

### Prvi model: dist~speed

Summary of the Linear Regression model (built using lm): Residuals:

Min 1Q Median 3Q Max -18.47 -6.48 -2.44 4.46 45.79

#### Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) -21.097 6.776 -3.11 0.0038 \*\* speed 3.971 0.418 9.49 5.9e-11 \*\*\*

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 12.9 on 33 degrees of freedom

Multiple R-squared: 0.732,

Adjusted R-squared: 0.724

F-statistic: 90.1 on 1 and 33 DF, p-value: 5.86e-11

==== ANOVA ====

Analysis of Variance Table

Response: dist

Df Sum Sq Mean Sq F value Pr(>F)
speed 1 14915 14915 90.1 5.9e-11 \*\*\*
Residuals 33 5462 166

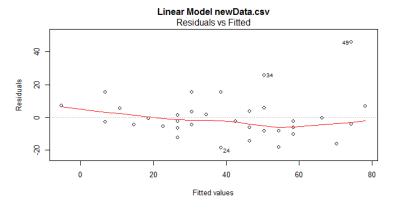
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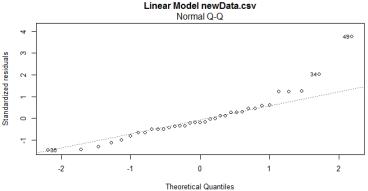
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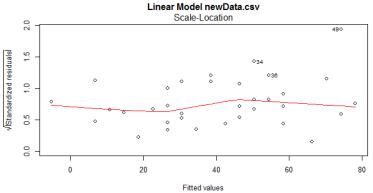
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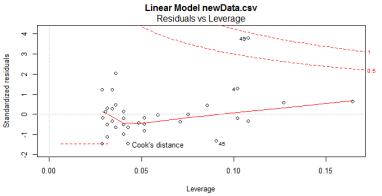
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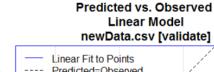
Rattle timestamp: 2018-02-01 01:20:26 admin

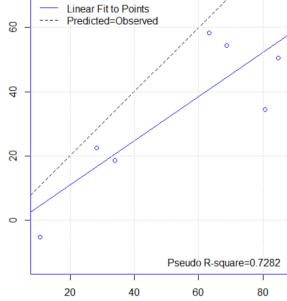












# Sqrt(dist)~speed

Summary of the Linear Regression model (built using lm):

#### Residuals:

Min 1Q Median 3Q Max -1.409 -0.597 -0.106 0.499 2.034

#### Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) 0.8150 0.4816 1.69 0.1 speed 0.3377 0.0297 11.36 6.1e-13 \*\*\*

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.914 on 33 degrees of freedom Multiple R-squared: 0.796, Adjusted R-squared: 0.79

F-statistic: 129 on 1 and 33 DF, p-value: 6.05e-13

==== ANOVA ====

Analysis of Variance Table

Response: sqrtDist

Residuals 33 27.6 0.8

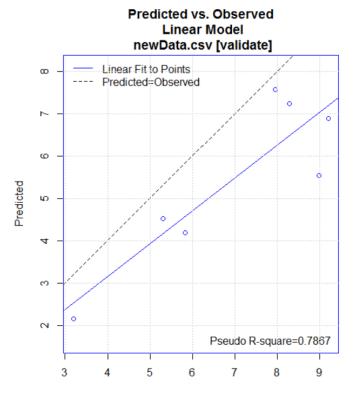
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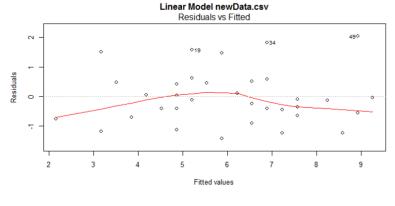
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

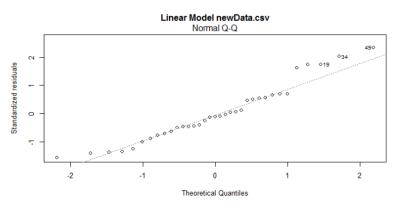
[1] "\n"

