Haumu orpanurence chocky Nyaccona

Ha mem 
$$\int h^2 + u^2 - V^2 = 0$$
 $\int V > 0$ 

(\*) Найти удобиць параметризацию пов-ти и высислить ск. П. в терм. этой парам.

$$h = 7 \text{ CMs}$$

$$h = 7 \text{ COS}$$

$$V = 8 \text{ COS}$$

$$7 \text{ COS}$$

16 110

$$C = R = const > 0$$

$$\begin{cases} h, u = \{h, x + y\} = 2v \\ h, v = 2u \end{cases}$$

$$\begin{cases} u, v = -2h \end{cases}$$

$$\frac{d}{dt} = \frac{d}{dt} = \frac{d}{dt}$$

$$\int S' dt = \cos_2 d \left( 5 + \frac{\mu_5}{5n_5} \right) = \cos_2 d \left( \frac{N_5}{5(\mu_5 + n_5)} \right) =$$

$$S[y] = \int_{0}^{1} dx \left( \frac{1}{4} (y')^{2} \log(y^{2}) + xy' + e^{\cos y} \right)$$

a) 
$$SS[y] = \int dx \left( \frac{\partial h}{\partial y} Sy + \frac{\partial h}{\partial y'} Sy' \right)$$

$$= \frac{1}{a} \cdot \frac{1}{4} (yi)^2 - \sin y e^{\cos y}$$

$$= \frac{1}{a} \cdot \frac{1}{4} (y^i)^2 - \sin \theta e^{-\frac{1}{4}}$$

$$\frac{\partial h}{\partial y'} = \frac{1}{4} \cdot 2y' \ln y^2 + x = \frac{1}{2}y' \ln y^2 + x$$

$$SS[y] = \int_{0}^{\infty} dx \left[ \frac{(y)^{2}}{2y} - siny e^{\cos y} \right] Sy + \left( \frac{1}{2}y' \ln y^{2} + x \right) Sy' \right] = \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y'^{2} + x \right) Sy' - \int_{0}^{\infty} \left( \frac{(y)^{2}}{2y'} - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y'^{2} - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy' dx + \left( \frac{1}{2}y' \ln y' - siny e^{\cos y} \right) Sy'$$

$$\left(\frac{3}{2}y - \sin y \in \cos y\right) = \frac{2}{1+1} \left[8y \, dx\right] = \frac$$

$$-\int_{0}^{\pi} \left[\frac{1}{2}(y'') \ln y^{2} + y' \cdot \frac{2}{y'}\right] + 1 \int_{0}^{\pi} Sy \, dx =$$

$$= \int_{0}^{\pi} \left(\frac{(y')^{2}}{2y'} - \sin y \cos y - \frac{1}{2}y'' \ln y^{2} - \frac{y'}{y'} - 1\right) Sy \, dx +$$

8) 
$$y(0) = A \rightarrow 8y(0) = 0$$
  
 $8y(1) \forall = 7 \frac{1}{2}y' \ln y^2 + x \Big|_{x=1} = 0$ 

$$F[y] + a C^{2}[o_{1}J] : y(1) = 0$$

$$F[y] = \int_{0}^{1} dx((y^{2})^{2} - 2xy)$$

$$\begin{array}{lll}
& = \int_{0}^{1} dx \left( (y' + 6y')^{2} - 2x(y + 8y') \right) & = \\
& = \int_{0}^{1} dx \left( (y' + 6y')^{2} - 2x(y + 8y') \right) & = \int_{0}^{1} dx \left( (y')^{2} - 2xy' \right) & = \\
& = \int_{0}^{1} dx \left( 2y'(8y') + (8y')^{2} - 2xy' - 2x8y - (yx')^{2} + 2xy' \right) & = \\
& = \int_{0}^{1} dx \left( 2y'(8y') + (8y')^{2} - 2x8y - 2x8y - (yx')^{2} + 2xy' \right) & = \\
& = \int_{0}^{1} dx \left( 2y'(8y') + (8y')^{2} - 2x8y - 2x8y - (yx')^{2} + 2xy' \right) & = \\
& = \int_{0}^{1} 2y'(8y') + 2y''(8y') & = \int_{0}^{1} 2x^{2} + 2xy''(8y') + 2y''(8y') & = \int_{0}^{1} 2x^{2} + 2xy''(8y') & = \int_{0}^{1} 2y''(8y') + 2y''(8y') & = \int_{0}^{1} 2y''(8y') & = \int_{0}^{1} 2x^{2} + 2xy''(8y') & = \int_{0}^{1} 2x^{2} + 2xy'' & = \int_{0}^{1} 2x^$$

