=1= 16.02,2021 Neexaneuca - 2021 Ceneurap N 6 Рассион рим примеры на примене-ние условией потенциальности сия в криволичестих кординалах. cusor F 6 R3 zagamon Kooppuravax Drunep & Kamorentos l'appureeranx x of a real y F = Free + Folo + Fyly Fz = 2 d+1 Sinde Cosp dER-- napamerp For = Cos (XD) e Cos 4 Fy = - Siny e Gs4 a) Harry, hom kaken znaremme napamer-pa & cuia F nomenimanona, harry Coors bein em byrousent novemmen UGO, 4). E upu nepaversenui 43 voria A(0,0,0) 6 vorky B(1,1,0).

Tregteptue d' van, remoter bourn = 2 = nemes neot xoquinore yarobres, nothinguaremocru:

(i)
$$\frac{\partial F_{\xi}}{\partial \theta} = \frac{\partial}{\partial \xi} \left(\xi F_{\theta} \right)$$

(ii)
$$\frac{\partial F_2}{\partial \phi} = \frac{\partial}{\partial r} \left(2 \sin \theta F_e \right)$$

(iii)
$$\frac{\partial}{\partial \theta} (rF_{\theta}) = \frac{\partial}{\partial \theta} (rF_{\theta})$$

Describeres gamme l'yenolem borpancehill que kommonent Fz, Fo n Fq, nonzerranne vakue yanobens:

(i)
$$\partial_{\theta} F_{z} = 2^{\alpha + 1} G_{\theta} \theta e^{G_{\theta} s \varphi}$$

 $\partial_{z} (z F_{\theta}) = G_{\theta} (x \theta) e^{G_{\theta} s \varphi}$

Palenesto 20 ux tacuentoix monestogousex observer benestie mu $\Delta z - 1$

Bam. He anotes pre na 70, two norpames?

A Hangly na nephore me many,

heosxogumo apobepultus bee The gardine
noteminaromoeth, Emosor yseputice le ux

nempora beperubocon (5.0, 6 rose, timo

Lz-1 nogxogut u gue gayeux yantim)

=3= (71) dFz = Extisind (-Sing)e Gosp $\frac{\partial}{\partial c}(z\sin\theta F_{\varphi}) = -\sin\theta \sin(e^{-2}\phi)) \Rightarrow \omega = -1$ (iii) $\partial_{\varphi}F_{\theta} = G_{S}(\chi\theta)(-Sin\varphi)e^{G_{S}\varphi}$ $\partial_{\varphi}(Sin\vartheta F_{\varphi}) = -G_{S}\partial h_{ii}(\varphi)e^{G_{S}\varphi}) = \Delta = \pm 1$ 3geel begnuisio 2 znavenus & [w.n. 618-Ténnae fyrumue), no znavenue d= 1 Re nograque que (i) a (ii). Work, nou $|\alpha = -1|$ bemorkens neodx. Увловия почениривности. В сину меть Myanicape, cinca dyzeur novempuaneana 6 insoes obsaeru R³, не содержения Voren oce Va. Kargén novemmen U(T, 8, 4/(npu d=-1) - BE = Singe God 4 Uz - 2 Sinde (0, 4) $-\frac{\partial u}{\partial \theta} = 2F_0 = 2GS\theta e^{GS}$ $-\frac{\partial u}{\partial \theta} = 2GS\theta e^{GS}$ $-\frac{\partial u}{\partial$ Reoppunator C.

- 34 = ESINDFq = - ESIND hile Cosq =1= 11-2 Sind hispe + 34(4) => \$\P(\phi) = \const Our bein: U(z, 0, 4)= -2 Sinde Cos 4 C) Oбраните внимание, вто почертенная J-yeu 25 - repuesquema no P, a => pasoura cuitor F no + zaunny roug Korutypy boxpyr ocu Oz pabna O u Cura F novemsuaubna bo bet u R3. 8). l'assire auch 43 r. Al 1 T. B. A-B= U(A)-U(B). Been Josepho nynopo akkypanisho nepe-beenin genapinobes kooppinatos Torker B 6 comparence : $x_{B} = y_{B} = 1 \quad x_{B} = 0$ $\frac{1}{2} = \sum_{i=1}^{n} \frac{1}{2} = \sum_{i=1}^{n$ $|UB| = -\sqrt{2} \sin \frac{\pi}{2} \exp(\cos \frac{\pi}{4}) + C = \int_{A \to B} \int_{a}^{\infty} e^{\sqrt{2}} dx$ $= -\sqrt{2} \exp(\sqrt{2}) \left[A_{A \to B} = \sqrt{2} e^{\sqrt{2}} \right]$

Пример 2. Этой пример =5= показывает, гио усло-вия поитенциальности достого сто orpaturu verente. 6 Appureence Dycurs F zagana Координатах. | Fz = & Sin 0 X (4) Fo = f(z) Y(0) Sin24 ρ = χ(ε, φ). Sged 2 - beerseewsbermons noeponeuerp, X(4), Y(8) u f(z) - npouzbououou magnue 6 R3/Oz Synkmu. The recepupo depunyus $\chi(z,y)$ genon-nucleusus uzbecieno, reas hon iganemus bgene supra $\chi=y$, $\chi=0$ na ∞ , ona legem cesse acumentoturecan Kak Hypnens nærre, uper kæraex d, X, X, L u f ceura F Sygent nouteeniquanbrow.

