1 Notes

The following notations may be used within VoxML specifications to structure voxeme instances, subject to the definitions below.

- \mathcal{E} the minimal embedding space (MES)
- \mathcal{E}_A the axis A of the MES
- loc(x) location of object x
- orient(x) orientation of object x
- vec(A) vector denoted by (positive unless otherwise specified) axis A
- opp(v) opposite vector of v
- reify(x, s) relabel object x (can be a collection $(c_1,...,c_n)$) as symbol s
- interior(x) the interior surface (and volumetric enclosed space) of object x
- exterior(x) the exterior surface of object x
- dimension(x) the number of dimensions defining entity x
- ullet while(c,e) operation e is executed as long as condition c is true
- $for(x \in y)$ following operation is executed for each element x in collection y
- def(x, y) defines y as the value of x
- as(i) comparator, returns input i as generic symbol
- align(A, B) defines vector A as aligned (parallel) with vector B

2 Templates

$$(1) \begin{bmatrix} \textbf{OBJECT} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \dots \\ \text{TYPE} = \dots \end{bmatrix} \\ \begin{bmatrix} \text{HEAD} = \dots \\ \text{COMPONENTS} = \dots \\ \text{CONCAVITY} = \dots \\ \text{ROTATSYM} = \{\dots\} \\ \text{ROTSTR} = \{\dots\} \end{bmatrix} \\ \text{HABITAT} = \begin{bmatrix} \text{INTR} = \dots \\ \text{EXTR} = \dots \end{bmatrix} \\ \text{AFFORD_STR} = \begin{bmatrix} A_n = H_{[\#]} \rightarrow [E(a_{1..n})]R(a_{1..n}) \end{bmatrix} \\ \text{EMBODIMENT} = \begin{bmatrix} \text{SCALE} = \dots \\ \text{MOVABLE} = \dots \end{bmatrix} \end{bmatrix}$$

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TYPE physobj, artifact
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HEAD prismatoid, pyramid, wedge, parallelepiped, cupola, frustum, cylindroid, ellipsoid, hemiellipsoid, bipyramid, rectangular_prism, toroid, sheet

CONCAVITY | convex, flat, concave

ROTATSYM X, Y, Z

REFLSYM XY, XZ, YZ

SCALE <agent, agent >agent

MOVABLE true, false

DENSITY 1...7

(2) $\begin{bmatrix} \textbf{PROGRAM} \\ \textbf{LEX} = \begin{bmatrix} \textbf{PRED} = ... \\ \textbf{TYPE} = ... \end{bmatrix} \\ \textbf{TYPE} = \begin{bmatrix} \textbf{HEAD} = ... \\ \textbf{ARGS} = \begin{bmatrix} \textbf{A}_1 = \textbf{x:a} \end{bmatrix} \\ \textbf{BODY} = \begin{bmatrix} \textbf{E}_n = E(a_{1..n}) \end{bmatrix} \end{bmatrix}$

TYPE process, transition_event

HEAD state, process, transition, assignment, test

(3) $\begin{bmatrix} ATTRIBUTE \\ LEX = \begin{bmatrix} PRED = ... \end{bmatrix} \\ TYPE = \begin{bmatrix} SCALE = ... \\ ARITY = ... \\ ARG = x:a \end{bmatrix} \end{bmatrix}$

SCALE nominal, binary, ordinal, interval, rational

ARITY intransitive, transitive

(4)
$$\begin{bmatrix} \textbf{RELATION} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \dots \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{CLASS} = \dots \\ \text{VALUE} = \dots \\ \text{ARGS} = \begin{bmatrix} A_n = \textbf{X:...} \end{bmatrix} \end{bmatrix}$$

CLASS config, force_dynamic

VALUE values of QSR calculus in use

(5)
$$\begin{bmatrix} \textbf{FUNCTION} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{...} \\ \text{PRED} = \textbf{...} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \textbf{x:a} \\ \text{REFERENT} = \textbf{x} \rightarrow \dots \\ \text{MAPPING} = \textbf{f(n):R} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{...} \\ \text{AXIS} = \textbf{...} \\ \text{ARITY} = \textbf{a}(\rightarrow \text{PARAM}) * [bool(p)]:condition \end{bmatrix} \end{bmatrix}$$

SPACE | world, object, pov

AXIS
$$+X$$
, $-X$, $+Y$, $-Y$, $+Z$, $-Z$

3 Thesis Test Set

3.1 Objects

$$[b] \begin{tabular}{l} \textbf{block} \\ \textbf{LEX} &= \begin{bmatrix} \texttt{PRED} &= \textbf{block} \\ \texttt{TYPE} &= \textbf{physobj}, \textbf{artifact} \end{bmatrix} \\ \textbf{TYPE} &= \begin{bmatrix} \texttt{HEAD} &= \textbf{rectangular_prism[1]} \\ \texttt{COMPONENTS} &= \textbf{nil} \\ \texttt{CONCAVITY} &= \textbf{flat} \\ \texttt{ROTATSYM} &= \{X,Y,Z\} \\ \texttt{REFLECTSYM} &= \{XY,XZ,YZ\} \end{bmatrix} \\ \textbf{HABITAT} &= \begin{bmatrix} \texttt{INTR} &= [2] [\texttt{CONSTR} &= \{X=Y+Z\}] \\ \texttt{EXTR} &= \dots \end{bmatrix} \\ \textbf{AFFORD_STR} &= \begin{bmatrix} \texttt{A}_1 &= H_{[2]} \rightarrow [put(x,on([1]))]support([1],x) \texttt{A}_3 &= H_{[2]} \rightarrow [grasp(x,[1])] \end{bmatrix} \\ \textbf{EMBODIMENT} &= \begin{bmatrix} \texttt{SCALE} &= \textbf{cagent} \\ \texttt{MOVABLE} &= \textbf{true} \end{bmatrix} \\ \end{tabular}$$

