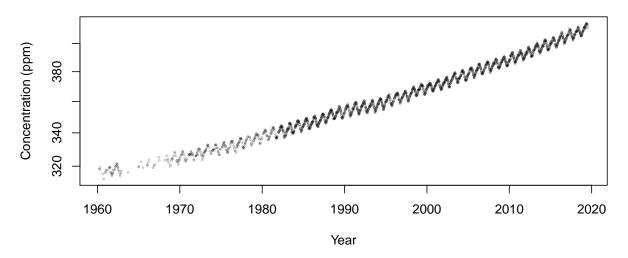
# Longitudinal Climate Change Analysis

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### Introduction

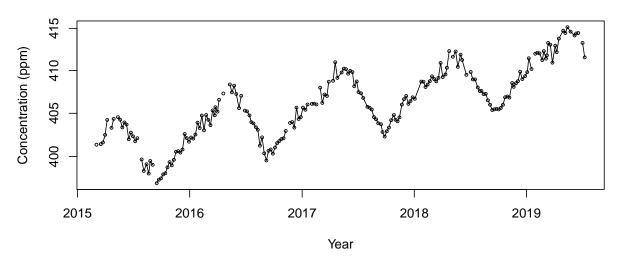
The Mauna Lao Observatory in Hawaii has been observing atmospheric carbon dioxide concentrations since the year 1960 to present day. This report will observe whether major world events have impacted the carbon dioxide concentrations in the world's atmosphere. The world events being: the OPEC oil embargo which began in October 1973, the global economic recessions around 1980-1982, the fall of the Berlin wall almost exactly 30 years ago, preceding a dramatic fall in industrial production in the Soviet Union and Eastern Europe, China joining the WTO on 11 December 2001, which was followed by rapid growth in industrial production, the bankruptcy of Lehman Brothers on 15 September 2008, regarded as the symbolic start of the most recent global financial crisis, and the signing of the Paris Agreement on 12 December 2015, intended to limit CO2 emissions.

# CO2 Concentration in Earth's Atmosphere 1960 – 2019



The Mauna Lao Observatory in Hawaii has been observing atmospheric carbon dioxide concentrations since the year 1960. Many of the early observations taken were low quality measurements. Low quality measurements have been removed in this report. Even with the removal of low quality measurements there is a clear upward trend in carbon dioxide concentrations.

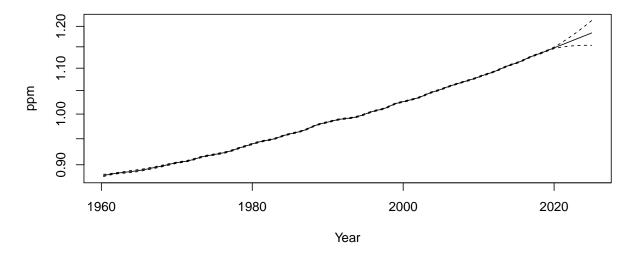
### **Recent Observations of CO2 Concentration in Earth's Atmosphere**



### Methods

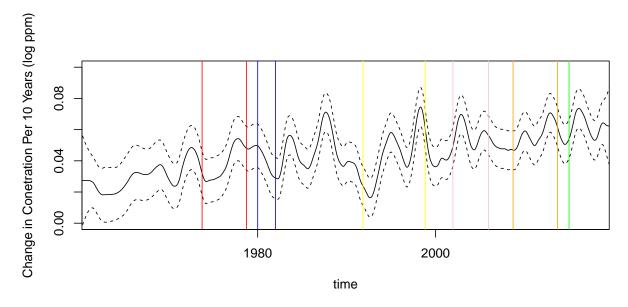
To model the observed data periodic annual and biannual effects have been used to account for seasonal effects on carbon dioxide concentrations. A gamma linear model was used to observe the trend of carbon dioxide concentrations  $log(CO2) = \beta_1 sin(2\pi * year) + \beta_2 cos(2\pi * year) + \beta_3 sin(4\pi * year) + \beta_4 cos(4\pi * year) + U(day) + V_i$  where  $\beta_1$  and  $\beta_2$  are annual temperature effects,  $\beta_3$  and  $\beta_4$  are biannual temperature effects, U(day) represents a second-order random walk. The prior chosen for the stardard deviation of the random walk is  $P(\sigma < \frac{log(1.01)}{26}) = 0.5$  with a prior on the variance of  $P(\sigma < 2) = 0.5$ 

