# Wolfram Mathematica funkcijas

#### Saskaitīšana

In[1]:= 2 + 3

Out[1]= **5** 

## Atņemšana

In[2]:= **7 - 1** 

Out[2]= **6** 

#### Reizināšana

In[3]:= 2 \* 8

Out[3]= **16** 

In[4]:= **16** 

Out[4]= 16

In[5]:= 2 \* 4 \* 2

Out[5]= **16** 

 $In[6]:= 2 \times 3$ 

Out[6]= **6** 

 $In[7]:= 2 \times 8$ 

Out[7]= **16** 

In[8]:=  $2 \times 8 \times 2 \times 3 \times 4 \times 5 \times 6$ 

Out[8]= 11520

In[9]:= 211 313 414 × 31 414 141 222

 $\mathsf{Out}[9] = \ 6\,638\,229\,429\,498\,951\,908$ 

In[10]:=  $\pi \star e // N$ 

Out[10]= 8.53973

Dalīšana

ln[11]:= 6/3

Out[11]= **2** 

Out[12]= 
$$\frac{11}{2}$$

Out[13]= 
$$\frac{11}{2}$$

$$ln[14]:= 1/2 + 7/3$$

Out[14]= 
$$\frac{17}{6}$$

In[15]:= 
$$\pi$$
 / @

Out[15]= 
$$\frac{\pi}{}$$

$$ln[17] = (3 + 2) * 4$$

$$ln[18] = (18 - 15) * (11 + 2)^3 / 6$$

Out[18]= 
$$\frac{2197}{2}$$

## Decimāldaļas veidā

$$ln[21]:= 1/2 + 7/3 // N$$

$$ln[22]:= N[\pi/e, 100]$$

Out[22]= 1.15572734979092171791009318331269629912085102316441582049970653532728863184091693944018: 8434235673559

e skaitļa tuvinājums līdz 20 zīmēm aiz komata (dot rezultātu ar 20 ciparu precizitāti)

Out[23]= 2.71828182845904523536028747135266249775724709369995957496697

```
In[25]:= 2^64
Out[25]= 18 446 744 073 709 551 616
 In[26]:= 9.81<sup>36</sup>
Out[26]= 5.01284 \times 10^{35}
                                Skaitļa faktoriāls
 In[27]:= 10!
Out[27]= 3628800
  In[28]:= 60!
\mathsf{Out}_{128|=} \ 8\ 320\ 987\ 112\ 741\ 390\ 144\ 276\ 341\ 183\ 223\ 364\ 380\ 754\ 172\ 606\ 361\ 245\ 952\ 449\ 277\ 696\ 409\ 600\ 000\ 000\ 000\ \cdots
                                      000
                                Kvadrātsakne
 In[29]:= Sqrt[2]
Out[29]= \sqrt{2}
                                Konstantes
  In[30]:= E
Out[30]= @
 In[31]:= Pi
Out[31]= π
  In[32]:= Sqrt[2]
Out[32]= \sqrt{2}
  In[33]:= Sqrt[3]
Out[33]= \sqrt{3}
  In[34]:= GoldenRatio // N
Out[34]= 1.61803
 In[35]:= N[E, 100]
\texttt{Out} \texttt{(35)} = \textbf{2.71828182845904523536028747135266249775724709369995957496696762772407663035354759457138} \\ \times \textbf{(35)} = \textbf{(35)} + \textbf
                                       2178525166427
 In[36]:= Pi // N
Out[36]= 3.14159
 In[37]:= N[Pi, 100]
4825342117068
```

Out[38]= 0

Out[39]= **3.14159** 

Out[40]= **0.0174533** 

Out[41]= 45 °

Out[42]= 6.28319

Out[43]= ∞

#### Kvadrātsaknes

Out[44]= 3

Out[45]= 1.73205

Out[46]= 1.732050808

## Kubsaknes tuvinājums

 $ln[47]:= \sqrt[3]{5} // N$ 

Out[47] = 1.70998

$$ln[48]:= \sqrt[3]{1414} // N$$

Out[48]= **11.2241** 

In[49]:= 
$$\sqrt[3]{\frac{2}{\sqrt{2}}}\sqrt{2}$$
 // N

Out[49]= **1.4916** 

## Logaritms

Out[50]= **5** 

Out[51]= **1** 

In[52]:= Log[10, 100 000 000]

