

show that  $P \Rightarrow (Q \Rightarrow R) = (P \wedge Q) \Rightarrow R$

$Q \Rightarrow P$   
 $P \Rightarrow Q$   
 $P \Rightarrow Q \Rightarrow F$   
 $T \Rightarrow F$

P	Q	R	$Q \Rightarrow R$	$P \Rightarrow (Q \Rightarrow R)$	$P \wedge Q$	$(P \wedge Q) \Rightarrow R$
0	0	0	T	T	F	T
0	0	1	T	T	F	T
0	1	0	F	T	F	T
0	1	1	T	T	F	T
1	0	0	T	F	F	T
1	0	1	T	F	F	T
1	1	0	F	T	T	F
1	1	1	T	T	T	T

$$(P \vee \sim Q) \vee (Q \wedge \sim P) \equiv (P \vee Q) \wedge \sim (P \wedge Q)$$

Contingency → A Compound statement which either be true or false or false depending upon Component proposition value.

T	F	-F
$P \rightarrow Q$		

Tautology (T)

Contradiction (C)

Contingency (Not Defined)

T	T	-T
F	F	-T
$P \leftrightarrow Q$		

$$(P \rightarrow Q) \wedge (Q \rightarrow P)$$

→  $P \rightarrow R$



statement is replaced by the variables.

statement formula is an expression which is a string consisting of variables, parentheses and connective symbols.

any string of these symbols is a statement formula.

ff:  $\rightarrow$

$\checkmark R_1$ : - A statement variable standing alone is wff.

$\checkmark R_2$ :  $\rightarrow$  If A is wff then  $\neg A$  is a wff.

$R_3$ :  $\rightarrow$  If A & B are wff, then  $(A \wedge B)$ ,  $(A \vee B)$ ,  $(A \rightarrow B)$  &  $(A \leftrightarrow B)$  are wff.

①

u: Acc. to this definition, the following well-formed formulas

$\neg(P \wedge Q)$ ,  $\neg(P \vee Q)$ ,  $(P \rightarrow (P \vee Q))$ ,  $(P \rightarrow (Q \rightarrow R))$  &

$((P \rightarrow Q) \wedge (Q \rightarrow R)) \Leftrightarrow (P \rightarrow R)$

2  $\neg P \wedge Q$  is Not wff because it would be either  $(\neg P \wedge Q)$  or  $\neg(P \wedge Q)$ . Here  $\neg P \wedge Q$  does not contain parentheses

$(P \rightarrow Q) \rightarrow (\overset{\text{Binary}}{P} \wedge Q)$  is not wff because  $\wedge Q$  is not statement variable. Here no other statement or variable.

②

$\rightarrow P \rightarrow Q$



statement variable, symbol, statement, connective symbols and parenthesis

! wff  $\neg P \wedge Q, (P \rightarrow Q) \rightarrow (\underline{\wedge Q}), (P \rightarrow Q$   
 $\rightarrow$  No parenthesis  
 Here only  
 or (, on preposition  
 $(P \wedge Q) \rightarrow Q) \rightarrow$  No left parenthesis.

! wff  $\rightarrow (P) \rightarrow$  No wff. (No bracket)

If P is wff then  $\neg P$  is also wff.

& Q are wff then  $(P \wedge Q), (P \vee Q), (P \rightarrow Q), (P \leftrightarrow Q)$

$P \wedge Q \leftarrow$  No wff

$P \rightarrow Q \rightarrow R \rightarrow$  No  $((P \rightarrow Q) \rightarrow R)$  or  $(P \rightarrow (Q \rightarrow R))$   
 well formed.  
 or  $\wedge$   $\wedge$  wff

$P \rightarrow (Q \rightarrow R) \rightarrow$  No wff

P is preposition then it is wff

$\neg P$  is also wff

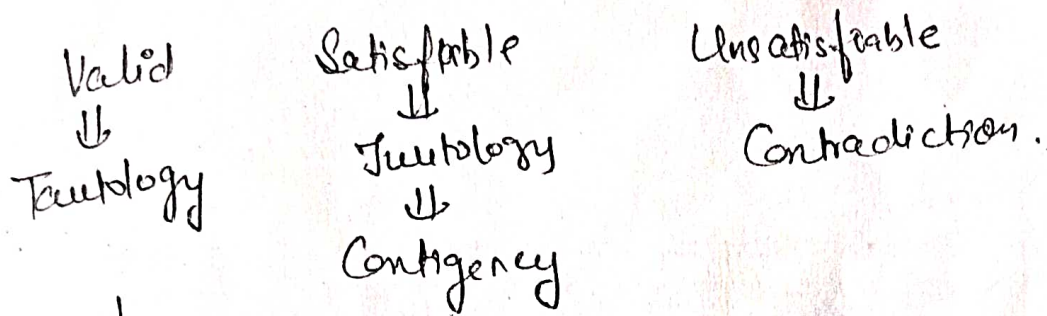
$\rightarrow \rightarrow Q) \rightarrow$  2 preposition 2 connect not pos No wff.

$\rightarrow Q)) \rightarrow$  No wff.

$Q) \vee (P \circ Q) \rightarrow$  No wff

Agar apke pass 2 preposition hai  
 uske saath ek logical connective  
 along with bracket mandgari





How to Distinguish.

if kbi baki hai → Satisfiable but not valid.

$$((P \rightarrow Q) \wedge (Q \rightarrow R)) \rightarrow (P \rightarrow R)$$

Last Column all T (come means Tautology means valid).

$$1) (P \rightarrow Q) \rightarrow (\sim P \rightarrow \sim Q)$$

$$2) (P \wedge (\sim P \vee \sim Q)) \rightarrow Q$$

$$3) ((P \rightarrow R) \vee (Q \rightarrow R)) \rightarrow ((P \vee Q) \rightarrow R)$$

$$4) (P \rightarrow (Q \vee R)) \rightarrow ((P \wedge Q) \rightarrow R) \rightarrow \text{all T one False}$$

1) Satisfiable but not valid

2) Valid

3) Contradiction

4) None of These