

A* Algorithm.

①

for Search

→ uses heuristic function of $h(n)$ & cost to reach the node 'n' from start state $g(n)$.

→ finds shortest path through search space.

→ Gives provides fast & optimal result.

$$f(n) = g(n) + h(n)$$

→ heuristic value (child node)
→ cost of each node

Algorithm :-

(i) Enter starting node in OPEN list

(ii) If open list is empty return FAIL

(iii) Select node from OPEN list which has smallest value ($g+h$)

→ if node = Goal
return Success

iv) Expand node 'n' and generate all Successors

↳ compute $(g+h)$ for each successor node

v) if node 'n' is already in OPEN / CLOSED, attached to backpointer.

step
vi) go to (ii)

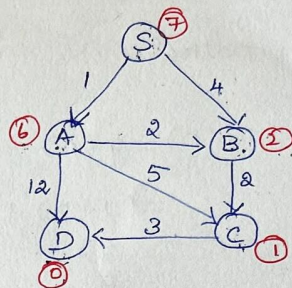
Advantages:-

- ① Best searching algorithm
- ② It is optimal & complete
- ③ helps in solving complex problems.

Disadvantages:

- i) Doesn't always produce shortest path
- 2) Complexity issues
- 3) Requires memory.

Ex:-



S → start state

D → Goal state

$$S \rightarrow A : f(n) = g(n) + h(n) = 1 + 6 = 7$$

$$S \rightarrow B : f(n) = g(n) + h(n) = 4 + 2 = 6$$

$$6 < 7$$

so choose path $S \rightarrow B$.

Explore $S \rightarrow B$ path:- & keep $S \rightarrow A$ in hold.

$$S \xrightarrow{1} B \xrightarrow{2} C : f(n) = g(n) + h(n) \\ = (4 + 2) + 1 \\ = 6 + 1 = 7$$

$$S \xrightarrow{1} B \xrightarrow{2} C \xrightarrow{3} D : f(n) = g(n) + h(n) \\ = (4 + 2 + 3) + 0 \\ = 9$$

$$S \rightarrow B \rightarrow C \rightarrow D : 9 \rightarrow \text{①}$$

Explore

S → A paths

(4)

$$S \xrightarrow{1} A \xrightarrow{2} B \xrightarrow{2} C = f(n) = g(n) + h(n) \\ = (1+2) + 2 \\ = 3 + 2 \\ = 5$$

$$S \xrightarrow{1} A \xrightarrow{5} C \xrightarrow{1} D = f(n) = g(n) + h(n) \\ = (1+5) + 1 \\ = 6 + 1 \\ = 7$$

$$S \xrightarrow{1} A \xrightarrow{12} D \xrightarrow{0} E = f(n) = g(n) + h(n) \\ = (1+12) + 0 \\ = 13$$

$$S \rightarrow A \rightarrow D : 13 \rightarrow (2)$$

from $S \rightarrow A \rightarrow B : 5 < S \rightarrow A \rightarrow C : 7$
so take smallest cost

Explore :- $S \rightarrow A \rightarrow B$ path

(5)

$$S \xrightarrow{1} A \xrightarrow{2} B \xrightarrow{2} C \xrightarrow{1} D = f(n) = g(n) + h(n) \\ = (1+2+2) + 1 \\ = 5 + 1 \\ = 6$$

$$S \xrightarrow{1} A \xrightarrow{2} B \xrightarrow{2} C \xrightarrow{3} D \xrightarrow{0} E = f(n) = g(n) + h(n) \\ = [1+2+2+3] + 0 \\ = 8$$

$$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D : 8 \rightarrow (3)$$

Now :: Explore
 $S \rightarrow A \rightarrow C$

$$S \xrightarrow{1} A \xrightarrow{5} C \xrightarrow{3} D \xrightarrow{0} E = f(n) = g(n) + h(n) \\ = [1+5+3] + 0 \\ = 9 + 0 \\ = 9$$

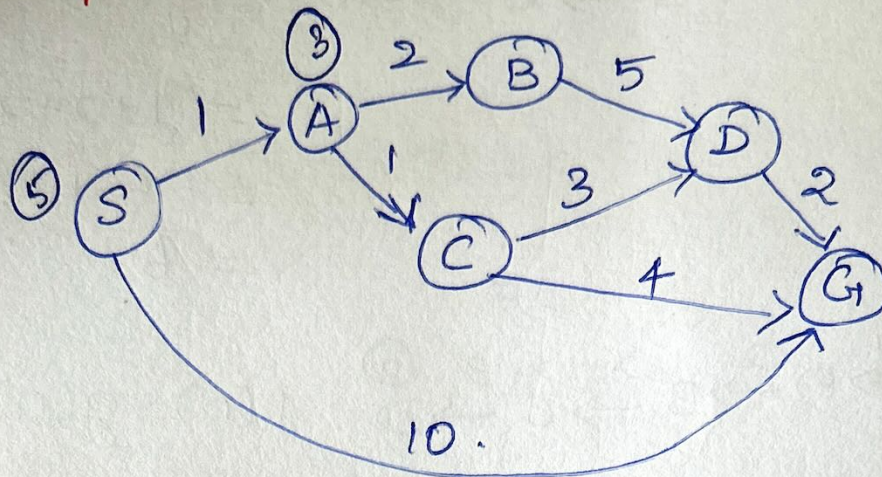
$$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D : 9 \rightarrow (4)$$

From (1), (2), (3) & (4) Paths.
Optimal path is

$$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D : 8$$

6

Example :- 2.



State $h(n)$

S \longrightarrow 5
A \longrightarrow 3
B \longrightarrow 4
C \longrightarrow 2
D \longrightarrow 6
G \longrightarrow 0.

Start state :- S

Goal state : G

Find optimal sol.

using A^* Alg.
Search.