Требуем выполнения кеобхоримых = 6= yellobret nomenguant noerce: (1) 2 Fz = 2 (2 Fo) Repenseure 200 palenceso, pasquiel neperientore: $\frac{Godd}{Y(\theta)} \cdot \frac{X(\psi)}{Sin^2 \phi} = \frac{(cf(z))'}{c^{\alpha}} = c_1 \cdot (x)$ Denvenna C, moner There voulons Koncrantoer & energ negable cuestocta Kooppinar E, du C. no auacommoet npercene uz (*) Horreward pabenciba: $\frac{Cosd}{Y(0)} = \frac{1}{C_2} \qquad \frac{X(4)}{Sin^24} = C_3, \quad 24e$ C2 4 C3 - Koncrantor le Igosuo vera [C3 = C1.C2] - 43 (x). Uran: | 2 (2 f(c)) = c1 2 d 2 (2 f(c)) = C2 60 d X (4) = C1 - C2 m2 4

Due dynnapur f(z) hougement Обыкновенное дифф. уравнение, контрое негко решает се в общем виде. f(z) = { (c, 2x+1 +2), Ze D-luse opna procepousonale (111) Nocucerous Fy he zabeccest or o yerobere 20 Fo = 20 (Sind Fa) gain paletier to. fa18(0) Sin (24) = Coso 2 (2,4) => => Z(2,41= f(z) Z(0) Sin(24) = C2 f(z) Sin(24) = = C2 (9 241 +2) Mid 4 Saver! Babecenescer set Kooppuneeron d'-- yeur l'aung npegoegyunex par-aux pensus. Ecren ou rois ne anyru-loeb, vo p-yeur Z(E, 4) governma Doura ercajasocie Zabreaement or d u mon nomman Dat k morn boperup (r.e. chela Fine Threa ou novembranous non y bretone hoepawerpol Jagaras.

W/robepeen (ii): Offez 2 of (2 Sin of Fe) = 8 = La noument as vouepeaubenno. U, navoners, bochoelsojyence acuento-TUKOUT [12,4). Myr X=y, 2=0 eto beraen le 2 1/4 $Z \mid \xrightarrow{\tau \to \infty} J$, τ , ℓ . => \$\\ \mathre{\pi} = 0, \quad \alpha = -2, \quad \qquad \quad \quad \qq \quad B Wroce: | Fr = - 2 Sind hi 24 | Fq = 2-2 Cos D m² φ | Fq = 2-2 mi 2 φ Kenggen novembre novembre U(2,0,4): U(c, 0, 0) = - & Sind Sind 4 Ones noughereace 25-nepropurlentale p-your no 4 2> F-noreusuantique cura 6 R3/0.

Mpunep 3. Apunep nocispoenen = 9= Лаграннива описание системы Co chiesto. Exepercens in and There (l'actively a rea copepe & R3). Saw | Greve I ggoons Rampabuenus ou OZ.

L- Me become crepner

lacienya m mureet × O e L - Me becomes crep men 2 стыстени Своборы, перависиными коорре-Onuco Collebec narianu Du 4. X = { Sin & Cos 4 (=> T= \(\langle (x^2+g^2+z^2) =\)
= \(\langle (\langle 2g^2+\langle 2sin^20\langle^2)\) y = l hind Sing Z= - Closo 3 ran Samen que noteny. Inextu 11 z mg 2 z - mgl 610 LzT-U= 2/822+82925in20)+mglbs - Le zabueux our 4 (tousse ex 4).

Trabuenue gleencenne no φ : $L_{\varphi} = \frac{\partial \left(\frac{\partial L}{\partial \dot{\varphi}}\right) - \frac{\partial L}{\partial \dot{\varphi}}}{\partial \dot{\varphi}} = \frac{\partial \left(n b^2 \dot{\varphi} \sin^2 \theta\right) = 0$ => Ml 24 mi 20 = y = Coust (A) Trées zaron coxpanence proexise de -ceeura menyebra na octo Da. Passenue gourcemens no 0: Lg= ml20-mlq2/molaso+mgl Sind=0 Ecries Eachine Cinamonaphoe no 9 [1.l. 2 = const) plemenue: Sin % (= - 4261%) = 0 Even 20 ± 0, TO noveyraem chelse yrubbet exapoets y a craemonapusa yrua do: $\phi^2 = \frac{9}{\ell \cos \theta}$

Dousee perme nue yparmenne $L_0 = 11 = 11$ Boenoubyyeure zavouver coxpanience E=T+U= ml202 + ml202 mino - mgl loto. Degemaber 6 cropa que 3 zaroqua Coxpanenue (A), moneno nocupouro pajo Abest hopitipet noney regulate Affectubures одномерноет системы и уберичься, силь Curaqueraproce pennence yourderacto.