0     | 0     |
| 11  | 2015 | 3.20  | 215   | yes | 1     | 0     |
| 12  | 2016 | 3.30  | 220   | yes | 1     | 0     |
| 13  | 2016 | 3.40  | 260   | no  | 0     | 0     |
| 14  | 2017 | 3.50  | 270   | no  | 0     | 0     |
| 15  | 2017 | 3.70  | 280   | no  | 0     | 0     |
| 16  | 2018 | 4.00  | 250   | yes | 1     | 0     |
| 17  | 2018 | 4.20  | 264   | yes | 1     | 0     |
| 18  | 2018 | 4.40  | 270   | yes | 1     | 0     |
| 19  | 2019 | 4.60  | 282   | no  | 0     | 0     |
| 20  | 2019 | 4.70  | 295   | no  | 0     | 0     |
| 21  | 2020 | 4.80  | 303   | no  | 0     | 0     |
| 22  | 2020 | 4.82  | 312   | no  | 0     | 0     |
| 23  | 2020 | 4.90  | 323   | yes | 1     | 0     |
| 24  | 2021 | 4.95  | 337   | yes | 1     | 0     |
| 25  | 2021 | 5.00  | 300   | yes | 1     | 0     |
| 26  | 2022 | 5.10  | 315   | yes | 1     | 0     |
| 27  | 2022 | 5.20  | 340   | yes | 1     | 0     |
| 28  | 2022 | 5.40  | 360   | no  | 0     | 0     |
| 29  | 2023 | 5.80  | 399   | yes | 1     | 1     |
| 1.0349999999999993 -2.3549999999977373 32.280599999998488 11.8300000000010772 |      |       |       |     |       |       |
| $w_0$ $w_1$ $w_2$ $w_3$   |      |       |       |     |       |       |

Clearly, a single layer perceptron provides a very bad fit for the given dataset even after 10000 epochs, as it has 3 features and 30 samples.

More layers would be required to get any substantial fit in a neural network.