

→ features can be of any domain

- Objective function should be some minimisation or maximisation

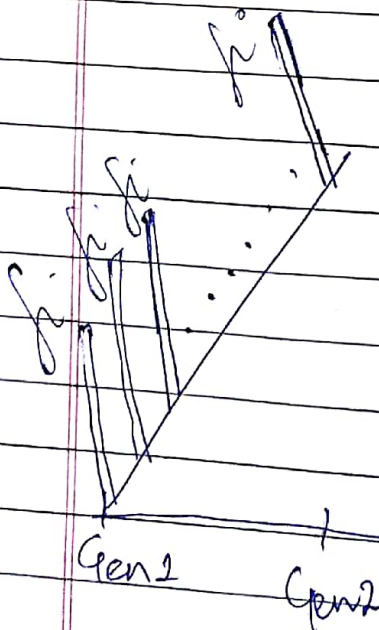
- fitness must lead to the objective function

- Determine the population size

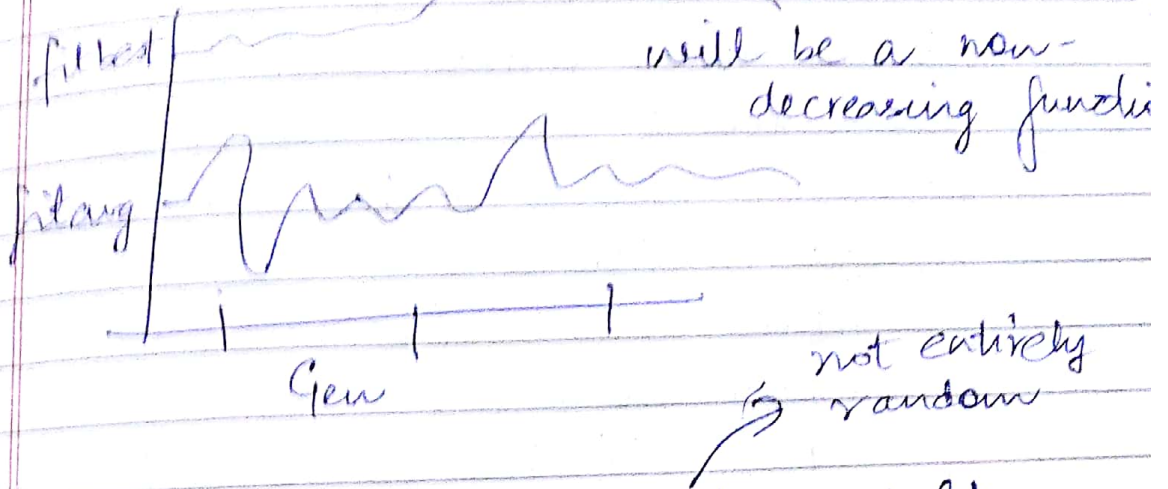
- If you have a smaller population, more evolution

Computational complexity = Populⁿ size * No. of generⁿ

- you need to explore the search space



If we use elitism:



→ Then we do a random walk.

— In crossover, you have to see whether the offspring does not violate any constraint.