$$[ball] \\ LEX = \begin{bmatrix} PRED = ball \\ TYPE = physobj, artifact \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = ellipsoid[1] \\ COMPONENTS = nil \\ CONCAVITY = convex \\ ROTATSYM = \{X, Y, Z\} \\ REFLECTSYM = \{XY, XZ, YZ\} \end{bmatrix} \\ [Total Description of the problem of the prob$$

$$\begin{bmatrix} \textbf{plate} \\ \texttt{LEX} = \begin{bmatrix} \texttt{PRED} = \textbf{plate} \\ \texttt{TYPE} = \textbf{physobj, artifact} \end{bmatrix} \\ \texttt{TYPE} = \begin{bmatrix} \texttt{HEAD} = \textbf{sheet}[1] \\ \texttt{COMPONENTS} = \textbf{base, surface}[1] \\ \texttt{CONCAVITY} = \textbf{concave} \\ \texttt{ROTATSYM} = \left\{ Y \right\} \\ \texttt{REFLECTSYM} = \left\{ XY, YZ \right\} \end{bmatrix}$$

$$\begin{bmatrix} \texttt{INTR} = [2] \\ \texttt{UP} = align(Y, \mathcal{E}_Y) \\ \texttt{TOP} = top(+Y) \end{bmatrix} \\ \texttt{EXTR} = [3] \begin{bmatrix} \texttt{UP} = align(Y, \mathcal{E}_{\perp Y}) \end{bmatrix}$$

$$\begin{bmatrix} \texttt{A}_1 = H_{[2]} \rightarrow [put(x, on([1]))]support([1], x) \\ \texttt{A}_2 = H_{[2]} \rightarrow [put(x, in([1]))]contain([1], x) \\ \texttt{A}_3 = H_{[2]} \rightarrow [grasp(x, [1])] \\ \texttt{A}_3 = H_{[2]} \rightarrow [grasp(x, [1])] \\ \texttt{A}_3 = H_{[2]} \rightarrow [slide(x, [1])] \\ \texttt{A}_3 = H_{[2]} \rightarrow [slide(x, [1])] \\ \texttt{A}_3 = H_{[3]} \rightarrow [roll(x, [1])] \end{bmatrix}$$

$$\texttt{EMBODIMENT} = \begin{bmatrix} \texttt{SCALE} = \langle \textbf{agent} \\ \texttt{MOVABLE} = \textbf{true} \end{bmatrix}$$

$$\begin{bmatrix} \textbf{disc} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{disc} \\ \text{TYPE} = \textbf{physobj, artifact} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{cylindroid[1]} \\ \text{COMPONENTS} = \textbf{nil} \\ \text{CONCAVITY} = \textbf{flat} \\ \text{ROTATSYM} = \left\{ Y \right\} \\ \text{REFLECTSYM} = \left\{ XY, YZ \right\} \end{bmatrix} \\ \text{HABITAT} = \begin{bmatrix} \text{INTR} = [2] \Big[\text{CONSTR} = \left\{ X < Y, Z > Y \right\} \Big] \\ \text{EXTR} = \begin{bmatrix} [3] \\ Z([1]) \geqslant Z(y:physobj), \\ [4] \Big[\text{UP} = align(Y, \mathcal{E}_{\perp Y}) \Big] \end{bmatrix} \end{bmatrix} \\ \text{AFFORD_STR} = \begin{bmatrix} A_1 = H_{[2]} \rightarrow [grasp(x, [1])] \\ A_2 = H_{[3]} \rightarrow [put([1], on(y)]close([1], y) \\ A_4 = H_{[4]} \rightarrow [roll(x, [1])] \end{bmatrix} \\ \text{EMBODIMENT} = \begin{bmatrix} \text{SCALE} = \langle \mathbf{agent} \\ \text{MOVABLE} = \mathbf{true} \end{bmatrix}$$

$$[SPOON] \label{eq:local_transform} \begin{bmatrix} \text{spoon} \\ \text{TYPE} = \text{physobj, artifact} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{PRED} = \text{sheet}[1] \\ \text{COMPONENTS} = \text{handle}[2], \text{bowl}[3] \\ \text{CONCAVITY} = \text{concave} \\ \text{ROTATSYM} = nil \\ \text{REFLECTSYM} = \{YZ\} \end{bmatrix} \\ \text{HABITAT} = \begin{bmatrix} \text{INTR} = [4] \begin{bmatrix} \text{CONSTR} = \{Z > X, Z \gg Y\} \\ \text{UP} = align(Y, \mathcal{E}_Y) \\ \text{FRONT} = top(+Y) \end{bmatrix} \\ \text{EXTR} = [5] \begin{bmatrix} \text{UP} = align(Y, \mathcal{E}_{\perp Y}) \end{bmatrix} \\ \text{AFFORD_STR} = \begin{bmatrix} A_1 = H_{[4]} \rightarrow [put(x, in([3]))]contain([3], x) \\ A_2 = H_{[4]} \rightarrow [put([1], in(x))]contain(x, [1]) \\ A_1 = H_{[5]}, contain(x, [1]) \rightarrow [stir(x, [1])] \end{bmatrix} \\ \text{EMBODIMENT} = \begin{bmatrix} \text{SCALE} = \langle \textbf{agent} \\ \text{MOVABLE} = \textbf{true} \end{bmatrix}$$