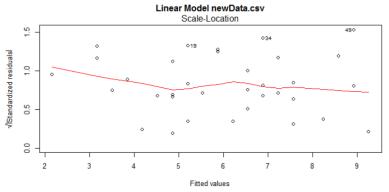
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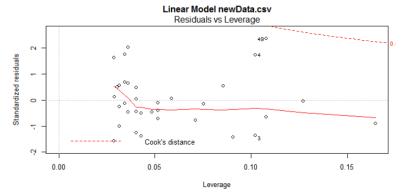
Rattle timestamp: 2018-02-01 00:51:46 admin











# log(dist)~log(speed)

Summary of the Linear Regression model (built using lm): Residuals:

Min 1Q Median 3Q Max -0.748 -0.167 -0.034 0.194 0.957

#### Coefficients:

logSpeed 1.833 0.148 12.35 6.4e-14 \*\*\*

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.351 on 33 degrees of freedom

Multiple R-squared: 0.822, Adjusted R-squared: 0.817

F-statistic: 152 on 1 and 33 DF, p-value: 6.44e-14

==== ANOVA ====

#### Analysis of Variance Table

Response: logDist

Df Sum Sq Mean Sq F value Pr(>F)

logSpeed 1 18.74 18.74 152 6.4e-14 \*\*\*

Residuals 33 4.06 0.12

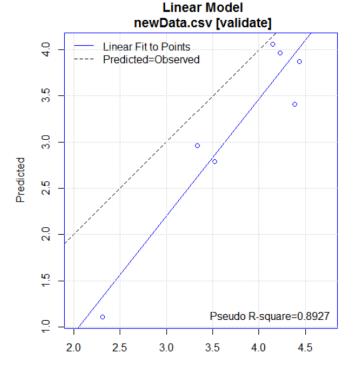
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

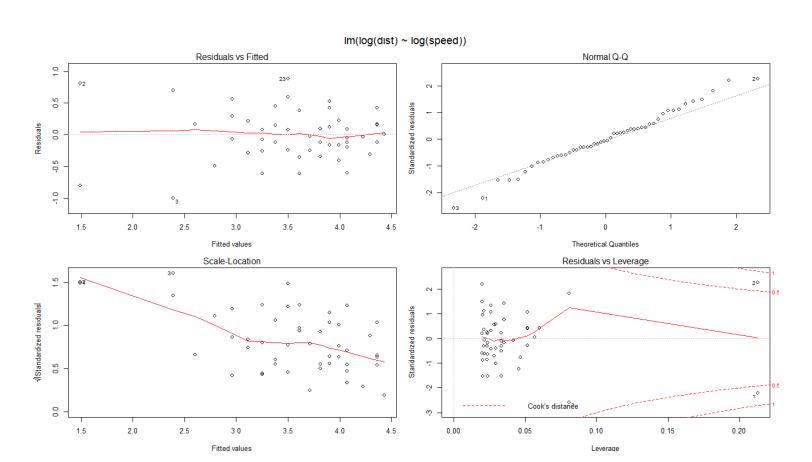
[1] "\n"

Time taken: 0.02 secs

Izvor: https://stat.ethz.ch/R-manual/R-devel/library/datasets/html/cars.html



Predicted vs. Observed



### dist~speed^2

Summary of the Linear Regression model (built using lm): Residuals:

Min 1Q Median 3Q Max -20.48 -6.44 -1.96 5.56 39.41

#### Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) 5.714 4.001 1.43 0.16 powSpeed 0.130 0.013 10.00 1.6e-11 \*\*\*

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 12.4 on 33 degrees of freedom Multiple R-squared: 0.752, Adjusted R-squared: 0.744

F-statistic: 100 on 1 and 33 DF, p-value: 1.61e-11

#### ==== ANOVA ====

Analysis of Variance Table

Response: dist

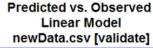
Df Sum Sq Mean Sq F value Pr(>F)
powSpeed 1 15323 15323 100 1.6e-11 \*\*\*
Residuals 33 5054 153

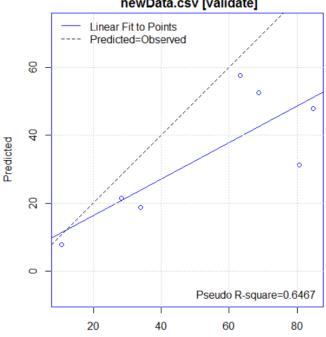
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

