P2 4A => Having 2 numbers reprezented as lists, add them. [1, 2, 3, 4] + [2, 4, 6] = [1, 4, 8, 0]

Mathematical model reverseList(I1..In) =

```
{reverseList(I2..In) U I1
```

```
1 % append(L - list, E - elemnt
2
3 % reverseList(L - list, C - colector, R - reversed list)
4 % flow model (i, o), (i, i)
5 reverseList([], C, C).
6 reverseList([H|T], C, R):-
7 NewC = [H|C],
8 reverseList(T, NewC, R).
9
10 reverseListCaller(L, R):-
11 reverseList(L, [], R).
Singleton variables: [H]
```

```
≡ ?- reverseListCaller([1, 2, 3, 4], R).
```



Mathematical model adder(I1..In, k1..km, Carry) =

```
{(I1 + Carry) / 10 U adder(I2..In, [], (I1 + Carry) mod 10), if m = 0
```

```
\{(k1 + Carry) / 10 U \text{ adder}([], k2..kn, (k1 + Carry) \text{ mod } 10), \text{ if } n = 0\}
```

{(I1 + k1 + Carry) / 10 U adder(I2..ln, k2..km, (I1 + k1 + Carry) mod 10), otherwise

```
1 % adder(L1 - list 1, L2 - list 2, C - carry, R - resulted list
2 % flow model (i, i, i, o) (i, i, i, i)
3 adder([], [], 0, []).
4 adder([], [], C, [C]).
5 adder([H|T], [], C, R):-
6 NewC is (H + C) // 10,
7 %write('NewC = '), write(NewC), nl,
```

```
8
       adder(T, [], NewC, NewR),
 9
       NewH is (H + C) \mod 10,
       R = [NewH|NewR].
10
11 adder([], [H|T], C, R):-
       NewC is (H + C) // 10,
12
       %write('NewC = '), write(NewC), nl,
13
14
       adder([], T, NewC, NewR),
       NewH is (H + C) \mod 10,
15
       R = [NewH|NewR].
16
17 adder([H1|T1], [H2|T2], C, R):-
       NewC is (H1 + H2 + C) // 10,
18
       %write('NewC = '), write(NewC), nl,
19
       adder(T1, T2, NewC, NewR),
20
       NewH is (H1 + H2 + C) \mod 10,
21
       R = [NewH|NewR].
22
23
24 adderCaller(L1, L2, R):-
25
       reverseListCaller(L1, L1R),
       reverseListCaller(L2, L2R),
26
27
       adder(L1R, L2R, 0, NewR),
```

```
≡ ?- adderCaller([1, 2, 3, 4], [1, 2, 3], R).
```

```
≡ ?- N is 5 // 2.
```

2B => Define a predicate to produce a list of pairs (atom n) from an initial list of atoms. In this initial list atom has n occurrences. - 27 min

Mathematical model count occurrences(I1..In, E) =

```
{1 + count_occurrences(I2..ln, E), if I1 = E
```

{count_occurrences(I2..In, E), otherwise

```
1 % countE(L - list, E - element, C - contor)
2 % flow model (i, i, o, o) (i, i, i, i)
3 count_occurrences([], _, 0).

▼
```

```
4 count_occurrences([H|T], E, C):-
5
      H = := E,
      count_occurrences(T, E, NewC),
6
      C is NewC + 1, !.
7
8 count_occurrences([_|T], E, C):-
      count_occurrences(T, E, C).
```

```
\equiv ?- countE([1, 2, 1, 3, 4, 1, 1, 1, 2], 1, C).
```

Mathematical model removeE(I1..In, E) =

```
{I1 U removeE(I2..In, E), if I1 =/= E
```

```
{removeE(I2..In, E), otherwise
```

```
1 % removeE(L - list, E - element, R - resulted list)
2 % flow model
3 removeE([], _, []).
4 removeE([E|T], E, R):- % if the head and the element are equal
5
      removeE(T, E, R).
6 removeE([H|T], E, R):-
      removeE(T, E, NewR),
7
      R = [H|NewR].
8
```

```
\blacksquare ?- removeE([1, 2, 3, 1, 2, 3, 1], 1, R).
```



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```
1 % frequency(L - list, R - resulted list)
2 % flow model (i, o), (i, i)
3 frequency([], []).
4 frequency([H|T], R):-
5
      count_occurrences([H|T], H, C),
6
      removeE([H|T], H, NewList),
7
      frequency(NewList, NewR),
8
      Pair = [H,C],
9
      R = [Pair|NewR].
```

```
\blacksquare ?- frequency([1, 2, 3, 1, 2, 4, 5, 1], R).
```



P2 7A=> Display the indexes of the occurences of the maximum element - 30 min

Mathematical model findMax(I1..In, M) =