$$\begin{bmatrix} \textbf{book} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{book} \\ \text{TYPE} = \textbf{physobj, artifactj} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{rectangular_prism[1]} \\ \text{COMPONENTS} = \textbf{cover[2]+, page[3]+} \\ \text{CONCAVITY} = \textbf{flat} \\ \text{ROTATSYM} = \textbf{nil} \\ \text{REFLECTSYM} = \left\{ XY \right\} \end{bmatrix} \\ \text{HABITAT} = \begin{bmatrix} \text{INTR} = [4] \\ \text{INTR} = [4] \\ \text{EXTR} = ... \end{bmatrix} \begin{bmatrix} \text{UP} = align(Y, \mathcal{E}_Y) \\ \text{TOP} = front(+Y) \end{bmatrix} \\ \text{EXTR} = \begin{bmatrix} A_1 = H \rightarrow [grasp(x, [2]), \\ move(x, [2], away(from([3])))]open(x, [1]) \\ A_2 = H \rightarrow [grasp(x, [2]), \\ move(x, [2], toward([3]))]close(x, [1]) \end{bmatrix} \\ \text{EMBODIMENT} = \begin{bmatrix} \text{SCALE} = \langle \textbf{agent} \\ \text{MOVABLE} = \textbf{true} \end{bmatrix}$$

$$\begin{bmatrix} \textbf{blackboard} \\ \textbf{LEX} = \begin{bmatrix} \textbf{PRED} = \textbf{blackboard} \\ \textbf{TYPE} = \textbf{physobj, artifactj} \end{bmatrix} \\ \textbf{TYPE} = \begin{bmatrix} \textbf{HEAD} = \textbf{sheet}[\textbf{1}] \\ \textbf{COMPONENTS} = \textbf{board, surface}[\textbf{1}], \textbf{back, leg}[\textbf{2}] + \\ \textbf{CONCAVITY} = \textbf{flat} \\ \textbf{ROTATSYM} = \textbf{nil} \\ \textbf{REFLECTSYM} = \{YZ\} \end{bmatrix} \\ \textbf{INTR} = \begin{bmatrix} \textbf{I} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{I} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} = \textbf{IMTR} \\ \textbf{IMTR} = \begin{bmatrix} \textbf{IMTR} = \textbf{I$$

$$\begin{bmatrix} \textbf{bottle} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{bottle} \\ \text{TYPE} = \textbf{physobj, artifact} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{cylindroid[1]} \\ \text{COMPONENTS} = \textbf{surface, interior} \\ \text{CONCAVITY} = \textbf{concave} \\ \text{ROTATSYM} = \{Y\} \\ \text{REFLECTSYM} = \{XY, YZ\} \end{bmatrix} \\ \text{HABITAT} = \begin{bmatrix} \text{INTR} = [2] \begin{bmatrix} \text{CONSTR} = \{Y > X, Y > Z\} \\ \text{UP} = align(Y, \mathcal{E}_Y) \\ \text{TOP} = top(+Y) \end{bmatrix} \\ \text{EXTR} = [3] \begin{bmatrix} \text{UP} = align(Y, \mathcal{E}_{\perp Y}) \end{bmatrix} \end{bmatrix} \\ \text{AFFORD_STR} = \begin{bmatrix} A_1 = H_{[2]} \rightarrow [put(x, on([1]))]support([1], x) \\ A_2 = H_{[2]} \rightarrow [put(x, in([1]))]contain([1], x) \\ A_3 = H_{[2]} \rightarrow [grasp(x, [1])] \\ A_4 = H_{[3]} \rightarrow [roll(x, [1])] \end{bmatrix} \\ \text{EMBODIMENT} = \begin{bmatrix} \text{SCALE} = \langle \textbf{agent} \\ \text{MOVABLE} = \textbf{true} \end{bmatrix}$$

$$\begin{bmatrix} \mathbf{grape} \\ \operatorname{LEX} = \begin{bmatrix} \operatorname{PRED} = \mathbf{grape} \\ \operatorname{TYPE} = \mathbf{physobj} \end{bmatrix} \\ \operatorname{TYPE} = \begin{bmatrix} \operatorname{HEAD} = \mathbf{ellipsoid[1]} \\ \operatorname{COMPONENTS} = \mathbf{fruit[1]} \\ \operatorname{CONCAVITY} = \mathbf{flat} \\ \operatorname{ROTATSYM} = \{Y\} \\ \operatorname{REFLECTSYM} = \{XY, YZ\} \end{bmatrix} \\ \operatorname{HABITAT} = \begin{bmatrix} \operatorname{INTR} = \dots \\ \operatorname{EXTR} = [2] [\operatorname{UP} = align(Y, \mathcal{E}_{\perp Y})] \end{bmatrix} \\ \operatorname{AFFORD_STR} = \begin{bmatrix} \operatorname{A}_1 = H \to [\operatorname{grasp}(x, [1])] \\ \operatorname{A}_1 = H \to [\operatorname{hold}(x, [1])] \operatorname{lift}(x, [1]) \\ \operatorname{A}_1 = H_{[2]} \to [\operatorname{rotl}(x, [1])] \\ \operatorname{A}_1 = H_{[2]} \to [\operatorname{rotl}(x, [1])] \end{bmatrix} \\ \operatorname{EMBODIMENT} = \begin{bmatrix} \operatorname{SCALE} = \langle \operatorname{\mathbf{agent}} \\ \operatorname{MOVABLE} = \operatorname{\mathbf{true}} \end{bmatrix} \\ \end{bmatrix}$$