- 5 { gdx (1,1 +x)

$$= -2 \int_{0}^{1} dx (y'' + x) \delta y + 2 y' \delta y \Big|_{0}^{2} = 0$$

$$d_{II} + \times = 0$$

$$y' = -\frac{x^2}{2} + C_1$$

$$y'' = -\int \frac{x^2}{2} dx + C_1 x = -\frac{1}{2} \cdot \frac{x^3}{3} + C_1 x + C_0$$

$$y(x) = -\frac{x^3}{6} + c_1 x + c_0 (*)$$

Tpauvenne youbbre 8 m. x = 0

$$2y' \mid_{X=0} = 0$$
 (Sy - npouzh. b m.  $x = 0$ )

$$\Rightarrow$$
  $c_0 = \frac{1}{6}$ .

$$y'(0) = -\frac{x^2}{2} + C_1 \Big|_{x=0} = + C_1 = 0 \Rightarrow C_1 = 0$$

$$= 7 \left[ y(x) = -\frac{x^3}{6} + \frac{1}{6} \right]$$

Mat. m. 8 
$$\mathbb{R}^2$$
 glunc hog quieté  $F: \overrightarrow{F} = (F_x, F_y)$ 

$$\forall x, y \in \mathbb{R} : \left| F_x = -2xy - \frac{(1+x)^2}{1+x^2} \right|$$

$$|F_y = -x^2 + \frac{2y}{1+y^2}$$

a) Rokajato: F-nomunquamna > Hauty U(x,y)=?

$$\alpha) \frac{3x}{3E^{\alpha}} = \frac{3\lambda}{3E^{\alpha}} \quad (*)$$

$$\frac{3F_{x}}{3F_{x}} = -2x$$

$$\Rightarrow (x) \text{ Benomino}$$

$$\Rightarrow b - 80 \text{ B}_{5} \text{ a chargehold}$$

$$\Rightarrow b - 80 \text{ B}_{5} \text{ a chargehold}$$

=> no remuse Nyankape (\*) abr-ce gormamorusu yenobulu=>
=> cura == nomenizuamua.

$$\exists U(x,y): \frac{\partial U}{\partial x} = -F_{x} = 2xy + \frac{(1+x)^{2}}{1+x^{2}}$$

$$\frac{\partial U}{\partial y} = -F_{y} = x^{2} - \frac{2y}{1+y^{2}}$$

$$= x + \int \frac{dx^{2}}{1+x^{2}} dx = x^{2} + \int \frac{(1+x)^{2}}{1+x^{2}} dx = x^{2} + \ln(x^{2}+1) + x + C(y)$$

$$x^{2} + C'(y) = x^{2} - \frac{2y}{1+y^{2}}$$

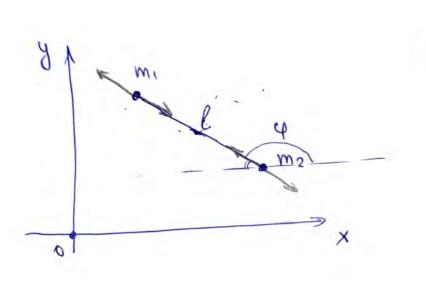
$$C'(y) = -\frac{2y}{1+y^{2}} - \frac{dq^{2}}{1+y^{2}}$$

$$C(y) = -2 \int \frac{dy}{1+y^{2}} dy = -\ln(y^{2}+1) + C$$

$$U(x_{1}y) = x^{2}y + \ln(x^{2}+1) + x - \ln(y^{2}+1) + C$$

T. k. cura nomunquanobla

$$= U(1,0) - U(0,1) = \ln 2 + 1 - \ln 2 = 1.$$



Oбобизенные координаты:

