

# Алгоритмизация и программирование

## Лекция 4

# Перечисления

# enum (перечисления)

```
void set_color(/*какой тип?*/ color){  
    /* Код */  
}
```

```
void set_color(int color){  
    /* Код */  
}
```

```
void set_color(std::string color){  
    /* Код */  
}
```

# enum

```
enum Color
{
    // Список перечислителей
    color_black,
    color_red,
    color_blue,
    color_green,
    color_white,
    color_cyan,
    color_yellow,
    color_magenta, //<- запятую можно оставить
}; // <- точкой с запятой

// Определяем несколько переменных перечислимого типа Color
Color paint = color_white;
Color house(color_blue);
Color apple { color_red };
```

# enum

```
void set_color(Color color){  
    /* Код */  
}  
  
set_color(color_red); // нормально  
set_color(1);         // ошибка
```

# enum

```
enum Color
{
    red,
    blue, // blue помещается в глобальное пространство имен
    green
};

enum Feeling
{
    happy,
    tired,
    blue // ошибка, blue уже использовался в enum Color в глобальном пространстве имен
};
```

# enum

```
// определяем новое перечисление с именем Animal
enum Animal
{
    animal_cat = -3,
    animal_dog, // присвоено -2
    animal_pig, // присвоено -1
    animal_horse = 5,
    animal_giraffe = 5, // имеет то же значение, что и animal_horse
    animal_chicken // присвоено 6
};

int pet = animal_pig;
Animal mypet = animal_pig;

std::cout << mypet; // перед передачей в std::cout вычисляется как int
std::cin >> mypet;  // вызовет ошибку компилятора
```

# enum

```
// Использовать в качестве базы для перечисления
// 8-битный целочисленный тип без знака.
enum Color : std::uint_least8_t
{
    color_black,
    color_red,
    // ...
};
```



# enum class

```
enum class Color
{
    red,
    blue, // blue помещается в пространство имен Color
    green
};

enum class Feeling
{
    happy,
    tired,
    blue // нормально, blue помещается в пространство имен Feeling
};

Color color = Color::blue;
Color color = blue; // ошибка
```

Объединения

# union (объединения)

```
// Структура
struct building
{
    std::string owner;
    std::string city;
    int amountRooms;
    float price;
};

building apartment;
apartment.owner = "John";
apartment.city = "NY";
apartment.amountRooms = 10;
apartment.price = 100;
```

```
// Объединение
union building
{
    std::string owner;
    std::string city;
    int amountRooms;
    float price;
};

building apartment;
// Только что-то одно
```

Объединение занимает в памяти столько места, сколько занимает самое большое его поле. После инициализации менять тип данных перечисления нельзя (хотя иногда можно)

Указатели

# Указатель

Составной тип данных предназначенный для хранения адреса некоторой программной сущности:

```
int a;                // Хранит целое число
int* ptr_a = nullptr; // Хранит адрес переменной типа int

std::string str;       // Хранит строку
std::string* ptr_str;  // Хранит адрес переменной типа std::string

double* ptr_d;         // Хранит адрес переменной типа double
double** ptr_ptr_d;    // Хранит адрес переменной типа double*
```

# & | Оператор взятия адреса

Позволяет узнать адрес в памяти, по которому находится программная сущность:

```
int a;  
int* ptr_a = &a;
```

```
std::string str;  
std::string* ptr_str = &str;
```

```
double d;  
double* ptr_d = &d;  
double** ptr_ptr_d = &ptr_d;
```

```
ptr_d = &a;          // Не соответствие типов  
ptr_a = ptr_str;    // Не соответствие типов
```

```
ptr_a = a;           // Не соответствие типов  
a = ptr_a;           // Не соответствие типов
```

# \* | Оператор разыменования (dereference)

Позволяет получить доступ к программной сущности по адресу:

```
int a;  
int* ptr_a = &a;  
int b = *ptr_a;
```

```
double d;  
double* ptr_d = &d;  
double** ptr_ptr_d = &ptr_d;  
double c = **ptr_ptr_d;
```

```
*ptr_a = 10; // Значение a изменилось на 10
```

