1 Introduction

2 Some basic knowledge about researching problem...

Parameters and constants we use in this work:

Constants (3):

e = 2.718282

pi = 3.141593

AbObA = 1337.228690

Variables (2):

x = 1.000000

opa = 13.000000

Parameters of exploration :

Number of differentiates : 3

Macloren's accuracy : 3

Tanget point : 0.200000

Delta coverage of tangent point: 2.500000

Graph diapasone : $[-1 : 15]$

So let's calculate smth with a given function: $f(x, opa) = \ln(1.000 + x \cdot opa)$

Firstly, let's simplify this expression (if possible): $f(x, opa) = \ln(1.000 + x \cdot opa)$

3 Exploration of the expression as a function of multiple variables

Calculation value of function in the point   BRITISH SCIENTISTS WERE SHOCKED, WHEN THEY COUNT IT!!!

In the point $M_0(x_0, opa_0) = (1.000, 13.000)$ **it's value** = 2.63906

Personally, I've always thought about first derivation of something like that function... Haven't you?

But now, by using informatics and math skills I feel that I'm prepared enough to calculate it!

1 step: Finding a derivation of opa

When I was child, my father always told me: "Remember, son:

$(opa)' = ... = $ [top secret] $= ... =$

$= 1.000$

2 step: Finding a derivation of x

thanks to the results of my colleagues' scientific work, I know that:

$(x)' = ... = $ [top secret] $= ... =$

$= 1.000$

3 step: Finding a derivation of $x \cdot opa$

What if:

$(x \cdot opa)' = ... = $ [top secret] $= ... =$

$= opa + x$

4 step: Finding a derivation of 1.000

If someone asked me that in the middle of the night, I wouldn't hesitate to say:

$(1.000)' = ... = $ [top secret] $= ... =$

$= 0.000$

5 step: Finding a derivation of $1.000 + x \cdot opa$

It's really easy to find:

$(1.000 + x \cdot opa)' = ... = $ [top secret] $= ... =$

$= opa + x$

6 step: Finding a derivation of $\ln(1.000 + x \cdot opa)$

My friends always beat me, because I didn't know that:

$(\ln(1.000 + x \cdot opa))' = ... = $ [top secret] $= ... =$

$= \frac{1.000}{1.000 + x \cdot opa} \cdot (opa + x)$

Congratulations! **The first derivation of the expression** is:

$f'(x, opa) = \frac{1.000}{1.000 + x \cdot opa} \cdot (opa + x)$

In the point $M_0(x_0, opa_0) = (1.000, 13.000)$ it's value = 1.00000

Finding the 3 derivation   Let's find **the 1 derivation** of the expression:

1 step: Finding a derivation of opa

Sounds logical that it is the same as:

$(opa)' = ... = $ [top secret] $= ... =$

$= 1.000$

2 step: Finding a derivation of x

My roommate mumbled it in his sleep all night:

$(x)' = ... = $ [top secret] $= ... =$

$= 1.000$

3 step: Finding a derivation of $x \cdot opa$

What if:

$(x \cdot opa)' = ... = $ [top secret] $= ... =$

$= opa + x$

4 step: Finding a derivation of 1.000

While preparing for exams, I learned a lot of new things, for example:

$(1.000)' = ... = $ [top secret] $= ... =$

$= 0.000$

5 step: Finding a derivation of $1.000 + x \cdot opa$

Sounds logical that it is the same as:

$(1.000 + x \cdot opa)' = ... = $ [top secret] $= ... =$

$= opa + x$

6 step: Finding a derivation of $\ln(1.000 + x \cdot opa)$

I was asked not to tell anyone that:

$(\ln(1.000 + x \cdot opa))' = ... = $ [top secret] $= ... =$

$= \frac{1.000}{1.000 + x \cdot opa} \cdot (opa + x)$

Let's find **the 2 derivation** of the expression:

1 step: Finding a derivation of x

Even my two-aged sister knows that:

$(x)' = ... = $ [top secret] $= ... =$

$= 1.000$

2 step: Finding a derivation of opa

I was asked not to tell anyone that:

$(opa)' = ... = $ [top secret] $= ... =$

$= 1.000$

3 step: Finding a derivation of $opa + x$

If someone asked me that in the middle of the night, I wouldn't hesitate to say:

$(opa + x)' = ... = $ [top secret] $= ... =$

$= 2.000$

4 step: Finding a derivation of opa

thanks to the results of my colleagues' scientific work, I know that:

$(opa)' = ... = $ [top secret] $= ... =$

$= 1.000$

5 step: Finding a derivation of x

My roommate mumbled it in his sleep all night:

$(x)' = ... = $ [top secret] $= ... =$

$= 1.000$

6 step: Finding a derivation of $x \cdot opa$

Even my two-aged sister knows that:

$(x \cdot opa)' = ... = $ [top secret] $= ... =$

$= opa + x$

7 step: Finding a derivation of 1.000

Man... Just look:

$(1.000)' = ... = $ [top secret] $= ... =$

$= 0.000$

8 step: Finding a derivation of $1.000 + x \cdot opa$

For centuries, people have hunted for the secret knowledge that:

$(1.000 + x \cdot opa)' = ... = $ [top secret] $= ... =$

$= opa + x$

9 step: Finding a derivation of 1.000

I was asked not to tell anyone that:

$(1.000)' = ... = $ [top secret] $= ... =$

$= 0.000$

10 step: Finding a derivation of $\frac{1.000}{1.000 + x \cdot opa}$

For centuries, people have hunted for the secret knowledge that:

$(\frac{1.000}{1.000 + x \cdot opa})' = ... = $ [top secret] $= ... =$

$= \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$

11 step: Finding a derivation of $\frac{1.000}{1.000 + x \cdot opa} \cdot (opa + x)$

When I was child, my father always told me: "Remember, son:

$(\frac{1.000}{1.000 + x \cdot opa} \cdot (opa + x))' = ... = $ [top secret] $= ... =$

$= \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} \cdot (opa + x) + 2.000 \cdot \frac{1.000}{1.000 + x \cdot opa}$

Let's find **the 3 derivation** of the expression:

1 step: Finding a derivation of opa

While preparing for exams, I learned a lot of new things, for example:

$(opa)' = ... = $ [top secret] $= ... =$

$= 1.000$

2 step: Finding a derivation of x

thanks to the results of my colleagues' scientific work, I know that:
$(x)' = ... = $ [top secret] $ = ... =$
$= 1.000$

3 step: Finding a derivation of $x \cdot opa$
Sounds logical that it is the same as:
$(x \cdot opa)' = ... = $ [top secret] $ = ... =$
$= opa + x$

4 step: Finding a derivation of 1.000
A true prince must know that:
$(1.000)' = ... = $ [top secret] $ = ... =$
$= 0.000$

5 step: Finding a derivation of $1.000 + x \cdot opa$
If someone asked me that in the middle of the night, I wouldn't hesitate to say:
$(1.000 + x \cdot opa)' = ... = $ [top secret] $ = ... =$
$= opa + x$

6 step: Finding a derivation of 1.000
If someone asked me that in the middle of the night, I wouldn't hesitate to say:
$(1.000)' = ... = $ [top secret] $ = ... =$
$= 0.000$

7 step: Finding a derivation of $\frac{1.000}{1.000 + x \cdot opa}$
My friends always beat me, because I didn't know that:
$(\frac{1.000}{1.000 + x \cdot opa})' = ... = $ [top secret] $ = ... =$
$= \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$

8 step: Finding a derivation of 2.000
What if:
$(2.000)' = ... = $ [top secret] $ = ... =$
$= 0.000$

9 step: Finding a derivation of $2.000 \cdot \frac{1.000}{1.000 + x \cdot opa}$
Sounds logical that it is the same as:
$(2.000 \cdot \frac{1.000}{1.000 + x \cdot opa})' = ... = $ [top secret] $ = ... =$
$= 2.000 \cdot \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$

10 step: Finding a derivation of x
thanks to the results of my colleagues' scientific work, I know that:
$(x)' = ... = $ [top secret] $ = ... =$
$= 1.000$

11 step: Finding a derivation of opa
Even my two-aged sister knows that:
$(opa)' = ... = $ [top secret] $ = ... =$
$= 1.000$