$$[AFFORD_STR = \begin{bmatrix} APRED & apple \\ TYPE & physobj \end{bmatrix}$$

$$[AFFORD_STR = \begin{bmatrix} APRED & ellipsoid[1] \\ COMPONENTS & fruit[1], stem, leaf \\ CONCAVITY & effat \\ ROTATSYM & = {Y} \\ REFLECTSYM & = {XY, YZ} \end{bmatrix}$$

$$[AAFFORD_STR = \begin{bmatrix} INTR & ... \\ EXTR & = [2][UP & align(Y, \mathcal{E}_{\perp Y})] \\ A_1 & = H \rightarrow [nold(x, [1])] lift(x, [1]) \\ A_1 & = H \rightarrow [slide(x, [1])] \\ A_1 & = H_{[2]} \rightarrow [roll(x, [1])] \end{bmatrix}$$

$$[EMBODIMENT = \begin{bmatrix} SCALE & = \langle \mathbf{agent} \\ MOVABLE & \mathbf{true} \end{bmatrix}$$

$$[TYPE] \begin{bmatrix} \textbf{banana} \\ TYPE = \textbf{physobj} \end{bmatrix} \\ TYPE = \begin{bmatrix} PRED = \textbf{banana} \\ TYPE = \textbf{physobj} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{cylindroid[1]} \\ COMPONENTS = \textbf{fruit[1], stem} \\ CONCAVITY = \textbf{convex} \\ ROTATSYM = \{Y\} \\ REFLECTSYM = \{YZ\} \end{bmatrix} \\ HABITAT = \begin{bmatrix} INTR = ... \\ EXTR = [2] [UP = align(Y, \mathcal{E}_{\perp Y})] \end{bmatrix} \\ AFFORD_STR = \begin{bmatrix} A_3 = H \rightarrow [grasp(x, [1])] \\ A_3 = H \rightarrow [hold(x, [1])]lift(x, [1]) \\ A_4 = H_{[2]} \rightarrow [slide(x, [1])] \end{bmatrix} \\ EMBODIMENT = \begin{bmatrix} SCALE = \langle \textbf{agent} \\ MOVABLE = \textbf{true} \end{bmatrix}$$

$$[table] \begin{tabular}{l} \textbf{table} \\ \textbf{LEX} &= \begin{bmatrix} \texttt{PRED} = \textbf{table} \\ \texttt{TYPE} = \textbf{physobj, artifactj} \end{bmatrix} \\ \textbf{TYPE} &= \begin{bmatrix} \texttt{HEAD} = \textbf{sheet[1]} \\ \texttt{COMPONENTS} = \textbf{surface[1], leg[2]+} \\ \texttt{CONCAVITY} &= \textbf{flat} \\ \texttt{ROTATSYM} &= \{Y\} \\ \texttt{REFLECTSYM} &= \{XY, YZ\} \end{bmatrix} \\ \textbf{HABITAT} &= \begin{bmatrix} \texttt{INTR} &= [3] \\ \texttt{INTR} &= [3] \end{bmatrix} \begin{bmatrix} \texttt{UP} = align(Y, \mathcal{E}_Y) \\ \texttt{TOP} = top(+Y) \\ \texttt{CONSTR[1]} &= \{Y \ll X, Y \ll Z\} \\ \texttt{EXTR} &= \dots \\ \end{bmatrix} \\ \textbf{EXTR} &= \dots \\ \textbf{AFFORD_STR} &= \begin{bmatrix} \texttt{A}_1 &= H \rightarrow [grasp(x, [1])] \\ \texttt{A}_1 &= H \rightarrow [hold(x, [1])]lift(x, [1]) \\ \texttt{A}_1 &= H \rightarrow [slide(x, [1])] \\ \texttt{A}_1 &= H_{[2]} \rightarrow [roll(x, [1])] \\ \texttt{EMBODIMENT} &= \begin{bmatrix} \texttt{SCALE} = \textbf{agent} \\ \texttt{MOVABLE} = \textbf{true} \end{bmatrix} \\ \end{bmatrix}$$

$$[TYPE] \begin{bmatrix} \textbf{bowl} \\ TYPE & = \textbf{physobj, artifact} \end{bmatrix}$$

$$TYPE = \begin{bmatrix} \text{HEAD} & = \textbf{cylindroid[1]} \\ \text{COMPONENTS} & = \textbf{base, interior} \\ \text{CONCAVITY} & = \textbf{concave} \\ \text{ROTATSYM} & = \{Y\} \\ \text{REFLECTSYM} & = \{XY, YZ\} \end{bmatrix}$$

$$[TOP] \begin{bmatrix} \text{INTR} & = [2] \\ \text{INTR} & = [2] \\ \text{UP} & = align(Y, \mathcal{E}_Y) \\ \text{TOP} & = top(+Y) \end{bmatrix}$$

$$[TOP] \begin{bmatrix} \text{EXTR} & = [3] \\ \text{EXTR} & = [3] \\ \text{EXTR} & = [3] \end{bmatrix} \begin{bmatrix} \text{UP} & = align(Y, \mathcal{E}_{\perp Y}) \end{bmatrix}$$

$$[TOP] \begin{bmatrix} \text{A}_1 & = H_{[2]} \rightarrow [put(x, on([1]))]support([1], x) \\ \text{A}_2 & = H_{[2]} \rightarrow [put(x, in([1]))]contain([1], x) \\ \text{A}_3 & = H_{[2]} \rightarrow [prasp(x, [1])] \\ \text{A}_3 & = H_{[2]} \rightarrow [prasp(x, [1])] \\ \text{A}_3 & = H_{[2]} \rightarrow [slide(x, [1])] \\ \text{A}_3 & = H_{[3]} \rightarrow [roll(x, [1])] \end{bmatrix}$$

