# **IMAGE COMPRESSION**

# Part A: Theory

# 1. Explain the need for image compression in multimedia applications. How does compression impact storage and transmission efficiency?

#### Ans:

Image compression is essential in multimedia applications for enhancing storage efficiency and transmission speed. Here's why it's crucial and how it impacts storage and transmission:

### **Storage Efficiency**

Digital images, especially high-resolution ones, require substantial storage space. In multimedia applications where thousands or millions of images may need to be stored (such as on social media platforms, streaming services, or cloud storage systems), storage requirements can be overwhelming. **Compression reduces file size**, making it possible to store more images within the same amount of storage space, which is essential for applications storing high volumes of high-quality images or videos, reducing the need for extensive storage infrastructure.

#### **Transmission Efficiency**

For multimedia applications that transmit images over the internet or mobile networks, transmission speed is critical. High-resolution images have large file sizes, leading to longer upload and download times, particularly on limited bandwidth connections. Compressed images, which use less data, can be transmitted faster, improving user experience by reducing loading times and enabling smooth streaming or browsing. This is especially beneficial for mobile devices with limited data plans, saving bandwidth and reducing data costs for users.

#### Impact of Compression on Storage and Transmission Efficiency:

- **Storage:** Compression minimizes the required disk space, allowing more images to be stored. Compressed images can take up only a fraction of the space needed for original files, significantly reducing storage costs.
- **Transmission:** Smaller file sizes from compression consume less bandwidth, leading to faster upload/download speeds and better performance on low-bandwidth networks, allowing efficient multimedia application use even in low-connectivity areas.

In summary, image compression optimizes storage and transmission efficiency in multimedia applications, enabling smoother user experiences and cost-effective storage solutions.

# 2. What is redundancy? Explain three types of Redundancy.

#### Ans:

Redundancy in multimedia applications, especially in image and video processing, refers to the presence of repetitive or unnecessary data that does not contribute meaningfully to the perceived quality of the content. By identifying and removing redundant data, compression algorithms can reduce file sizes without significantly affecting quality. There are several types of redundancy:

# 1. Spatial Redundancy

- **Definition**: Spatial redundancy, also known as intra-frame redundancy, refers to repetitive information within a single frame or image. Nearby pixels in an image often have similar or identical color values, creating patterns that compression algorithms can identify and encode more efficiently.
- **Example**: In an image of a blue sky, many adjacent pixels might have nearly the same shade of blue. Instead of encoding each pixel separately, compression algorithms can record the color once and repeat it for all similar pixels in the area.

#### 2. Temporal Redundancy

- **Definition**: Temporal redundancy, also known as inter-frame redundancy, occurs in video data, where consecutive frames often contain similar or identical information. This redundancy allows compression algorithms to store only changes between frames instead of storing each frame independently.
- **Example**: In a video of a stationary object, the background remains consistent across frames. Compression algorithms can reduce file size by only recording changes, like object movements, instead of re-encoding the entire frame.

#### 3. Psycho-visual Redundancy

- **Definition**: Psycho-visual redundancy is based on human perception, where certain visual information is less noticeable or irrelevant to the viewer. Compression algorithms exploit this by reducing details that the human eye is unlikely to detect, especially in areas where slight color or brightness variations are imperceptible.
- **Example**: In JPEG compression, psycho-visual redundancy is used by discarding high-frequency details in an image, which humans typically do not notice, to achieve significant compression without perceived loss of quality.

By removing these types of redundancy, compression techniques reduce file sizes efficiently while maintaining adequate quality for storage and transmission.

# 3. Define coding redundancy. Provide examples of how coding redundancy is used to reduce image file sizes.

#### Ans:

**Coding redundancy** refers to the inefficiencies in how data is represented, often due to uniform or fixed-length coding, where each symbol or pixel value is represented by the same number of bits, regardless of how frequently it occurs. In images, some pixel values (e.g., certain colors or intensities) appear more often than others. Compression algorithms can reduce file sizes by representing these frequent values with shorter codes and less common values with longer codes.