a) 
$$x_{m_1} = l \cos q + x$$
  
 $y_{m_1} = l \sin q + y$ 

$$= \frac{m_{z}}{2} (\dot{x}^{2} + \dot{y}^{2}) + \frac{m_{1}}{2} (\dot{x}^{2} + \dot{y}^{2} + \ell^{2}\dot{q}^{2} + \ell^{2}\dot{q}^{2} + \ell^{2}\dot{q}^{2} + \ell^{2}\dot{q}^{2} + \ell^{2}\dot{q}^{2}) + 2\ell\sin^{2}\dot{q}^{2})$$

$$U = -G \frac{m_1 m_2}{e}$$

$$L_{x} := \frac{d}{dt} \left( m_{2} \dot{x} + m_{1} \dot{x} + m_{1} l \dot{\varphi} \cos \varphi \right) = 0$$

$$hy := \frac{d}{dt} \left( (m_1 + m_2)\dot{q} + m_2 \ell \dot{q} \sin \varphi \right) = 0$$

$$L\varphi := \frac{d}{dt} \left( m_i \ell^2 \dot{\psi} + m_i \ell \cos \dot{\psi} + m_i \ell \sin \dot{\psi} \right) - \left( m_i \ell \cos \dot{\psi} \dot{\psi} \right) - m_i \ell \sin \dot{\psi} \dot{\psi} = 0$$

$$- m_i \ell \sin \dot{\psi} \dot{\psi} \dot{\psi} = 0$$

$$y(1) = 0$$

$$-2xy \Rightarrow y_{3} = x_{cmp}(x) = 7$$

$$F[y], y \in C^{2}[0,1], y(1) = 0$$

$$F[y] = \int dx((y')^{2} - 2xy) \Rightarrow y_{3}kcmp(x) = ?$$
A. F. T. T. T.

$$[A] = \int dx ((A_i)_5 - 5xA) \Rightarrow \lambda^{3} \times (5A_1 + 6A_2) = \int dx (5A_1 + 6A_2$$

$$\Delta F[y] = F[y + sy] - F[y] = \int_{0}^{\infty} dx (sy'sy' - sxsy) + o(1sy11)$$

$$8F[y] = 2 \int_{0}^{1} dx (y' \delta y' - x \delta y) =$$

$$\partial u = x \int dx (d, gd, -x gd) =$$

$$= 2y' \, \delta y \, |'_0 - 2 \int dx \, (y'' + x) = 0$$

$$dy' \delta y = 0$$
 -  $2 \int dx (y'' + x) = 0$ 

$$y(1) = 0 \implies 5y(1) = 0 \implies y' \in m. \quad x = 1$$
 workern inpulminate  $\forall y$  war.

$$g(0)$$
 He jagukcupoban  $\Rightarrow$  Sy B m.  $x=0$  m.d.  $\forall \Rightarrow g'(0)=0$ 

$$A_{u} + x = 0$$

$$y'' + x = 0$$
  
 $y'' + x = 0$   
 $y'' + x = 0$ 

$$\begin{cases} y(1) = 0, \ y'(0) = 0 \\ y(x) = -\frac{1}{6} x^3 + c_1 x + c_2 \\ c_1 = 0, \ c_2 = \frac{1}{6} \end{cases}$$

$$f. \ \forall \Rightarrow (y'(0) = 0)$$

 $A^{3\kappa} cmb(x) = -\frac{9}{4}(x_3-1)$ 

$$(0) = 0$$

$$S[x,y] = \int dt (x^{2}y^{-4} + y^{2}t^{2} - x^{2}y^{2}t)$$

$$\tilde{X} = e^{E}x, \quad \tilde{y} = e^{aE}y, \quad \tilde{t} = e^{bE}t$$

$$S[\tilde{x},\tilde{y}] = \int d\tilde{t} e^{-bE} \left[ e^{a(b-1)} (\tilde{x}^{1})^{2} e^{4aE} \tilde{y}^{-4} + e^{a(b-a)E} (\tilde{y}^{1})^{2} e^{-abE} \tilde{t}^{2} - e^{-2aE-2E} \tilde{x}^{2} \tilde{y}^{2}. e^{-bE} \tilde{t} \right] =$$

$$= \int d\tilde{t} \left( e^{(ab-2-b+4a)E} (\tilde{x}^{1})^{2} \tilde{t}^{2} - e^{(2b-2a-b-2b)E} (\tilde{y}^{1})^{2} \tilde{t}^{2} - e^{-(2a+2b+2)E} \tilde{x}^{2} \tilde{y}^{2} \tilde{t} \right)$$