$$[TOP] \begin{bmatrix} \text{EMBODIMENT} & \text{EMBO$$

$$[ABITAT] \begin{bmatrix} \textbf{knife} \\ LEX = \begin{bmatrix} PRED = \textbf{knife} \\ TYPE = \textbf{physobj, artifact} \end{bmatrix} \\ HABITAT = \begin{bmatrix} HEAD = \textbf{rectangular_prism[1]} \\ COMPONENTS = \textbf{handle[2], blade} \\ CONCAVITY = \textbf{flat} \\ ROTATSYM = nil \\ REFLECTSYM = \{XY\} \end{bmatrix} \\ HABITAT = \begin{bmatrix} INTR = [3] \begin{bmatrix} CONSTR = \{X > Y, X \gg Z\} \\ FRONT = front(+X) \end{bmatrix} \\ EXTR = ... \\ AFFORD_STR = \begin{bmatrix} A_1 = H_{[3]} \rightarrow [grasp(x, [1])] \\ A_2 = H_{[3]} \rightarrow [grasp(x, [2]) \rightarrow grasp(x, [1])] \end{bmatrix} \\ EMBODIMENT = \begin{bmatrix} SCALE = \langle \textbf{agent} \\ MOVABLE = \textbf{true} \end{bmatrix}$$

$$[PRED] = pencil \\ LEX = \begin{bmatrix} PRED = pencil \\ TYPE = physobj, artifact \end{bmatrix} \\ HEAD = cylindroid[1] \\ COMPONENTS = shaft[1], eraser, nib \\ CONCAVITY = convex \\ ROTATSYM = \{Z\} \\ REFLECTSYM = \{XZ, YZ\} \end{bmatrix} \\ [ABITAT] = \begin{bmatrix} INTR = [4] \\ FORWARD = align(Z, \mathcal{E}_Z) \\ FRONT = front(+Z) \\ EXTR = [5] \\ FORWARD = align(Z, \mathcal{E}_{\perp Y}) \end{bmatrix} \\ AFFORD_STR = \begin{bmatrix} A_3 = H_{[4]} \rightarrow [grasp(x, [1])] \\ A_3 = H_{[4]} \rightarrow [hold(x, [1])]lift(x, [1]) \\ A_4 = H_{[5]} \rightarrow [roll(x, [1])] \\ EMBODIMENT = \begin{bmatrix} SCALE = \langle agent \\ MOVABLE = true \end{bmatrix}$$

$$\begin{bmatrix} \mathbf{paper sheet} \\ \mathrm{LEX} = \begin{bmatrix} \mathrm{PRED} = \mathbf{paper_sheet} \\ \mathrm{TYPE} = \mathbf{physobj, artifactj} \end{bmatrix} \\ \mathrm{HEAD} = \mathbf{sheet[1]} \\ \mathrm{COMPONENTS} = \mathbf{nil} \\ \mathrm{CONCAVITY} = \mathbf{flat} \\ \mathrm{ROTATSYM} = \{Y\} \\ \mathrm{REFLECTSYM} = \{XY, YZ\} \end{bmatrix} \\ (22) \\ \mathrm{HABITAT} = \begin{bmatrix} \mathrm{INTR} = [2] \begin{bmatrix} \mathrm{UP} = align(Y, \mathcal{E}_Y) \\ \mathrm{TOP} = top(+Y) \\ \mathrm{CONSTR} = \{Y \ll X, Y \ll Z\} \end{bmatrix} \\ \mathrm{EXTR} = \dots \\ \\ \mathrm{AFFORD_STR} = \begin{bmatrix} \mathrm{A}_1 = H_{[2]} \rightarrow [grasp(x, [1])] \\ \mathrm{A}_1 = H_{[2]} \rightarrow [hold(x, [1])]lift(x, [1]) \\ \mathrm{A}_1 = H_{[2]} \rightarrow [slide(x, [1])] \\ \mathrm{EMBODIMENT} = \begin{bmatrix} \mathrm{SCALE} = \langle \mathbf{agent} \\ \mathrm{MOVABLE} = \mathbf{true} \end{bmatrix} \end{bmatrix}$$

3.2 Programs

(23)
$$\begin{bmatrix} \mathbf{grasp} \\ \mathrm{LEX} = \begin{bmatrix} \mathrm{PRED} = \mathbf{grasp} \\ \mathrm{TYPE} = \mathbf{transition_event} \end{bmatrix} \\ \mathrm{TYPE} = \begin{bmatrix} \mathrm{HEAD} = \mathbf{transition} \\ \mathrm{ARGS} = \begin{bmatrix} \mathrm{A_1} = \mathbf{x:agent} \\ \mathrm{A_2} = \mathbf{y:physobj} \end{bmatrix} \\ \mathrm{BODY} = \begin{bmatrix} \mathrm{E_1} = \mathbf{grasp}(x, y) \end{bmatrix} \end{bmatrix}$$

(24)
$$\begin{bmatrix} \textbf{hold} \\ LEX = \begin{bmatrix} PRED = \textbf{hold} \\ TYPE = \textbf{state} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{state} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = maintain_rel(x, y) \end{bmatrix} \end{bmatrix}$$

(25)
$$\begin{bmatrix} \textbf{touch} \\ LEX = \begin{bmatrix} PRED = \textbf{touch} \\ TYPE = \textbf{transition_event} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{transition} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = \neg EC(x, y) \rightarrow move(x, toward(y)) \end{bmatrix} \end{bmatrix}$$

