

Practical Techniques for Searches on Encrypted Data——Literature Notes

Section one: abstract & introduction

Part one: Motivation:

in order to solve **How to support searching functionality without any loss if data confidentiality.**

Why searches on encrypted data?

- Searching on encrypted e-mails on servers
- Searching on encrypted files on file servers
- Searching on encrypted database

Why is this hard?

- perform computations on encrypted data is often hard
- security and functionality

part two: methods:

five different schemes based on **probabilistic searching**(all positions with erroneous positions($l/2^m$), l means the length of document)

part three: the two main parts:

- cryptographic schemes for the problem of **searching on encrypted data**
- **proofs of security** for the resulting crypto systems.

part four: Provable security:

- provide **provably secure**, untrusted server cannot get any information from the data storage
- provide **query isolation** for searchers, means limited information(searching results) for untrusted server
- provide **controlled searching**, cannot search other information without authorization
- provide **Hidden queries**, does not reveal the search words.

part five: Efficiency

- Low computation overhead
- Low space and communication overhead
- Low management overhead

Other information about the algorithm:

- $O(n)$ for a document of length n , fast and simple
- efficient and practical

section two: Background and Definition

part one: two types of approaches:

- build up an index
- perform a sequential scan without index

comparison:

- index may be faster when the documents are large, but storing and updating the index can be substantial overhead.
- the index-based schemes require less sophisticated construction and which are more suitable for mostly-read-only data.

part two: Definition

notion	description
R -breaks	attacks algorithm with resource specified by R
R -secure	no algorithm can R -breaks it
Advantage of A	distinguishing probability of A
A	an arbitrary algorithm: $\{0, 1\}^n \rightarrow \{0, 1\}$
G :(t,e)-secure	A pseudorandom generator: $\mathcal{K}_G \rightarrow S$
F :(t,q,e)-secure	A pseudorandom function: $\mathcal{K}_F \times \mathcal{X} \rightarrow \mathcal{Y}$
E :(t,q,e)-secure	A pseudorandom permutation: $\mathcal{K}_E \times \mathcal{Z} \rightarrow \mathcal{Z}$

notion	Adv A
A	$AdvA = Pr[A(X) = 1] - Pr[A(Y) = 1] $
G	$AdvA = Pr[(A(G(U_{\mathcal{K}_G}))) = 1] - Pr[A(U_S) = 1] $
F	$AdvA = Pr[A^{F_k} = 1] - Pr[A^R = 1] $
E	$AdvA = Pr[A^{E_k, E_k^{-1}} = 1] - Pr[A^{\pi, \pi^{-1}} = 1] $

Section three: Solution with sequential scan

Part one: Scheme I - The Basic Scheme

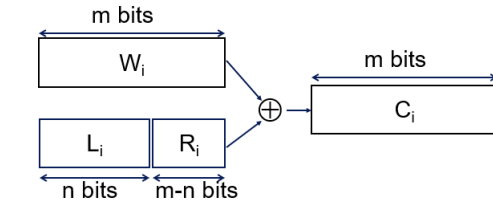
step one: generates a sequence of pseudorandom values S_1, \dots, S_l via the pseudorandom generator G . and each S is $n - m$ bits long.

step two: then, take S_i to set $T_i := \langle S_i, F_{k_i}(S_i) \rangle$, the length of T_i is the same as the length of a word(n), and let $L_i = S_i$ and $R_i = F_{k_i}(S_i)$

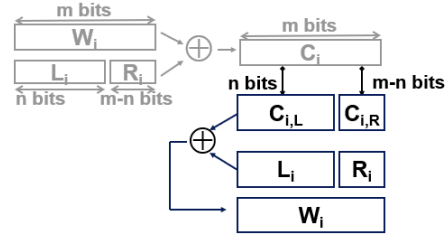
step three: output the ciphertext: $C_i := W_i \oplus T_i$

the Key value: k_i is stored by Alice, not the server. so only Alice can generate the pseudorandom bits to encrypt and decrypt.