# **Examples of Coding Redundancy in Image Compression:**

# 1. Huffman Coding

- **Description**: Huffman coding is a variable-length coding technique that assigns shorter codes to more frequent symbols and longer codes to less frequent ones. By using fewer bits for common pixel values, Huffman coding reduces the total number of bits required to store an image.
- **Example**: In a grayscale image with a dark background and occasional light areas, the dark pixels may represent 90% of the image. Instead of using 8 bits for each pixel, Huffman coding can use shorter codes for these common dark values, significantly reducing the file size.

# 2. Run-Length Encoding (RLE)

- **Description**: Run-Length Encoding compresses data by replacing sequences (or "runs") of the same value with a single value and a count. This is especially effective in images with large areas of uniform color, such as logos or cartoons.
- **Example**: In an image with a long sequence of white pixels, RLE would store this as "white, 100" instead of repeating "white" 100 times, resulting in a more compact representation and a smaller file size.

#### 3. Arithmetic Coding

- **Description**: Arithmetic coding encodes an entire message as a single number between 0 and 1, based on the probabilities of different symbols. This can achieve higher compression ratios than Huffman coding by handling non-integer bits per symbol.
- **Example**: In an image with specific color intensities that are more probable, arithmetic coding would assign a unique range to each intensity based on its probability, storing the entire image data in a compact, encoded format.

These coding techniques leverage coding redundancy by tailoring bit usage to symbol frequency, resulting in significant image file size reduction without losing any data.

# 4. Discuss inter-pixel redundancy and how it is exploited in image compression algorithms. Provide examples of common methods to reduce inter-pixel redundancy.

#### Ans:

**Inter-pixel redundancy** refers to the repetitive information between neighboring pixels in an image. Since adjacent pixels often have similar or identical values (especially in areas of smooth color or gradual gradient changes), this redundancy allows compression algorithms to represent the data more efficiently by reducing the amount of information that needs to be stored for each pixel individually.

#### How Inter-pixel Redundancy Is Exploited in Image Compression

Image compression algorithms reduce inter-pixel redundancy by identifying similar pixel values in neighboring areas and encoding them in a way that minimizes repetition. By reducing these redundancies, algorithms achieve higher compression ratios, leading to smaller file sizes without noticeably affecting image quality.

#### **Common Methods to Reduce Inter-pixel Redundancy**

## 1. Transform Coding (e.g., Discrete Cosine Transform - DCT)

- **Description**: Transform coding, often used in JPEG compression, converts spatial pixel values into frequency components. DCT, in particular, identifies patterns in small blocks of pixels (e.g., 8x8 pixels) and represents these patterns in terms of frequencies.
- **How It Reduces Redundancy**: By focusing on frequencies instead of individual pixels, DCT allows high-frequency details (which represent rapid changes between adjacent pixels) to be compressed more aggressively, while retaining the low-frequency components (smooth areas with less pixel variation) more accurately.
- **Example**: In a 10x10 area of sky with gradual color changes, DCT might encode the entire block in terms of low-frequency components, requiring fewer bits than representing each pixel independently.

#### 2. Predictive Coding

- **Description**: Predictive coding, used in lossless compression formats like PNG, predicts the value of each pixel based on its neighboring pixels and encodes only the difference (or "residual") between the actual and predicted values. Since the residuals are often small, they can be stored in fewer bits.
- How It Reduces Redundancy: Predictive coding minimizes the information stored by only recording changes from the predicted values. It effectively compresses smooth areas by storing small differences instead of repeating similar pixel values.
- **Example**: In a grayscale image with a gradient from dark to light, the pixel values can be predicted using the previous pixel. Instead of encoding each pixel, predictive coding encodes the gradual change, saving space.