# Адресная арифметика

Позволяет получить доступ к другому адресу:

```
int a[10] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};  
int* ptr_a = &a[0];  
int* end_a = &a[9];
```

```
ptr_a = ptr_a + 1; // a[1]  
ptr_a = ptr_a + 2; // a[3]  
ptr_a++;           // a[4]  
ptr_a--;           // a[3]  
ptr_a = ptr_a - 3; // a[0]
```

```
int size = end_a - ptr_a; // 10
```



Ссылки

# Ссылка (на l-value)

Альтернативное имя для переменной:

```
int a;           // Хранит целое число  
int& fer_a = a;  // Ничего не хранит, просто имя
```

```
std::string str;           // Хранит строку  
std::string& fef_str = str; // Ничего не хранит, просто имя
```

```
int& fer_a2 = fer_a; // Тоже ссылка на a
```

```
int& fer_a;           // Нельзя  
int&& fer_fer_a;       // Другой тип ссылки  
int&&& fer_fer_fer_a; // Не существует
```

**Псевдонимы**

# Псевдоним | альтернативное имя

```
// typedef
typedef int integer;
integer a = 1;

typedef int vector[10];
vector vect;
vector matrix[5]; // arr[5][10]

typedef int (*foo)(int a, int b);

// using
using integer = int;

using vector = int[10];
using matrix = vector[5];

using foo = int (*)(int a, int b);
```

# Типы данных из STL

```
string s = "I'm sorry, Dave.";
           0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 indices
```

non-mutating

s.size()	→ 16	(number of characters)
s[2]	→ 'm'	(character at index 2)
s.find("r")	→ 6	(first match from start)
s.rfind("r")	→ 7	(first match from end)
s.find("X")	→ string::npos	(not found, invalid index)
s.find(' ', 5)	→ 10	(first match after index ≥ 5)
s.substr(4, 6)	→ string{"sorry,"}	
s.contains("sorry")	→ true	(C++23)
s.starts_with('I')	→ true	(C++20)
s.ends_with("Dave.")	→ true	(C++20)
s.compare("I'm sorry, Dave.")	→ 0	(identical)
s.compare("I'm sorry, Anna.")	→ > 0	(same length, but 'D' > 'A')
s.compare("I'm sorry, Saul.")	→ < 0	(same length, but 'D' < 'S')

mutating

size

index based

iterator based

s += " I'm afraid I can't do that."	⇒ s = "I'm sorry, Dave. I'm afraid I can't do that."
s.append("...")	⇒ s = "I'm sorry, Dave..."
s.clear()	⇒ s = ""
s.resize(3)	⇒ s = "I'm"
s.resize(20, '?')	⇒ s = "I'm sorry, Dave.?????";
s.insert(4, "very ")	⇒ s = "I'm very sorry, Dave."
s.erase(5, 2)	⇒ s = "I'm srry, Dave."
s[15] = '!'	⇒ s = "I'm sorry, Dave!"
s.replace(11, 5, "Frank")	⇒ s = "I'm sorry, Frank"
s.insert(s.begin(), "HAL: ")	⇒ s = "HAL: I'm sorry, Dave."
s.insert(s.begin()+4, "very ")	⇒ s = "I'm very sorry, Dave."
s.erase(s.begin()+5)	⇒ s = "I'm srry, Dave."
s.erase(s.begin(), s.begin()+4)	⇒ s = "sorry, Dave."

## Constructors

```
string{'a','b','c'} → a b c
string(4, '$') → $ $ $ $
string(@firstIn, @lastIn) → e f g h
                        source ↓ iterator range ↓
                        b c d e f g h i j
string( a b c d ) copy/move → a b c d
                        source string object
```

## Obtain Iterators

## or Reverse Iterators

```
.begin() → @first
           ↓
           a b c d e f

.end() → @one_behind_last
           ↓
           a b c d e f
           don't use to access elements!
```

```
.rbegin() → reverse@last
           ↓
           a b c d e f
           ↓
           a b c d e f
           don't use to access elements!
```

## String → Number Conversion

```
int      stoi (●, ●, ●);
long     stol (●, ●, ●);
long long stoll(●, ●, ●);
const string&
input string
std::size_t* p = nullptr
output for
number of processed characters

unsigned long stoul (●, ●, ●);
unsigned long long stoull(●, ●, ●);
int base = 10
base of target system;
default: decimal

float      stof (●, ●, ●);
double     stod (●, ●, ●);
long double stold(●, ●, ●);
```