Out[52]= **8** 

In[53]:= Log[E^100]

Out[53]= 100

In[54]:= Log10[100]

Out[54]= **2** 

Trigonometriskās funkcijas

Out[55]= 
$$\frac{\sqrt{3}}{2}$$

In[56]:= Sin[346 Degree] // N

Out[56]= -0.241922

In[57]:= Cos [0 Degree]

Out[57]= **1** 

Out[58]= **0.866025** 

Out[59]=  $\sqrt{3}$ 

Out[60]= 0.481575

In[61]:= Tan [40 Degree] // N

Out[61]= **0.8391** 

In[62]:= Cot[Pi]

Out[62]= ComplexInfinity

In[63]:= ArcCos 
$$\left[\frac{\sqrt{3}}{2}\right]$$

Out[63]= 
$$\frac{\pi}{6}$$

In[64]:= ArcSin[1]

Out[64]= 
$$\frac{\pi}{2}$$

Out[65]= **0** 

Out[66]= **0.808449** 

In[67]:= ArcTan[1]

Out[67]= 4

In[68]:= ArcCot[1]

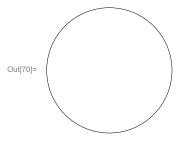
Out[68]=  $\frac{\pi}{4}$ 

In[69]:= ArcCot[0] // N

Out[69]= 1.5708

Riņķis

In[70]:= Graphics[Circle[]]



## Modulis

Out[71]= 64

In[72]:= **Abs [64]** 

Out[72]= **64** 

Maksimuma un minimuma atrāšana no saraksta

$$ln[73]:=$$
 Max $\left[\pi$ , e,  $\sqrt{2}$ ,  $\sqrt{3}$ , Log $\left[2,3\right]$ , GoldenRatio $\left]$ 

Out[73]= π

$$ln[74]:=$$
 Min $[\pi$ , e,  $\sqrt{2}$ ,  $\sqrt{3}$ , Log $[2,3]$ , GoldenRatio $]$ 

Out[74]=  $\sqrt{2}$ 

In[75]:= Max [52 214 214, 12 414 611, 88 886 119, 57 612 877, 24 322 211, 51 231 213, 11 111 110, 9 999 999]