$$\int b + 4a - 2a = 0$$

$$2a + b = 0$$

$$2a + 2b + 2 = 0$$

$$1 = 1$$

$$1 = 0$$

$$2a + 2b + 2 = 0$$

Npu 
$$\varepsilon = 0$$
 hpeodpajobanue mongeembenner
$$\xi_0 = \frac{\partial \xi}{\partial \varepsilon} \Big|_{\varepsilon=0} = -2t$$

$$\xi x = \frac{3\xi}{3\xi} \Big|_{\xi=0} = x$$

$$I = \frac{\partial L}{\partial \dot{x}} \xi_{x} + \frac{\partial L}{\partial \dot{y}} \xi_{y} + \left( L - \dot{x} \frac{\partial L}{\partial \dot{x}} - \dot{y} \frac{\partial L}{\partial \dot{y}} \right) \xi_{0}$$

$$I = 2 \times \dot{x} y^{-4} + 2 y \dot{y} t^{2} + 2 t \dot{x}^{2} y^{-4} + 2 t^{3} \dot{y}^{2} + 2 x^{2} y^{2} t^{3}$$

$$b = -mc^2 \left( 1 - \frac{\dot{\chi}^2}{C^2} \right)$$

a) 
$$p_i = \frac{\partial h}{\partial \dot{x}_i} = \frac{m \dot{x}_i}{1 - \frac{\dot{x}^2}{C^2}} \Rightarrow \vec{p} = \frac{m \dot{x}}{1 - \frac{\dot{x}^2}{C^2}}$$

$$\vec{p}^2 = \frac{\vec{m}^2 \vec{x}^2}{1 - \frac{\vec{x}^2}{C^2}} \Rightarrow \vec{x}^2 = \frac{\vec{p}^2 C^2}{\vec{p}^2 + \vec{m}^2 C^2}$$

$$1 - \frac{\dot{x}^{2}}{C^{2}} = \frac{m^{2}C^{2}}{\dot{p}^{2} + m^{2}C^{2}} \implies \dot{p} = \frac{\dot{x}}{c} \sqrt{\dot{p}^{2} + m^{2}C^{2}} \implies$$

$$\Rightarrow \dot{X} = \frac{\dot{p}c}{\sqrt{\dot{p}^2 + m^2c^2}}$$

$$E = \frac{\dot{x}}{x} \frac{3\dot{x}}{3\dot{x}} - \lambda = \frac{MC^2}{\sqrt{1 - \frac{\dot{x}^2}{C^2}}}$$

$$H = E |_{\dot{X} = \dot{X}(\dot{p})} = H = C \sqrt{\dot{p}^{2} + m^{2}c^{2}}$$

$$\begin{cases} \hat{x}_i = \frac{\partial H}{\partial p_i} = \frac{\partial P_i}{\partial p_i^2 + m^2 C^2} \\ \hat{p}_i = -\frac{\partial H}{\partial x_i} = 0 \implies p_i(t) = p_i = const \end{cases}$$

$$6) H = C \sqrt{\vec{p}^2 + m^2 C^2} = \text{const} = \mathcal{E}$$

$$\dot{\vec{z}} = \frac{C^2}{\mathcal{E}} \vec{p} = \frac{C^2}{\mathcal{E}} \vec{p}_0$$

$$\vec{X}(t) = \frac{\varepsilon}{c^2} \vec{p}_0 t + \vec{X}^{(0)} \cdot \vec{X}^{(0)} = 0$$

$$\vec{p}(t) = \vec{p}_0; \vec{\chi}(t) = \frac{c^2}{\varepsilon} \vec{p}_0 t \log \varepsilon = c \sqrt{\vec{p}_0^2 + m^2 c^2}$$

$$\beta R^3$$
:  $h^2 + u^2 - v^2 = 0$ 

 $N = V\cos\varphi$ ,  $u = V\sin\Psi$ , v = v  $V \in (0, +\infty)$  $V \in [0, +2\pi)$ 

$$f(h,u,v)=0$$
  $\beta \mathbb{R}^3$ 

$$h = h(\xi, \eta), \quad u = u(\xi, \eta), \quad v = v(\xi, \eta)$$

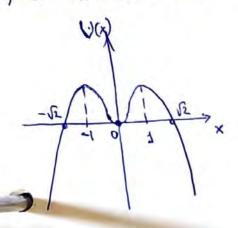
$$\cos \varphi = \frac{h}{v} \implies \{\cos \varphi, v\} = -\sin \varphi \, \{ \psi, v \}$$

$$\left\{\frac{h}{v},v\right\} = \frac{1}{v}\left\{h,v\right\} = \frac{2u}{v}$$

5-munymka.
[18.20.21]

