

①

MERGING is a process of combining two sorted list into single list.

Ex:-

| A                  | B                | C (Merge)        |
|--------------------|------------------|------------------|
| $i \rightarrow 2$  | $5 \leftarrow j$ | $2 \leftarrow k$ |
| $i \rightarrow 8$  | $9 \leftarrow j$ | $5 \leftarrow k$ |
| $i \rightarrow 15$ | $12$             | $8 \leftarrow k$ |
| $i \rightarrow 18$ | $17$             | $9$              |
|                    |                  | $12$             |
|                    |                  | $15$             |
|                    |                  | $17$             |
|                    |                  | $18$             |

if  $A[i] < B[j]$   
then  $A[i]$   
Copy to  $C$   
 $i++$

Now check  
 $A[i] < B[j]$   
 $A[2] < B[1]$   
 $8 < 5$   
then Copy  $B[j]$   
to  $C$   
 $j++$

Same way

In general  
let  $m$  element

0

directly  
paste

let  $n$  element

$(m+n)$  element.

$\downarrow$   
 $O(m+n)$  complexity

ALGORITHM MERGE (A, B, m, n)

{  
 $i=1, j=1, k=1$

while ( $i \leq m \ \& \ j \leq n$ )

{ if  $A[i] < B[j]$

$C[k++] = A[i++];$

else

$C[k++] = B[j++];$

}

for ( $i \leq m; i++$ )

$C[k++] = A[i];$

for ( $j \leq n; j++$ )

$C[k++] = B[j];$

// or  $C[k] = A[i]$   
 $i++;$   
 $k++;$

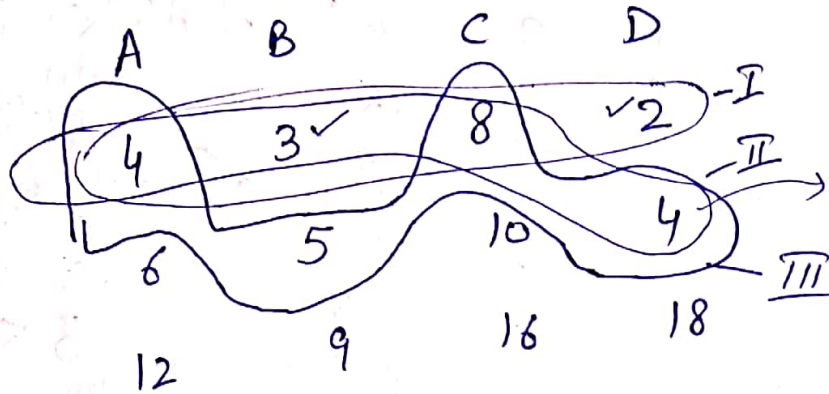
when size of Two list Diff:-  
for remaining  
elements then  
simply copy in  
 $C$

same or  
current place  
of  $i$  don't  
initialize it

}

★ If more than 2 list is given then  
How Merging is done?

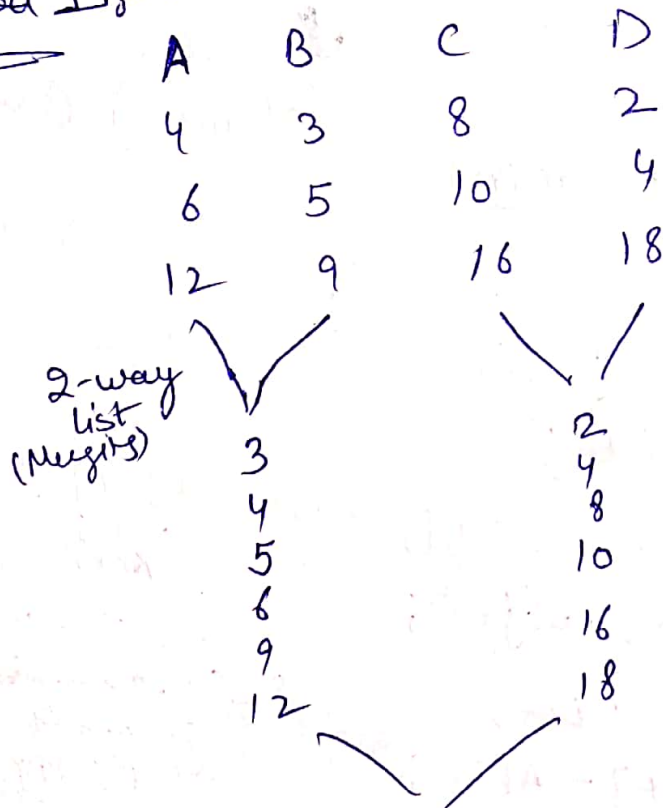
Example:- let 4 list we have to Merge called 4-way Merge List.