Out[75]= 88 886 119

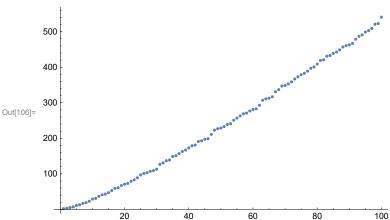
```
ոլ76: Min[52 214 214, 12 414 611, 88 886 119, 57 612 877, 24 322 211, 51 231 213, 11 111 110, 9 999 999]
Out[76]= 9999999
      Dalīšanas atlikums
In[77]:= Mod [7, 2]
Out[77]= 1
In[78] = Mod[4, 3]
Out[78]= 1
      Dalījums
In[79]:= Quotient[7, 2]
Out[79]= 3
In[80]:= Quotient[34, 12]
Out[80]= 2
In[81]:= Quotient [49 644, 1215]
Out[81]= 40
      Mazākais kopīgais dalāmais (MKD)
In[82]:= LCM[5, 6, 7]
Out[82]= 210
In[83]:= LCM[5121, 6123, 7123, 1515, 5167, 8888]
Out[83]= 17 095 162 630 763 800 440
      Lielākais kopīgais dalītājs (LKD)
In[84]:= GCD[4, 8, 16]
Out[84]= 4
In[85]:= Divisors [121]
Out[85]= \{1, 11, 121\}
In[86]:= Divisors [177]
Out[86]= \{1, 3, 59, 177\}
In[87]:= Divisors [1771551]
Out[87]= \{1, 3, 9, 27, 81, 21871, 65613, 196839, 590517, 1771551\}
      Uzzināt no kādiem pirmreizinātājiem sastāv skaitlis. {2, 3}, {7,1} nozīme, ka skaitlis sastāv no 2*2*2*7*1
In[88]:= FactorInteger[56]
Out[88]= \{\{2, 3\}, \{7, 1\}\}
```

```
In[89]:= FactorInteger [465 416]
Out[89]= \{\{2, 3\}, \{7, 1\}, \{8311, 1\}\}
In[90]:= FactorInteger [111 111 111 111]
 \text{Out} [90] = \ \left\{ \left. \left\{ 3\text{, 1} \right\},\ \left\{ 7\text{, 1} \right\},\ \left\{ 11\text{, 1} \right\},\ \left\{ 13\text{, 1} \right\},\ \left\{ 37\text{, 1} \right\},\ \left\{ 101\text{, 1} \right\},\ \left\{ 9901\text{, 1} \right\} \right\} 
In[91]:= Random[]
Out[91]= 0.673223
In[92]:= Round [44 / 17]
Out[92]= 3
ln[93] = 12 + Round[(8 - 2) RandomInteger[{1, 10}]]
Out[93]= 42
        Nejaušs vesels skaitlis diapazonā no 1 līdz 100
In[94]:= RandomInteger[{1, 100}]
Out[94]=~95
In[95]:= Random[Integer, 12]
Out[95]= 7
In[96]:= Random[Real, {1, 13}]
        10
Out[96]= 7.95187
Out[97]= 10
In[98]:= Random[Integer, {1, 13}]
Out[98]= 1
In[99]:= Random[Real, 1]
Out[99]= 0.324777
In[100]:=
        Nejaušs pirmskaitlis diapazonā no 1 līdz 100
In[101]:= RandomPrime[{1, 100}]
```

Atrod 100 pirmskaitļus pēc kārtas augoša secība

Out[101]= 43

```
In[102]:= Prime[Range[100]]
101, 103, 107, 109, 113, 127, 131, 137, 139, 149, 151, 157, 163, 167, 173, 179, 181, 191, 193,
       197, 199, 211, 223, 227, 229, 233, 239, 241, 251, 257, 263, 269, 271, 277, 281, 283, 293, 307,
       311, 313, 317, 331, 337, 347, 349, 353, 359, 367, 373, 379, 383, 389, 397, 401, 409, 419, 421,
       431, 433, 439, 443, 449, 457, 461, 463, 467, 479, 487, 491, 499, 503, 509, 521, 523, 541}
In[103]:= PrimeQ[1]
Out[103]= False
In[104]:= PrimeQ[2]
Out[104]= True
In[105]:= PrimeQ[214 214 141]
Out[105]= True
     Atrod 100 pirmskaitļus pēc kārtas augoša secība un atliek skaitļus grafikā
In[106]:= ListPlot[Table[Prime[n], {n, 100}]]
     500
     400
     300
Out[106]=
```



In[107]:= PrimePi[8]

Out[107]= 4

Skaitļu noapaļošana

In[108]:= Round [3.57534]

Out[108]= **4** 

In[109]:= 4!!

Out[109]= **8** 

In[110]:= % / 4

Out[110]= 2

Out[111]= **1** 

Out[112]= 1.

Out[113]= 
$$\{\{2, 3\}\}$$

Out[114]//BaseForm=

Out[116]= **3** i

Out[117]= 
$$10 - 3i$$

$$In[119]:= Im[z]$$

$$\mathsf{Out}[\mathsf{119}] = -3$$

Out[120]= 
$$10 + 3 i$$

Out[121]= 
$$\sqrt{109}$$

Out[122]= 
$$-ArcTan\left[\frac{3}{10}\right]$$

Out[123]= 
$$-0.291457$$

$$ln[127] = (X/3)/6$$

Out[127]= 
$$\frac{5}{9}$$

Out[129]= 
$$x^3$$

Out[130]= 
$$3 x$$

Out[132]= 
$$-11 x + 12 x^2$$

$$ln[133]:= \frac{x/20 + 20 - 400 x}{8} /. x \rightarrow 8$$

Out[133]= 
$$-\frac{7949}{20}$$

$$ln[134]:= (2x+3) (2x-10) (3x^2-6x-7)$$

$$\text{Out[134]=} \quad \left( -\,10\,+\,2\,\,x \right) \ \left( \,3\,+\,2\,\,x \right) \ \left( \,-\,7\,-\,6\,\,x\,+\,3\,\,x^2 \,\right)$$

