Firstly, let's simplify this expression (if possible): $f(x) = \arcsin x$

2 Some basic knowledge about researching problem... Let's calculate smth with a given function: $f(x) = \arcsin x$ 3 Exploration of the expression Calculation value of function in the point BRITISH SCIENTISTS WERE SHOCKED, WHEN THEY COUNT IT!!! In the point $M_0(x_0) = (0.000)$ it's value = 0.00000 Personally, I've always thought about first derivation of something like that function... Haven't you? But now, by using informatics and math skills I feel that I'm prepared enough to calculate it! 1 step: Finding a derivation of x While preparing for exams, I learned a lot of new things, for example: $(x)' = \dots = [\text{top secret}] = \dots =$ = 1.0002 step: Finding a derivation of $\arcsin x$ It's really easy to find: $(\arcsin x)' = \dots = [\text{top secret}] = \dots =$ $=\frac{1.000}{\sqrt{1.000-x^{2.000}}}$ Congratulations! The first derivation of the expression is: $f'(x) = \frac{1.000}{\sqrt{1.000 - x^{2.000}}}$ In the point $M_0(x_0) = (0.000)$ it's value = 1.00000 Finding the 3 derivation Let's find the 1 derivation of the expression: 1 step: Finding a derivation of x My roommate mumbled it in his sleep all night: $(x)' = \dots = [\text{top secret}] = \dots =$ = 1.0002 step: Finding a derivation of $\arcsin x$ Sounds logical that it is the same as: $(\arcsin x)' = \dots = [\text{top secret}] = \dots =$ $= \frac{1.000}{\sqrt{1.000 - x^{2.000}}}$ Let's find the 2 derivation of the expression: 1 step: Finding a derivation of x For centuries, people have hunted for the secret knowledge that: $(x)' = \dots = [\text{top secret}] = \dots =$ = 1.0002 step: Finding a derivation of $x^{2.000}$ Sounds logical that it is the same as: $(x^{2.000})' = \dots = [\text{top secret}] = \dots =$ $= 2.000 \cdot x$ 3 step: Finding a derivation of 1.000 It's really easy to find: $(1.000)' = \dots = [\text{top secret}] = \dots =$ = 0.0004 step: Finding a derivation of $1.000 - x^{2.000}$ My roommate mumbled it in his sleep all night: $(1.000 - x^{2.000})' = \dots = [\text{top secret}] = \dots =$ $= (-1.000) \cdot 2.000 \cdot x$ 5 step: Finding a derivation of $\sqrt{1.000-x^{2.000}}$ What if: $(\sqrt{1.000 - x^{2.000}})' = \dots = [\text{top secret}] = \dots =$ $= \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x$ 6 step: Finding a derivation of 1.000 It's really easy to find: $(1.000)' = \dots = [\text{top secret}] = \dots =$ = 0.0007 step: Finding a derivation of $\frac{1.000}{\sqrt{1.000-x^{2.000}}}$ Even my two-aged sister knows that: $= \frac{\left(\frac{1.000}{\sqrt{1.000-x^{2.000}}}\right)' = \dots = [\text{top secret}] = \dots = }{\left(\frac{-1.000}{\sqrt{1.000-x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x}{\left(\sqrt{1.000-x^{2.000}}\right)^{2.000}}}$ Let's find the 3 derivation of the expression: 1 step: Finding a derivation of x When I was child, my father always told me: "Remember, son: $(x)' = \dots = [\text{top secret}] = \dots =$ = 1.0002 step: Finding a derivation of $x^{2.000}$ I spend the hole of my life to find the answer and finally it's: $(x^{2.000})' = \dots = [\text{top secret}] = \dots =$ $= 2.000 \cdot x$ 3 step: Finding a derivation of 1.000 Man... Just look: $(1.000)' = \dots = [\text{top secret}] = \dots =$ = 0.0004 step: Finding a derivation of $1.000 - x^{2.000}$ For centuries, people have hunted for the secret knowledge that: $(1.000 - x^{2.000})' = \dots = [\text{top secret}] = \dots =$

 $= (-1.000) \cdot 2.000 \cdot x$ 5 step: Finding a derivation of $\sqrt{1.000 - x^{2.000}}$ It's really easy to find: $(\sqrt{1.000 - x^{2.000}})' = \dots = [\text{top secret}] = \dots =$ $= \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x$ 6 step: Finding a derivation of $(\sqrt{1.000 - x^{2.000}})^{2.000}$ It's simple as fuck:

 $((\sqrt{1.000 - x^{2.000}})^{2.000})' = \dots = [\text{top secret}] = \dots = 2.000 \cdot \sqrt{1.000 - x^{2.000}} \cdot \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x$ 7 step: Finding a derivation of xthanks to the results of my colleagues' scientific work, I know that: $(x)' = \dots = [\text{top secret}] = \dots =$ = 1.0008 step: Finding a derivation of 2.000 When I was child, my father always told me: "Remember, son:

 $(2.000)' = \dots = [\text{top secret}] = \dots =$ = 0.0009 step: Finding a derivation of $2.000 \cdot x$ It's really easy to find: $(2.000 \cdot x)' = \dots = [\text{top secret}] = \dots =$ = 2.00010 step: Finding a derivation of -1.000I was asked not to tell anyone that:

 $(-1.000)' = \dots = [\text{top secret}] = \dots =$

 $(x)' = \dots = [\text{top secret}] = \dots =$

= 0.000

11 step: Finding a derivation of $(-1.000) \cdot 2.000 \cdot x$ For centuries, people have hunted for the secret knowledge that: $((-1.000) \cdot 2.000 \cdot x)' = \dots = [\text{top secret}] = \dots =$ = -2.00012 step: Finding a derivation of xMy roommate mumbled it in his sleep all night:

= 1.00013 step: Finding a derivation of $x^{2.000}$ What if: $(x^{2.000})' = \dots = [\text{top secret}] = \dots =$ $= 2.000 \cdot x$ 14 step: Finding a derivation of 1.000 Even my two-aged sister knows that: $(1.000)' = \dots = [\text{top secret}] = \dots =$

17 step: Finding a derivation of 0.500

= 0.00015 step: Finding a derivation of $1.000 - x^{2.000}$ I spend the hole of my life to find the answer and finally it's: $(1.000 - x^{2.000})' = \dots = [\text{top secret}] = \dots =$ $= (-1.000) \cdot 2.000 \cdot x$ 16 step: Finding a derivation of $\sqrt{1.000 - x^{2.000}}$ Even my two-aged sister knows that: $(\sqrt{1.000 - x^{2.000}})' = \dots = [\text{top secret}] = \dots = \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x$

While preparing for exams, I learned a lot of new things, for example: $(0.500)' = \dots = [\text{top secret}] = \dots =$ = 0.00018 step: Finding a derivation of $\frac{0.500}{\sqrt{1.000-x^{2.000}}}$ When I was child, my father always told me: "Remember, son: $\left(\frac{0.500}{\sqrt{1.000-x^{2.000}}}\right)' = \dots = [\text{top secret}] = \dots =$

 $\frac{(-1.000) \cdot 0.500 \cdot \frac{0.500}{\sqrt{1.000 - x^2.000}} \cdot (-1.000) \cdot 2.000 \cdot x}{(\sqrt{1.000 - x^2.000})^{2.000}}$ 19 step: Finding a derivation of $\frac{0.500}{\sqrt{1.000-x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x$ Sounds logical that it is the same as: $\left(\frac{0.500}{\sqrt{1.000-x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x\right)' = \dots = [\text{top secret}] = \dots =$ $\frac{(-1.000) \cdot 0.500 \cdot \frac{0.500}{\sqrt{1.000 - x^2.000}} \cdot (-1.000) \cdot 2.000 \cdot x}{(\sqrt{1.000 - x^2.000})^{2.000}} \cdot (-1.000) \cdot 2.000 \cdot x + (-2.000) \cdot \frac{0.500}{\sqrt{1.000 - x^2.000}}$ 20 step: Finding a derivation of -1.000

A true prince must know that: $(-1.000)' = \dots = [\text{top secret}] = \dots =$ = 0.00021 step: Finding a derivation of $(-1.000) \cdot \frac{0.500}{\sqrt{1.000-x^2.000}} \cdot (-1.000) \cdot 2.000 \cdot x$ My roommate mumbled it in his sleep all night:

 $((-1.000) \cdot \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x)' = \dots = [\text{top secret}] = \dots = \\ (-1.000) \cdot (\frac{(-1.000) \cdot 0.500 \cdot \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x}{(\sqrt{1.000 - x^{2.000}})^{2.000}} \cdot (-1.000) \cdot 2.000 \cdot x + (-2.000) \cdot \frac{0.500}{\sqrt{1.000 - x^{2.000}}})$

