PHY 4210-01 Senior Lab Lab M-1: Magnetic Field Mapping

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Abstract

In this experiment the magnetic field inside a Helmholtz coil was measured and compared to theoretical calculations determined from the Smythe derivation of the Biot-Sarvat Law for a plane displaced from the central axis, with coordinates z, ρ , and ϕ . When determining the magnetic field inside a Helmholtz coil, a Hall probe is used to obtain the magnitude of the magnetic field at varying positions inside the coil. Theoretically the axial component of the magnetic field that is produced inside the Helmholtz coil is, to some extent, of uniform magnitude.

Contents

1	Objective of the Experiment	3
2	Theory of the Experiment	3
3	Equipment Utilized	3
	3.1 The Helmholtz coil	. 3
	3.2 The Hall Effect Probe	. 4
	3.3 Position Controls	. 4
4	Procedure	4
	4.1 Measuring the External Field	. 5
	4.2 Procedural Modifications	
	4.3 Additional Sources of Error	
5	Data Analysis	6
	5.1 Calculating Supply Voltage	. 6
	5.2 Determining the Number of Turns in a Coil	
6	Results	6
	6.1 Comparing the directions of the Magnetic Field	. 6
7	Conclusion	7
8	Appendices	7
	8.1 Appendix A: Data	. 7
	8.2 Appendix B: Source Code	. 7

1 Objective of the Experiment

During this lab, the number of turns of wire inside a Helmholtz coil was determined for use in theoretical calculations. Then a 3-dimensional and 2-dimensional mapping of the magnetic field inside the Helmholtz coil was created in order to investigate the presence of a uniform field, running along its axial direction.

2 Theory of the Experiment

Recall for a straight current-carrying wire, circular magnetic field lines are generated around the wire in accordance with the curling right-hand rule. The Helmholtz coil contains two regions of circularly wound wires. Due to the the circular symmetry, all components of each infinitesimal segment of the wire will cancel *except* for that in the axial direction. In summary, a circular current produces a linear magnetic field.

The field point of the system has before been typically placed along the axis of the direction of the magnetic field, we will call this the z-direction. This was due to the ease of solving the Biot-Savart Law under these simple conditions, as the direction and strength of the magnetic field will follow along the z-axis of the system, which is where the field point is placed. When this is applied to the co-axial coils of the Helmholtz apparatus the evaluation of the Biot-Savart Law becomes too trivial. One then chooses the field point to be placed off of the z-axis as more information about the magnetic field of the coils can be determined. This is the more general scenario and thus more complex. The off axis form can be used for any point that is off of the z-axis, while the on axis is a specific and simplified form of the general case. The general form is best represented by Smythe's derivation of the Biot-Savart Law.

$$B_{z} = \frac{\mu_{0}IN}{2\pi} \left[\frac{1}{\sqrt{(a+\rho)^{2} + (a-z)^{2}}} \left[K_{1} + \left(\frac{a^{2} - \rho^{2} - (a-z)^{2}}{(a-\rho)^{2} + (a-z)^{2}} \right) E_{1} \right] + \frac{1}{\sqrt{(a+\rho)^{2} + z^{2}}} \left[K_{2} + \left(\frac{a^{2} - \rho^{2} - z^{2}}{(a-\rho)^{2} + z^{2}} \right) E_{2} \right] \right]$$
(1)

3 Equipment Utilized

3.1 The Helmholtz coil

The Helmholtz coil consists of two concentric sets of coils, each with the same radius and separated by a distance equal to their radius. This configuration allows the contribution of each set of coils to produce a uniform field in the center of the coils. The current in each set of coils must be oriented in a particular direction so that their contributions constructively interfere. The circuit is shown in figure 1.

Figure 1: Flow of current through the Helmholtz coil, oriented such that the produced fields are constructive.

3.2 The Hall Effect Probe

A DC Gaussmeter (AlphaLab Model GM-1-HS) was connected to a Hall Effect Probe in order to measure the field strength inside the Helmholtz coil. The Hall Effect Probe contains a semiconductor junction that, when exposed to a magnetic field, produces a voltage proportional to the field strength.