## Number → String Conversion

```
string to_string( ● );
           {
int | long | long long |
unsigned | unsigned long | unsigned long long |
float | double | long double
           }
```

# Последовательные контейнеры

# C++ Standard Library Sequence Containers

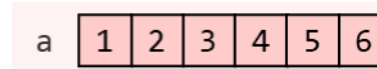
h/cpp/ hackingcpp.com

## `array<T, size>`

fixed-size array

```
#include <array>
```

```
std::array<int,6> a {1,2,3,4,5,6};  
cout << a.size();    // 6  
cout << a[2];        // 3  
a[0] = 7;             // 1st element ⇒ 7
```



contiguous memory; random access; fast linear traversal

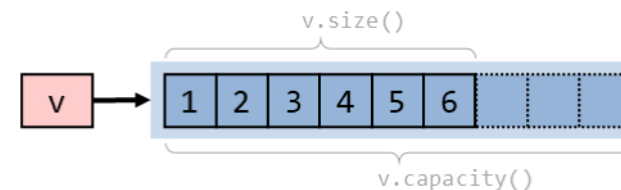
## `vector<T>`

dynamic array

C++'s "default" container

```
#include <vector>
```

```
std::vector<int> v {1,2,3,4,5,6};  
v.reserve(9);  
cout << v.capacity();    // 9  
cout << v.size();        // 6  
v.push_back(7);          // appends '7'  
v.insert(v.begin(), 0);  // prepends '0'  
v.pop_back();            // removes last  
v.erase(v.begin()+2);    // removes 3rd  
v.resize(20, 0);         // size ⇒ 20
```



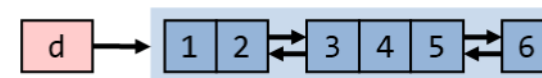
contiguous memory; random access;  
fast linear traversal; fast insertion/deletion at the ends

## `deque<T>`

double-ended queue

```
#include <deque>
```

```
std::deque<int> d {1,2,3,4,5,6};  
// same operations as vector  
// plus fast growth/deletion at front  
d.push_front(-1); // prepends '-1'  
d.pop_front();    // removes 1st
```



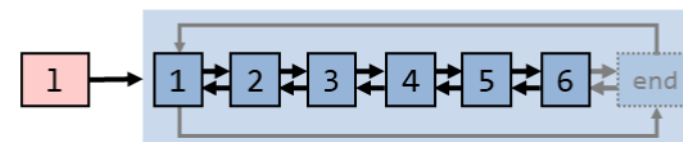
fast insertion/deletion at both ends

## `list<T>`

doubly-linked list

```
#include <list>
```

```
std::list<int> l {1,5,6};  
std::list<int> k {2,3,4};  
// O(1) splice of k into l:  
l.splice(l.begin()+1, std::move(k))  
// some special member function algorithms:  
l.reverse();  
l.sort();
```



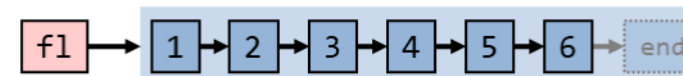
fast splicing; many operations without copy/move of elements

## `forward_list<T>`

singly-linked list

```
#include <forward_list>
```

```
std::forward_list<int> fl {2,2,4,5,6};  
fl.erase_after(begin(fl));  
fl.insert_after(begin(fl), 3);  
fl.insert_after(before_begin(fl), 1);
```



lower memory overhead than std::list; only forward traversal



# std::vector<ValueType>

C++'s "default"  
dynamic array

#include <vector>

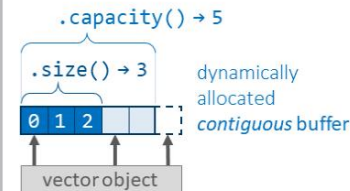
h/cpp hackingcpp.com

## Construct A New Vector Object

```
vector<int> v1 {2,9,1,8,5,4} → [2, 9, 1, 8, 5, 4]
vector<int> v2 (begin(v1)+3, end(v1)) → [8, 5, 4]
vector<int> v3 (5, 3) → [3, 3, 3, 3, 3]
vector<int> deep_copy_of_v1 (v1) → [2, 9, 1, 8, 5, 4]
```