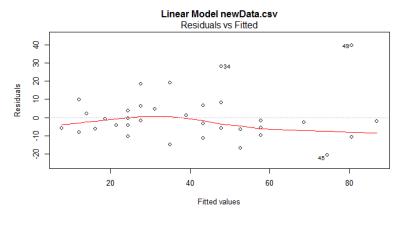
[1] "\n"

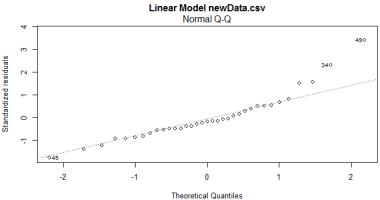
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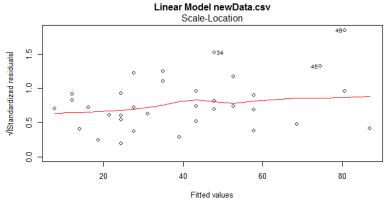
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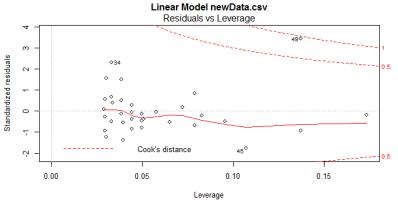








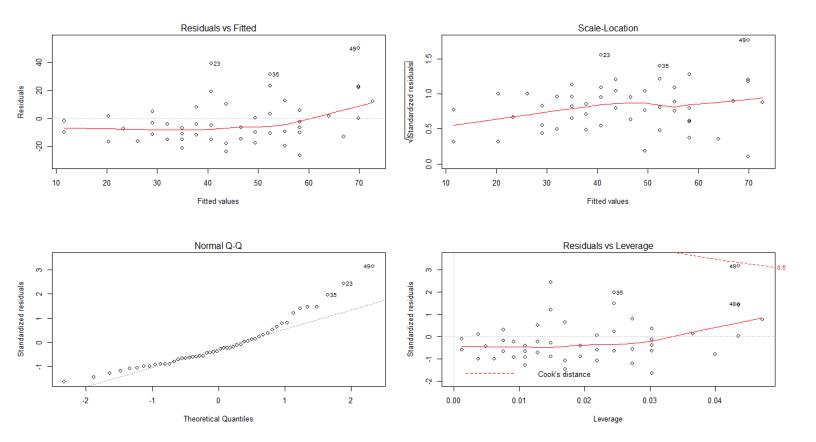




# Razvoj modela linearne regresije u programskom okruženju R

R sintaksa	Model	Komentar
Y ~ A	$Y = \beta_0 + \beta_1 \cdot A$	
Y ~ -1 + A	$Y = \beta_1 \cdot A$	
Y ~ A + I(A^2)	$Y = \beta_0 + \beta_1 \cdot A + \beta_2 \cdot A^2$	

```
> y = lm(formula = dist ~ (-1+speed), data=cars)
    summary(y)
lm(formula = dist \sim (-1 + speed), data = cars)
Residuals:
   Min
           1Q Median
                          30
-26.18 -12.64 -5.46
                        4.59
                               50.18
Coefficients:
      Estimate Std. Error t value Pr(>|t|)
                                    <2e-16 ***
speed
         2.909
                     0.141
                               20.6
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 16.3 on 49 degrees of freedom
Multiple R-squared: 0.896, Adjusted R-squared: 0.894 F-statistic: 423 on 1 and 49 DF, p-value: <2e-16
    anova(y)
Analysis of Variance Table
Response: dist
          Df Sum Sq Mean Sq F value Pr(>F)
           1 111949
                     111949
                                 423 <2e-16 ***
Residuals 49 12954
                         264
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```



