

Nash theorem, Nash equilibria

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1 Basics; notation, definitions

Normal form game of $n \in \mathbb{N}$ players is $G = (P, A, w)$, where P is a finite set of n players.

$$A = A_1 \times \cdots \times A_n$$

Is a set of action profiles. Action profile is (a_1, a_2, \dots, a_n) where $a_i \in A_i$ = set of actions of player i .

$u = (u_1, \dots, u_n)$ where $u_i : A \rightarrow \mathbb{R}$ is the utility function of i - how good this action is for player i .

Every player i selects an action $a_i \in A_i$ - all players select at once. Every player wants to maximize u_i

EXAMPLE:

Rock paper scissors:

$$P = \{1, 2\}, A_1 = \{ROCK, PAPER, SCISSORS\} = A_2, A = A_1 \times A_2$$

$$M = (M_a)_a \in A, M_a = (u_1(a), u_2(a)) : \begin{pmatrix} 1/2 & R & P & S \\ R & 0, 0 & -1, 1 & 1, -1 \\ P & 1, -1 & 0, 0 & 1, -1 \\ S & -1, 1 & 1, -1 & 0, 0 \end{pmatrix}$$