12 step: Finding a derivation of $opa + x$
While preparing for exams, I learned a lot of new things, for example:
$(opa + x)' = ... = $ [top secret] $ = ... =$
$= 2.000$

13 step: Finding a derivation of opa
When I was child, my father always told me: "Remember, son:
$(opa)' = ... = $ [top secret] $ = ... =$
$= 1.000$

14 step: Finding a derivation of x
It's really easy to find:
$(x)' = ... = $ [top secret] $ = ... =$
$= 1.000$

15 step: Finding a derivation of $x \cdot opa$
For centuries, people have hunted for the secret knowledge that:
$(x \cdot opa)' = ... = $ [top secret] $ = ... =$
$= opa + x$

16 step: Finding a derivation of 1.000
If someone asked me that in the middle of the night, I wouldn't hesitate to say:
$(1.000)' = ... = $ [top secret] $ = ... =$
$= 0.000$

17 step: Finding a derivation of $1.000 + x \cdot opa$
Sounds logical that it is the same as:
$(1.000 + x \cdot opa)' = ... = $ [top secret] $ = ... =$
$= opa + x$

18 step: Finding a derivation of $(1.000 + x \cdot opa)^{2.000}$
I spend the hole of my life to find the answer and finally it's:
$((1.000 + x \cdot opa)^{2.000})' = ... = $ [top secret] $ = ... =$
$= 2.000 \cdot (1.000 + x \cdot opa) \cdot (opa + x)$

19 step: Finding a derivation of x
While preparing for exams, I learned a lot of new things, for example:
$(x)' = ... = $ [top secret] $ = ... =$
$= 1.000$

20 step: Finding a derivation of opa
I spend the hole of my life to find the answer and finally it's:
$(opa)' = ... = $ [top secret] $ = ... =$
$= 1.000$

21 step: Finding a derivation of $opa + x$
When I was child, my father always told me: "Remember, son:
$(opa + x)' = ... = $ [top secret] $ = ... =$
$= 2.000$

22 step: Finding a derivation of -1.000
For centuries, people have hunted for the secret knowledge that:
$(-1.000)' = ... = $ [top secret] $ = ... =$
$= 0.000$

23 step: Finding a derivation of $(-1.000) \cdot (opa + x)$
What if:
$((-1.000) \cdot (opa + x))' = ... = $ [top secret] $ = ... =$
$= -2.000$

24 step: Finding a derivation of $\frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$
A true prince must know that:
$(\frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}})' = ... = $ [top secret] $ = ... =$
$= \frac{(-2.000) \cdot (1.000 + x \cdot opa)^{2.000} - 2.000 \cdot (1.000 + x \cdot opa) \cdot (opa + x) \cdot (-1.000) \cdot (opa + x)}{((1.000 + x \cdot opa)^{2.000})^{2.000}}$

25 step: Finding a derivation of $\frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} \cdot (opa + x)$
Man... Just look:
$(\frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} \cdot (opa + x))' = ... = $ [top secret] $ = ... =$
$= \frac{(-2.000) \cdot (1.000 + x \cdot opa)^{2.000} - 2.000 \cdot (1.000 + x \cdot opa) \cdot (opa + x) \cdot (-1.000) \cdot (opa + x)}{((1.000 + x \cdot opa)^{2.000})^{2.000}} \cdot (opa + x) + 2.000 \cdot \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$

26 step: Finding a derivation of $\frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} \cdot (opa + x) + 2.000 \cdot \frac{1.000}{1.000 + x \cdot opa}$
I was asked not to tell anyone that:
$(\frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} \cdot (opa + x) + 2.000 \cdot \frac{1.000}{1.000 + x \cdot opa})' = ... = $ [top secret] $ = ... =$
$= \frac{(-2.000) \cdot (1.000 + x \cdot opa)^{2.000} - 2.000 \cdot (1.000 + x \cdot opa) \cdot (opa + x) \cdot (-1.000) \cdot (opa + x)}{((1.000 + x \cdot opa)^{2.000})^{2.000}} \cdot (opa + x) + 2.000 \cdot \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} + 2.000 \cdot \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$

