

TOPIC: REGULAR EXPRESSIONS

Write Regular Expression for following languages:

1. $\Sigma = \{0, 1\}$ and String in the Language ends with 1
2. $\Sigma = \{0, 1, 2\}$ and String in the Language ends with 010
3. $\Sigma = \{a, b\}$ and All Strings in the Language contain exactly three b's.
4. $\Sigma = \{0, 1\}$ and All Strings in the Language starts and ends with different symbols.
5. $\Sigma = \{0, 1\}$ and All Strings in the Language starts and ends with same symbols
6. $\Sigma = \{0, 1\}$ and All Strings in the Language starts and ends with same symbols
7. $\Sigma = \{a, b, c\}$ and All Strings in the Language contain exactly three b's.
8. $\Sigma = \{a, b\}$ and All Strings in the Language contain at least three b's.
9. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at least three 1's.
10. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at most three 1's.
11. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language contain at most three 1's
12. $\Sigma = \{0, 1\}$ and All Strings in the Language contain 00 or 11 as substring.
13. $\Sigma = \{0, 1\}$ and All Strings in the Language contain both 00 and 11 as substring.
14. $\Sigma = \{a, b\}$ and String in the Language contain 'aa' as substring.
15. $\Sigma = \{0, 1\}$ and All Strings in the Language end with 00.
16. $\Sigma = \{0, 1\}$ and All Strings in the Language does not end with 00.
17. $\Sigma = \{0, 1\}$ and All Strings in the Language do not contain 00 as substring.
18. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language do not contain 00 as substring.
19. $\Sigma = \{0, 1\}$ and All Strings in the Language contain exactly one pair of 0's
20. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language contain exactly one pair of 1's
21. $\Sigma = \{0, 1\}$ and All Strings in the Language contain exactly one pair of 0's
22. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at most one pair of 0's.
23. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at most one pair of 0's and at most one pair of 1's
24. $\Sigma = \{0, 1\}$ and All Strings in the Language neither contain 00 nor 11 as substring.
25. $\Sigma = \{0, 1\}$ and in each string there are at least two 1's between every pair of 0's.
26. $\Sigma = \{0, 1\}$ and there are equal number of 0's and 1's in every string number of 0's differs from number of 1's by at most 1 and vice versa.
27. $\Sigma = \{0, 1\}$ and string starts with 01 or ends with 01
28. $\Sigma = \{0, 1\}$ and there are even number of 0's and even no of 1's.
29. $\Sigma = \{a, b\}$ and string starts with a and has even length.

30. $\Sigma = \{a, b\}$ and string starts with b and have odd length.
31. $\Sigma = \{a, b\}$ and string ends with a and have even length.
32. $\Sigma = \{a, b\}$ and string ends with b and have odd length.
33. $\Sigma = \{a, b\}$ and if string starts with 'a' have odd length, and if it starts with 'b' then have even length.
34. $L = (01)^n(11)^m, n \geq 1, m \geq 1$
35. $L = a^i b^j, i \geq 2, j \geq 3$
36. $\Sigma = \{a, b, c\}$ where every string contains any number of a's followed by any number of b's followed by any number of c's.
37. $\Sigma = \{a, b, c\}$ and last symbol appears somewhere earlier in the string. E.g. abcac is accepted while abac is rejected.
38. $\Sigma = \{0, 1\}$ and All Strings in the Language do not contain 000 as substring.
39. $\Sigma = \{0, 1\}$ and each string starts with 00 or end with 00
40. $\Sigma = \{0, 1\}$ and each string starts with 00 and end with 00
41. Write R.E. for language containing strings of a's & b's not containing 'ab' as substring.
42. Write R.E. for language containing strings w of a's & b's where $|w| \bmod 3 = 2$
43. Write R.E. for language containing strings of a's & b's with length multiple of 3.
44. Write R.E. for language containing strings of a's & b's with even length.
45. Write R.E. for language containing strings of a's & b's with odd length.
46. Write R.E. for language containing strings of a's & b's with length exactly 2
47. Write R.E. for language containing strings of a's & b's with length atleast 2
48. Write R.E. for language containing strings of a's & b's with length atmost 2.
49. Regular expression for language $L = a^n b^m$ over $\Sigma = \{a, b\}$, with even number of a's followed by odd number of b's.
50. Regular expression over $\Sigma = \{0, 1\}$ and 3rd symbol from right end is 1.
51. $L = \{w: w \in (0/1)^* \text{ and there are strings that begins and ends with 00 or 11.}\}$
52. $L = \{w: w \in (0/1)^* \text{ and there are strings that begins or ends with 00 or 11.}\}$
53. $L = a^m b^n c^p$ where $m, n, p \geq 1$
54. $L = a^m b^{2n} c^{3p}$ where $m, n, p \geq 1$
55. $L = \{w \mid w \in 0^n 1^m \text{ and } n + m \text{ is even}\}$

TOPIC: REGULAR EXPRESSIONS

Write Regular Expression for following languages:

1. $\Sigma = \{0, 1\}$ and String in the Language ends with 1

Sol: $(0+1)^*1$

2. $\Sigma = \{0, 1, 2\}$ and String in the Language ends with 010

Sol: $(0+1+2)^*010$

3. $\Sigma = \{a, b\}$ and All Strings in the Language contain exactly three b's.