### Plot of the Time Random Effect



The rate of change of carbon dioxide concentrations is modelled by predicting the derivative of the fitted model. The figures below show prediction of the monthly and overall rate of change of carbon dioxide concentrations. Major world events are highlighted at 5 year intervals after their occurance. The red interval highlights the OPEC oil embargo which began in October 1973, blue

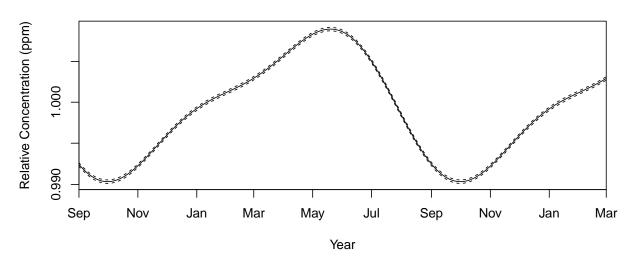
interval highlights the global economic recessions around 1980-1982, yellow interval highlights the fall of the Berlin wall, pink interval highlights China joining the WTO, Orange interval highlights the bankruptcy of Lehman Brothers, the symbolic start of the most recent global financial crisis, and the green line marks the signing of the Paris Agreement intended to limit CO2 emissions.



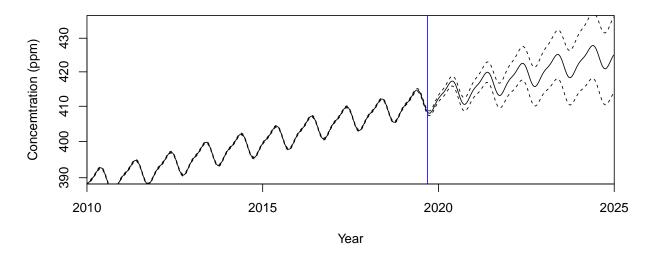
The world events that have impacted the rate of carbon dioxide emissions are: the OPEC oil embargo which began in October 1973 where the rate of emissions saw a considerable increase in emissions, the global economic recessions around 1980-1982 where the rate of emissions saw a large decrease in the two year period, and the largest change in emissions seen in the five years after the fall of the berlin wall, though the fall of the Berlin wall was the begining of the a dramatic fall in industrial production in the Soviet Union and Eastern Europe global carbon dioxide emission rates grew at an all time high. The five years following the events of China joining the WTO and the bankruptcy of Lehman Brothers saw no considerable difference in the rate of emmissions. The Paris Agreement intended to limit CO2 emissions has shown some visual decrease in emmissions.

The figures below show seasonal and future predicted carbon dioxide concentrations given by the fitted model.

# **Seasonal CO2 Concentration**



# **Plot of Fitted Predicitons**



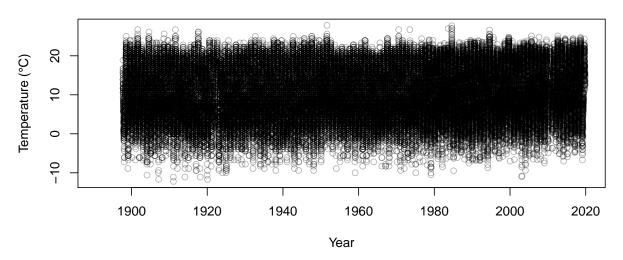
### Introduction

The IPCC states that Human activities are estimated to have caused approximately  $1.0\text{Å}^{\circ}\text{C}$  of global warming above preindustrial levels, with a likely range of  $0.8\text{Å}^{\circ}\text{C}$  to  $1.2\text{Å}^{\circ}\text{C}$ . Global warming is likely to reach  $1.5\text{Å}^{\circ}\text{C}$  between 2030 and 2052 if it continues to increase at the current rate. (high confidence)

There have been recent arguements made against the existance of climate change and its impacts. This report will examine data recorded on Sable Island, off the coast of Nova Scotia to determine whether there is evidence to show a change in global temperature.