Pazobata nopmpem-jabucumocmi \*(x)

(1) 
$$\ddot{x} + 2x - 2x^3 = 0 \iff m\ddot{x} = F = -U'(x)$$



$$\ddot{x} + 2x - 2x^3 = 0 \iff \ddot{y} = -2x + 2x^3$$

(0,0), (1,0), (-1,0)

morku nokol

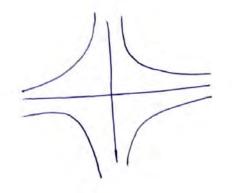
стационарные реш-ше x = 0, x = 1, x = -7

Линеаризуем в окр-ти особых точк

$$(\pm 1,0)$$
  $\dot{x} = 4$   
 $\dot{y} = -2(x \mp 1) + 2(x \mp 1)^3 = 4x + 2x^3 \mp 6x^2$ 

$$\begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = A_{\pm 1} \begin{pmatrix} x \\ y \end{pmatrix}, \quad A_{\pm 1} = \begin{pmatrix} 0 & 1 \\ 4 & 0 \end{pmatrix}$$

$$\chi_{\pm} = \chi_{5-4} \Rightarrow \chi_{4,2} = \pm \ell \operatorname{cegno}_{1}$$

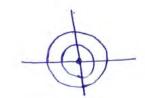


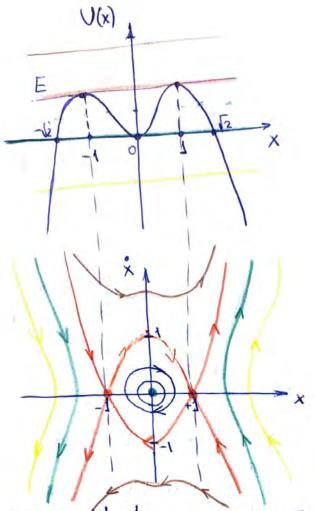
$$(0,0) \quad \begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = A_0 \begin{pmatrix} x \\ y \end{pmatrix}, \quad A_0 = \begin{pmatrix} 0 & 1 \\ -2 & 0 \end{pmatrix}$$

$$x_0 = \lambda^2 + 2 \implies \lambda_{1,2} = \pm \sqrt{2}i$$

Real XI,2 = 0 => mu npudmike. He gocmamoruo, amoder ombemumi ha Bonpoc od ycmoticubocmu.

$$\frac{d}{dt}\left(\frac{\dot{x}^2}{2} + x^2 - \frac{x^4}{2}\right) = 0 \implies E(x, \dot{x}) = \dot{x}^2 + 2x^2 - x^4 - \text{unbapuaum}$$
360 subquu





$$U'(x) = 4(x-x^3) = 0$$

$$\dot{X} = -X^2 + 1$$

$$E = 0 = 73$$
 payobne kp.  $E = 1 = > 8$  spayobne kp.

$$E = -1 \Rightarrow 2$$
 grayobre kp  $E = 2 \Rightarrow 2$  grayobre kp.

$$\begin{cases}
m\ddot{x} = -k_1x - k_2(x-y) \\
m\ddot{y} = k_2(x-y)
\end{cases}$$

$$TI J-H HEHOMOHQ$$

$$F_q = -F_{np}$$

$$\ddot{x} = -AX, \quad \chi(t) = \begin{pmatrix} \chi(t) \\ y(t) \end{pmatrix}$$

$$A = \frac{1}{m} \begin{pmatrix} k_1 + k_2 & -k_2 \\ -k_2 & k_2 \end{pmatrix} = \frac{k}{m} \begin{pmatrix} 5 & -2 \\ -2 & 2 \end{pmatrix}$$

$$\lambda_1 = \omega_1^2 = \frac{k}{m}$$
,  $\lambda_2 = \omega_2^2 = \frac{6k}{m}$   
 $\lambda_1 = \omega_1^2 = \frac{k}{m}$   
 $\lambda_2 = \omega_2^2 = \frac{6k}{m}$ 