$$ln[135]$$
:= Expand [ (2 x + 3) (2 x - 10) (3 x^2 - 6 x - 7)]

$$\mathsf{Out}[\mathsf{135}] = \ 210 + 278 \ x - 34 \ x^2 - 66 \ x^3 + 12 \ x^4$$

$$ln[136]$$
:= Factor [ (2 x + 3) (2 x - 10) (3 x^2 - 6 x - 7)]

$$\text{Out} \text{[136]= 2 (-5+x) } \left(3+2\,x\right) \, \left(-7-6\,x+3\,x^2\right)$$

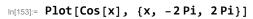
$$ln[137] = (2 x + 3) / (2 x - 10)$$

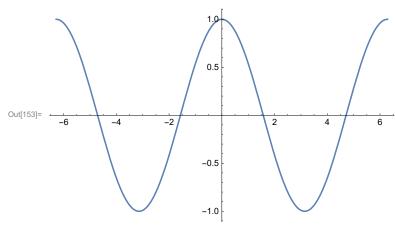
Out[137]= 
$$\frac{3 + 2 x}{-10 + 2 x}$$

Atvasināšana

```
In[138]:= D[x^2, x]
Out[138]= 2 x
In[139] = D[Cos[x], x]
Out[139]= -Sin[x]
In[140]:= D[Sin[x], x]
Out[140]= Cos [x]
        Integrēšana
In[141]:= Integrate[2x, x]
Out[141]= x^2
In[142]:= Integrate[Cos[x], x]
Out[142]= Sin[x]
In[143]:= Integrate[Sin[x], x]
Out[143]= -\cos[x]
In[144]:= Integrate [Cos[x]/x, x]
Out[144]= CosIntegral[x]
ln[145]:= a = 3
        a == b
        a < b
        a >= b
        a != b
        a>0
Out[145]= 3
Out[146]= 4
Out[147]= False
Out[148]= True
Out[149]= False
Out[150]= True
Out[151]= True
ln[152]:= FindRoot[Sin[x] == x, {x, 1}]
Out[152]= \{x \rightarrow 2.8012 \times 10^{-8}\}
```

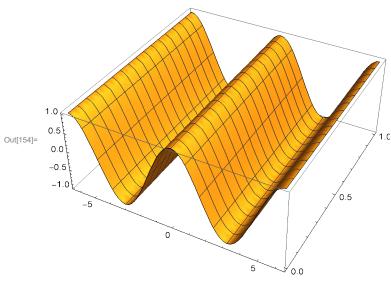
Funkcijas grafiks





Funkcijas grafiks telpā

ln[154]:= Plot3D[Cos[x], {x, -2 Pi, 2 Pi}, {y, 0, 1}]