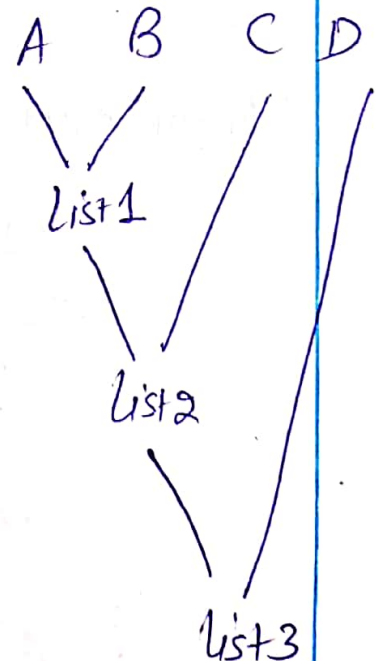
L (Merge list)  
 ② (smallest)  
 ③ (smallest)  
 ④ (smallest)  
 ...

If M-list have to merge then  
called as M-way Merging

Method 1:-

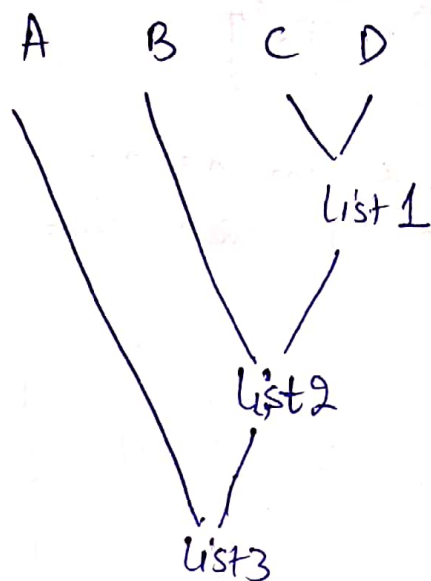


Method 2:-



Method 3:-

↳ Various Method:-



\* So, when we go for 2-way Merging & you have multiple list then you can merge them in various patterns.

2-way Merge Sort :-

2-way merge sort is a iterative process / ~~repeating~~ repeating procedure using loop.

& Merge Sort → is a recursive procedure using recursive algorithm.