Sol: $a^*ba^*ba^*ba^*$

4. $\Sigma = \{0, 1\}$ and All Strings in the Language starts and ends with different symbols.

Sol: $0(0+1)^*1 + 1(0+1)^*0$

5. $\Sigma = \{0, 1\}$ and All Strings in the Language starts and ends with same symbols

Sol: $0(0+1)^*0 + 1(0+1)^*1 + 0 + 1 + \epsilon$

6. $\Sigma = \{0, 1\}$ and All Strings in the Language starts with 01 or ends with 01

Sol: $01(0+1)^* + (0+1)^*01$

7. $\Sigma = \{a, b, c\}$ and All Strings in the Language contain exactly three b's.

Sol: $(a+c)^*b(a+c)^*b(a+c)^*b(a+c)^*$

8. $\Sigma = \{a, b\}$ and All Strings in the Language contain at least three b's.

Sol: $a^*ba^*ba^*b(a+b)^*$ or $(a+b)^*b(a+b)^*b(a+b)^*b(a+b)^*$

9. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language contain at least three 1's.

Sol: $(0+2)^*1(0+2)^*1(0+2)^*1(0+1+2)^*$

Or $(0+1+2)^*1(0+1+2)^*1(0+1+2)^*1(0+1+2)^*$

10. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at most three 1's.

Sol: $0^* + 0^*10^* + 0^*10^*10^* + 0^*10^*10^*10^*$

11. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language contain at most three 1's

Sol: $(0+2)^* + (0+2)^*1(0+2)^* + (0+2)^*1(0+2)^*1(0+2)^* + (0+2)^*1(0+2)^*1(0+2)^*1(0+2)^*$

12. $\Sigma = \{0, 1\}$ and All Strings in the Language contain 00 or 11 as substring.

Sol: $(0+1)^*(00+11)(0+1)^*$

13. $\Sigma = \{0, 1\}$ and All Strings in the Language contain both 00 and 11 as substring.

Sol: $(0+1)^*00(0+1)^*11(0+1)^* + (0+1)^*11(0+1)^*00(0+1)^*$

14. $\Sigma = \{a, b\}$ and String in the Language contain 'aa' as substring.

Sol: $(a + b)^* aa (a + b)^*$

15. $\Sigma = \{0, 1\}$ and All Strings in the Language end with 00.

Sol: $(0 + 1)^* 00$

16. $\Sigma = \{0, 1\}$ and All Strings in the Language does not end with 00.

Sol: $(0 + 1)^* (1 + 10) + 0 + \epsilon$

17. $\Sigma = \{0, 1\}$ and All Strings in the Language do not contain 00 as substring.

Sol: $(1 + 01)^*(0 + \epsilon)$

Or $(0 + \epsilon) (1 + 10)^*$

18. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language do not contain 00 as substring.

Sol: $(1 + 2 + 01 + 02)^*(0 + \epsilon)$ or $(0 + \epsilon) (1 + 2 + 10 + 12)^*$

19. $\Sigma = \{0, 1\}$ and All Strings in the Language contain exactly one pair of 0's

Sol: $(1 + 01)^* 00 (1 + 10)^*$

20. $\Sigma = \{0, 1, 2\}$ and All Strings in the Language contain exactly one pair of 1's

Sol: $(0 + 2 + 10 + 12)^* 11 (0 + 2 + 01 + 21)^*$

21. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at most one pair of 0's.

Sol: $(1 + 01)^*(0 + \epsilon) + (1 + 01)^* 00 (1 + 10)^*$

22. $\Sigma = \{0, 1\}$ and All Strings in the Language contain at most one pair of 0's and at most one pair of 1's

Sol: Case 1: No pair of 0's or 1's

$$r1 = (1 + \epsilon) (01)^* (0 + \epsilon)$$

Case 2: No pair of 0's but one pair of 1's

$$r2 = (0 + \epsilon) (10)^* 11 (01)^* (0 + \epsilon)$$

Case 3: One pair of 0's but No pair of 1's

$$r3 = (1 + \epsilon) (01)^* 00 (10)^* (1 + \epsilon)$$

Case 4: one pair of 0's and pair of 1's

$$r4 = (1 + \epsilon) (01)^* 00 (10)^* 11 (01)^* (0 + \epsilon) + (0 + \epsilon) (10)^* 11 (01)^* 00 (10)^* (1 + \epsilon)$$

$$RE = r1 + r2 + r3 + r4$$

23. $\Sigma = \{0, 1\}$ and All Strings in the Language neither contain 00 nor 11 as substring.

Sol: $(1 + \epsilon) (01)^* (0 + \epsilon)$

24. $\Sigma = \{0, 1\}$ and All Strings in the Language neither contain 00 nor 11 as substring.

Sol: $(1 + \epsilon) (01)^* (0 + \epsilon)$

25. $\Sigma = \{0, 1\}$ and in each string there are at least two 1's between every pair of 0's.