(26)
$$\begin{bmatrix} \mathbf{move} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{move} \\ \text{TYPE} = \mathbf{process} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \mathbf{process} \\ \text{ARGS} = \begin{bmatrix} A_1 = \mathbf{x:agent} \\ A_2 = \mathbf{y:physobj} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = [while(hold(x, y), move(x, y)] \end{bmatrix} \end{bmatrix}$$

(27)
$$\begin{bmatrix} \mathbf{turn} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{turn} \\ \text{TYPE} = \mathbf{process} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \mathbf{process} \\ \text{ARGS} = \begin{bmatrix} A_1 = \mathbf{x:agent} \\ A_2 = \mathbf{y:physobj} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = [while(hold(x, y), rotate(y)] \end{bmatrix} \end{bmatrix}$$

$$[28) \begin{bmatrix} \textbf{roll} \\ \textbf{LEX} = \begin{bmatrix} \textbf{PRED} = \textbf{roll} \\ \textbf{TYPE} = \textbf{process} \end{bmatrix} \\ \textbf{TYPE} = \begin{bmatrix} \textbf{HEAD} = \textbf{process} \\ \textbf{ARGS} = \begin{bmatrix} \textbf{A}_1 = \textbf{x:agent} \\ \textbf{A}_2 = \textbf{y:physobj} \\ \textbf{A}_3 = \textbf{z:physobj} \end{bmatrix} \\ \textbf{BODY} = \begin{bmatrix} \textbf{E}_1 = grasp(x, y) \\ \textbf{E}_2 = [while(hold(x, y), while(EC(y, z), translocate(x, y), rotate(x, y)))] \end{bmatrix}]$$

$$\begin{bmatrix} \textbf{slide} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{slide} \\ \text{TYPE} = \textbf{process} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{process} \\ \text{ARGS} = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \\ A_3 = \textbf{z:physobj} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = [while(hold(x, y), while(EC(y, z), move(x, y)))] \end{bmatrix} \end{bmatrix}$$

$$(30) \begin{bmatrix} \textbf{spin} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{spin} \\ \text{TYPE} = \textbf{process} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{process} \\ \text{ARGS} = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = rotate(x, y) \\ E_3 = ungrasp(x, y) \end{bmatrix} \end{bmatrix}$$

(31)
$$\begin{bmatrix} \textbf{lift} \\ LEX = \begin{bmatrix} PRED = \textbf{lift} \\ TYPE = \textbf{process} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{process} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = [while(hold(x, y), move(x, y, vec(\mathcal{E}_Y))))] \end{bmatrix} \end{bmatrix}$$

$$[32] \begin{bmatrix} \textbf{stack} \\ LEX = \begin{bmatrix} PRED = \textbf{stack} \\ TYPE = \textbf{transition_event} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{transition} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y[]:physobj} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = def(y[0], as(z)), for(o \in y[1..n]) \\ [put(o, on(z)), reify((z, o), as(z)] \end{bmatrix} \end{bmatrix}$$

$$[33] \begin{bmatrix} \textbf{put} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{put} \\ \text{TYPE} = \textbf{transition_event} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{transition} \\ \text{ARGS} = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \\ A_3 = \textbf{z:location} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = \begin{bmatrix} while(hold(x, y), move(x, y)] \\ E_3 = [at(y, z) \rightarrow ungrasp(x, y)] \end{bmatrix} \end{bmatrix}$$

$$[34] \begin{bmatrix} \textbf{lean} \\ LEX = \begin{bmatrix} PRED = \textbf{lean} \\ TYPE = \textbf{transition_event} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{transition} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \\ A_3 = \textbf{z:location} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = [while(hold(x, y), rotate(x, y)] \\ E_3 = [support(y, z) \rightarrow ungrasp(x, y)] \end{bmatrix} \end{bmatrix}$$

$$[35] \begin{bmatrix} \textbf{flip} \\ LEX = \begin{bmatrix} PRED = \textbf{flip} \\ TYPE = \textbf{transition_event} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{transition} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = def(w, as(orient(y)))[grasp(x, y)] \\ E_2 = [while(hold(x, y), rotate(x, y)] \\ E_3 = [(orient(y) = opp(w)) \rightarrow ungrasp(x, y)] \end{bmatrix} \end{bmatrix}$$

$$[36] \begin{bmatrix} \textbf{close} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{close} \\ \text{TYPE} = \textbf{transition_event} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{transition} \\ \text{ARGS} = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x,y) \\ E_2 = [while(hold(x,y), move(x,y))] \\ E_3 = [EC(interior(y), \mathcal{E}) \rightarrow ungrasp(x,y)] \end{bmatrix} \end{bmatrix}$$

(37)
$$\begin{bmatrix} \textbf{open} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{open} \\ \text{TYPE} = \textbf{transition_event} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{HEAD} = \textbf{transition} \\ \text{ARGS} = \begin{bmatrix} A_1 = \textbf{x:agent} \\ A_2 = \textbf{y:physobj} \end{bmatrix} \\ \text{BODY} = \begin{bmatrix} E_1 = grasp(x, y) \\ E_2 = [while(hold(x, y), move(x, y))] \\ E_3 = [DC(interior(y), \mathcal{E}) \rightarrow ungrasp(x, y)] \end{bmatrix} \end{bmatrix}$$

3.3 Relations

(38)
$$\begin{bmatrix} \mathbf{on} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{on} \end{bmatrix} \\ \text{CLASS} = \mathbf{config} \\ \text{VALUE} = \mathbf{EC} \\ \text{ARGS} = \begin{bmatrix} A_1 = \mathbf{x} : \mathbf{3D} \\ A_2 = \mathbf{y} : \mathbf{3D} \end{bmatrix} \\ \text{CONSTR} = \mathbf{y} \rightarrow \text{HABITAT} \rightarrow \text{INTR}[align] \end{bmatrix}$$