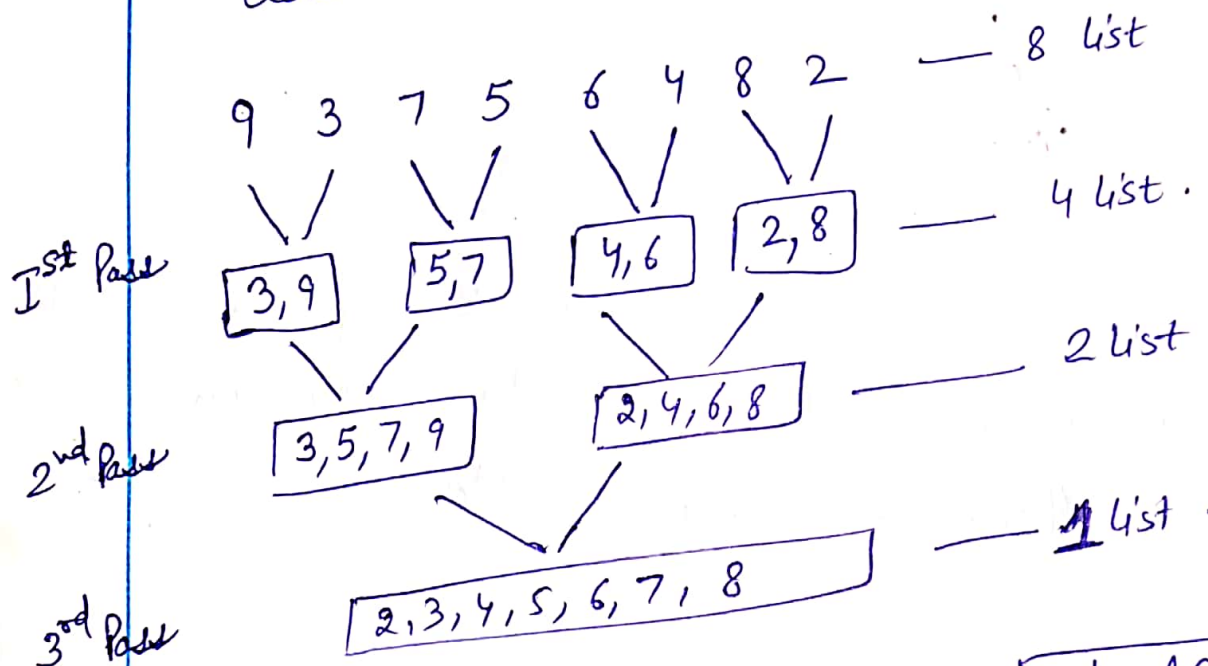
Example 8-

2-way Merge Sort.

A = 

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 9 | 3 | 7 | 5 | 6 | 4 | 8 | 2 |

Assume that each element in array is a list. So, there are 8 list containing 1 element in each list.



$$\frac{8}{2} = 1$$

$$\frac{2}{2} = 1$$

$$\frac{8}{2^3} = 1$$

$$8 = 2^3$$

$$\log_2 8 = 3$$

n element merge

n element merge

n element merge

No. of Passes =  $\log n$  required

$$O(n \log n)$$

# MERGE SORT :-

MERGE-SORT (A, p, r)

- 1) if  $p < r$
- 2)  $q = \lfloor (p+r)/2 \rfloor$
- 3) MERGE-SORT (A, p, q) —  $T(n/2)$
- 4) MERGE-SORT (A, q+1, r) —  $T(n/2)$
- 5) MERGE (A, p, q, r) —  $n$  (element)

when something is raising by 2 every time & is power of 2 lastly.

So,  $\frac{8}{2^3} = 1$

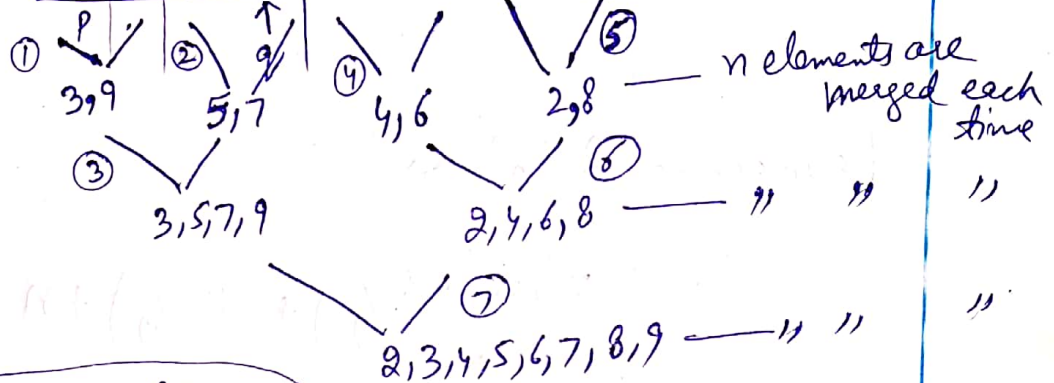
$8 = 2^3$

$\log_2 8 = 3$

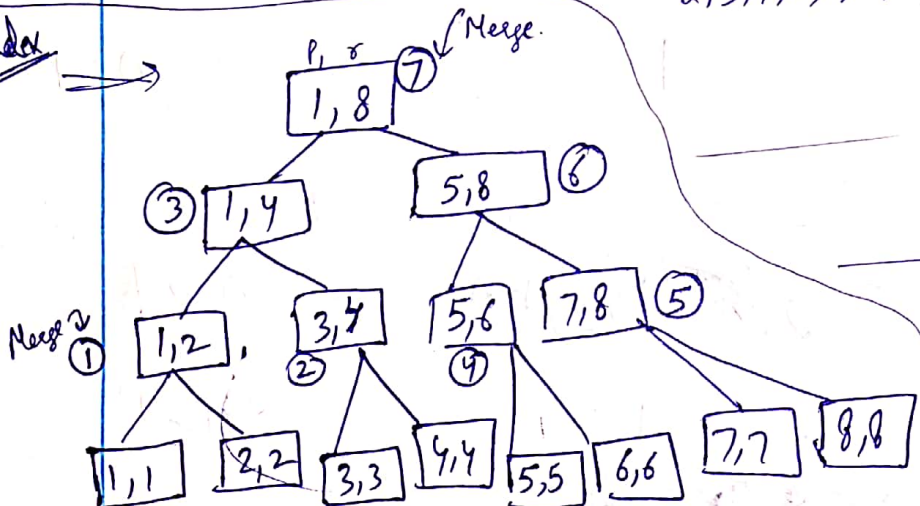
$\log n$  — In general

Example:-

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 9 | 3 | 7 | 5 | 6 | 4 | 8 | 2 |