C++17 value type deducible from argument type  
`vector w {7,4,2}; // vector<int>`

## Typical Memory Layout



## Assign New Content To An Existing Vector

```
vector<int> v1 {8,5,3}; (deep copy from source)
vector<int> v2 {6,8,1,9};
v1 = v2;
new state of v1: [6, 8, 1, 9]
[8, 5, 3].assign({4,1,3,5}) → [4, 1, 3, 5]
[8, 5, 3].assign(2, 1) → [1, 1]
[8, 5, 3].assign(@InBeg, @InEnd) → [2, 1, 1, 2]
source container: [3, 2, 1, 1, 2, 3]
```

## Query/Change Size (= Number of Elements)

```
[8, 5, 3].empty() → false
[8, 5, 3].size() → 3
[8, 5, 3].resize(2) → [8, 5, +]
[8, 5, 3].resize(4, 1) → [8, 5, 3, 1]
[8, 5, 3].resize(6, 1) → [8, 5, 3, 1, 1, 1]
[8, 5, 3].clear() → [+, +, +]
```

## Query/Grow Capacity (= Memory Buffer Size)

```
[8, 5, 3].capacity() → 4
[8, 5, 3].reserve(6) → [8, 5, 3, +, +, +]
```

## Get Element Values $O(1)$ Random Access

```
[2, 8, 5, 3][1] → 8
[2, 8, 5, 3].front() → 2
[2, 8, 5, 3].back() → 3
```

## Change Element Values

```
[2, 8, 5, 3][1] = 7 → [2, 7, 5, 3]
[2, 8, 5, 3].front() = 7 → [7, 8, 5, 3]
[2, 8, 5, 3].back() = 7 → [2, 8, 5, 7]
```

## Out of Bounds Access

```
[2, 8, 5, 3][6] → Undefined Behavior (Invalid Index!)
[2, 8, 5, 3].at(6) → Throws Exception (std::out_of_range)
```

## Erase Elements $O(n)$ Worst Case

```
vector<int> v {4,8,5,6};
[4, 8, 5, 6].pop_back() → [4, 8, 5, +]
[4, 8, 5, 6].erase(begin(v)+2) → [4, 8, 6, +]
[4, 8, 5, 6].erase(begin(v)+1, begin(v)+3) → [4, 6, +, +]
```

## Shrink The Capacity (might be inefficient)

Erasing, resizing or clearing will not shrink the capacity!

```
vector<int> v (1024, 0); // capacity is at least 1024
v.resize(40); // capacity unchanged!
v.shrink_to_fit(); // may shrink (not guaranteed)
v.swap(vector<int>(v)); // shrinks but has copy overhead
```

## Obtain Iterators

$O(1)$  Random Incrementing

```
[0, 1, 2, 3].begin() → @first
[0, 1, 2, 3].end() → @one_behind_last
```

## Obtain Reverse Iterators

```
[0, 1, 2, 3].rbegin() → rev@last
[0, 1, 2, 3].rend() → rev@one_before_first
```

```
v.begin() v.end()
v.rend() v.rbegin()
@pos = rev@pos.base() - 1
rev@pos.base()
```

```
[2, 8, 5, 3].data() → pointer_to_first
```

Avoid expensive memory allocations:  
**.reserve** capacity before appending / inserting if you know the (approximate) number of elements to be stored in advance!

## Append Elements $O(1)$ Amortized Complexity

```
[8, 5, 3].push_back(7) → [8, 5, 3, 7]
```

## Insert Elements at Arbitrary Positions $O(n)$ Worst Case

```
vector<int> v {8,5,3};
[8, 5, 3].insert(begin(v), 2) → [2, 8, 5, 3]
[8, 5, 3].insert(begin(v)+1, 7) → [8, 7, 5, 3]
[8, 5, 3].insert(begin(v)+1, 3, 7) → [8, 7, 7, 7, 5, 3]
[8, 5, 3].insert(begin(v)+1, {6,9,7}) → [8, 6, 9, 7, 5, 3]
[8, 5, 3].insert(begin(v)+1, @InBeg, @InEnd) → [8, 1, 8, 9, 5, 3]
source container: [3, 1, 8, 9, 2, 3]
```

