V64

Interferometry

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Durchführung: DATUM Abgabe: DATUM

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1 Theorie

[sample]

2 Durchführung

3 Analysis

3.1 Kontrast

In order to study the usage of interferometrie to determine refraction indices, first of all the kontrast of the used Sagnac Interferometer was calculated. The kontrast was calculated with equation (??) and the values of table 1. Table 1 also contains the calculated kontrast values. The maximum contrast K=0.92 was measured at $\Phi=130^\circ$ Therefore the polarization filter was set to $\Phi=130^\circ$ for the following measurements. In addition, a fit of the form

$$K = A \cdot |\cos(\Phi)\sin(\Phi)| \tag{1}$$

is performed with the mean values of the measured values. This can be seen for the determined value of $A=1.76\pm0.07$ in graph 1.

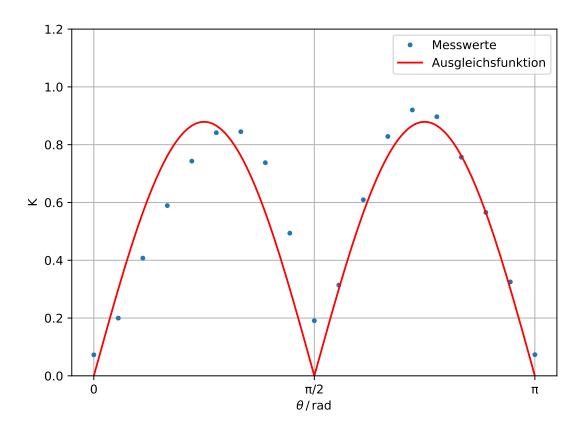


Abbildung 1: The measured values of the contrast according to equation (??) and the fit calculation according to equation (??).

Tabelle 1: Recorded measured values for contrast measurement, as well as the respective contrast value.

| $\Phi/^{\circ}$ | $U_{ m min,1}/{ m V}$ | $U_{\mathrm{max},1}/\mathrm{V}$ | K_1 | $U_{\mathrm{min,2}}/\mathrm{V}$ | $U_{\mathrm{max,2}}/\mathrm{V}$ | K_2 | $U_{\mathrm{min,3}}/\mathrm{V}$ | $U_{\rm max,3}/{\rm V}$ | K_3 |
|-----------------|-----------------------|---------------------------------|-------|---------------------------------|---------------------------------|-------|---------------------------------|-------------------------|-------|
| 0 | 1.73 | 1.98 | 0.06 | 1.8 | 2.1 | 0.07 | 1.76 | 2.04 | 0.07 |
| 10 | 1.21 | 1.8 | 0.19 | 1.16 | 1.78 | 0.21 | 1.24 | 1.83 | 0.19 |
| 20 | 0.69 | 1.65 | 0.41 | 0.7 | 1.63 | 0.39 | 0.69 | 1.66 | 0.41 |
| 30 | 0.36 | 1.44 | 0.60 | 0.39 | 1.46 | 0.57 | 0.38 | 1.47 | 0.58 |
| 40 | 0.21 | 1.48 | 0.75 | 0.23 | 1.47 | 0.72 | 0.21 | 1.46 | 0.74 |
| 50 | 0.14 | 1.7 | 0.84 | 0.15 | 1.64 | 0.83 | 0.14 | 1.66 | 0.84 |
| 60 | 0.17 | 1.98 | 0.84 | 0.16 | 1.93 | 0.84 | 0.16 | 1.92 | 0.84 |
| 70 | 0.37 | 2.35 | 0.72 | 0.32 | 2.15 | 0.74 | 0.33 | 2.25 | 0.74 |
| 80 | 0.85 | 2.36 | 0.47 | 0.7 | 2.22 | 0.52 | 0.79 | 2.31 | 0.49 |
| 90 | 1.64 | 2.36 | 0.18 | 1.48 | 2.28 | 0.21 | 1.62 | 2.33 | 0.17 |
| 100 | 1.43 | 2.93 | 0.34 | 1.46 | 2.68 | 0.29 | 1.49 | 2.79 | 0.30 |
| 110 | 1.08 | 4.13 | 0.58 | 0.92 | 3.78 | 0.60 | 0.91 | 4.06 | 0.63 |
| 120 | 0.52 | 5.06 | 0.81 | 0.49 | 5.06 | 0.82 | 0.44 | 5.36 | 0.84 |
| 130 | 0.24 | 5.53 | 0.91 | 0.25 | 5.56 | 0.91 | 0.21 | 5.76 | 0.92 |
| 140 | 0.34 | 5.92 | 0.89 | 0.33 | 5.91 | 0.89 | 0.3 | 5.99 | 0.90 |
| 150 | 0.73 | 5.26 | 0.75 | 0.77 | 5.39 | 0.75 | 0.73 | 5.45 | 0.76 |
| 160 | 1.16 | 4.13 | 0.56 | 1.22 | 4.25 | 0.55 | 1.16 | 4.38 | 0.58 |
| 170 | 1.63 | 3.18 | 0.32 | 1.67 | 3.19 | 0.31 | 1.62 | 3.29 | 0.34 |
| 180 | 1.86 | 2.08 | 0.05 | 1.85 | 2.18 | 0.08 | 1.79 | 2.11 | 0.08 |