### 3. Subsampling (e.g., Chroma Subsampling)

- **Description**: Chroma subsampling is based on the fact that human eyes are less sensitive to color details (chrominance) than brightness (luminance). This technique reduces the resolution of the color channels while keeping the brightness information intact.
- **How It Reduces Redundancy**: By storing less color information in areas where pixels are similar in color, chroma subsampling reduces the amount of data without perceptible quality loss.
- **Example**: In an image with a red and blue gradient, chroma subsampling might downsample the color channels, keeping only a subset of pixel information, which is then interpolated back, reducing data size while maintaining visual fidelity.

These methods are central to popular image compression algorithms like JPEG, PNG, and even video codecs, enabling efficient compression by leveraging inter-pixel redundancy in various ways.

# 5. Compare and contrast lossy and lossless image compression techniques. Provide examples of when each type of compression is more appropriate.

#### Ans:

Here's a comparison of **lossy** and **lossless** image compression techniques presented in table form:

Feature	Lossy Compression	<b>Lossless Compression</b>			
Definition	Reduces file size by permanently eliminating some data.	Compresses data without losing any information.			
Data Integrity	Some original data is lost; the reconstructed image may differ from the original.  All original data can be perfect restored.				
File Size	Generally results in smaller file sizes, making it suitable for web use.  Results in larger file compared to lossy compression no data is lost.				
Image Quality	Quality may degrade significantly at high compression levels, leading to artifacts.	Maintains the original image quality, with no artifacts introduced.			
Encoding Techniques	Common techniques include JPEG, WebP, and some forms of MP3 audio.	Common techniques include PNG, TIFF, and GIF.			
Application Areas	Best suited for photographs, videos, and web images where smaller file size is crucial and minor quality loss is acceptable.	fidelity, such as medical imaging,			
Reusability	Not suitable for repeated editing, as quality can degrade with each save.	Allows for repeated editing and saving without quality loss.			

Use Cases	- Web graphics (JPEG for photos) - Medical imaging (DICOM)
	- Streaming video (MP4, AV1) - Archival of photographs
	- Social media uploads (JPEG, WebP) - Technical diagrams or
	illustrations

#### **Conclusion**

Both lossy and lossless compression techniques have their specific applications, advantages, and limitations. The choice between them depends on the requirements for image quality, file size, and the context in which the images will be used. Lossy compression is often preferred for everyday photography and online use, while lossless compression is essential for applications requiring exact reproduction of original images.

# 6. Explain Compression Ratio with an Example. What other metrics helps in understanding the quality of the compression.

#### Ans:

**Compression Ratio** is a metric that measures how much an image (or other data) has been compressed relative to its original size. It is calculated as the ratio of the original file size to the compressed file size. A higher compression ratio indicates more significant compression, meaning the file size has been reduced more substantially.

#### **Formula**

Compression Ratio = Original File Size / Compressed File Size

The compression ratio is calculated as:

$$\label{eq:compression} \begin{aligned} \text{Compression Ratio} &= \frac{\text{Original File Size}}{\text{Compressed File Size}} \end{aligned}$$

Alternatively, it can be expressed as a percentage of reduction using:

$$Compression \ Percentage = \left(1 - \frac{Compressed \ File \ Size}{Original \ File \ Size}\right) \times 100\%$$

Suppose you have an uncompressed image with a file size of 10 MB, and after compression, the file size is reduced to 2 MB. The compression ratio would be calculated as:

Compression Ratio=10MB / 2MB=5:1

Compression Ratio = 
$$\frac{10 \text{ MB}}{2 \text{ MB}} = 5:1$$

This means that the compressed file is 5 times smaller than the original. Alternatively, the compression percentage can be calculated as:

$$ext{Compression Percentage} = \left(1 - rac{2}{10}
ight) imes 100\% = 80\%$$

So, the compression technique achieved an 80% reduction in file size.

This means that the compressed file is five times smaller than the original file.

#### **Additional Metrics for Assessing Compression Quality**

Besides compression ratio, several other metrics help assess the quality and effectiveness of image compression, particularly with lossy methods:

# 1. Peak Signal-to-Noise Ratio (PSNR)

- **Definition**: PSNR measures the difference between the original and compressed images. It is expressed in decibels (dB), with higher values indicating better quality and closer resemblance to the original image.
- **Use**: PSNR is widely used in image processing to quantify the quality of lossy compression.

