



UNIVERSITAT<sub>DE</sub>  
BARCELONA

OPTIMIZATION

MASTER IN FUNDAMENTAL PRINCIPLES OF DATA SCIENCE

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## OPTIMIZATION PROBLEM 2

CONCRETE MIXING PROBLEM

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## 1 Problem description

*Suppose that we are mixing concrete and are using  $n$  different gravel sizes  $s_1, \dots, s_n$ .*

*The ideal mixture is given by  $c = (c_1, \dots, c_n)$ , where  $c_i$  ( $0 \leq c_i \leq 1$ ) is the fraction of size  $s_i$  in the mix, and  $\sum_{i=1}^n c_i = 1$ .*

*Gravel mixtures come from  $m$  different mines:  $C_1, \dots, C_m$ . The gravel composition at each mine  $C_j$  is given by  $C_j = (c_1^j, \dots, c_n^j)$ , where  $0 \leq c_i^j \leq 1$  for all  $i = 1, \dots, n$  and  $\sum_{i=1}^n c_i^j = 1$ .*

*Let  $x = (x_1, \dots, x_m)$  be the vector which represents the fraction of the gravel of the mine  $C_j \in C$  in the mixture, where  $0 \leq x_j \leq 1$  for all  $j = 1, \dots, m$  and  $\sum_{j=1}^m x_j = 1$ .*

*Find the best possible approximation  $x = (x_1, \dots, x_m)$  of the ideal mixture,  $c = (c_1, \dots, c_n)$ , by using the material from the  $m$  mines.*

## 2 Solution