(39)
$$\begin{bmatrix} \mathbf{in} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{in} \end{bmatrix} \\ \text{CLASS} = \mathbf{config} \\ \text{VALUE} = \mathbf{PO} \parallel \mathbf{TPP} \parallel \mathbf{NTPP} \\ \text{ARGS} = \begin{bmatrix} A_1 = \mathbf{x} : \mathbf{3D} \\ A_2 = \mathbf{y} : \mathbf{3D} \end{bmatrix} \\ \text{CONSTR} = \mathbf{y} \rightarrow \text{HABITAT} \rightarrow \text{INTR}[align]?} \end{bmatrix}$$

$$(40) \begin{bmatrix} \textbf{against} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{against} \end{bmatrix} \\ \text{CLASS} = \textbf{force_dynamic} \\ \text{VALUE} = \textbf{EC} \\ \text{ARGS} = \begin{bmatrix} A_1 = \textbf{x:3D} \\ A_2 = \textbf{y:3D} \end{bmatrix} \\ \text{CONSTR} = \textbf{nil} \end{bmatrix}$$

$$(41) \begin{bmatrix} \mathbf{at} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{at} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{CLASS} = \mathbf{config} \\ \text{VALUE} = \mathbf{DC} \parallel \mathbf{EC} \\ \text{ARGS} = \begin{bmatrix} A_1 = \mathbf{x:3D} \\ A_2 = \mathbf{y:3D} \end{bmatrix} \\ \text{CONSTR} = dist(x, y) < \epsilon \end{bmatrix}$$

3.4 Functions

(42)
$$\begin{bmatrix} \mathbf{edge} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{edge} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \mathbf{x} : \mathbf{physobj} \\ \text{REFERENT} = \mathbf{x} \to \text{HEAD} \\ \text{MAPPING} = \mathbf{dimension(n):1} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \mathbf{object} \\ \text{AXIS} = \mathbf{ref:after} \\ \text{ARITY} = \mathbf{x} \to \text{HABITAT} \to \\ \text{INTR}[axis] \end{bmatrix}$$

$$(43) \begin{bmatrix} \textbf{center} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{center} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \rightarrow \text{HEAD} \\ \text{MAPPING} = \textbf{dimension(n):0} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{object} \\ \text{AXIS} = \textbf{nil} \\ \text{ARITY} = intransitive} \end{bmatrix}$$

4 General Voxeme List

$$[44] \begin{bmatrix} \textbf{top} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{top} \end{bmatrix} \\ \text{ARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \rightarrow \text{HEAD} \\ \text{MAPPING} = \textbf{dimension(n):n-1} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{world} \\ \text{AXIS} = +\textbf{Y} \\ \text{ARITY} = \textbf{x} \rightarrow \text{HABITAT} \rightarrow \\ \text{INTR}[top(axis)]: \\ intransitive \end{bmatrix} \end{bmatrix}$$

(45)
$$\begin{bmatrix} \textbf{bottom} \\ LEX = \begin{bmatrix} PRED = \textbf{bottom} \end{bmatrix} \\ ARG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \rightarrow HEAD \\ MAPPING = \textbf{dimension(n):n-1} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{world} \\ AXIS = -\textbf{Y} \\ ARITY = \textbf{x} \rightarrow HABITAT \rightarrow \\ INTR[bottom(axis)]: \\ intransitive \end{bmatrix}$$

(46)
$$\begin{bmatrix} \textbf{front} \\ LEX = \begin{bmatrix} PRED = \textbf{front} \end{bmatrix} \\ RAG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \rightarrow HEAD \\ MAPPING = \textbf{dimension(n):n-1} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{world} \\ AXIS = \textbf{+Z} \\ ARITY = \textbf{x} \rightarrow HABITAT \rightarrow \\ INTR[front(axis)]: \\ intransitive \end{bmatrix}$$

$$[47] \begin{bmatrix} \textbf{back} \\ LEX = \begin{bmatrix} PRED = \textbf{back} \end{bmatrix} \\ ARG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \rightarrow HEAD \\ MAPPING = \textbf{dimension(n):n-1} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{world} \\ AXIS = \textbf{-Z} \\ ARITY = \textbf{x} \rightarrow HABITAT \rightarrow \\ INTR[back(axis)]: \\ intransitive \end{bmatrix} \end{bmatrix}$$

(48)
$$\begin{bmatrix} \textbf{right} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{right} \end{bmatrix} \\ \text{ARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \rightarrow \text{HEAD} \\ \text{MAPPING} = \textbf{dimension(n):n-1} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{world} \\ \text{AXIS} = +\textbf{X} \\ \text{ARITY} = \textbf{x} \rightarrow \text{HABITAT} \rightarrow \\ \text{INTR}[right(axis)]: \\ intransitive \end{bmatrix}$$

(49)
$$\begin{bmatrix} \textbf{left} \\ LEX = \begin{bmatrix} PRED = \textbf{left} \end{bmatrix} \\ RAG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \rightarrow HEAD \\ MAPPING = \textbf{dimension(n):n-1} \end{bmatrix}$$

$$ORIENTATION = \begin{bmatrix} SPACE = \textbf{world} \\ AXIS = -\textbf{X} \\ ARITY = \textbf{x} \rightarrow HABITAT \rightarrow \\ INTR[left(axis)]: \\ intransitive \end{bmatrix}$$