Hope. moget 4: coswit, 4: sinwit = 1.2 moget

$$\begin{cases} x & x \\ x & x \\ y & x \\ y$$

$$\begin{cases} m\ddot{x} = -k_{1}x - k_{2}(x-y) & \text{nocenny Hem } \mathbb{Z}? \\ 2m\ddot{y} = +k_{2}(x-y) - k_{2}(y-\mathbb{Z}) \\ m\ddot{z} = +k_{2}(y-\mathbb{Z}) - k_{1}\mathbb{Z} \end{cases}$$

$$X = -AX$$

$$A = \frac{1}{m} \begin{pmatrix} k_1 + k_2 & -k_2 & 0 \\ -\frac{k_2}{2} & k_2 & -\frac{k_2}{2} \\ 0 & -k_2 & k_1 + k_2 \end{pmatrix} = \frac{k}{m} \begin{pmatrix} 5 & -2 & 0 \\ -1 & 2 & -1 \\ 0 & 2 & 5 \end{pmatrix}$$

$$y_3 = M_{5_5}^2 = \frac{M}{K} \longrightarrow A_7 = \begin{pmatrix} 1 \\ 5 \end{pmatrix}$$

$$y_4 = M_{5_5}^2 = \frac{M}{K} \longrightarrow A_7 = \begin{pmatrix} 1 \\ 5 \end{pmatrix}$$

$$y_5 = M_{5_5}^2 = \frac{M}{K} \longrightarrow A_7 = \begin{pmatrix} 1 \\ 5 \end{pmatrix}$$

$$y_6 = M_{5_5} = \frac{M}{K} \longrightarrow A_7 = \begin{pmatrix} 1 \\ 5 \end{pmatrix}$$

$$y_7 = M_{5_5} = \frac{M}{K} \longrightarrow A_7 = \begin{pmatrix} 1 \\ 5 \end{pmatrix}$$

$$y_8 = \begin{pmatrix} 1 \\ 5 \end{pmatrix}$$

$$L(\vec{x}, \vec{x}) = (-mc^2)\sqrt{1 - \frac{\dot{\vec{x}}^2}{c^2}}$$
KOUCTANTA

$$b^{x} = \frac{3x}{3y} = -mc^{2} \frac{1/2}{\sqrt{1-\frac{x^{2}}{2}}} \left(-\frac{2x}{2}\right) =$$

$$= + \frac{mc^2}{2^2\sqrt{1-\frac{\dot{\chi}^2}{C^2}}}$$

$$=\frac{m\overset{\bullet}{x}}{\sqrt{1-\overset{\bullet}{x}^2}}=\sqrt{1-\frac{\overset{\bullet}{x}}{C^2}}=\frac{m\overset{\bullet}{x}}{p_x}$$

$$H = p_{x} \dot{\vec{x}} + b = \frac{m\dot{\vec{x}}}{\sqrt{1 - \frac{\dot{x}^{2}}{C^{2}}}} \dot{\vec{x}} + mc^{2} \sqrt{1 - \frac{\dot{x}^{2}}{C^{2}}} \left| \dot{\vec{x}} = \frac{p_{x}^{2}c^{2}}{mc^{2}+b} \right|$$

$$\dot{x} = \sqrt{\frac{w_3 C_5 + b x_5}{b x_5 C_5}}$$

$$b \times \sqrt{1 - \frac{C_5}{x_5}} = m x$$

$$H = \frac{1 - \frac{w_5 G_5 + b_{x_5}}{b_{x_5}}}{w_5 G_5 + w_{G_5}} + w_{G_5} \sqrt{1 - \frac{w_5 G_5 + b_{x_5}}{b_{x_5}}} =$$

$$H = \frac{\sqrt{m_3C_3 + bx_5}}{bx_5c} + \frac{bx}{m_5c_5} \cdot \frac{\sqrt{m_3C_3 + bx_5}}{bx_5c} = \frac{\sqrt{m_3C_3 + bx_5}}{bx_5c + m_5c_3}$$