Finally... The 3 derivation of the expression:
$f^{(3)}(x, opa) = \frac{(-2.000) \cdot (1.000 + x \cdot opa)^{2.000} - 2.000 \cdot (1.000 + x \cdot opa) \cdot (opa + x) \cdot (-1.000) \cdot (opa + x)}{((1.000 + x \cdot opa)^{2.000})^{2.000}} \cdot (opa + x) + 2.000 \cdot \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}} + 2.000 \cdot \frac{(-1.000) \cdot (opa + x)}{(1.000 + x \cdot opa)^{2.000}}$
BRITISH SCIENTISTS WERE SHOCKED AGAIN, WHEN THEY COUNT THE 3 DERIVATION OF THIS EXPRESSION!!!
In the point $M_0(x_0, opa_0) = (1.000, 13.000)$ it's value $= 1.57143$

Finding partical derivations Partial derivation of the expression on the variable x:
$\frac{\partial f}{\partial x} = 13.000 \cdot \frac{1.000}{1.000 + 13.000 \cdot x}$
In the point $M_0(x_0, opa_0) = (1.000, 13.000)$ it's value $= 0.92857$!!!
Partial derivation of the expression on the variable opa:
$\frac{\partial f}{\partial opa} = \frac{1.000}{1.000 + opa}$
In the point $M_0(x_0, opa_0) = (1.000, 13.000)$ it's value $= 0.07143$!!!

Finding full derivation Full derivation:
$\sqrt{(13.000 \cdot \frac{1.000}{1.000 + 13.000 \cdot x})^{2.000} + (\frac{1.000}{1.000 + opa})^{2.000}}$
In the point $M_0(x_0, opa_0) = (1.000, 13.000)$ it's value $= 0.93131$!!!

4 Exploration the expression as a function of the first variable

Now let's consider the expression as a function of x variable: $f(x) = \ln(1.000 + 13.000 \cdot x)$

Decomposing on Macloren's formula Maklorens formula for $x \to x_0 = 1.000$:
$f(x) = 2.639 + 0.929 \cdot (x - 1.000) + (-0.431) \cdot (x - 1.000)^{2.000} + 0.267 \cdot (x - 1.000)^{3.000} + o((x - 1.000)^{3.000})$

Graphics Graph $f(x) = \ln(1.000 + 13.000 \cdot x)$ on the diapasone $x \in [-1 : 15]$:
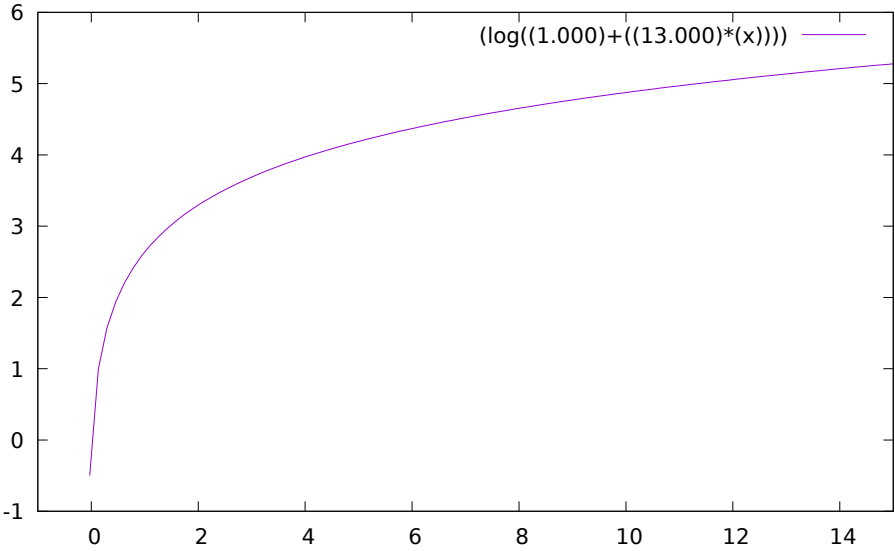
Equations in the point Tangent equation in the point $x_0 = 0.200$:
$f(x) = 3.611 \cdot (x - 0.200) + 1.281$
Normal equation in the point $x_0 = 0.200$:
$f(x) = (-0.277) \cdot (x - 0.200) + 1.281$
Their graphs in $\delta = 2.50000$ coverage of the point $x_0 = 0.200000$