```
> summary(y)
        call:
        lm(formula = dist \sim (1 + speed), data = cars)
        Residuals:
                      1Q Median
           Min
                                        3Q
        -29.07
                 -9.53 - 2.27
                                      9.21
                                             43.20
        Coefficients:
                       Estimate Std. Error t value Pr(>|t|)
                                                                0.012 *
        (Intercept)
                         -17.579
                                          6.758
                                                    -2.60
                                                     9.46 1.5e-12 ***
                           3.932
                                         0.416
        speed
        Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
        Residual standard error: 15.4 on 48 degrees of freedom
       Multiple R-squared: 0.651, Adjusted R-squared: 0.644 F-statistic: 89.6 on 1 and 48 DF, p-value: 1.49e-12
             anova(y)
        Analysis of Variance Table
        Response: dist
                     Df Sum Sq Mean Sq F value Pr(>F)
                      1 21185
                                    21185
                                                89.6 1.5e-12 ***
        Residuals 48 11354
                                       237
        Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
             layout(matrix(1:4,2,2))
             plot(y)
                       Residuals vs Fitted
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                                                                                                            0.10
                  -1
                            0
                                                                                           0.06
                       Theoretical Quantiles
                                                                                        Leverage
```

> y = lm(formula = dist ~ (1+speed), data=cars)

Standardized residuals

```
lm(formula = dist \sim (speed + speed^2), data = cars)
           Residuals:
                         1Q Median
              Min
                                           3Q
           -29.07
                    -9.53
                             -2.27
                                        9.21
                                                43.20
           Coefficients:
                          Estimate Std. Error t value Pr(>|t|)
                                                                  0.012 *
           (Intercept)
                            -17.579
                                            6.758
                                                       -2.60
                                                        9.46 1.5e-12 ***
                              3.932
                                            0.416
           speed
           Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
           Residual standard error: 15.4 on 48 degrees of freedom
          Multiple R-squared: 0.651, Adjusted R-squared: 0.644 F-statistic: 89.6 on 1 and 48 DF, p-value: 1.49e-12
                anova(y)
           Analysis of Variance Table
           Response: dist
                       Df Sum Sq Mean Sq F value Pr(>F)
                         1 21185
                                       21185
                                                   89.6 1.5e-12 ***
           Residuals 48 11354
                                          237
           Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
                layout(matrix(1:4,2,2))
                plot(y)
                          Residuals vs Fitted
                                                                                            Scale-Location
                                                                                               023
                                                      490
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                                                               Standardized residuals
   8
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                             Fitted values
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                             Normal Q-Q
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Standardized residuals
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                                                                                        0.04
                                                                                                         0.08
                                                                                                                  0.10
                                                                                                0.06
                           Theoretical Quantiles
                                                                                              Leverage
```

> y = lm(formula = dist ~ (speed+speed^2), data=cars)

> summary(y)

call:

```
set.seed(100)
trainingRowIndex = sample(1:nrow(cars), 0.8*nrow(cars))
trainingdata = cars[trainingRowIndex,]
testData = cars[-trainingRowIndex, ]
> y = lm(formula = dist ~ (-1+speed), data=trainingdata)
> summary(y)
call:
lm(formula = dist \sim (-1 + speed), data = trainingdata)
Residuals:
             1Q Median
   Min
                              3Q
-25.09 -15.37
                 -7.07
                            4.68
                                   47.85
Coefficients:
       Estimate Std. Error t value Pr(>|t|)
                                           <2e-16 ***
speed
           3.006
                        0.166
                                   18.1
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 17.2 on 39 degrees of freedom
Multiple R-squared: 0.894,
                                    Adjusted R-squared:
F-statistic: 330 on 1 and 39 DF, p-value: <2e-16
> anova(y)
Analysis of Variance Table
Response: dist
            Df Sum Sq Mean Sq F value Pr(>F)
                                      330 <2e-16 ***
                97524
                          97524
                11543
Residuals 39
                             296
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
  \bar{1}ayout(matrix(1:4,2,2))
    plot(y)
dobar na train podacima
             Residuals vs Fitted
                                                                          Scale-Location
                 023
                                               (Standardized residuals
                                                  0.
                                                  0.5
        30
               40
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                Fitted values
                                                                           Fitted values
               Normal Q-Q
                                                                       Residuals vs Leverage
                                                Standardized residuals
                                                                               ♦35
                                                  0
                                                                       0
                                                                   Cook's distance
                                       2
                  0
                                                     0.00
                                                              0.01
                                                                      0.02
                                                                              0.03
                                                                                      0.04
                                                                                              0.05
```

Leverage

y = Im(formula = dist ~ (-1+speed), data=cars) dobar na cijeloj bazi ^^

4

2

0

2

Standardized residuals

0

Theoretical Quantiles

10