Examining the scatterplot of the complete record of Sable Island temperature records shown below initially shows no relationship.

### **Scatter Plot of Sable Island Temperature Recordings**



When examining the maximum temperatures recorded in the past five years we can visually see that there is a upward trend in summer peak temperatures. We will consider only summer temperatures when modelling historical temperature since winter temperatures are governed by a different and much more complex physical process.

### Method

To model the Sable Island temperature data the model  $Temperature = \beta_0 + \beta_1 sin(\frac{2\pi day}{365.25}) + \beta_2 cos(\frac{2\pi day}{365.25}) + \beta_3 sin(\frac{4\pi day}{365.25}) + \beta_4 cos(\frac{4\pi day}{365.25}) + U(week) + V(week) + W(year)$  was chosen where  $\beta_1$  and  $\beta_2$  are annual temperature effects,  $\beta_3$  and  $\beta_4$  are biannual temperature effects, U(week) is a second-order random walk for week, V(week) is the random effect for week, and W(year) is the random effect for year.

The prior chosen for the standard deviation of the second-order random walk is  $P(\sigma < \frac{0.1}{52*100}) = 0.05$ , the prior for the standard deviation of the random intercept for week is  $P(\sigma < 1) = 0.5$ , the prior chosen for the standard deviation of the random intercept for year is  $P(\sigma < 1) = 0.5$ .

	0.5quant	0.025quant	0.975quant
sin12	-4.676	-5.192	-4.161
$\cos 12$	4.763	4.473	5.052
$\sin 6$	-2.049	-2.272	-1.826
$\cos 6$	-0.152	-0.324	0.019

# Scatter Plot of Sable Island Temperature Recordings (2016–2019)

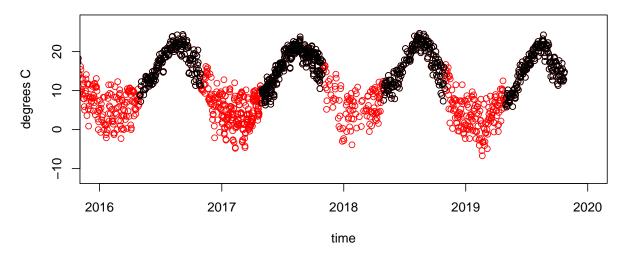


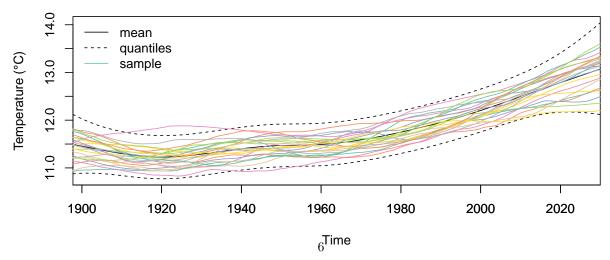
Figure 1: Summer months are shown in black

	mean	0.025quant	0.975quant
sd for t	1.770	1.749	1.793
sd for week	0.000	0.000	0.000
sd for weekIid	1.092	1.057	1.132
sd for yearFac	0.706	0.610	0.833

There was very little deviation in the second-order random walk with a standard deviation of 0.000017694 between weeks with a 95% confidence interval  $(1.231*10^{-5}, 2.388*10^{-5})$ , the standard deviation in the random intercepts for week is 1.092 from the mean with a 95% confidence interval (1.056, 1.132), the standard deviation in the random intercepts for year is 0.707 with a 95% confidence interval (0.6104, 0.8328).

The figure below shows a plot of 24 posterior samples. The samples show an upwards trend in temperature. The dotted lines represent the 95% confidence interval of the mean of the trend. With future predictions of 1.5 degree increase since the year 1900.





# Conclusion

In conclusion data supports evidence to show that there is an increase in global temperatures coinciding with IPCC reports of 1.0 degree of global warming above preindustrial levels, with a likely range of 0.8 degrees to 1.2 degrees. Future predictions of 1.5 degree increase in temperature coincide with the predictions made using the Sable Island data.