# Partially Optimal Cubic Subspace Clustering

Research Project Machine Learning

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Introduction

1 Partial Optimality for Cubic Clique Partition Problem

3 Cubic Subspace Instance Construction

4 Experiments and Evaluation

6 Research Results

Construct **Improving Maps** for the clustering y in the cubic clique partition problem

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CUT-conditions can be applied simultaneously JOIN-conditions cannot be applied simultaneously!

Construct **Improving Maps** for the clustering y in the cubic clique partition problem  $\rightarrow$  **Partial Optimality Conditions**:

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#### Partial Optimality Algorithm:

Input: clustering y without fixed labels
while condition applied do
apply subproblem-CUT-condition exhaustively
apply one of JOIN-conditions (in effective order)
end while

apply CUT-conditions exhaustively

**Output:** partially optimal clustering y with some fixed labels

### Program Structure

Class Diagram Algorithm implementation in ClusteringProblem Features: ClusteringProblem is generally defined for all types of Cubic Clique Partition Problem (not necessarily points), cost function + sparse costs!, label computation, cut triples, logs joins and cuts! (add screenshots)

# Subproblem-CUT

A couple of words about the split and the implementation (with picture of splitting)

#### JOIN-conditions

Special attention to 3.11 (+ my adjustment) Mention reduction to Min-Cut problem and the complexity!!!

### JOIN-conditions

Overview of the other join-conditions (with pictures)

### **CUT-conditions**

Overview of the cut-conditions (with pictures)

### Example

Pyramid example for my algorithm