3.2 Refraction index of glas

To determine the refractive index of glass, the number of intensity maxima M was recorded. The refractive index was determined using the equation (??). The thickness of the plates is D=1 mm, the wavelength of the laser $\lambda_0=632.990$ nm and $\Omega_0=10^\circ$ as the two plates are each Ω_0 inclined. The measured values, as well as the refractive index determined in each case, can be found in Table 2. On average, the refractive index determined for glass is

$$n_{\rm Glas} = 1.64 \pm 0.13.$$

Tabelle 2: AMeasured values to determine the refractive index of glass and the determined refractive index.

| Durchgang | M | $n_{ m Glas}$ |
|-----------|----|---------------|
| 1 | 38 | 1.652392 |
| 2 | 38 | 1.652392 |
| 3 | 38 | 1.652392 |
| 4 | 37 | 1.624503 |
| 5 | 38 | 1.652392 |
| 6 | 38 | 1.652392 |
| 7 | 37 | 1.624503 |
| 8 | 38 | 1.652392 |
| 9 | 38 | 1.652392 |
| 10 | 37 | 1.624503 |

3.3 Refraction index of air

To determine the refractive index of air, the measured values were recorded as described in chapter ?? and determined using equation ??. The length of the gas chamber is $L=(100.0\pm0.1)$ mm and the temperature $T=20.6~^{\circ}\mathrm{C}$. The recorded values as well as the calculated reflection indices are shown in Table 3.

Tabelle 3: Measured values recorded to determine the refractive index of air next to the refractive index calculated according to equation (??). Here, M_i denotes the number of interference minima or maxima that have passed up to that point, where i indicates the passage.

| p/mbar | M_1 | n_1 | M_2 | n_2 | M_3 | n_3 | M_4 | n_4 |
|-------------------|-------|--------------|-------|----------------|-------|----------------|-------|----------------|
| 50 | 2 | 1,00001266 | 2 | $1,\!00001266$ | 2 | $1,\!00001266$ | 3 | 1,00001899 |
| 100 | 4 | 1,00002532 | 4 | 1,00002532 | 4 | 1,00002532 | 5 | $1,\!00003165$ |
| 150 | 7 | 1,00004431 | 6 | 1,00003798 | 6 | 1,00003798 | 7 | 1,00004431 |
| 200 | 9 | 1,00005697 | 8 | 1,00005064 | 8 | 1,00005064 | 9 | $1,\!00005697$ |
| 250 | 11 | 1,00006963 | 10 | 1,00006330 | 10 | 1,00006330 | 11 | 1,00006963 |
| 300 | 13 | 1,00008229 | 12 | $1,\!00007596$ | 12 | 1,00007596 | 13 | $1,\!00008229$ |
| 350 | 15 | 1,00009495 | 15 | $1,\!00009495$ | 15 | 1,00009495 | 15 | $1,\!00009495$ |
| 400 | 17 | 1,00010761 | 17 | $1,\!00010761$ | 17 | 1,00010761 | 18 | $1,\!00011394$ |
| 450 | 20 | 1,00012660 | 19 | $1,\!00012027$ | 19 | 1,00012027 | 20 | $1,\!00012660$ |
| 500 | 22 | 1,00013926 | 21 | 1,00013293 | 21 | 1,00013293 | 22 | 1,00013926 |
| 550 | 24 | 1,00015192 | 23 | 1,00014559 | 23 | 1,00014559 | 24 | 1,00015192 |
| 600 | 26 | 1,00016458 | 25 | 1,00015825 | 25 | 1,00015825 | 26 | 1,00016458 |
| 650 | 28 | 1,00017724 | 27 | 1,00017091 | 27 | 1,00017091 | 28 | 1,00017724 |
| 700 | 30 | 1,000 189 90 | 30 | 1,00018990 | 29 | 1,00018357 | 30 | 1,00018990 |
| 750 | 32 | 1,00020256 | 31 | 1,00019623 | 32 | 1,00020256 | 33 | 1,00020889 |
| 800 | 35 | 1,00022155 | 34 | 1,00021522 | 34 | 1,00021522 | 35 | 1,00022155 |
| 850 | 37 | 1,00023421 | 36 | 1,00022788 | 36 | 1,00022788 | 37 | 1,00023421 |
| 900 | 39 | 1,00024687 | 38 | 1,00024054 | 38 | 1,00024054 | 39 | $1,\!00024687$ |
| 950 | 41 | 1,00025953 | 40 | 1,000 253 20 | 40 | 1,000 253 20 | 41 | 1,000 259 53 |

