

$$ii) f(x) = \frac{1}{2} x^T Q x + b^T x + c$$

$$\nabla f(x) = Qx + b$$

$$\|\nabla f(x) - \nabla f(y)\| =$$

$$\| (Qx + b) - (Qy + b) \| = \| Qx - Qy \| =$$

$$= \| Q(x-y) \| \stackrel{\text{lemma 0.1.}}{\leq} \|Q\| \cdot \|x-y\| = L \cdot \|x-y\|$$

L-LIPSCHITZ GRADIENT  $\Rightarrow$  L-smooth

$$iii) \frac{\partial f(b, w)}{\partial b} = \sum_{i=1}^n (2b + w^T x_i - y_i) = \sum_{i=1}^n 2b + w^T \sum_{i=1}^n x_i - \sum_{i=1}^n y_i$$

$$\sum_{i=1}^n y_i = 2nb + w^T \cdot 0 - 0 = 2nb$$

$$2nb^* = 0$$

$$b^* = 0$$