S) in man 18 4m

18:15

$$x = \frac{9b^{2}}{9H} = \frac{8b \times C}{(8b \times C) \sqrt{m_{3}c_{5} + bx_{5}}} - \frac{2}{\sqrt{\frac{2b^{2}c_{5} + bx_{5}}{8b^{2}}}} \left(bx_{5}c_{5} + m_{5}c_{5}\right)$$

$$= 5b \times (m_5 c_5 + b_5) - b \times (b_5 c + m_5 c_3)$$

WARREN - WIR BERN

好女

Mat. m. 8 
$$\mathbb{R}^2$$
 glunc hog quieté  $F: \overrightarrow{F} = (F_x, F_y)$ 

$$\forall x, y \in \mathbb{R} : \left| F_x = -2xy - \frac{(1+x)^2}{1+x^2} \right|$$

$$\left| F_y = -x^2 + \frac{2y}{1+y^2} \right|$$

a) Nokajato: F-homunynamna > Hañty U(x,y)=?

$$\alpha) \frac{3x}{3E^{4}} = \frac{3\lambda}{3E^{x}} \quad (*)$$

$$\frac{3F_{x}}{3F_{x}} = -2x$$

$$\Rightarrow (x) \text{ Benomino}$$

$$\Rightarrow b - 80 \text{ B}_{5} \text{ a chargehold}$$

$$\Rightarrow b - 80 \text{ B}_{5} \text{ a chargehold}$$

=> no remuse Nyankape (\*) abr-ce gormamorusu yenobulu=>
=> cura == nomenizuamua.

$$\exists U(x,y): \frac{\partial U}{\partial x} = -F_{x} = \lambda xy + \frac{(1+x)^{2}}{1+x^{2}}$$

$$\frac{\partial V}{\partial y} = -F_{y} = x^{2} - \frac{2y}{1+y^{2}}$$

$$U(x,y) = + \int dx \left(2xy + \frac{(1+x)^{2}}{1+x^{2}}\right) = 2y \frac{x^{2}}{x} + \int \frac{(1+x)^{2}}{1+x^{2}} dx =$$

$$= x^{2}y + \ln(x^{2}+1) + x + C(y)$$

$$x^{2} + c'(y) = x^{2} - \frac{2y}{1+y^{2}}$$

$$c'(y) = -\frac{2y}{1+y^{2}} - \frac{dg^{2}}{1+g^{2}}$$

$$c(y) = -2 \int \frac{dy}{1+y^{2}} dy = -\ln(y^{2}+1) + C$$

$$U(x_{1}y) = x^{2}y + \ln(x^{2}+1) + x - \ln(y^{2}+1) + C$$

T. k. cura nomunquanobla

$$= U(1,0) - U(0,1) = \ln 2 + 1 - \ln 2 = 1.$$

$$F[y] + a C^{2}[o_{1}J] : y(1) = 0$$

$$F[y] = \int_{0}^{1} dx((y^{2})^{2} - 2xy)$$

$$\begin{array}{lll}
& = \int_{0}^{1} dx \left( (y' + 6y')^{2} - 2x(y + 8y') \right) & = \\
& = \int_{0}^{1} dx \left( (y' + 6y')^{2} - 2x(y + 8y') \right) & = \int_{0}^{1} dx \left( (y')^{2} - 2xy' \right) & = \\
& = \int_{0}^{1} dx \left( 2y'(8y') + (8y')^{2} - 2xy' - 2x8y - (yx')^{2} + 2xy' \right) & = \\
& = \int_{0}^{1} dx \left( 2y'(8y') + (8y')^{2} - 2x8y - 2x8y - (yx')^{2} + 2xy' \right) & = \\
& = \int_{0}^{1} dx \left( 2y'(8y') + (8y')^{2} - 2x8y - 2x8y - (yx')^{2} + 2xy' \right) & = \\
& = \int_{0}^{1} 2y'(8y') + 2y''(8y') & = \int_{0}^{1} 2x^{2} + 2xy''(8y') + 2y''(8y') & = \int_{0}^{1} 2x^{2} + 2xy''(8y') & = \int_{0}^{1} 2y''(8y') + 2y''(8y') & = \int_{0}^{1} 2y''(8y') & = \int_{0}^{1} 2x^{2} + 2xy''(8y') & = \int_{0}^{1} 2x^{2} + 2xy'' & = \int_{0}^{1} 2x^$$

