

Practical 4 – Naïve Bayes Classifier and KNN (Solutions)

CS5062 – Machine Learning

Overview

In this exercise, you will work on Naïve Bayes Classifier and use Python to implement the KNN algorithm introduced in the Lecture.

Naïve Bayes Classifier

Given the training data in the table below (Buy Computer data), we need to predict the classes of a new example using Naïve Bayes classification. E = age \leq 30, income=medium, student=yes, credit-rating=fair. E_1 is age \leq 30, E_2 is income=medium, E_3 is student=yes, E_4 is credit

RID	age	income	student	credit_rating	Class: buys_computer
1	≤ 30	high	no	fair	no
2	≤ 30	high	no	excellent	no
3	31 ... 40	high	no	fair	yes
4	> 40	medium	no	fair	yes
5	> 40	low	yes	fair	yes
6	> 40	low	yes	excellent	no
7	31 ... 40	low	yes	excellent	yes
8	≤ 30	medium	no	fair	no
9	≤ 30	low	yes	fair	yes
10	> 40	medium	yes	fair	yes
11	≤ 30	medium	yes	excellent	yes
12	31 ... 40	medium	no	excellent	yes
13	31 ... 40	high	yes	fair	yes
14	> 40	medium	no	excellent	no

According to given data, please work on the following questions:

- 1) Please compute $P(\text{yes})$ and $P(\text{no})$.

Solution:

$$P(\text{yes}) = \frac{9}{14} = 0.643$$

$$P(\text{no}) = \frac{5}{14} = 0.357$$

- 2) After obtaining $P(\text{yes})$ and $P(\text{no})$ from (1), please compute $P(E_i|\text{yes})$ and $P(E_i|\text{no})$, where $i = 1, 2, 3, 4$.

Solution:

$$P(E_1|\text{yes}) = \frac{2}{9} = 0.222, P(E_1|\text{no}) = \frac{3}{5} = 0.6$$

$$P(E_2|\text{yes}) = \frac{4}{9} = 0.444, P(E_2|\text{no}) = \frac{2}{5} = 0.4$$

$$P(E_3|yes) = \frac{6}{9} = 0.667, P(E_3|no) = \frac{1}{5} = 0.2$$

$$P(E_4|yes) = \frac{6}{9} = 0.667, P(E_4|no) = \frac{2}{5} = 0.4$$

3) Please compute $P(yes|E)$ and $P(no|E)$.

Solution:

$$P(yes|E) = \frac{0.222 \times 0.444 \times 0.667 \times 0.668 \times 0.643}{P(E)} = \frac{0.028}{P(E)}$$

$$P(no|E) = \frac{0.6 \times 0.4 \times 0.2 \times 0.4 \times 0.357}{P(E)} = \frac{0.007}{P(E)}$$

Hence, the Naïve Bayes classifier predicts buys_computer=yes for the new example.

K-Nearest Neighbours

The task of this exercise is to write Python code to implement KNN algorithm on a classification problem:

- 1) We use IRIS data for this workshop. The data can be loaded from 'sklearn' using Python. (from sklearn import datasets; iris=datasets.load_iris()) This data has 150 observations of iris flowers from three different species, hence three classes: setosa, versicolor and virginica. There are four attributes in the data: sepal length, sepal width, petal length and petal width.
- 2) Your code to implement KNN algorithm should include the following functions:
 - a. Load the data set; return 90% as train data and 10% as test data
 - b. Normalize the features
 - c. Calculate the Euclidean distance between any two points
 - d. Find the neighbours given a test data point and number k=3
 - e. Get the class labels; you should also handle ties
 - f. Calculate prediction accuracy
- 3) Apply your KNN algorithm to the iris data.

Source codes:

```
import numpy as np
import matplotlib.pyplot as plt
from sklearn import neighbors, datasets
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score
```

```
n_neighbors = 3
```

```
# import some data to play with
iris = datasets.load_iris()
```

```
X = iris.data
y = iris.target
```

```
X_train, X_test, y_train, y_test = train_test_split\
(X, y, test_size=0.1, random_state=42)
```

```
# Function of computing euclidean distance between two points
def dist(x, y):
    return np.sqrt(np.dot(x,x) - 2*np.dot(x, y) + np.dot(y, y))

print('Euclidean distance: ', dist(X[0,:],X[1,:]))

# we create an instance of Neighbours Classifier and fit the data.
KNN_clf = neighbors.KNeighborsClassifier(n_neighbors,
weights='uniform')
KNN_clf.fit(X_train, y_train)

# Predictions of test dataset
preds = KNN_clf.predict(X_test)

# Show the accuracy
print(accuracy_score(y_test,preds))
```