

# 正态总体均值、方差的置信区间与单侧置信限（置信水平为 $1-\alpha$ ）

	待估参数	其他参数	枢轴量 $W$ 的分布	置信区间	单侧置信限
一个正态总体	$\mu$	$\sigma^2$ 已知	$Z = \frac{\bar{X} - \mu}{\sigma / \sqrt{n}} \sim N(0,1)$	$(\bar{X} \pm \frac{\sigma}{\sqrt{n}} z_{\alpha/2})$	$\bar{\mu} = \bar{X} + \frac{\sigma}{\sqrt{n}} z_{\alpha} \quad \underline{\mu} = \bar{X} - \frac{\sigma}{\sqrt{n}} z_{\alpha}$
	$\mu$	$\sigma^2$ 未知	$t = \frac{\bar{X} - \mu}{S / \sqrt{n}} \sim t(n-1)$	$(\bar{X} \pm \frac{S}{\sqrt{n}} t_{\alpha/2}(n-1))$	$\bar{\mu} = \bar{X} + \frac{S}{\sqrt{n}} t_{\alpha}(n-1) \quad \underline{\mu} = \bar{X} - \frac{S}{\sqrt{n}} t_{\alpha}(n-1)$
	$\sigma^2$	$\mu$ 未知	$\chi^2 = \frac{(n-1)S^2}{\sigma^2} \sim \chi^2(n-1)$	$(\frac{(n-1)S^2}{\chi_{\alpha/2}^2(n-1)}, \frac{(n-1)S^2}{\chi_{1-\alpha/2}^2(n-1)})$	$\overline{\sigma^2} = \frac{(n-1)S^2}{\chi_{1-\alpha}^2(n-1)} \quad \underline{\sigma^2} = \frac{(n-1)S^2}{\chi_{\alpha}^2(n-1)}$
两个正态总体	$\mu_1 - \mu_2$	$\sigma_1^2, \sigma_2^2$ 已知	$Z = \frac{\bar{X} - \bar{Y} - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} \sim N(0,1)$	$(\bar{X} - \bar{Y} \pm z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}})$	$\overline{\mu_1 - \mu_2} = \bar{X} - \bar{Y} + z_{\alpha} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$ $\underline{\mu_1 - \mu_2} = \bar{X} - \bar{Y} - z_{\alpha} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$
	$\mu_1 - \mu_2$	$\sigma_1^2 = \sigma_2^2 = \sigma^2$ 未知	$t = \frac{(\bar{X} - \bar{Y}) - (\mu_1 - \mu_2)}{S_w \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \sim t(n_1 + n_2 - 2)$ $S_w^2 = \frac{(n_1-1)S_1^2 + (n_2-1)S_2^2}{n_1 + n_2 - 2}$	$(\bar{X} - \bar{Y} \pm t_{\alpha/2}(n_1 + n_2 - 2) S_w \sqrt{\frac{1}{n_1} + \frac{1}{n_2}})$	$\overline{\mu_1 - \mu_2} = \bar{X} - \bar{Y} + t_{\alpha}(n_1 + n_2 - 2) S_w \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$ $\underline{\mu_1 - \mu_2} = \bar{X} - \bar{Y} - t_{\alpha}(n_1 + n_2 - 2) S_w \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$
	$\frac{\sigma_1^2}{\sigma_2^2}$	$\mu_1, \mu_2$ 未知	$F = \frac{S_1^2 / S_2^2}{\sigma_1^2 / \sigma_2^2} \sim F(n_1 - 1, n_2 - 1)$	$(\frac{S_1^2}{S_2^2} \frac{1}{F_{\alpha/2}(n_1 - 1, n_2 - 1)}, \frac{S_1^2}{S_2^2} \frac{1}{F_{1-\alpha/2}(n_1 - 1, n_2 - 1)})$	$\overline{\frac{\sigma_1^2}{\sigma_2^2}} = \frac{S_1^2}{S_2^2} \frac{1}{F_{1-\alpha}(n_1 - 1, n_2 - 1)}$ $\underline{\frac{\sigma_1^2}{\sigma_2^2}} = \frac{S_1^2}{S_2^2} \frac{1}{F_{\alpha}(n_1 - 1, n_2 - 1)}$