- 5 { gdx (1,1 +x)

$$= -2 \int_{0}^{1} dx (y'' + x) \delta y + 2 y' \delta y \Big|_{0}^{2} = 0$$

$$d_{II} + \times = 0$$

$$y' = -\frac{x^2}{2} + C_1$$

$$y'' = -\int \frac{x^2}{2} dx + C_1 x = -\frac{1}{2} \cdot \frac{x^3}{3} + C_1 x + C_0$$

$$y(x) = -\frac{x^3}{6} + c_1 x + c_0 (*)$$

Tpauvenne youbbre 8 m. x = 0

$$2y' \mid_{X=0} = 0$$
 (Sy - npouzh. b m.  $x = 0$ )

$$\Rightarrow$$
  $c_0 = \frac{1}{6}$ .

$$y'(0) = -\frac{x^2}{2} + C_1 \Big|_{x=0} = + C_1 = 0 \Rightarrow C_1 = 0$$

$$= 7 \left[ y(x) = -\frac{x^3}{6} + \frac{1}{6} \right]$$

$$S[y] = \int_{0}^{1} dx \left( \frac{1}{4} (y')^{2} \log(y^{2}) + xy' + e^{\cos y} \right)$$

a) 
$$SS[y] = \int dx \left( \frac{\partial h}{\partial y} Sy + \frac{\partial h}{\partial y'} Sy' \right)$$

$$\frac{\partial L}{\partial y} = \frac{1}{4} (y')^2 \cdot 2y' + e^{\cos y} (-\sin y) =$$

$$= \frac{1}{a} \cdot \frac{1}{4} (y')^2 - \sin \theta e^{\cos \theta}$$

$$= \frac{1}{a} \cdot \frac{1}{4} (yi)^2 - \sin y e^{\cos y}$$

$$= \frac{1}{a} \cdot \frac{1}{3} (y')^2 - \sin \theta e^{-\frac{1}{3}}$$

$$\frac{\partial h}{\partial u'} = \frac{1}{4} \cdot 2y' \ln y^2 + x = \frac{1}{2}y'^2$$

$$= \int_{S}^{S} \left( \frac{(y')^2}{2y} - \sin y e^{\cos y} - \frac{1}{2} y'' \ln y^2 - \frac{y'}{y} - 1 \right) Sy dx +$$

8) 
$$y(0) = A \rightarrow 8y(0) = 0$$
  
 $8y(1) \forall = 7 \frac{1}{2}y' \ln y^2 + x |_{x=1} = 0$ 

$$S[y] = \int_{0}^{1} dx \left( \frac{1}{4} (y^{i})^{2} \log(y^{2}) + xy^{i} + e^{\cos y} \right)$$

a) 
$$8S[y] = \int_0^1 dx \left( \frac{\partial y}{\partial h} \delta y + \frac{\partial y}{\partial y} \delta y' \right)$$

$$\frac{\partial A}{\partial r} = \frac{A}{4} \cdot (A_1)_5 \cdot \frac{\partial R}{\partial r} \cdot \frac{A}{4} \cdot 3A + 6\cos A \left(-2i\lambda A\right) =$$

$$= \frac{1}{a} \cdot \frac{1}{4} (y')^2 - \sin y e^{\cos y}$$

$$\frac{\partial L}{\partial y'} = \frac{1}{4} \cdot 2y' \ln y^2 + x = \frac{1}{2}y' \ln y^2 + x$$

$$8S[y] = \int_{0}^{\infty} dx \left[ \left( \frac{(y')^2}{2y} - \sin y \cos y \right) Sy + \left( \frac{1}{2}y' \ln y^2 + x \right) Sy' \right] = \frac{1}{2} \left[ \frac{1}{2}y' \ln y^2 + x \right]$$

$$= \int_{-\infty}^{\infty} \left( \frac{(y_1)^2}{2y} - \sin y e^{\cos y} - \frac{1}{2} y'' e^{-y} - 1 \right) 8y dx + \left( \frac{1}{2} y' e^{-y} + x \right) 8y \Big|_{0}^{1}$$