Mainīgo definēšana un to izmantošana

In[155]:= **Z = ii - 2** 

Out[155]= -2 + i

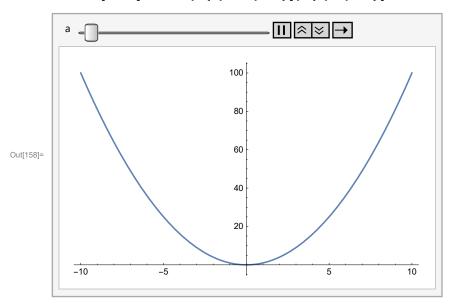
In[156]:= t = 2 i + 5

Out[156]= 5 + 2i

In[157]:= **z + t** 

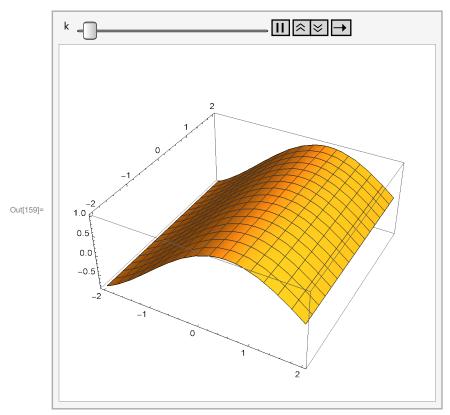
Out[157]= 3 + 3 i

Animācija. x^2 + x\*a funkcijas animācija, kur a mainās no 0 līdz 10. {x, -10, 10} nosaka animācijas robežas pēc x ass.



Animācija. Sin(x+k) funkcijas animācija, kur k mainās no 1 līdz 10. {x, -2, 2} nosaka animācijas robežas pēc x ass, {y, -2, 2} nosaka animācijas robežas pēc y ass.

In[159]:= Animate[Plot3D[Sin[x+k], {x, -2, 2}, {y, -2, 2}], {k, 1, 10}]



Matricas atspoguļošana

$$ln[160]:=$$
 mat = {{2, 8, -5}, {0, 1, 3}, {10, 2, 4}} // MatrixForm

Out[160]//MatrixForm=

Matricas determinanta noteikšana

Out[161]= 400

In[162]:= 
$$Det \left[ \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} \right]$$

Out[162]= 
$$-3_{12} \times 3_{21} + 3_{11} \times 3_{22}$$

$$\label{eq:loss_loss} \text{In[163]:= } \textbf{Det} \left[ \left( \begin{array}{ccc} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{array} \right) \right]$$

$$\text{Out} [\textbf{163}] = -3_{13} \times 3_{22} \times 3_{31} + 3_{12} \times 3_{23} \times 3_{31} + 3_{13} \times 3_{21} \times 3_{32} - 3_{11} \times 3_{23} \times 3_{32} - 3_{12} \times 3_{21} \times 3_{33} + 3_{11} \times 3_{22} \times 3_{33} + 3_{11} \times 3_{22} \times 3_{33} + 3_{11} \times 3_{22} \times 3_{23} \times 3_{23} \times 3_{24} \times$$

In[164]:= 
$$Det \begin{bmatrix} 4 & 2 & -1 \\ 1/3 & 11/27 & 5/9 \\ 900 & 90 & 180 \end{bmatrix}$$

Out[164]= 1310

In[165]:= 
$$Det \begin{bmatrix} a+b & a-b & b \\ c+b & 2c-b & b \\ b & -b & b \end{bmatrix}$$

Out[165]= 12 c

$$ln[166]:= \{\{1, 2\}, \{3, 4\}\} * 2$$

Out[166]= 
$$\{\{2, 4\}, \{6, 8\}\}$$

Out[167]= 
$$\{ \{5, 3\}, \{4, 7\} \}$$

Out[168]= 
$$\left\{ \left\{ -2, 1 \right\}, \left\{ \frac{3}{2}, -\frac{1}{2} \right\} \right\}$$

Bezgalīga summa

In[169]:= 
$$\sum_{n=1}^{\infty} \frac{1}{n^2}$$

Out[169]= 
$$\frac{\pi^2}{6}$$

In[170]:= 
$$\sum_{n=0}^{\infty} \frac{1}{2^n}$$

In[171]:= 
$$\sum_{n=0}^{\infty} \frac{1}{n!}$$

## Bezgalīgs reizinājums

In[172]:= 
$$\prod_{n=1}^{\infty} \left( \frac{4 n^2}{4 n^2 - 1} \right)$$

Out[172]= 
$$\frac{\pi}{2}$$

## Robeža

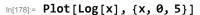
$$\ln[173] := \lim_{x \to \infty} \left( 1 + \frac{1}{x} \right)^{x}$$

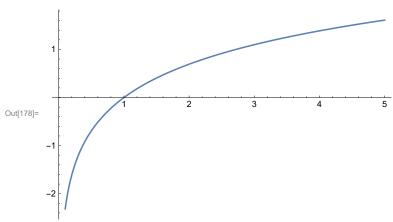
In[174]:= Limit 
$$[1/x, x \rightarrow \infty]$$

$$ln[175]:=$$
 Limit  $[1/x, x \rightarrow 0, Direction \rightarrow 1]$ 

$$ln[176]:=$$
 Limit  $[1/x, x \rightarrow 0, Direction \rightarrow -1]$ 

## Logaritms





In[179]:= Log[3.]