3.3 Position Controls

The position of the Hall Effect Probe can be modified in the ρ direction by sliding the ruler bar through the acrylic cube shown in figure 2. The position can be modified in the ϕ direction by rotation the ruler bar about the central pole. However, for the sake of this experiment, this did not have to be modified because measurements were taken in a single ρ , z plane. The z coordinate was modified by sliding the acrylic cube and ruler bar up and down the central pole.

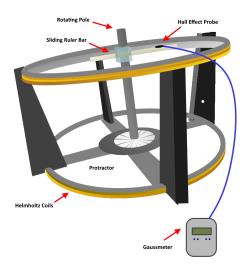


Figure 2: Two concentric Helmholtz coils separated by a distance equal to their radius. Rotating pole and sliding ruler allow for modification of the probe's position.

4 Procedure

Note that, per suggestion of the laboratory manual, the procedural steps of this experiment have been omitted. The discussion section provides sufficient detail on what actions were taken.

4.1 Measuring the External Field

The Helmholtz coil is oriented such that the Earth's magnetic field is parallel to the z-axis of the coils. This allows us to produce an applied magnetic field that is exactly anti-parallel to the Earth's field. From there, we can compute the applied field by subtracting the Earth's field from the total resultant field.

Note that there was an apparent offset in the Gaussmeter reading, as the 0.36G measurement for Earth's field was consistently higher than the expected value for Earth's field of 0.24G. However, if there truly exists such an offset in the measurement device, it would appear in both the measurement of Earth's field and in the measurement of the total field inside the Helmholtz coil. Subtracting these two to obtain the strength of the applied field would cancel any contribution from such an offset.

4.2 Procedural Modifications

Upon initial inspection of the equipment, it appeared the center pole running along the z axis of the Helmholtz coil was misaligned. In order to mitigate this error and ensure that coordinates were modified independently, a chord was used to realign the pole as closely as possible to the true z axis. However, since this alignment was not quantified, it is possible that there the pole is misaligned to some degree. This would result in a systematic error intrinsic to the experimental set-up. If the pole deviates from the z-axis, the experimentally recorded z-values are underestimated, causing the experimental field strengths to trend lower than the theoretical field strengths.

The majority of field strength measurements collected for the 3-dimensional mapping were taken on the same day of experimentation. After resuming this data collection on the next day, the values appeared to be systematically higher. Possible causes of this offset were investigated. Before taking measurements and intermittently during the data collection, the hall effect probe was zeroed and observed with the power supply off in order to ensure a consistent reading of the Earth's magnetic field. The reference measurement taken at the start of this lab session was similar to those taken during the previous session (zeroed field measurements were between 0.36G and 0.4G on both days), so a discrepancy in the Earth's field strength measurement was eliminated as the source of this error. Note that any small variation in the Earth's field measurement could be due to misalignment of the probe (a systematic error in measurement that would under-report the field strength) or simply a random error in measurement due to the limited performance of the probe.

An ammeter was also used to ensure a 2A current was consistently applied on both days of data collection, thus a change in the applied current was eliminated as a source of error. Because the source of this error was ultimately not determined and eliminated, the effect had to be compensated for with a procedural modification. In order to recreate the data points from the previous lab session, the current from the power supply was modified until the field strength matched previous measurements in several locations. This ultimately required lowering the applied current from 2000mA to 1790mA.

Upon further investigation, it appeared the current from the power supply was unstable, as it would decrease and increase every few minutes. This produced a source of random intrinsic error, which was mitigated by fine tuning the current value before each measurement after the issue was discovered.

4.3 Additional Sources of Error

Because the experimental set-up was restricted to a small area, the contribution from the field produced by the power supply may be non-negligible. From the perspective of the experimenter, the power supply sits behind and to the right of the Helmholtz coil. Therefore, by the curling right hand rule, this would produce an upward magnetic field on the side of the wire nearest the Helmholtz coil. This would produce a systematic intrinsic error that causes the external field measurements to be overestimated. Similarly, the power supply itself may be producing a small field that could also contribute a systematic error, although the exact effect could not be determined without knowing the orientation of such a field.

