

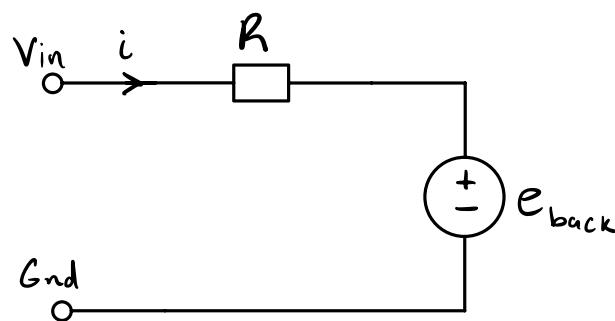
LTSPICE MODEL

3V DC motor

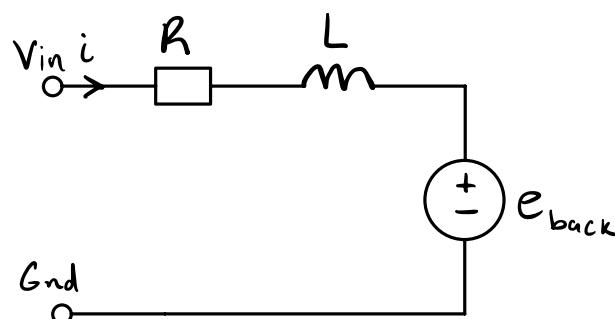
First, we define the Voltage drop across a steady state DC motor as:

$$V = e_{\text{back}} + iR$$

where e_{back} is the opposing electromotive force and iR is the resistive voltage drop. This gives us a model:



But this model only works at steady state. We must also account for the inductance of the motor due to the loops within it:



where L is the inductance of the motor. This gives us a new equation:

$$V = e_{\text{back}} + iR + L \cdot \frac{di}{dt}$$

For the model, we need values. We can find R and L by measuring the current at $t > 0$ for:

$$x(t) = 3u(t)$$

For e_{back} :

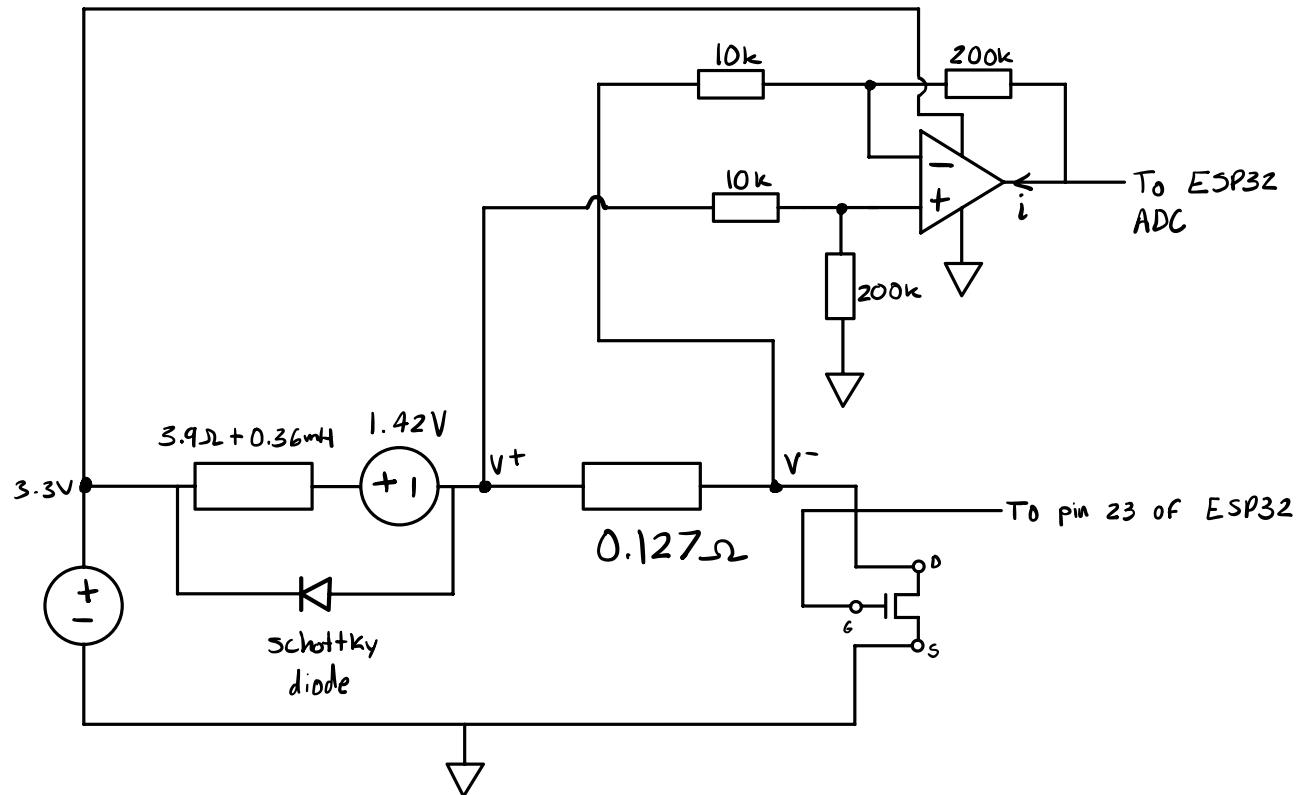
$$e_{\text{back}} = k_v \cdot \omega$$

Where k_v is a constant with units $\frac{V}{\text{rad/s}}$ and ω is the angular speed in rad/s. Right now, we are only simulating for testing, so we can set e_{back} to a measured constant of 1.42V.

Current Sensor with Op-Amp

We will use an operational amplifier and the voltage across a shunt resistor (0.127Ω), in series with the DC motor, to find current ($\frac{V}{I}$). To model this, we will measure the load resistance value to find 3.9Ω and guess the inductance as 0.36mH . The full circuit with inductance protection becomes:

COMPLETE MODEL



RESULTS

The results matched the simulated graph perfectly in terms of shape. The time constant was found as $\tau = 20.3\text{ms}$. This makes the inductance of the motor $R \cdot \tau = L \rightarrow 20.3\text{ms} \cdot 3.9\Omega = 79.17\mu\text{H}$.

CONCLUSION

Overall, results matched the simulation. This system can be used to find the inductance of any motor rated $\leq 12\text{V}$.

CHALLENGES & SOLUTIONS

1) ESP32 Sampling Rate

The sampling rate of the ESP32 is only about 100kS/s. This means it can sample properly once every ten microseconds. The problem here is that the time constant for a motor can range from six microseconds to 100. Due to this, I decided to sample in discrete time intervals (0μs, 2μs, 4μs) per run. After 126 runs, I was able to get a matching graph.

2) Heating

The motor draws a lot of current, which heats up the wires and coils. To solve this, we wait two seconds before each new sample.