Out[179]= 1.09861

Kvadrātvienādojumu atrisināšana

$$ln[180] = Solve[2x^2 + x - 3 == 0, x]$$

Out[180]= 
$$\left\{ \left\{ X \to -\frac{3}{2} \right\}, \{X \to 1\} \right\}$$

Vienādojumu sistēmas atrisināšana

$$ln[181]:=$$
 Solve[ $\{x^2 + 8y == 3, -3x + 24y == -9\}, \{x, y\}$ ]

Out[181]= 
$$\left\{\left\{x \to -3, y \to -\frac{3}{4}\right\}, \left\{x \to 2, y \to -\frac{1}{8}\right\}\right\}$$

$$ln[182] = Solve[{Tan[x] = Sqrt[2]/2, 0 < x < 2 Pi}]$$

$$\text{Out[182]= } \left\{ \left\{ \mathbf{X} \to \mathsf{ArcTan} \left[ \, \frac{\mathbf{1}}{\sqrt{2}} \, \right] \right\}, \, \left\{ \mathbf{X} \to \pi + \mathsf{ArcTan} \left[ \, \frac{\mathbf{1}}{\sqrt{2}} \, \right] \right\} \right\}$$

$$ln[183] = Solve[Cos[x]^2 + Sin[x]^2 = x]$$

Out[183]= 
$$\{\{x \rightarrow 1\}\}$$

$$ln[184]:=$$
 Solve[{x^2 == (y - 6) ^2, x \* (x - y) == y^2 \* (x - y)}, {x, y}]

$$\begin{array}{ll} \text{Out[184]=} & \left\{ \left\{ x \to 3 \text{, } y \to 3 \right\} \text{, } \left\{ x \to 9 \text{, } y \to -3 \right\} \text{, } \left\{ x \to 4 \text{, } y \to 2 \right\} \text{,} \\ & \left\{ x \to \frac{1}{2} \, \left( -11 - \mathbb{i} \, \sqrt{23} \, \right) \text{, } y \to \frac{1}{2} \, \left( 1 - \mathbb{i} \, \sqrt{23} \, \right) \right\} \text{, } \left\{ x \to \frac{1}{2} \, \left( -11 + \mathbb{i} \, \sqrt{23} \, \right) \text{, } y \to \frac{1}{2} \, \left( 1 + \mathbb{i} \, \sqrt{23} \, \right) \right\} \right\} \end{array}$$

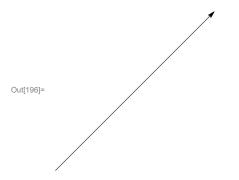
$$\left\{ \left\{ x \to 3 \,,\, y \to 3 \right\} ,\, \left\{ x \to 9 \,,\, y \to -3 \right\} ,\, \left\{ x \to 4 \,,\, y \to 2 \right\} , \\ \left\{ x \to \frac{1}{2} \, \left( -11 - \dot{\mathbb{1}} \,\, \sqrt{23} \, \right) \,,\, y \to \frac{1}{2} \, \left( 1 - \dot{\mathbb{1}} \,\, \sqrt{23} \, \right) \right\} ,\, \left\{ x \to \frac{1}{2} \, \left( -11 + \dot{\mathbb{1}} \,\, \sqrt{23} \, \right) \,,\, y \to \frac{1}{2} \, \left( 1 + \dot{\mathbb{1}} \,\, \sqrt{23} \, \right) \right\} \right\}$$