5 Data Analysis

5.1 Calculating Supply Voltage

Using a multimeter, the resistance of a set of coils was measured to be 3.4Ω . In order to determine the necessary voltage to send 3A of current through the coils, we make a simply calculation using Ohm's law.

$$V = IR$$
$$= (3 A)(3.4 \Omega)$$
$$= 10.2V$$

5.2 Determining the Number of Turns in a Coil

Further calculations will require knowing the number of turns of wire in each set of coils. MORE TEXT TO COME HERE

Theoretical values for what the strength of the magnetic field ought to be within the Helmholtz coils were determined by translating Equation 1 into Julia code, provided in Appendix B ??.

6 Results

6.1 Comparing the directions of the Magnetic Field

When measuring at a probe height of a/2 (16cm), where 'a' is the separation distance between the coils, the strength of the magnetic field in the 'z' direction was measured to be -3.13 Gauss. When measuring t he magnetic field in the 'z' direction at a probe height of 5cm, the magnetic field strength was measure d to be -3.28 Gauss. These results follow with the theory as it is expected that the magnetic field is p ropagated in the 'z' direction. The measured magnetic field strength for the ρ direction was -0.46 and -0.05 Gauss for a probe height

of 16cm and 5cm respectfully. The measured magnetic field strength for the ϕ direction was -0.51 and -0.31 Gauss for a probe height of 16cm and 5cm respectfully. For a probe height of 16cm the percentage for the magnitude of the magnetic field that is measured to be in the ρ direction is 14% while the percentage for the magnitude of the magnetic field that is measured to be in the ϕ direction is 16%. For a probe height of 5cm the percentage for the magnitude of the magnetic field that is measured to be in the ρ direction is 1% while the percentage for the magnitude of the magnetic field that is measured to be in the ϕ direction is 9%. The magnetic field produced by the Helmholtz coils should be directed along the 'z' axis. These small measuredvalues f ollow the aforementioned theoryand we can determine that the magnetic field produced by the Helmholtz c oil is indeed axial. Furthermore, we can determine that the magnetic field is axial along the 'z' direct ion.