Index



for 8 element = 3 levels

ie  $\log_2 8 = 3$

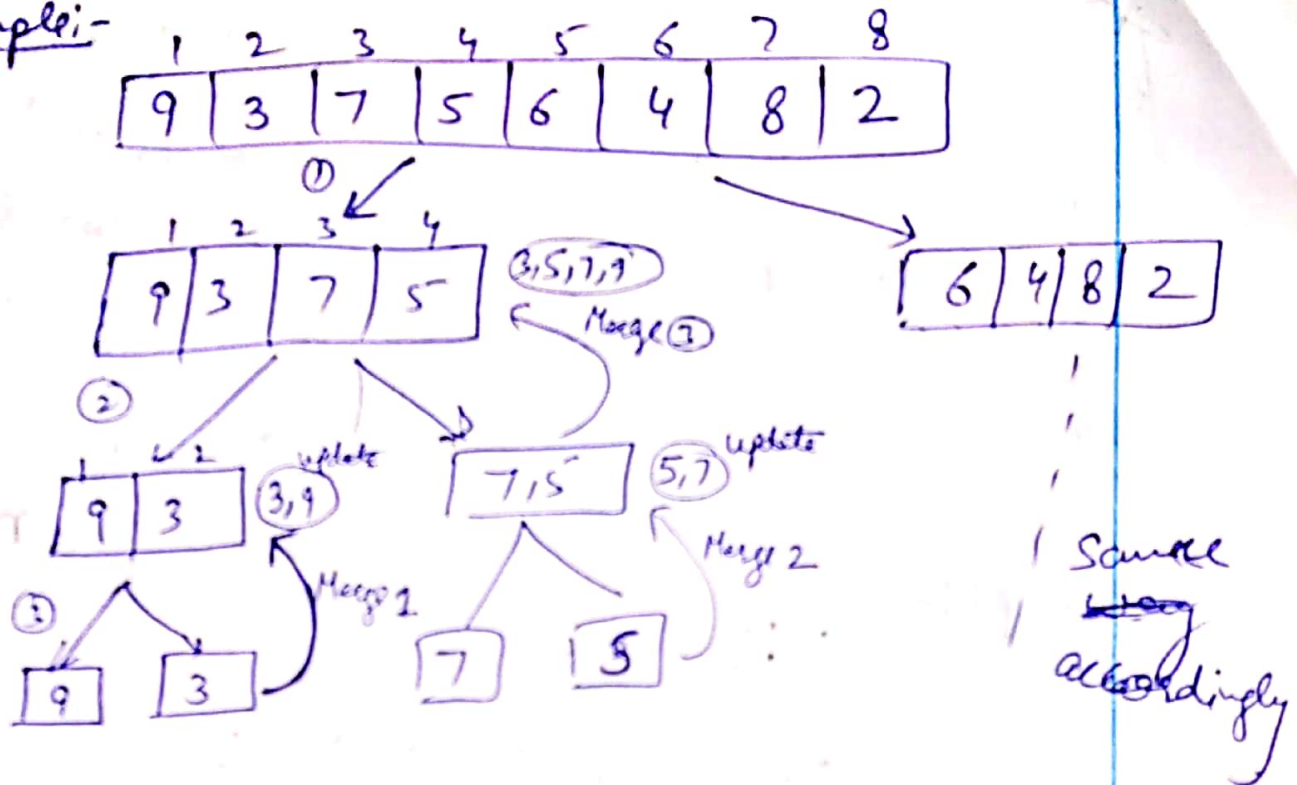
$n \times \log n$

total level

$O(n \log n)$

Acc. to algorithm:-

Example:-



Recurrence Relation:-

$$T(n) = \begin{cases} T(n/2) + T(n/2) + n & n > 1 \\ 1 & n = 1 \end{cases}$$

$$= \begin{cases} 2T(n/2) + n & n > 1 \\ 1 & n = 1 \end{cases}$$

Using Master's Theorem

$$O(n \log n) \text{ ans.}$$