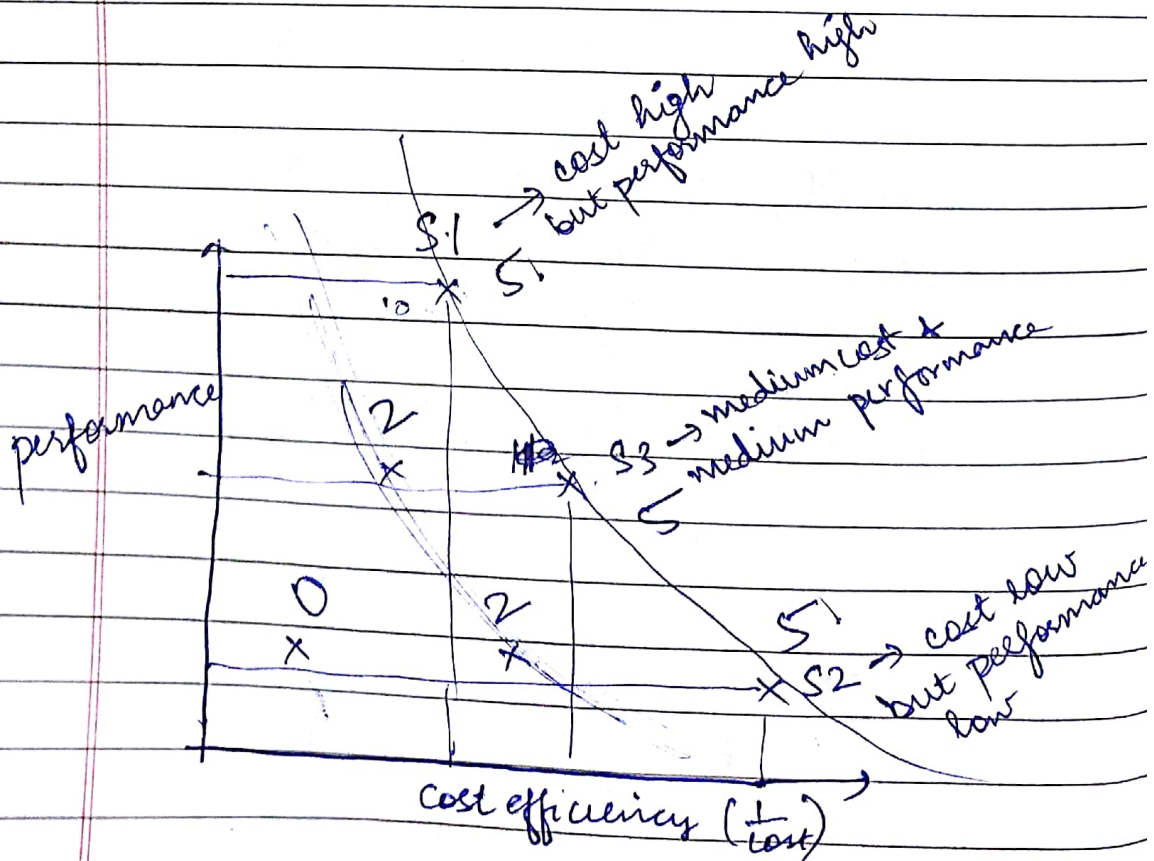
$$\frac{w_1 OF_1}{\sum w} - \frac{w_2 OF_2}{\sum w} + \frac{w_3 OF_3}{\sum w}$$

$$\frac{w_1 OF_1 + \frac{w_2}{OF_2} + w_3 OF_3}{\sum w}$$

$$\frac{OF_1 + OF_3}{1 + OF_2}$$

- Non-inferior solutions :
Those solutions who are not better than other non-inferior solutions in all respects.
- Step 1 : features
Step 2 : constraints
Step 3 : threshold
Step 4 : objective function

$$OF = \frac{w_1}{\sum w_i} f_1 + \frac{w_2}{\sum w_i} f_2$$



S_1, S_2, S_3 are non-inferior solutions.

Through weighted mean, I will get the averagely best soln S_3 . S_1 and S_2 will be lost.

I would rather have a set of ^{non-}inferior solutions

↳ Pareto-optimal solution

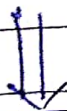
Rank: No. of solutions which are not superior in all dimensions

FORAGING BY ANIMALS:

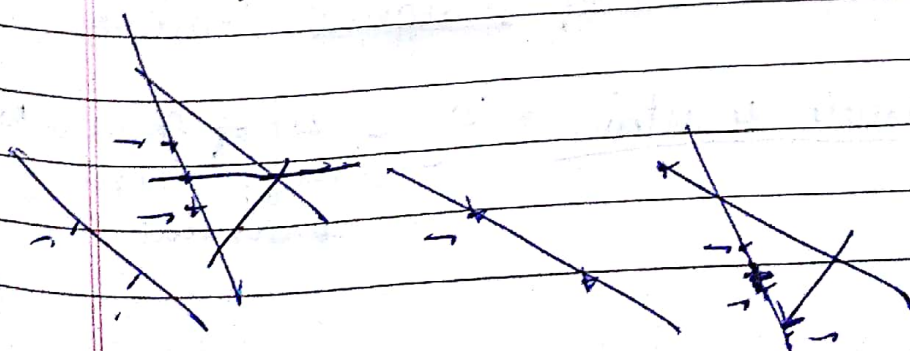
Ant family:

↓
release pheromone

Other ants sense pheromone & follow path with high ~~pheromone~~ pheromone

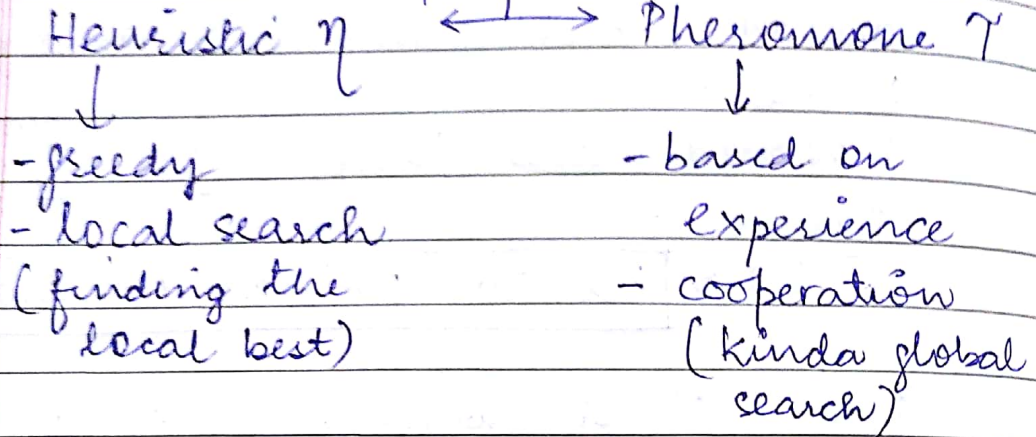


Ant Colony Optimisation



Ant Colony Optimisation

Two parameters



Combinatorial Optimisation Problem:

$$\langle S, C, f: S \rightarrow \mathbb{R}_0^+ \rangle$$

↗ optimisation fn.

S : set of features = $\{x_i\} \quad i=1 \text{ to } N$

C : set of constraints

f : Objective function

Features have values which belong to some domain

Solution \equiv Set of assigned features

→ Feasible solution: $S_C \rightarrow$ set of features which satisfy certain constraints

Define global minima/ max → you may not reach it but still we define it, because that is the ultimate goal

$$f(s_c^*) \leq f(s_i) \quad \forall s_i \in S_c$$

↑
global optima

TSP using ACO:

Initialize

Set Parameters

Initialize pheromone levels for some paths

Do

Begin

Construct Ant Solution

→ five random starting points to ants

Synchronise (optional)

→ greedy / probabilistic

Update pheromone

End

Until (stop criteria)

↳ convergence criteria

↑
In ACO, it is often 'n' iterations

Construct Ant's solution \Rightarrow

Probability of choosing a next node, given a set of neighbours

$$P(C_{ij} | SP) = \frac{T_{ij}^{\alpha} \eta_{ij}^{\beta}}{\sum_{C_{i \rightarrow l} \in SP} T_{il}^{\alpha} \eta_{il}^{\beta}}$$

neighbours

where:

$T_{ij} \equiv$ Pheromone trail b/w i & j

$\eta \equiv$ local factor (min distance)

$$\eta \propto \frac{1}{L_{ij}} = \frac{1}{L_{ij}}$$

Synchronise \Rightarrow

In GAs, solutions interact with each other using crossovers. That is not directly present here.

In ACO, there may also be communication between ants

\therefore This optional step.

Update \Rightarrow

$$\tau_{ij} \leftarrow (1 - \rho) \tau_{ij} + \rho \sum F(s)$$

evaporation rate

fitness fn of all the solutions

$$s \in \{ \} \mid c_{ij} \in s$$

What should this set be?

- All the ants who travelled from i to j
- Or only the fittest ones who travel the $i \rightarrow j$

$$Supd = \underset{s \in S_{iter}}{\operatorname{argmax}} (F_s)$$

when you want to consider the one whose argument has max value