## Insert & Construct Elements in Place $O(n)$ Worst Case

```
vector<pair<string,int>> v {{"a",1}, {"w",7}};
[a,1][w,7].emplace_back("b",4) → [a,1][w,7][b,4]
[a,1][w,7].emplace(begin(v)+1, "z",5) → [a,1][z,5][w,7]
```

# Ассоциативные контейнеры

## set<Key>

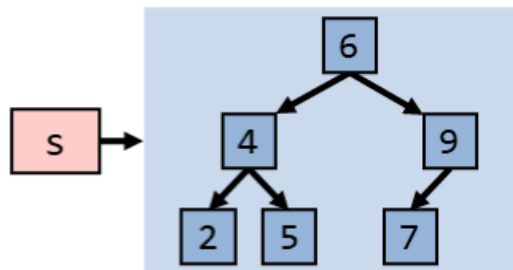
unique, ordered keys

## multiset<K>

(non-unique) ordered keys

```
std::set<int> s;  
s.insert(7); ...  
s.insert(5);  
auto i = s.find(7); // → iterator  
if(i != s.end())    // found?  
    cout << *i;    // 7  
if(s.contains(7)) {...}
```

C++20



usually implemented  
as balanced binary tree  
(red-black tree)

## map<Key, Value>

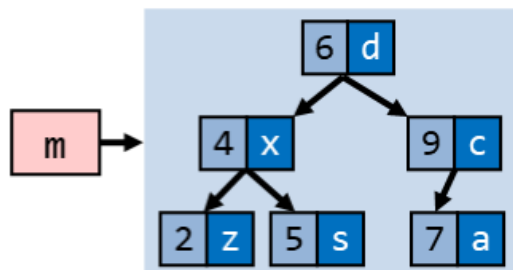
unique key → value-pairs; ordered by keys

## multimap<K, V>

(non-unique) key → value-pairs, ordered by keys

```
std::map<int, char> m;  
m.insert({7, 'a'}); ...  
m[4] = 'x'; // insert 4 → x  
auto i = s.find(7); // → iterator  
if(i != s.end())    // found?  
    cout << i->first // 7  
        << i->second; // a  
if(s.contains(7)) {...}
```

C++20



usually implemented  
as balanced binary tree  
(red-black tree)

## unordered\_set<Key>

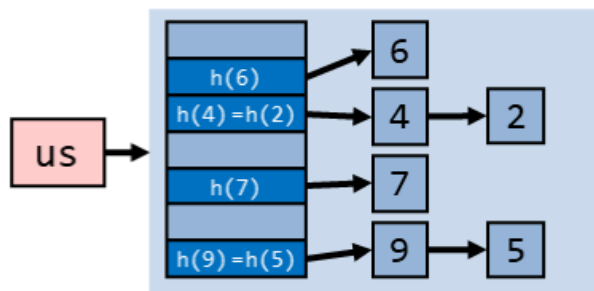
unique, hashable keys

## unordered\_multiset<Key>

(non-unique) hashable keys

```
std::unordered_set<int> us;  
us.insert(7); ...  
us.insert(5);  
auto i = us.find(7); // → iterator  
if(i != us.end())    // found?  
    cout << *i;    // 7  
if(s.contains(7)) {...}
```

C++20



hash table for  
key lookup,  
linked nodes  
for key storage

## unordered\_map<Key, Value>

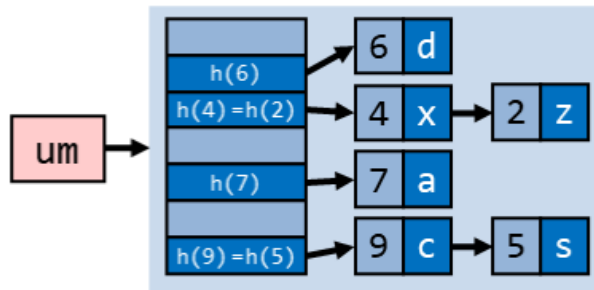
unique key → value-pairs; hashed by keys

