

```
• #loading packages  
• begin  
•     using PlutoUI      ,ExtendableGrids      ,VoronoiFVM      ,GridVisualize      , PlutoVista  
•  
•     using HypertextLiteral  
•     using DifferentialEquations  
•     GridVisualize.default_plotter!(PlutoVista)  
• end;
```

0

```
• begin  
•     #defining constants  
•     const k = 100;  
•     const g = [0 -1];  
•     const c = 0.001;  
•     const α = 0.01;  
•     const λ = 0.01;  
•     const ρ_ref = 1;  
•     const T_ref = 0;  
•     const P_ref = 0;  
• end
```

Porous_medium (generic function with 2 methods)

```

• function Porous_medium(N_x,N_y,T_heat,steady_state,tend = 10)
•
•     #defining grid
•     X = collect(range(0,300,length=N_x))
•     Y = collect(range(0,150,length=N_y))
•     grid=simplexgrid(X,Y)
•
•     #defining flux
•     function flux!(f,u, edge)
•         f[1] = -p_ref*k*(u[1,1]-u[1,2]) -α*0.5*(u[2,1]+u[2,2])*project(edge,g)
•         f[2] = λ*(u[2,1] - u[2,2])
•     end
•
•     #defining storage(what is under the timed derivative)
•     function storage!(f,u,node)
•         f[1]=0
•         f[2]=c*u[2]
•     end
•
•     #defining boundary conditions
•     function bcondition!(f,u,bnode)
•         boundary_dirichlet!(f,u,bnode,species=2,region=1,value=T_heat)
•         boundary_dirichlet!(f,u,bnode,species=2,region=3,value=0)
•         boundary_dirichlet!(f,u,bnode,species=1,region=3,value=0)
•     end
•
•     #defining voronoi system
•     system=VoronoiFVM.System(grid;
•     flux=flux!,
•     bcondition = bcondition!,
•     storage = storage!,
•     species=[1,2])
•
•     if steady_state
•         #solving steadystate solution
•         sol=VoronoiFVM.solve(system)
•         nf=nodeflux(system,sol)
•         return grid,sol,nf
•     else
•         #solving transient solution
•         sol=VoronoiFVM.solve(system,inival = 0,times=
• (0,tend),Δu_opt=T_heat,Δt_min=1.0e-2, Δt=1.0e-1)
•         #inival=unknowns(system,inival=0)
•         #problem = ODEProblem(system,inival,(0,tend))
•         #odesol = DifferentialEquations.solve(problem)
•         #sol=reshape(odesol,system)
•         nf=nodeflux(system,sol[1])
•         return grid,sol,nf
•     end
• end

```

```
(ExtendableGrids.ExtendableGrid{Float64, Int32};
 dim: 2 nodes: 2312 cells: 4422 bfaces: 200, edges: 6733, t: 21-element Vector{Float64}
 0.0
 0.1
 0.2
 0.32
 0.464
 0.6368
 0.84416
 ⋮
 5.94966
 6.94966
 7.94966
 8.94966
 9.94966
 10.0
 u: 21-element Vector{Matrix{F
 [0.0 0.0 ... 0.0 0.0; 0.0 0.0
 [0.002483 0.002483 ... -4.4982
 [0.00268437 0.00268437 ... -2.
 [0.00291444 0.00291444 ... -2.
 [0.00317572 0.00317572 ... -2.
 [0.00347063 0.00347063 ... -5.
 [0.00380149 0.00380149 ... -3.
 ⋮
 [0.00879543 0.00879543 ... -5.
 [0.009481 0.009481 ... -4.5189
 [0.0101225 0.0101225 ... -3.02
 [0.0107273 0.0107273 ... -4.52
 [0.0113008 0.0113008 ... -6.72
 [0.0113296 0.0113296 ... -5.45
```

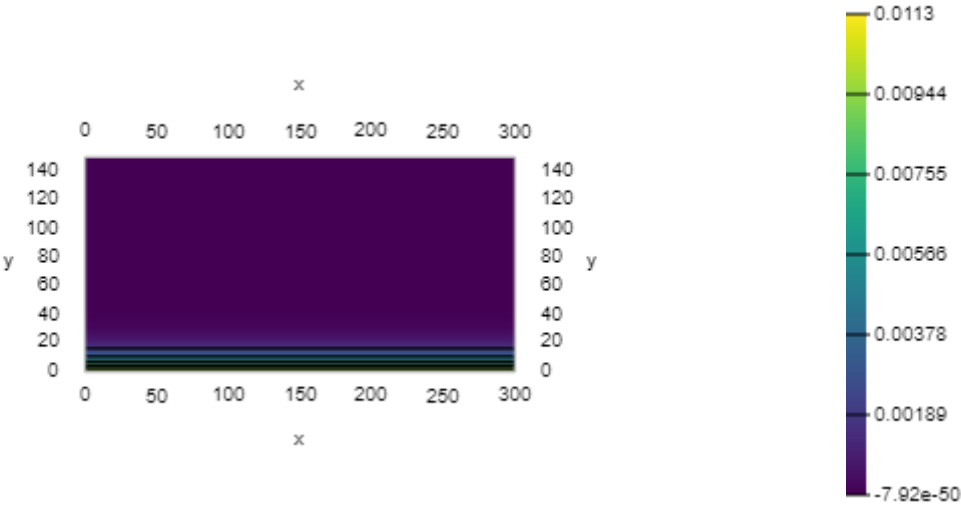
```
• begin
•   tend = 10 #final time
•  steadystate = false #solving for steady state or transient depending on boolean
• value
    grid,sol,nf = Porous_medium(68,34,10,steadystate,tend)
end
```

