

We want to display analysis results using both logarithmic and linear scale (and maybe some other scales). This document discusses the implementations of `LinearScale` and `LogarithmicScale`.

So far, zoom is implemented in the way that it changes the size of container (`JComponent`) containing graph (of either verification result or time course). The scale should adjust accordingly. Furthermore, we know dimension of given model value (including time).

Therefore, scale is a transformation between intervals $[b_m, t_m]$ (domain of model value) and $[b_v = 0, t_v]$ (size of container), i.e. a function f and its inverse, such that $f(b_m) = 0$ and $f(t_m) = t_v$.

1 Linear Scale

In the case of linear scale f is linear. As the inverse is linear too, it is easier to consider $f^{-1}(x) = ax + b$. Hence $b_m = f^{-1}(0) = b$, and $t_m = f^{-1}(t_v) = at_v + b_m$, implying $a = \frac{t_m - b_m}{t_v}$.

2 Logarithmic Scale

In logarithmic scale f is an logarithm of a certain base. However, we want $f(b_m) = 0$. If $f = \log_a$, this condition holds only if $b_m = 1$. Therefore, we have to identify b_m with one. This is done by putting $f(x) = \log_a(x - b_m + 1)$ (division is not possible since it would not work for negative b_m).

$$\log_a(t_m - b_m + 1) = t_v \quad \implies \quad \frac{\ln(t_m - b_m + 1)}{\ln a} = t_v \quad \implies \quad \ln a = \frac{\ln(t_m - b_m + 1)}{t_v}$$

$$f : x \rightarrow \frac{\ln(x - b_m + 1)}{\ln a}$$

$$f^{-1} : x \rightarrow e^{x \ln a} - 1 + b_m$$

Since java does not implement general logarithm, `LogarithmicScale` stores the value of $\ln a$. Furthermore, for additional precision, functions $\log1p(x) = \ln(x + 1)$ and $\expm1(x) = e^x - 1$ are used when possible.

In practise, however, this kind of scale does not work (or, closely resembles linear scale).

2.1 Adjusted Logarithmic Scale

First, we assume, b_m and t_m both being positive (if both are negative, the $-\log(-x)$ function can be used). Then we construct the logarithmic scale in the manner similar to linear scale, only $t'_m = \log_{10} t_m$ and $b'_m = \log_{10} b_m$.