7 Conclusion

- 8 Appendices
- 8.1 Appendix A: Data
- 8.2 Appendix B: Source Code

```
# Source code for calculating the theoretical data and plotting it in both 2D
   # and 3D.
     ----BEGIN PACKAGES-----
   # enable the addition of packages
   using Pkg
   # integration
   Pkg.add("QuadGK")
10
   using QuadGK
11
12
   # plotting
13
   Pkg.add("Plots")
14
   using Plots
15
16
   # displaying data
17
   Pkg.add("Printf")
18
   using Printf
19
20
   # -----END PACKAGES-----
22
   # -----BEGIN CONSTANTS-----
23
24
   # Permeability of Free Space rac{Tm}{\Delta}
   \mu_0 = 1.256e-6
```

```
27
      ----END CONSTANTS-----
29
    # -----BEGIN BIOT-SAVART ON AXIS-----
30
31
    # Biot-Savart (one loop, on axis)
    B1(z,I,a) = ((\mu_0 * I * (a ^2)) / 2) * (1 / (((a ^2) + (z ^2)) ^ (3/2)))
33
34
    # Biot-Savart (two loops, on axis)
35
    B2(z,I,a) = ((\mu_0 * I * (a ^ 2)) / 2) *
        ((1 / (((a^2) + (z^2))^{(3/2)})) +
37
         (1 / (((a^2) + ((a - z)^2))^2 (3/2))))
38
39
    # -----END BIOT-SAVART ON AXIS-----
40
41
    # ----BEGIN BIOT-SAVART OFF AXIS-----
42
43
    # the full Biot-Savart equation (two loops, off axis)
44
    B(z,I,N,a,\rho) =
45
        ((\mu_0 * I * N) / (2 * pi)) *
46
47
            (1 / sqrt(( (a + \rho) ^ 2) + ((a - z) ^ 2))) *
48
49
                K(1,a,\rho,z) +
50
51
                     (((a^2) - (\rho^2) - ((a - z)^2)) /
52
                      (((a - \rho) \hat{2}) + ((a - z) \hat{2})) *
53
                     E(1,a,\rho,z)
                )
            ) +
56
57
                 (1 / sqrt(((a + \rho) ^ 2) + (z ^ 2))) *
                     K(2,a,\rho,z) +
60
                     (
61
                         (((a^2) - (\rho^2) - (z^2)) /
62
                          (((a - \rho) ^2) + (z ^2))) *
                         E(2,a,\rho,z)
64
                     )
65
                )
            )
67
        )
68
69
    # elliptic integrals of first kind (series expansion)
    K(j,a,\rho,z, precision = 4) =
71
        (pi / 2) * (
72
            1 + sum([
73
                 ((reduce(*, [n - 1 \text{ for } n \text{ in } 2:2:precision]) /
                   reduce(*, [n for n in 2:2:precision])) ^ 2) *
75
                 (k(j,a,abs(\rho),z) \hat{n})
76
```

```
for n in 2:2:precision
77
            ])
79
        )
80
    # elliptic integrals of the second kind (series expansion)
81
    E(j,a,\rho,z, precision = 4) =
        (pi / 2) * (
83
            1 - foldl(-,[
84
                 ((reduce(*, [n-1 for n in 2:2:precision]) /
                   reduce(*, [n for n in 2:2:precision])) ^ 2) *
                 ((k(j,a,abs(\rho),z) \hat{n}) / (n-1))
87
                 for n in 2:2:precision
88
            ])
        )
90
91
    # the collections of variables k_1 and k_2
92
    k(j,a,\rho,z) = (j == 1)?
        sqrt((4 * a * \rho) / (((a + \rho) ^ 2) + ((a - z) ^ 2))) :
94
        sqrt((4 * a * \rho) / (((a + \rho) ^ 2) + (z ^ 2)))
95
96
    # ----END BIOT-SAVART OFF AXIS-----
97
98
    # ----BEGIN CONDITIONS-----
99
100
    # heights at which measurements were taken (meters)
101
    heightLevels = 0.03:0.02:0.33
102
103
    # current applied to the coils (amperes)
104
    current = 2
106
    # turns of wire in each coil
107
    turns = 73
108
109
    # radius of the coils (meters)
110
    radius = 0.332
111
112
    # radial distances at which measurements were taken (meters)
    rhos = -0.22:0.02:0.22
114
115
    # ----END CONDITIONS-----
116
117
    # -----BEGIN CALCULATIONS-----
118
119
    # list of Biot-Savart functions for each height level
    BHeights = [futureRho -> B(heightLevel, current, turns, radius, futureRho) * 1e6
121
                 for heightLevel in heightLevels ]
122
123
    # apply the list of radial distances to each height level's function (rhos are rows)
    allBs = [ map(heightLevelFunction, rhos) for heightLevelFunction in BHeights ]
125
```

126

```
----END CALCULATIONS-----
    # -----BEGIN MAKE DATA POINTS-----
129
130
    # convert column number (1:23) to radial distance value (-22:2:22)
131
    colNum2RadialDist(col) = col + (col - 24)
133
    # convert row number (1:16) to height value (3:2:33)
134
    rowNum2Height(row) = row + (row + 1)
135
    # data points for a row of data at the same height level
137
    getRow(row) = [ (rowNum2Height(row), colNum2RadialDist(col), allBs[row][col])
138
                     for col in 1:23 ]
139
140
    # data points as triples with rows as heights and columns as radial distances
141
    allPts = map(getRow, 1:16)
142
    # -----END MAKE DATA POINTS-----
145
    # ----BEGIN FORMAT DATA-----
146
147
    # split up coords into their own lists
148
    formatRow(row) = ( [ coords[1] for coords in row ],
149
                        [ coords[2] for coords in row ],
150
                        [ coords[3] for coords in row ] )
152
    # format all rows into form ([zs], [rs], [Bs])
153
    listOfRows = map(formatRow, allPts)
154
    # all these lists must be combined
156
    tripleData = ( foldl(hcat, map(x -> x[1], listOfRows)),
157
                    foldl(hcat, map(x -> x[2], listOfRows)),
                    foldl(hcat, map(x -> x[3], listOfRows)) )
159
160
    # print the data in neat columns
161
    function displayFormatedData(data)
162
        # print header
164
        Qprintf("z \rho B\n")
165
        # iterate through each data point
167
        for ii in 1:length(data[1])
168
            Oprintf("%f %f %f\n", data[1][ii], data[2][ii], data[3][ii])
169
        end
170
171
    end
172
173
    # apply the data printing function onto our data
    displayFormatedData(tripleData)
175
```

176

```
# ----END FORMAT DATA-----
177
    # -----BEGIN GENERATE 2D PLOT-----
179
180
    # extract the Bs from the list of row triples
181
    rowsBs = [ row[3] for row in listOfRows ]
182
183
    # generate height level labels for each line
184
    heightLevelLabels = map(string, 3:2:33)
185
186
    # generate the plot
187
    theoPlot2d = Plots.plot(listOfRows[1][2], rowsBs, label = heightLevelLabels,
188
                            title = "Theoretical Magnetic Field 2D",
                            size = (550, 550),
190
                            legendtitle = "Height Levels (cm)",
191
                            legend = :top,
192
                            xlabel = "Radial Distance from Axis (cm)",
                            ylabel = "Magnetic Field Strength (uT)"
194
195
196
    # save the plot to disk
    savefig(theoPlot2d, "2DPlotTheoretical")
198
199
    # -----END GENERATE 2D PLOT-----
200
201
    # ----BEGIN GENERATE 3D PLOT-----
202
203
    # generate the plot
204
    theoPlot3d = Plots.plot(tripleData[3], tripleData[2], tripleData[1],
                       seriestype = :scatter, legend = :topright, legendtitle = "Rows",
206
                       title = "Theoretical Magnetic Field 3D", size = (550,550),
207
                       xlabel = "Magnetic Field Strength (uT)",
                       ylabel = "Height Relative to Bottom Coil (cm)",
209
                       zlabel = "Radial Distance from Axis (cm)"
210
211
212
    # save the plot to disk
    savefig(theoPlot3d, "3DPlotTheoretical.png")
214
215
    # -----END GENERATE 3D PLOT-----
216
    # Generate 2D and 3D plots of the experimental data collected during the
    # experiment.
    # -----BEGIN PACKAGES-----
    # add other packages
    using Pkg
```

```
# interpreter for reading CSV files
   Pkg.add("CSV")
11
   using CSV
12
   # convenient container for data extracted from CSV files
   Pkg.add("DataFrames")
   using DataFrames
15
   # plotting
17
   Pkg.add("Plots")
   using Plots
19
20
   # format data output
   Pkg.add("Printf")
   using Printf
   # -----END PACKAGES-----
   # -----BEGIN EXTRACT DATA-----
27
28
   # read data from CSV into a DataFrame
   data = CSV.File("2dMappingTesla.csv") |> DataFrame
30
   # convert row number (1:16) to height value (3:2:33)
   rowNum2Height(row) = row + (row + 1)
34
   # reverse the order of the incoming heights
   heightReversal(z) = z + (16 - (z - 1) - z)
   # extract the data from a row into a triple representing that row
38
   extractRow(row) = (
39
       fill(rowNum2Height(row), 23),
       -22:2:22,
       [(Bval + 0.000024) * 1e6 for Bval in [data[ii] [heightReversal(row)] for ii in 2:24]]
42
43
44
   # list of triples, each representing a row, of the form ([zs, [rs], [Bs])
   listOfRows = map(extractRow, 1:16)
46
47
   # ----END EXTRACT DATA----
   # ----BEGIN FORMAT DATA-----
50
51
   # now, a "row" is of the form ([zs], [rs], [Bs]); all these lists must be combined
   tripleData = ( foldl(hcat, map(x -> x[1], listOfRows)),
                  foldl(hcat, map(x -> x[2], listOfRows)),
54
                  foldl(hcat, map(x -> x[3], listOfRows)) )
55
   # print the data in neat columns (display only, does not need to be included)
   function displayFormatedData(data)
```

```
# print header
        Qprintf("z \rho B\n")
61
62
        # iterate through each data point
        for ii in 1:length(data[1])
            @printf("%f %f %f\n", data[1][ii], data[2][ii], data[3][ii])
65
        end
66
67
    end
68
69
    # apply the display function to the data
70
    displayFormatedData(tripleData)
72
    # ----END FORMAT DATA----
73
74
    # -----BEGIN GENERATE 2D PLOT-----
75
    # extract the Bs from the list of row triples
77
    rowsBs = [ row[3] for row in listOfRows ]
78
    # generate height level labels for each line
    heightLevelLabels = map(string, 3:2:33)
81
82
    # generate the plot
    expPlot2d = Plots.plot(listOfRows[1][2], rowsBs, label = heightLevelLabels,
84
                           title = "Experimental Magnetic Field 2D",
85
                           size = (550,550),
86
                           legendtitle = "Height Levels (cm)",
                           legend = :bottom,
88
                           xlabel = "Radial Distance from Axis (cm)",
89
                           ylabel = "Magnetic Field Strength (uT)"
92
    # save the plot to disk
93
    savefig(expPlot2d, "2DPlotExperimental")
94
    # -----END GENERATE 2D PLOT-----
96
97
    # -----BEGIN GENERATE 3D PLOT-----
99
    # generate the plot
100
    expPlot3d = Plots.plot(tripleData[3], tripleData[2], tripleData[1],
101
                       seriestype = :scatter, legend = :topleft,
                        legendtitle = "Rows",
103
                       title = "Experimental Magnetic Field", size = (550,550),
104
                       xlabel = "Magnetic Field Strength (uT)",
105
                       ylabel = "Height Relative to Bottom Coil (cm)",
                       zlabel = "Radial Distance from Axis (cm)"
107
108
```

```
# save the image to disk
    savefig(expPlot3d, "3DPlotExperimental.png")
111
112
    # -----END GENERATE 3D PLOT-----
113
    # -----BEGIN PACKAGES-----
    # enable the addition of packages
    using Pkg
    # interpreter for reading CSV files
    Pkg.add("CSV")
    using CSV
    # convenient container for data extracted from CSV files
10
    Pkg.add("DataFrames")
12
    using DataFrames
13
    # plotting
14
    Pkg.add("Plots")
    using Plots
16
17
    # -----BEGIN GENERATE THEORETICAL DATA-----
18
    # Permeability of Free Space (T*m)/A
20
    \mu_0 = 1.256e-6
21
22
    # the full Biot-Savart equation (two loops, off axis)
    B(z,I,N,a,\rho) =
24
        ((\mu_0 * I * N) / (2 * pi)) *
25
             (1 / sqrt(( (a + \rho) ^ 2) + ((a - z) ^ 2))) *
27
28
                 K(1,a,\rho,z) +
29
                 (
                     (((a^2) - (\rho^2) - ((a - z)^2)) /
31
                      (((a - \rho) \hat{2}) + ((a - z) \hat{2})) *
32
                     E(1,a,\rho,z)
                 )
            ) +
36
                 (1 / sqrt(((a + \rho) ^2) + (z ^2))) *
37
                     K(2,a,\rho,z) +
39
40
                         (((a^2) - (\rho^2) - (z^2)) /
                          (((a - \rho) \hat{2}) + (z \hat{2})) *
                         E(2,a,\rho,z)
43
```

109

```
)
                )
            )
46
        )
47
48
    # elliptic integrals of first kind (series expansion)
   K(j,a,\rho,z, precision = 4) =
50
        (pi / 2) * (
51
            1 + sum([
                 ((reduce(*, [n - 1 for n in 2:2:precision]) /
                   reduce(*, [n for n in 2:2:precision])) ^ 2) *
54
                 (k(j,a,abs(\rho),z) \hat{n})
                for n in 2:2:precision
            ])
        )
58
    # elliptic integrals of the second kind (series expansion)
   E(j,a,\rho,z, precision = 4) =
        (pi / 2) * (
62
            1 - foldl(-,[
63
                ((reduce(*, [n-1 for n in 2:2:precision]) /
                   reduce(*, [n for n in 2:2:precision])) ^ 2) *
                 ((k(j,a,abs(\rho),z) \hat{n}) / (n-1))
66
                for n in 2:2:precision
            ])
        )
69
70
    # the collections of variables k_1 and k_2
   k(j,a,\rho,z) = (j == 1) ?
        sqrt((4 * a * \rho) / (((a + \rho) ^ 2) + ((a - z) ^ 2))) :
73
        sqrt((4 * a * \rho) / (((a + \rho) ^ 2) + (z ^ 2)))
74
    # heights at which measurements were taken (meters)
   heightLevels = 0.03:0.02:0.33
77
78
    # current applied to the coils (amperes)
79
   current = 2
    # turns of wire in each coil
82
   turns = 73
    # radius of the coils (meters)
85
   radius = 0.332
    # radial distances at which measurements were taken (meters)
   rhos = -0.22:0.02:0.22
89
    # list of Biot-Savart functions for each height level
   BHeights = [ futureRho -> B(heightLevel, current, turns, radius, futureRho) * 1e6
                for heightLevel in heightLevels ]
93
```

```
# apply the list of radial distances to each height level's function (rhos are rows)
    # list of lists of Bs where each internal list is a row
96
    theoBs = [ map(heightLevelFunction, rhos) for heightLevelFunction in BHeights ]
97
    # ----END GENERATE THEORETICAL DATA-----
100
      ----BEGIN EXTRACT EXPERIMENTAL DATA-----
101
102
    # read data from CSV into a DataFrame
103
    data = CSV.File("2dMappingTesla.csv") |> DataFrame
104
105
    # convert row number (1:16) to height value (3:2:33)
    rowNum2Height(row) = row + (row + 1)
107
108
    # reverse the order of the incoming heights
109
    heightReversal(z) = z + (16 - (z - 1) - z)
110
    # apply corrections to data (Earth's magnetic field & correct units)
112
    corrB(b) = ((b + 0.000024) * 1e6)
113
114
    # extract the data from a row into a triple representing that row
115
    extractRow(row) = (
116
        fill(rowNum2Height(row), 23),
117
        -22:2:22,
        [ corrB(Bval) for Bval in [ data[ii][heightReversal(row) ] for ii in 2:24 ] ]
119
120
121
    # list of triples, each representing a row
    expRows = map(extractRow, 1:16)
123
124
    # ----END EXTRACT EXPERIMENTAL DATA-----
126
    # -----BEGIN PLOT THE DIFFERENCE-----
127
128
    # list of triples, each representing a row, where the Bs are (theoB-expB)
129
    diffRows = [ (expRows[ii][1], expRows[ii][2], theoBs[ii] .- expRows[ii][3])
                 for ii in 1:length(expRows) ]
131
132
    # now, a "row" is of the form ([zs], [rs], [Bs]); all these lists must be combined
    tripleData = ( foldl(hcat, map(x -> x[1], diffRows)),
134
                   foldl(hcat, map(x -> x[2], diffRows)),
135
                   foldl(hcat, map(x -> x[3], diffRows)) )
136
    # plot the difference between the theoretical and experimental data
138
    diffPlot = Plots.plot(tripleData[3], tripleData[2], tripleData[1],
139
                        seriestype = :scatter, legend = :topright, legendtitle = "Rows",
140
                        title = "Difference Between Theoretical and Experimental Magnetic Field
                        size = (550, 550),
142
                        xlabel = "Magnetic Field Strength (uT)",
143
```