22 step: Finding a derivation of $\frac{(-1.000) \cdot \frac{0.500}{\sqrt{1.000 - x^2.000}} \cdot (-1.000) \cdot 2.000 \cdot x}{(\sqrt{1.000 - x^2.000})^{2.000}}$ My roommate mumbled it in his sleep all night: $\left(\frac{(-1.000) \cdot \frac{0.500}{\sqrt{1.000 - x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x}{(\sqrt{1.000 - x^{2.000}})^{2.000}}\right)' = \dots = [\text{top secret}] = \dots =$ $(-1.000) \cdot (\frac{(\sqrt{1.000-x^{2.000}})}{(\sqrt{1.000-x^{2.000}})^{2.000}} \cdot (-1.000) \cdot 2.000 \cdot x}{(\sqrt{1.000-x^{2.000}})^{2.000}} \cdot (-1.000) \cdot 2.000 \cdot x + (-2.000) \cdot \frac{0.500}{\sqrt{1.000-x^{2.000}}}) \cdot (\sqrt{1.000-x^{2.000}})^{2.000} - 2.000 \cdot \sqrt{1.000-x^{2.000}} \cdot \frac{0.500}{\sqrt{1.000-x^{2.000}}} \cdot (-1.000) \cdot 2.000 \cdot x \cdot (-1.000) \cdot 2.000 \cdot x} \cdot (-1.000) \cdot 2.000 \cdot x \cdot (-1.000) \cdot 2.000$

 $((\sqrt{1.000-x^{2.000}})^{2.000})^{2.000})$ Finally... The 3 derivation of the expression: $\underbrace{(-1.000)\cdot(\frac{(-1.000)\cdot0.500\cdot\frac{1}{\sqrt{1.000-x^2.000}}\cdot(-1.000)\cdot2.000\cdot x}{(\sqrt{1.000-x^2.000})^2.000}\cdot(-1.000)\cdot2.000\cdot x}_{(\sqrt{1.000-x^2.000})}\cdot(-1.000)\cdot2.000\cdot x + (-2.000)\cdot\frac{0.500}{\sqrt{1.000-x^2.000}})\cdot(\sqrt{1.000-x^2.000})^2.000} - 2.000\cdot\sqrt{1.000-x^2.000}\cdot(-1.000)\cdot2.000\cdot x \cdot (-1.000)\cdot2.000\cdot x}_{(\sqrt{1.000-x^2.000})}\cdot(-1.000)\cdot2.000\cdot x}_{(\sqrt{1.000-x^2.000})}\cdot(-1.000)\cdot2.000\cdot x}_{(\sqrt{1.000-x^2.000})}\cdot(-1.000)\cdot2.000\cdot x \cdot (-1.000)\cdot2.000\cdot x}_{(\sqrt{1.000-x^2.000})}\cdot(-1.000)\cdot2.000\cdot x}_{(\sqrt{1.000-x^2.000})}$

 $((\sqrt{1.000-x^{2.000}})^{2.000})^{2.000}$ BRITISH SCIENTISTS WERE SHOCKED AGAIN, WHEN THEY COUNT THE 3 DERIVATION OF THIS EXPRESSION!!! In the point $M_0(x_0) = (0.000)$ it's value = 1.00000

Finding partical derivations Partial derivation of the expression on the variable x:

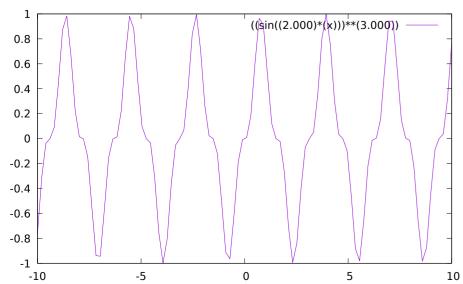
In the point $M_0(x_0) = (0.000)$ it's value = 1.00000 !!!

Finding full derivation Full derivation: $\sqrt{\left(\frac{1.000}{\sqrt{1.000 - x^{2.000}}}\right)^{2.000}}$

In the point $M_0(x_0) = (0.000)$ it's value = 1.00000 !!!

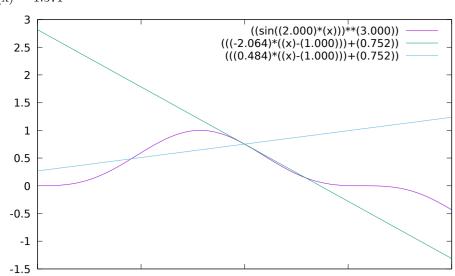
Decomposing on Macloren's formula Maklorens formula for $x \to x_0 = 0.000$: $f(x) = x + 0.167 \cdot x^{3.000} + 0.075 \cdot x^{5.000} + o(x^{6.000})$

Graphics Graph $f(x) = \arcsin x$ on the diapasone $x \in [-10:10]$:



Equations in the point Tangent equation in the point $x_0 = 1.000$: $f(x) = inf \cdot (x - 1.000) + 1.571$ Normal equation in the point $x_0 = 1.000$: f(x) = 1.571

0.5



1.5