$$\begin{array}{l} \text{Out[185]=} \; \left\{ \, \left\{ \, x \, \to \, 3 \, , \; y \, \to \, 3 \, \right\} \, , \; \left\{ \, x \, \to \, 9 \, , \; y \, \to \, - \, 3 \, \right\} \, , \; \left\{ \, x \, \to \, 4 \, , \; y \, \to \, 2 \, \right\} \, , \\ \left\{ \, x \, \to \, \frac{1}{2} \; \left( - \, 11 \, - \, \dot{\mathbb{1}} \; \sqrt{23} \, \right) \, , \; y \, \to \, \frac{1}{2} \; \left( 1 \, - \, \dot{\mathbb{1}} \; \sqrt{23} \, \right) \, \right\} \, , \; \left\{ \, x \, \to \, \frac{1}{2} \; \left( - \, 11 \, + \, \dot{\mathbb{1}} \; \sqrt{23} \, \right) \, , \; y \, \to \, \frac{1}{2} \; \left( 1 \, + \, \dot{\mathbb{1}} \; \sqrt{23} \, \right) \, \right\} \, \right\} \, . \end{array}$$

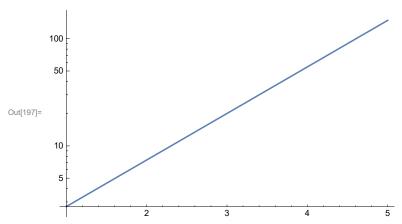
```
ln[186] = Roots[x^2 + 3x - 4 = 0, x]
Out[186]= x == -4 \mid x == 1
       Kopu apvienojums
ln[187] = \{a, b, c\} \cup \{b, c, d\}
Out[187]= \{3, 4, c, d\}
In[188]:= \{a, b, c, d\}
Out[188]= \{3, 4, c, d\}
In[189]:= Union[{a, b, c}, {b, c, d}]
Out[189]= \{3, 4, c, d\}
       Kopu šķēlums
ln[190] = \{a, b, c\} \cap \{b, c, d\}
Out[190]= \{4, c\}
In[191]:= Intersection[{a, b, c}, {b, c, d}]
Out[191]= \{4, c\}
       Atrast kopas visas iespējamās apakškopas
In[192]:= Subsets[{1, 2, 3}]
Out[192]= \{\{\}, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}
       Atrast lenki starp vektoriem
In[193]:= VectorAngle[{2, 0}, {1, 1}]
Out[193]=
In[194]:=
Out[194]=
       Vektora grafiskā interpretācija
```

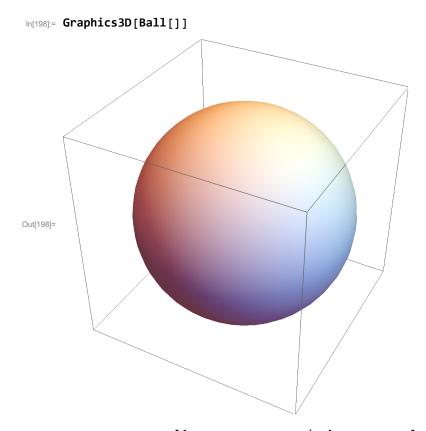
In[195]:= Graphics[Arrow[{{0,0},{2,0}}]]

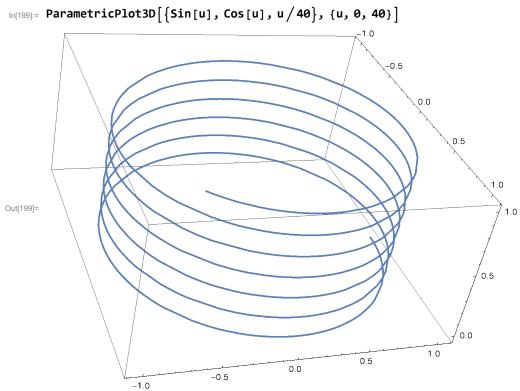
# In[196]:= Graphics[Arrow[{{0,0},{1,1}}]]



# In[197]:= LogPlot[E^x, {x, 1, 5}]







Ielādēt no konkrēta ģeogrāfiskā reģiona karogus





