

values of α 's given by
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CLASSMATE

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Hyperplane

$$H = \alpha_1 a_1 + \alpha_2 a_2 + \dots + \alpha_n a_n + \alpha_{n+1}$$

I want to find a suitable hyperplane

which is able to distinguish
b/w objects of diff.
decision classes

u_i, u_j where $d(u_i) \neq d(u_j)$

Info system

$$\text{Conflict}(IS) = \frac{1}{2} |\{u_i, u_j\}|$$

since $(u_i, u_j) = (u_j, u_i)$

So I make a collection C

left hand side of Hyperplane

$$C_i^L(H) = \{u \mid \sum \alpha_k a_k < 0; u \in X_i\}$$

decision
class

H

$$C_i^R(H) = \{u \mid \sum \alpha_k a_k \geq 0; u \in X_i\}$$

For every pair of decision class,

majority of one ⁱⁿ $C_i^L(H)$ &
majority of other in $C_j^R(H)$

$$\text{award}(H) = \sum_{i \neq j} |C_i^L(H)| \cdot |C_j^R(H)|$$

has to be
maximized to get the most
suitable hyperplane

other ways : max minority
sum minority
entropy calc
Leave it

⇒ we finally get some rules.

we need to have a metric to
check how good a soln it is
(we want most optimised
soln)

- 1) Best possible soln (using least resources)
- 2) Define metrics & talk in ^{classmate} terms
- 3) Have the ability to ^{Date} ^{Page} validate your results

$$\text{Significance}(C, D) = \frac{|POS_C|}{|U|}$$

support of a rule : antecedent \downarrow consequent decision

$$\gamma(x)(C, D) = \frac{|[x]_C \cap D(x)|}{|U|}$$

rule

Segment	Incoming calls	Outgoing calls	change	Churn
1	Med	Med	low	no
2	High	high	low	no
3	low	low	low	no
4	low	low	high	yes
5	Med	Med	low	yes
6	Med	low	low	yes

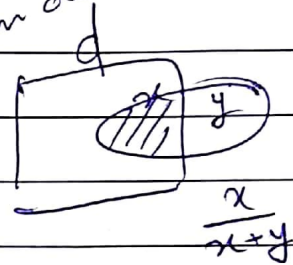


support

Decision Rule	Strength	Certainty	Coverage
1	$200/1000 = 0.2$	$200/420 = 0.48$	$\frac{200}{200+200+100} = 0.33$
2	0.1	1.00	0.17
3	0.3	1.00	0.5
4	0.15	1.00	0.38
5	0.22	0.52	0.55
6	0.03	1.00	0.07

→ probability that these features will lead to certain decision

Certainty of given rule :



$$Cer_x(C, D) = \frac{|[x]_C \cap D(x)|}{|[x]_C|}$$

for 1 :

$$\frac{(200 + 220) \cap (200)}{(200 + 220)}$$

$$= 200/420$$

~~certainty~~
COVERAGE

→ To what extent this rule cover this decision class

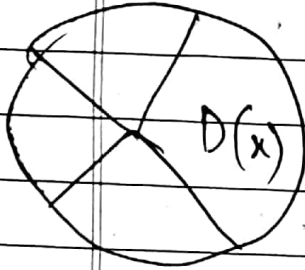
$$Cov_x(C, D) = \frac{|[x]_C \cap D(x)|}{|D(x)|}$$

(All this is going towards theory of total probability)

classmate

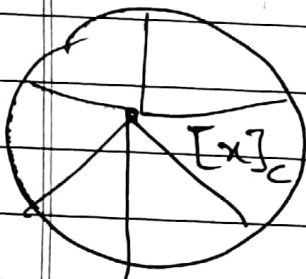
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$$\text{Cov}_x(C, D) = \frac{|[x]_C \cap D(x)| / |U|}{|D(x)| / |U|}$$



$$= \frac{\gamma_x(C, D)}{\pi(D(x))}$$

$$\text{Cls}_x(C, D) = \frac{|[x]_C \cap D(x)| / |U|}{|[x]_C| / |U|}$$



$$= \frac{\gamma_x(C, D)}{\pi([x]_C)}$$

∥

If $[x]_C$ would be the entire universe, Cls_x would tell what would be the support

Strength = Sum of certainties weighted of an equivalence class with $\pi([x]_C)$

Strength_d = Sum of coverages weighted with decision class $\pi(D(x))$

If you have many rules, we may eliminate rules ^{classifiers & strength}

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⇒ Now, we have a compact rule base.

Now, we start classifying.

We have test objects and ^{what} we do is:

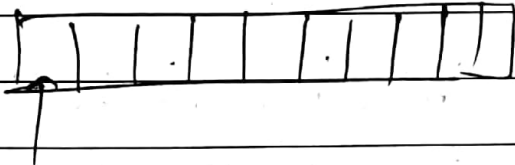
We have database initially.

we keep 90% for train or 80%
10% for test or 20%

⇒ This is called cross-validation.

We go for n-fold cross validation

eg: 10-fold cross



Step 1: Set 1: Test
Rest: Train

Step 2: Set 2: Test
Rest: Train

⇒ we have 10 ^{sets of rule} sets

Step 10 —

Confusion matrix

		Actual			
		d_1	d_2	d_3	d_4
Predicted decisions	d_1	tp	fp		
	d_2		tn		
	d_3				
	d_4	fn			

we count the no. of cases where actual decision matches with predicted decision. \Rightarrow True positive

Predicted : True
 Actual : No } false positive

$$\text{Recall} = \frac{tp}{tp + fn} \rightarrow \text{also called sensitivity or true positive rate}$$

$$\text{Precision} = \frac{tp}{tp + fp} \rightarrow \text{also called as PPV (Positive predicted value)}$$

generally as one \uparrow , other \downarrow .

\Rightarrow we take harmonic mean of both

F1 score

$$F_1 = \frac{2}{\frac{1}{\text{recall}} + \frac{1}{\text{precision}}}$$

There is another metric 'accuracy' that sometimes comes into picture:

$$\text{Accuracy} = \frac{tp + tn}{tp + tn + fp + fn}$$

entire population

Specificity

diagnostic odd
rate

FP rate

etc etc etc