## unordered\_multimap<Key, Value>

(non-unique) key → value-pairs; hashed by keys

```
unordered_map<int, char> um;  
um.insert({7, 'a'}); ...  
um[4] = 'x'; // insert 4 → x  
auto i = um.find(7); // → iterator  
if(i != um.end())    // found?  
    cout << i->first // 7  
        << i->second; // a  
if(s.contains(7)) {...}
```

C++20

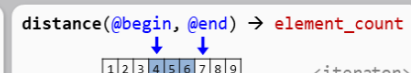
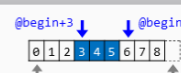


hash table for  
key lookup,  
linked nodes  
for (key, value)  
pair storage

# Некоторые стандартные алгоритмы

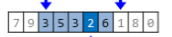
# C++ Standard Library Algorithms

Iterator  
Ranges

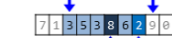


## Non-Modifying Sequence Operations

`min_element(@begin, @end) → @minimum`

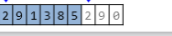


`minmax_element(@begin, @end) → { @minimum, @maximum }`

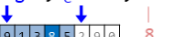


C++11

`any_of(@begin, @end, f(o)→bool) →` true, if `f` yields true for any, all or none elements in the input range  
`all_of(@begin, @end, f(o)→bool) →`  
`none_of(@begin, @end, f(o)→bool) →` false otherwise



`find_if(@begin, @end, f(o)→bool) →` 1st match  
`find(@begin, @end, value) →` @end if no match



`count_if(@begin, @end, f(o)→bool) →` number of occurrences  
`count(@begin, @end, value) →`



`equal(@begin1, @end1, @begin2) → true` if all elements in both ranges are equal



`mismatch(@begin1, @end1, @begin2) → { @mismatch_in1, @mismatch_in2 }`

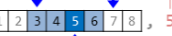


`search(@beg1, @end1, @beg2, @end2) →` 1st occurrence of sequence 2 inside sequence 1  
@end1 otherwise



## Binary Search On Sorted Sequences ⇒ $O(\log n)$

`lower_bound(@begin, @end, value) →` 1st element not < value  
@end if no such element exists



`upper_bound(@begin, @end, value) →` 1st element > value  
@end if no such element exists



`equal_range(@begin, @end, value) → { 1st item not < value or @end if none such found, 1st item > value or @end if none such found }`



## Reordering Elements

`reverse(@begin, @end)`

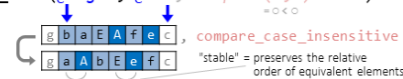


`sort(@begin, @end, f(o,o)→bool)`

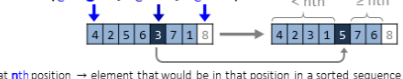
`sort(@begin, @end, std::less)`



`stable_sort(@begin, @end, compare(o,o)→bool)`



`nth_element(@begin, @nth, @end)`



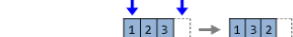
`partition(@begin, @end, f(o)→bool) → @part2`



`rotate(@begin, @newfst, @end) → @old_begin`



`next_permutation(@begin, @end) → true` if new permutation is lexicographically greater

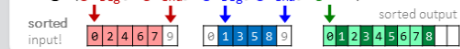


`shuffle(@begin, @end, random_engine)`



## Manipulate Sorted Sequences ⇒ $O(n)$

`merge(@1beg, @1end, @2beg, @2end, @out)`

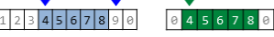


`set_union(@1beg, @1end, @2beg, @2end, @out)`



## Changing Values

`copy(@begin, @end, @out)`



`transform(@begin, @end, @out, f(o)→■)`



`generate(@begin, @end, f()→■)`



`replace(@begin, @end, old, new)`



`replace_if(@begin, @end, f(o)→bool, new)`



`remove(@begin, @end, value) → @end_of_remove`  
`remove_if(@begin, @end, f(o)→bool) → remaining`



`unique(@begin, @end) → @end_of_remaining`



`erase(container, value) → erased_count`



## Numeric Algorithms

`reduce(@begin, @end, w = ●(), ⊕ = ○+○) →` arbitrary evaluation order!  
`reduce(@begin, @end, w, ⊕(□,○)→■) →`