Encryption and Decryption as follows.



$$L_i \leftarrow G_i(\text{seed}), \quad R_i \leftarrow F_K(L_i)$$



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Problems with Basic Scheme

- Queries are not hidden, server learn word
- Query isolation is not satisfied, server learns K and search for arbitrary word.

Alice must reveal all the k_i (thus potentially revealing the entire document), or Alice must know in advance which locations W may appear at.

Part two: Scheme II - Controlled Searching

Instead of $R_i \leftarrow F_k(L_i)$, just generate S_i where $K_i = F'_k(W_i)$.

$T_i := \langle R_i, F_{k_i}(R_i) \rangle$, where $K_i = F'_k(W_i)$.

So there an additional pseudorandom function: $f : \mathcal{K}_F \times \{0, 1\}^* \rightarrow \mathcal{K}_F$, using this function to choose keys as $k_i := f_{k'}(W_i)$.

take this idea further by using a hierarchical key management scheme. set $k_i := f_l(< 0, C >)$ and $l := f_{k'}(< 1, W_i >)$

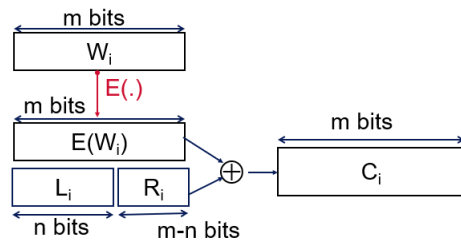
Part three: Scheme III - Hidden Searches

pre-encrypt each word W of the clear text separately using a deterministic encryption algorithm $E_{k''}$

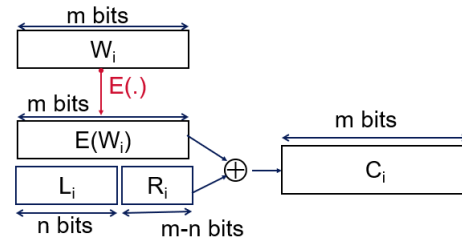
About the $E_{k''}$:

- not allowed to use any randomness.
- the computation $E_{k''}(x)$ may depend only on x and not the position i

Hidden Queries schemes and improved Security(Change K):



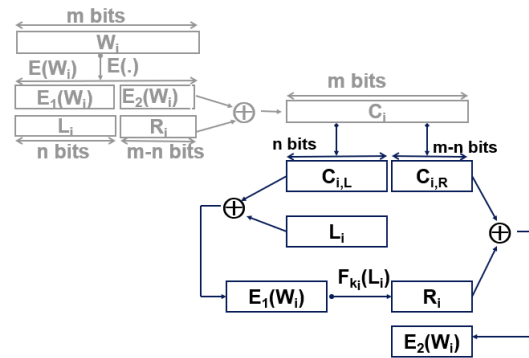
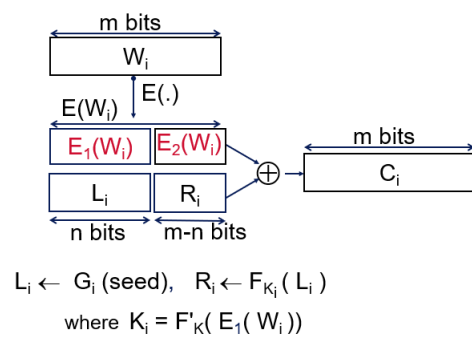
$$L_i \leftarrow G_i(\text{seed}), \quad R_i \leftarrow F_K(L_i)$$



$$L_i \leftarrow G_i(\text{seed}), \quad R_i \leftarrow F_{K_i}(L_i) \\ \text{where } K_i = F'_K(E(W_i))$$

Part four: Scheme IV - Final Scheme

Encryption and decryption as follows:



Section four: Variable length words encryption scheme

in order to deal with the fact that English words differ in length:

