

Sliding Window Technique

This technique shows how a nested for loop in few problems can be converted to single for loop and hence reducing the time complexity.

Let's start with a problem for illustration where we can apply this technique:

```
Given an array of integers of size 'n'.  
Our aim is to calculate the maximum sum of 'k'  
consecutive elements in the array.  
  
Input : arr[] = {100, 200, 300, 400}  
        k = 2  
Output : 700  
  
Input : arr[] = {1, 4, 2, 10, 23, 3, 1, 0, 20}  
        k = 4  
Output : 39  
We get maximum sum by adding subarray {4, 2, 10, 23}  
of size 4.  
  
Input : arr[] = {2, 3}  
        k = 3  
Output : Invalid  
There is no subarray of size 3 as size of whole  
array is 2.
```

The **Naive Approach** to solve this problem is to calculate sum for each of the blocks of K consecutive elements and compare which block has the maximum sum possible. The time complexity of this approach will be $O(n * k)$.

Window Sliding Technique

The above problem can be solved in Linear Time Complexity by using Window Sliding Technique by avoiding the overhead of calculating sum repeatedly for each block of k elements.

The technique can be best understood with the window pane in bus, consider a window of length **n** and the pane which is fixed in it of length **k**. Consider, initially the pane is at extreme left i.e., at 0 units from the left. Now, co-relate the window with array `arr[]` of size **n** and pane with `current_sum` of size **k** elements. Now, if we apply force on the window such that it moves a unit distance ahead. The pane will cover next **k** consecutive elements.

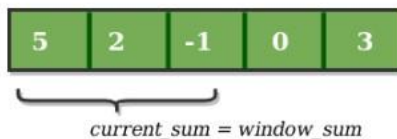
Consider an array `arr[] = {5, 2, -1, 0, 3}` and value of **k** = 3 and **n** = 5

Applying sliding window technique :

1. We compute the sum of first k elements out of n terms using a linear loop and store the sum in variable `window_sum`.
2. Then we will graze linearly over the array till it reaches the end and simultaneously keep track of maximum sum.
3. To get the current sum of block of k elements just subtract the first element from the previous block and add the last element of the current block.

The below representation will make it clear how the window slides over the array.

This is the initial phase where we have calculated the initial window sum starting from index 0. At this stage the window sum is 6. Now, we set the `maximum_sum` as `current_window` i.e 6.



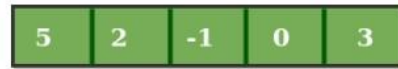
Now, we slide our window by a unit index. Therefore, now it discards 5 from the window and adds 0 to the window. Hence, we will get our new window sum by subtracting 5 and then adding 0 to it. So, our window sum now becomes 1. Now, we will compare this window sum with the maximum_sum. As it is smaller we won't change the maximum_sum.



$$\text{current_sum} = \text{window_sum} + (-5) + (0)$$

Similarly, now once again we slide our window by a unit index and obtain the new window sum to be 2. Again we check if this current window sum is greater than the maximum_sum till now. Once, again it is smaller so we don't change the maximum_sum.

Therefore, for the above array our maximum_sum is 6.



$$\text{current_sum} = \text{window_sum} + (-2) + (3)$$