Sol: $(1 + 011)^*(\epsilon + 0 + 01)$

26. $\Sigma = \{0, 1\}$ and there are equal number of 0's and 1's in every string, in any prefix number of 0's differs from number of 1's by at most 1 and vice versa.

Sol: $(01 + 10)^*$

27. $\Sigma = \{0, 1\}$ and string starts with 01 or ends with 01

Sol: $01(0+1)^* + (0+1)^*01$

28. $\Sigma = \{0, 1\}$ and there are even number of 0's and even no of 1's.

Sol: $(00+11+(01+10)(00+11)^*(01+10))^*$

29. $\Sigma = \{a, b\}$ and string starts with a and has even length.

Sol: $a(a+b)((a+b)(a+b))^*$

30. $\Sigma = \{a, b\}$ and string starts with b and have odd length.

Sol: $b((a+b)(a+b))^*$

31. $\Sigma = \{a, b\}$ and string ends with a and have even length.

Sol: $((a+b)(a+b))^*(a+b)a$

32. $\Sigma = \{a, b\}$ and string ends with b and have odd length.

Sol: $((a+b)(a+b))^*b$

33. $\Sigma = \{a, b\}$ and if string starts with 'a' have odd length, and if it starts with 'b' then have even length.

Sol: $a((a+b)(a+b))^* + b(a+b)((a+b)(a+b))^*$

34. $L = (01)^n(11)^m, n \geq 1, m \geq 1$

Sol: $01(01)^*(11)^*11$

35. $L = a^ib^j, i \geq 2, j \geq 3$

Sol: aaa^*bbbb^*

36. $\Sigma = \{a, b, c\}$ where every string contains any number of a's followed by any number of b's followed by any number of c's.

Sol: $a^*b^*c^*$

37. $\Sigma = \{a, b, c\}$ and last symbol appears somewhere earlier in the string. E.g. abcac is accepted while abac is rejected.

Sol: $(a+b+c)^*(a(a+b+c)^*a+b(a+b+c)^*b+c(a+b+c)^*c)$

38. $\Sigma = \{0, 1\}$ and All Strings in the Language do not contain 000 as substring.

Sol: $(1+01+001)^*(00+0+\epsilon)$

39. $\Sigma = \{0, 1\}$ and each string starts with 00 or end with 00

Sol: $00(0+1)^* + (0+1)^*00$

40. $\Sigma = \{0, 1\}$ and each string starts with 00 and end with 00

Sol: $00(0+1)^*00+000$

41. Write R.E. for language containing strings of a's & b's not containing 'ab' as substring.

Sol: b^*a^*

42. Write R.E. for language containing strings w of a's & b's where $|w| \bmod 3 = 2$

Sol: $((a + b)(a + b)(a + b))^* (a + b) (a + b)$

43. Write R.E. for language containing strings of a's & b's with length multiple of 3.

Sol: $((a + b)^3)^*$

44. Write R.E. for language containing strings of a's & b's with even length.

Sol: $((a + b)(a + b))^*$

45. Write R.E. for language containing strings of a's & b's with odd length.

Sol: $((a + b)(a + b))^* (a + b)$

46. Write R.E. for language containing strings of a's & b's with length exactly 2

Sol: $(a + b) (a + b)$

47. Write R.E. for language containing strings of a's & b's with length at least 2

Sol: $(a + b) (a + b)(a + b)^*$

48. Write R.E. for language containing strings of a's & b's with length at most 2.

Sol: $(\epsilon + a + b) (\epsilon + a + b)$

49. Regular expression for language $L = a^n b^m$ over $\Sigma = \{a, b\}$, with even number of a's followed by odd number of b's.

Sol: $(aa)^*(bb)^*b$

50. Regular expression over $\Sigma = \{0, 1\}$ and 3rd symbol from right end is 1.

Sol: $(0 + 1)^* 1 (0 + 1) (0 + 1)$

51. $L = \{w : w \in (0/1)^* \text{ and there are strings that begins and ends with 00 or 11.}$

Sol: $00 (0 + 1)^* 00 + 11 (0 + 1)^* 11$

52. $L = \{w : w \in (0/1)^* \text{ and there are strings that begins or ends with 00 or 11.}$

Sol: $00 (0 + 1)^* + (0 + 1)^* 00 + 11 (0 + 1)^* + (0 + 1)^* 11$

53. $L = a^m b^n c^p$ where $m, n, p \geq 1$

Sol: $aa^*bb^*cc^*$

54. $L = a^m b^{2n} c^{3p}$ where $m, n, p \geq 1$

Sol: $aa^*bb(bb)^*ccc(ccc)^*$

55. $L = \{w \mid w \in 0^n 1^m \text{ and } n + m \text{ is even}\}$

Sol: $(00)^*(11)^* + 0(00)^*(11)^*1 \quad \{\text{either both are even or both are odd}\}$

56. $L = \{w \mid w \in 0^n 1^m \text{ and } n + m \text{ is odd}\}$

Sol: $(00)^*(11)^*1 + 0(00)^*(11)^* \quad \{\text{even 0's with odd 1's or Odd 0's with even 1's}\}$