t= 

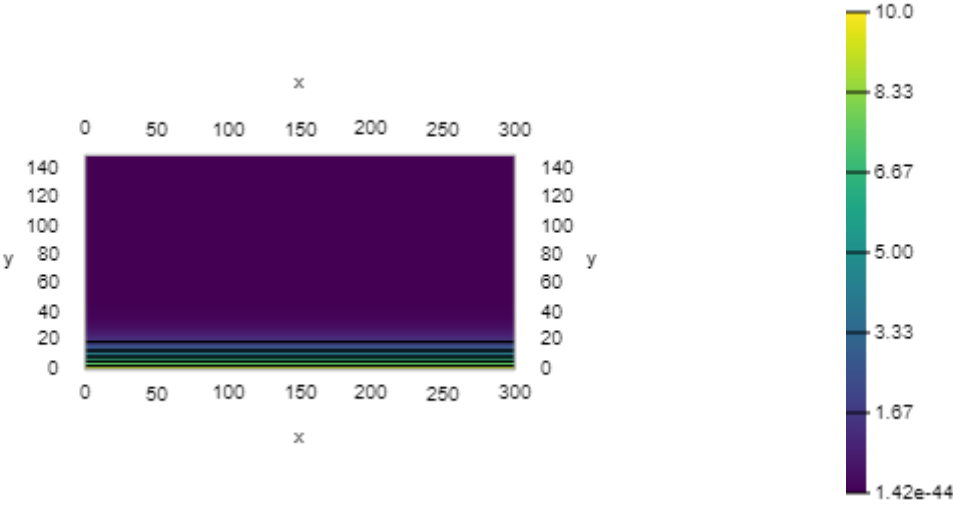
```
• if steadystate
• else
•   md"""
•   t= $(@bind t_plot Slider(0:tend/10000:tend,default=0))
•   """
end
```

```
2×2312 Matrix{Float64}:
 0.0113296  0.0113296  0.0113296  0.0113296  ...  -5.45398e-50  -5.43986e-50
 10.0       10.0       10.0       10.0       ...  1.42092e-44  1.42092e-44
```

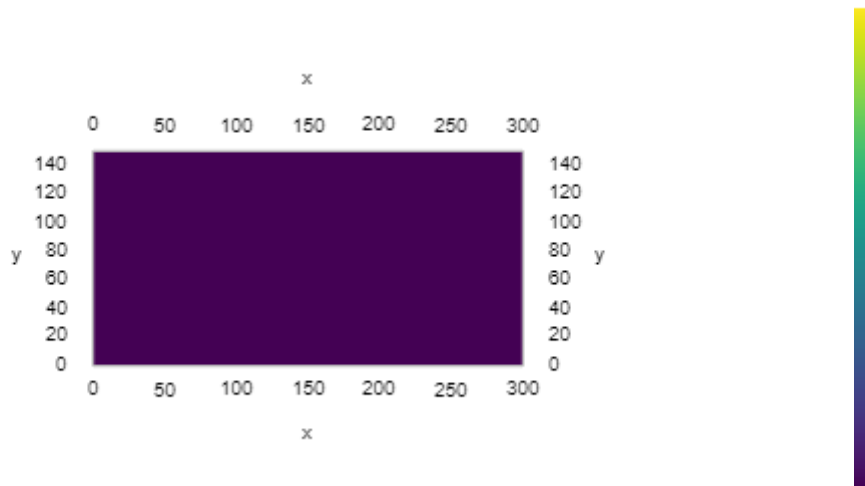
```
• if steadystate
•   tsol = sol
• else
•   tsol = sol(t_plot);
end
```



• `begin#plotting pressure`



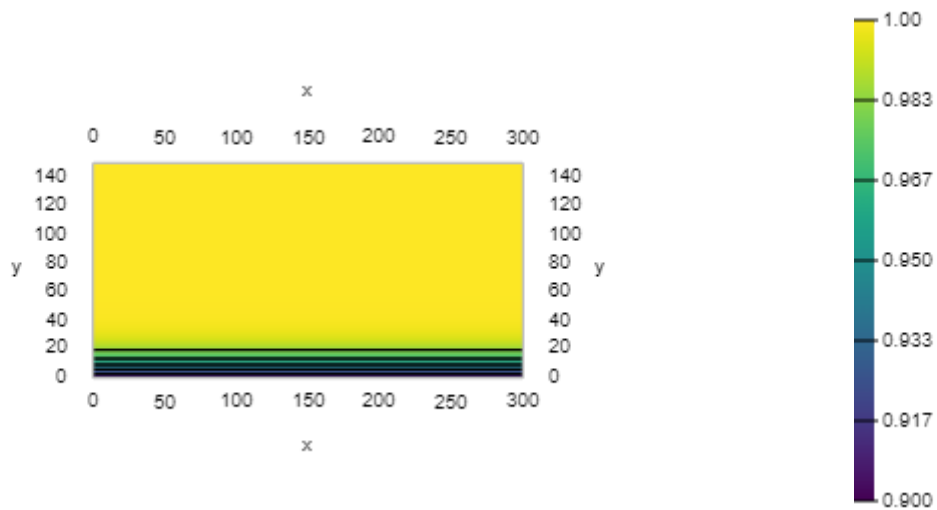
• `begin#plotting temperature`



```

• begin#plotting q in x direction
•   vis3=GridVisualizer(size=(600,300),xlabel="x",legend=:rt);vis3
•   scalarplot!(vis3,grid,-p_ref*k*nf[1,1,:],color=:red,label="u_2")
•   reveal(vis3)
end

```



```

• begin#plotting q in y direction

```