3.4 Lorentz-Lorenz law

Since the refractive index also dependents on temperature and pressure according to the Lorentz-Lorenz law, an fit calculation is carried out according to equation ?? . The fit has the form

$$n = \frac{a}{TR} \cdot p + b \tag{2}$$

The temperate is T=20.6 °C and R describes the universal gas constant. This results in the in table 4 shown values for a and b.

Tabelle 4: The results of the fit for the variables a and b for each run.

| Messung | $a/\left(10^{-2}\mathrm{m}^3/\mathrm{mol}\right)$ | b |
|---------|---|-----------------------------|
| 1 | $0.00066776 \pm 0.00000394$ | $1.00000056 \pm 0.00000092$ |
| 2 | $0.00065800 \pm 0.00000397$ | $0.99999789 \pm 0.00000093$ |
| 3 | $0.00065854 \pm 0.00000364$ | $0.99999778 \pm 0.00000085$ |
| 4 | $0.00066017 \pm 0.00000370$ | $1.00000344 \pm 0.00000086$ |

The fits and thus the calculated refractive indices are shown in Figure 2 . The average values for the variables are:

$$a = 0.0006611 \pm 0.0000019 \frac{m^3}{\text{mol}}$$
$$b = 0.9999999 \pm 0.0000004.$$

According to the Loretz-Lorenz law, this results in the following refractive index in a normal atmosphere with T=15 °C and p=1013 hPa:

$$n = 1.0002795 \pm 0.0000009 \tag{3}$$

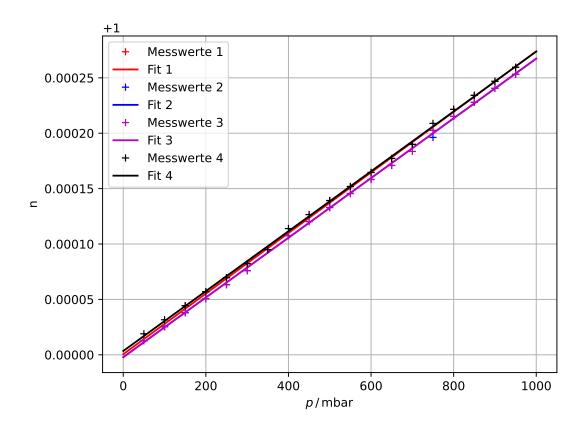


Abbildung 2: The calculated refractive indices n for air and the fit.

4 Diskussion

The measured values and the results obtained are in line with the expectations. An overview of the determined and theoretical values, as well as the respective deviation, can

be found in table Tabelle 5. The determined contrasts follow the expected distribution and no major deviations are recognizable. As expected, the extremes can also be found at multiples of 45°.

For the refractive index of glass, $n_{\rm glass}=1.64\pm0.13$ was determined. The theoretical value is $n_{\rm glass,\ theo}=1.45$ [1]. The determined value therefore has a deviation of 13,10%. One reason for this slightly higher deviation may lie in the way the experiment was carried out. Here, the intensity maxima and minima were only recorded with one diode instead of two.

The theoretical value for air is $n_{\rm air, theo} = 1.000292$ [1]. Averaged over all measurement series, the refractive index of air in a standard atmosphere is $n_{\rm air} = 1.0002795 \pm 0.0000009$, which represents a deviation of $\ll 1\%$ from the theoretical value.

Tabelle 5: The refractive indices determined for glass and air compared to the respective theoretical values.

| | $n_{ m Glas}$ | $n_{ m Luft}$ |
|------------|-----------------|---------------------------|
| Theorie | $1,\!45$ | 1,000292 |
| Versuch | 1.64 ± 0.13 | $1.0002795\ \pm0.0000009$ |
| Abweichung | 13.10~% | 0.0012~% |

Literatur

[1] chemie.de. *Brechzahl*. URL: http://www.chemie.de/lexikon/Brechzahl.html (besucht am 13.04.2022).