```
{M = I1 & findMax(I2..In, M), if I1 > M
```

{findMax(I2..In, M), otherwise

```
1 % findMax(L - list, M - temporary Maximum)
 2 % flow model (i, o), (i, i)
 3 findMax([], M, M). % if the list is empty simply
 4 findMax([H|T], M, R):-
 5
       H > M
 6
       NewM is H,
 7
       %write(NewM), nl,
       findMax(T, NewM, R), !.
 9 findMax([_|T], M, R):-
10
       findMax(T, M, R).
11 findMaxCaller([H|T], R):-
12
       findMax(T, H, R).
```

```
≡ ?- findMaxCaller([1, 2, 3, 20, 4, 5, 10], M).
```

Mathematical model indexesOfElem(I1..In, I, E) =

```
{I U indexesOfElem(I2..In, I + 1, E), if I1 = E
```

{indexesOfElem(I2..In, I + 1, E), otherwise

```
1 % indexesOfElem(L - list, I - index, E - element, R - list of indexes)
2 % flow model (i, i, i, o)
3 indexesOfElem([], _, _, []).
4 indexesOfElem([E|T], I, E, R):- % the head is equal to the element
NewI is I + 1,
```

```
indexesOfElem(T, NewI, E, NewR),
R = [I|NewR], !.
indexesOfElem([_|T], I, E, R):- % the head is not equal to the element
NewI is I + 1,
indexesOfElem(T, NewI, E, R).
indexesOfElemCaller(L, E, R):-
indexesOfElem(L, 1, E, R).
```

Mathematical model indexMaxElem(I1..In) = indexesOfElem(I1..In, findMaxCaller(I1..In))

```
1 % indexMaxElem(L - list, R - resulted list)
2 % flow model (i, o), (i, i)
3 indexMaxElem(L, R):-
4  findMaxCaller(L, Max),
5  indexesOfElemCaller(L, Max, R).
```

```
≡ ?- indexMaxElem([1, 2, 5, 3, 5, 5], R).
```

P2 5A => Substitute all the occurrences of an element in the first list with all the elements in the other list L1 = [1, 2, 1], nr = 1, L2 = [8, 9] => R = [8, 9, 2, 8, 9] - 30 min

Mathematical Model appendList(I1..In, k1..km) =

```
{ k1..km, if n = 0
```

{ I1 U appendList(I2..In, k1..km), otherwise

```
1 % appendList(L1 - first list, L2 - second list, R - resulted list)
2 % flow model (i, i, o), (i, i, i)
3 appendList([], L, L).
4 appendList([H|T], L, R):-
5     appendList(T, L, NewR),
```

```
R = [H|NewR].
    6
                                                                                          ℱ ▶
\equiv ?- appendList([1, 2, 3], [4, 5, 6], R).
                     Create a
                               Program Query Markdown HTML
                                                                 cell here
Mathematical Model subEList(I1..In, E, k1..km) =
   \{ k1..km U subEList(12..ln, E, k1..km), if I1 = E \}
   { I1 U subEList(I2..ln, E, k1..km), otherwise
    1 % substitutes every element E with the second list
    2 % subEList(L1 - first list, E - element, L2 - second list, R - resulted list/ co
    3 % flow model (i, i, i, o), (i, i, i, i)
    4 subEList([], _, _, R, R).
    5 subEList([Elem|T], Elem, L2, R, FR):- % when the head is equal with Element
          appendList(R, L2, NewR),
    7
          % write(NewR), nl,
          subEList(T, Elem, L2, NewR, FR), !.
    9 subEList([H|T], Elem, L2, R, FR):-
   10
          appendList(R, [H], NewR),
          subEList(T, Elem, L2, NewR, FR), !.
   11
   12
   13 subEListCaller(L1, E, L2, R):-
          subEList(L1, E, L2, [], R).
   14
                                                                                          ℱ ▶
\equiv ?- subEListCaller([1, 2, 1], 1, [8, 9], R).
### 15A => Transform a list in a set keeping the first appearance of the elements [1, 2, 2]
3, 2, 1 -> [1, 2, 3]
Empty markdown cell. Double click to edit
    1 % toSet(L - list, R - resulted list
    2 % flow model
    3 toSet([], []).
    4 toSet([H|T], R):-
    5
          removeE(T, H, NewL),
          toSet(NewL, NewR),
    6
    7
          R = [H|NewR], !.
```

= ?-

```
toSet([1, 2, 3, 2, 1], R).

R = [1, 2, 3]
```

13A => Transform a list in a set keeping the last appearance of the elements [1, 2, 3, 2, 1] -> [3, 2, 1]

```
1 % toSetLast(L - list, R - resulted list)
   2 % flow model (i, o), (i, i)
   3 toSetLast([], []).
   4 toSetLast([H|T], R):-
          count_occurrences(T, H, C),
   6
          C =:= 0, % if there are not any duplicates of this number
   7
          toSetLast(T, NewR),
          R = [H|NewR], !.
   9 toSetLast([_|T], R):-
  10
          toSetLast(T, R).
                                                                                            F
\equiv ?- toSetLast([1, 2, 3, 2, 1], R).
\mathbf{R} = [3, 2, 1]
```

3A => Define a predicate to remove from a list all repetitive elements.





removeDuplicates([1,2,1,4,1,3,4], R).

R = [2, 3]