`transform_reduce(@begin, @end, @begin2, @end2, w, ⊕ = □+○, ⊗ = ○×○) → R0`  
`transform_reduce(@begin, @end, @begin2, @end2, w, ⊕(□,○)→■, ⊗(○,○)→■) → R0`  
`transform_reduce(@begin, @end, @begin2, @end2, w, ⊕(□,○)→■, f(○)→■) → Rf`



`inclusive_scan(@begin, @end, @out, ⊕ = □+○) →`  
`inclusive_scan(@begin, @end, @out, ⊕(□,○)→■, w) → @end`



## Sequence Queries

`all_of` (C++11)  
`any_of` (C++11)  
`none_of` (C++11)  
`count` (C++11)  
`count_if` (C++11)  
`find` (C++11)  
`find_if` (C++11)  
`find_if_not` (C++11)  
`find_end` (C++11)  
`find_first_of` (C++11)  
`adjacent_find` (C++11)  
`for_each` (C++11)  
`for_each_n` (C++17)  
`sample` (C++20)  
`equal` (C++11)  
`mismatch` (C++11)  
`search` (C++11)  
`search_n` (C++11)  
`lexicographical_compare` (C++11)  
`lexicographical_compare_three_way` (C++20)

## Reordering Elements

`reverse` (C++11)  
`reverse_copy` (C++11)  
`rotate` (C++11)  
`rotate_copy` (C++11)  
`shift_left` (C++20)  
`shift_right` (C++20)  
`shuffle` (C++11)  
`swap` (C++11)  
`swap_ranges` (C++11)  
`iter_swap` (C++11)

## Partitioning

`is_partitioned` (C++11)  
`partition` (C++11)  
`stable_partition` (C++11)  
`partition_copy` (C++11)  
`partition_point` (C++11)

## Permutations

`is_permutation` (C++11)  
`next_permutation` (C++11)  
`prev_permutation` (C++11)

## Sorting

`sort` (C++11)  
`stable_sort` (C++11)  
`partial_sort` (C++11)  
`partial_sort_copy` (C++11)  
`is_sorted` (C++11)  
`is_sorted_until` (C++11)  
`nth_element` (C++11)

## Changing Elements

`copy` (C++11)  
`copy_backward` (C++11)  
`copy_if` (C++11)  
`copy_n` (C++11)  
`move` (C++11)  
`move_backward` (C++11)  
`fill` (C++11)  
`fill_n` (C++11)  
`generate` (C++11)  
`generate_n` (C++11)  
`transform` (C++11)  
`transform_copy` (C++11)  
`transform_copy_if` (C++11)  
`replace` (C++11)  
`replace_copy` (C++11)  
`replace_copy_if` (C++11)  
`remove` (C++11)  
`remove_copy` (C++11)  
`remove_copy_if` (C++11)  
`unique` (C++11)  
`unique_copy` (C++11)

## Binary Search on Sorted Ranges

`binary_search` (C++11)  
`lower_bound` (C++11)  
`upper_bound` (C++11)  
`equal_range` (C++11)  
`includes` (C++11)

## Merging of Sorted Ranges

`merge` (C++11)  
`replace_merge` (C++11)  
`set_union` (C++11)  
`set_intersection` (C++11)  
`set_difference` (C++11)  
`set_symmetric_difference` (C++11)

## Heaps

`make_heap` (C++11)  
`sort_heap` (C++11)  
`push_heap` (C++11)  
`pop_heap` (C++11)  
`is_heap` (C++11)  
`is_heap_until` (C++11)

## Minimum/Maximum

`min` (C++11)  
`max` (C++11)  
`min_element` (C++11)  
`max_element` (C++11)  
`minmax` (C++11)  
`minmax_element` (C++11)  
`clamp` (C++17)

## Numeric

`accumulate` (C++11)  
`adjacent_difference` (C++11)  
`inner_product` (C++11)  
`partial_sum` (C++11)  
`iota` (C++11)  
`reduce` (C++17)  
`inclusive_scan` (C++17)  
`exclusive_scan` (C++17)  
`transform_reduce` (C++17)  
`transform_inclusive_scan` (C++17)  
`transform_exclusive_scan` (C++17)