(50)
$$\begin{bmatrix} \mathbf{center} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \mathbf{center} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \mathbf{x:physobj} \\ \text{REFERENT} = \mathbf{x} \rightarrow \text{HEAD} \\ \text{MAPPING} = \mathbf{dimension(n):0} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \mathbf{object} \\ \text{AXIS} = \mathbf{nil} \\ \text{ARITY} = intransitive} \end{bmatrix}$$

$$(51) \begin{bmatrix} \textbf{edge} \\ LEX = \begin{bmatrix} PRED = \textbf{edge} \end{bmatrix} \\ TYPE = \begin{bmatrix} ARG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \rightarrow HEAD \\ MAPPING = \textbf{dimension(n):1} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{object} \\ AXIS = (\textbf{see linked attribute}) \\ ARITY = (seelinkedattribute) \end{bmatrix} \end{bmatrix}$$

(52)
$$\begin{bmatrix} \textbf{corner} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{corner} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \rightarrow \text{HEAD} \\ \text{MAPPING} = \textbf{dimension(n):0} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{object} \\ \text{AXIS} = (\textbf{see linked attribute}) \\ \text{ARITY} = (seelinked attribute) \end{bmatrix}$$

(53)
$$\begin{bmatrix} \textbf{diagonal} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{diagonal} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \rightarrow \text{HEAD} \\ \text{MAPPING} = \textbf{dimension(n):1} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{object} \\ \text{AXIS} = axes(\text{REFERENT} \rightarrow \text{HEAD}) \\ \text{ARITY} = (seelinkedattribute) \end{bmatrix} \end{bmatrix}$$

$$[54] \begin{bmatrix} \textbf{above} \\ LEX = \begin{bmatrix} PRED = \textbf{above} \end{bmatrix} \\ TYPE = \begin{bmatrix} ARG = \textbf{x:physobj} \\ REFERENT = \textbf{X} \\ MAPPING = \textbf{dimension(n):n} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{world} \\ AXIS = +\textbf{Y} \\ ARITY = intransitive \end{bmatrix} \end{bmatrix}$$

(55)
$$\begin{bmatrix} \textbf{below} \\ LEX = \begin{bmatrix} PRED = \textbf{below} \end{bmatrix} \\ TYPE = \begin{bmatrix} ARG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \\ MAPPING = \textbf{dimension(n):n} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{world} \\ AXIS = -\textbf{Y} \\ ARITY = intransitive \end{bmatrix}$$

(56)
$$\begin{bmatrix} in_front \\ LEX = \begin{bmatrix} PRED = in_front \end{bmatrix} \\ TYPE = \begin{bmatrix} ARG = x:physobj \\ REFERENT = x \\ MAPPING = dimension(n):n \\ ORIENTATION = \begin{bmatrix} SPACE = pov \\ AXIS = +Z \\ ARITY = intransitive \end{bmatrix}$$

$$(57) \begin{bmatrix} \textbf{behind} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{behind} \end{bmatrix} \\ \text{TYPE} = \begin{bmatrix} \text{ARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \\ \text{MAPPING} = \textbf{dimension(n):n} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{pov} \\ \text{AXIS} = \textbf{-Z} \\ \text{ARITY} = intransitive} \end{bmatrix}$$

(58)
$$\begin{bmatrix} \textbf{to_the_left} \\ \text{LEX} = \begin{bmatrix} \text{PRED} = \textbf{to_the_left} \end{bmatrix} \\ \text{RARG} = \textbf{x:physobj} \\ \text{REFERENT} = \textbf{x} \\ \text{MAPPING} = \textbf{dimension(n):n} \\ \text{ORIENTATION} = \begin{bmatrix} \text{SPACE} = \textbf{pov} \\ \text{AXIS} = \textbf{-X} \\ \text{ARITY} = intransitive} \end{bmatrix} \end{bmatrix}$$

(59)
$$\begin{bmatrix} \textbf{to_the_right} \\ LEX = \begin{bmatrix} PRED = \textbf{to_the_right} \end{bmatrix} \\ TYPE = \begin{bmatrix} ARG = \textbf{x:physobj} \\ REFERENT = \textbf{x} \\ MAPPING = \textbf{dimension(n):n} \\ ORIENTATION = \begin{bmatrix} SPACE = \textbf{pov} \\ AXIS = +\textbf{X} \\ ARITY = intransitive \end{bmatrix} \end{bmatrix}$$

(60)
$$\begin{bmatrix} \textbf{reach} \\ LEX = \begin{bmatrix} PRED = \textbf{reach} \\ TYPE = \textbf{process} \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = \textbf{process} \\ ARGS = \begin{bmatrix} A_1 = \textbf{x} : \textbf{agent} \\ A_2 = \textbf{y} : \textbf{physobj} \end{bmatrix} \\ BODY = \begin{bmatrix} E_1 = [while(!at(x, y), extend(x, align(loc(y) - loc(x))))] \end{bmatrix} \end{bmatrix}$$

$$[box] \\ LEX = \begin{bmatrix} PRED = box \\ TYPE = physobj \end{bmatrix} \\ TYPE = \begin{bmatrix} HEAD = rectangular_prism \\ COMPONENTS = nil \\ CONCAVITY = flat \\ ROTATSYM = \{X,Y,Z\} \\ REFLECTSYM = \{XY,XZ,YZ\} \end{bmatrix} \\ HABITAT = \begin{bmatrix} INTR = \cdots \\ EXTR = \cdots \end{bmatrix} \\ AFFORD_STR = \begin{bmatrix} A_1 = H_1 \rightarrow [E_1]R \\ A_2 = \cdots \\ A_3 = \cdots \\ A_3 = \cdots \end{bmatrix} \\ EMBODIMENT = \begin{bmatrix} SCALE = \langle agent \\ MOVABLE = true \end{bmatrix}$$