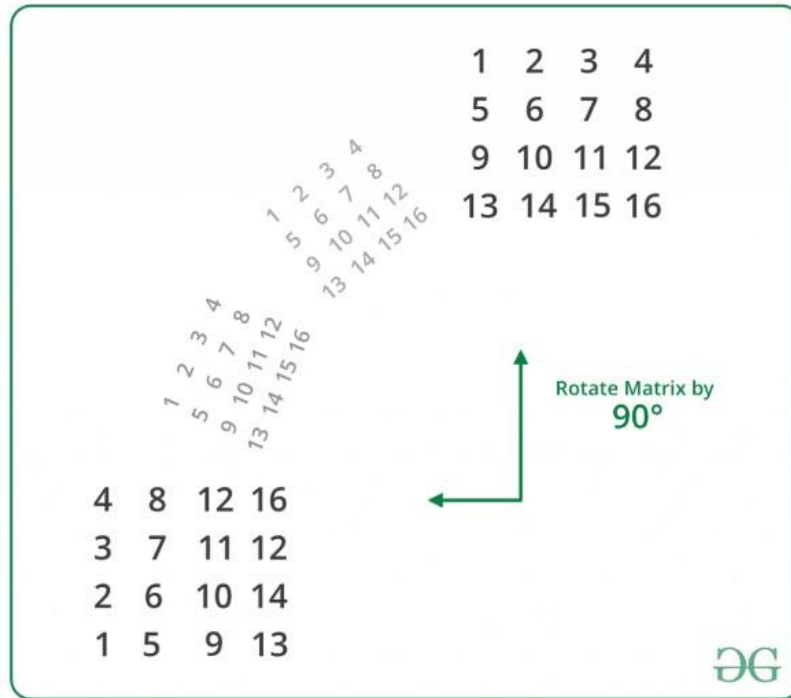


Matrix Rotation

Given a **Square Matrix** of dimension $N \times N$. The task is to rotate the matrix in anti-clock wise direction by 90 degrees.



On observing carefully, we can easily conclude that:

```
first row of destination -----> last column of source
second row of destination -----> second last column of source
.
.
.
.
last row of destination -----> first column of source
```

Therefore, rotating a matrix in anti-clockwise direction by 90 degrees is equivalent to replacing rows from top of the matrix by columns from the end.

Implementation of above approach: This method can be easily implemented by using extra space. The idea is to create a temporary matrix of same dimensions as that of the original matrix and copy the original matrix into this temporary matrix. Finally, replace each row in the original matrix one by one by columns of the temporary matrix from last to first.

Algorithm:

```
Original Matrix: mat[N][N].
Temporary Matrix: temp[N][N].

Copy original matrix into temporary matrix:
for(i = 0; i < N; i++)
{
    for(j = 0; j < N; j++)
    {
        temp[i][j] = mat[i][j];
    }
}

Updating Original Matrix by Rotated Matrix:
// Replace each row in the original matrix one by
// one by columns of the temporary matrix from
// last to first
for(i = 0; i < N; i++)
{
    for(j = 0; j < N; j++)
    {
        mat[i][j] = temp[j][N-i-1];
    }
}
```

Without Using Extra Space

The above problem can also be solved without using any additional matrix or extra-space. This is also called in-place rotating a square matrix by 90 degrees in anti-clockwise direction.

An $N \times N$ matrix will have $\text{floor}(N/2)$ square cycles. For example, a 4×4 matrix will have 2 cycles. The first cycle is formed by its 1st row, last column, last row and 1st column. The second cycle is formed by 2nd row, second-last column, second-last row and 2nd column.

The idea is for each square cycle, we swap the elements involved with the corresponding cell in the matrix in anti-clockwise direction i.e. from top to left, left to bottom, bottom to right and from right to top one at a time. We use nothing but a temporary variable to achieve this.

Below steps demonstrate the idea:

First Cycle (Involves Red Elements)

```
1 2 3 4
5 6 7 8
9 10 11 12
13 14 15 16
```

Moving first group of four elements (First elements of 1st row, last row, 1st column and last column) of first cycle in counter clockwise.

```
4 2 3 16
5 6 7 8
9 10 11 12
1 14 15 13
```

Moving next group of four elements of first cycle in counter clockwise

```
4 8 3 16
5 6 7 15
2 10 11 12
1 14 9 13
```

Moving final group of four elements of first cycle in counter clockwise

```
4 8 12 16
3 6 7 15
2 10 11 14
1 5 9 13
```

Second Cycle (Involves Blue Elements)

```
4 8 12 16
3 6 7 15
2 10 11 14
1 5 9 13
```

Fixing second cycle

```
4 8 12 16
3 7 11 15
2 6 10 14
1 5 9 13
```

Below function in-place rotates a square matrix by 90 degrees counter-clockwise:

```
1 |
2 | // An Inplace function to rotate a N x N matrix
3 | // by 90 degrees in anti-clockwise direction
4 | void rotateMatrix(int mat[][N])
5 | {
6 |     // Consider all squares one by one
7 |     for (int i = 0; i < N / 2; i++)
8 |     {
9 |         // Consider elements in group of 4 in
10 |         // current square
11 |         for (int j = i; j < N-i-1; j++)
12 |         {
13 |             // store current cell in temp variable
14 |             int temp = mat[i][j];
15 |
16 |             // move values from right to top
17 |             mat[i][j] = mat[j][N-1-i];
18 |
19 |             // move values from bottom to right
20 |             mat[j][N-1-i] = mat[N-1-i][N-1-j];
21 |
22 |             // move values from left to bottom
23 |             mat[N-1-i][N-1-j] = mat[N-1-j][i];
24 |
25 |             // assign temp to left
26 |             mat[N-1-j][i] = temp;
27 |         }
28 |     }
29 | }
30 |
```