Formula: PSNR (in decibels) is calculated using Mean Squared Error (MSE) as:

$$ext{PSNR} = 10 \cdot \log_{10} \left( rac{ ext{MAX}^2}{ ext{MSE}} 
ight)$$

where MAX is the maximum pixel value (usually 255 for 8-bit images).

• **Example**: If a compressed image has a PSNR of 40 dB, it indicates a high-quality compression with minimal perceptible difference from the original.

#### 2. Structural Similarity Index (SSIM)

- **Definition**: SSIM is a metric that evaluates visual quality by comparing structural information, luminance, and contrast between the original and compressed images. The SSIM score ranges from -1 to 1, with values closer to 1 indicating higher similarity.
- Use: SSIM is useful because it aligns more closely with human visual perception than PSNR alone, making it a better indicator of visual quality.
- **Example**: An SSIM score of 0.98 for a compressed image suggests it is very similar to the original in perceived quality.
  - Formula (simplified):

$$ext{SSIM}(x,y) = rac{(2\mu_x \mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)}$$

#### 3. Mean Squared Error (MSE)

- **Definition**: MSE measures the average squared difference between pixel values in the original and compressed images. A lower MSE indicates a closer resemblance between the images.
- Use: MSE helps quantify the amount of distortion introduced by compression.
- **Example**: If an image has an MSE of 10, the compression has introduced only minor distortion, while a higher MSE would suggest more noticeable quality loss.

$$ext{MSE} = rac{1}{MN} \sum_{i=1}^{M} \sum_{i=1}^{N} \left(I(i,j) - K(i,j)
ight)^2$$

# 4. Bitrate (or Bits per Pixel - BPP)

- **Definition**: Bitrate, often measured in bits per pixel (BPP), indicates the amount of information stored per pixel in the compressed image. Lower BPP values mean smaller file sizes but may also lead to quality loss, depending on the compression method.
- Use: Bitrate is particularly relevant for lossy compression, as it allows users to balance quality and compression level.
- **Example**: A BPP of 0.5 for a compressed image suggests a high level of compression, while a BPP of 2.0 would indicate higher image quality at the expense of a larger file size.

In summary, while **compression ratio** tells us about file size reduction, metrics like **PSNR**, **SSIM**, **MSE**, and **bitrate** provide insights into the quality of the compressed image and help determine how well it preserves the visual fidelity of the original image.

# 7. Identify Pros and Cons of the following algorithms-

- I. Huffman coding,
- II. Arithmetic coding,
- III. LZW coding,
- IV. Transform coding,
- V. Run length coding

#### Ans:

Here are the pros and cons of five widely used compression algorithms:

#### I. Huffman Coding

#### **Pros**:

- **Optimal for Fixed-Length Symbols**: Provides efficient encoding for data with known symbol frequencies, making it suitable for text and images with common symbols.
- **Simple and Widely Used**: Easy to implement and widely adopted in formats like JPEG and MP3.
- **Lossless Compression**: Ensures data integrity, as it is a lossless method.

#### Cons:

- **Inefficiency for Small Data Sets**: Less effective on data with a small number of symbols or low variability.
- **Static Compression Scheme**: Needs a separate Huffman tree for each data set, which may require extra space to store the tree or to repeat the encoding process with each file.
- **Suboptimal for Low-Frequency Data**: Doesn't handle low-frequency symbols as efficiently as some other methods (e.g., Arithmetic Coding).

#### **II. Arithmetic Coding**

#### **Pros**:

- **Better Compression Ratios**: Often achieves higher compression than Huffman coding, especially for data with highly variable probabilities.
- **Adaptive**: Can adjust to changing symbol probabilities over time, making it suitable for dynamic data.
- **Flexible Symbol Encoding**: Works well with fractional bits per symbol, leading to more efficient compression.

#### Cons:

- **Complexity**: More computationally intensive and challenging to implement than Huffman coding.
- **Vulnerability to Errors**: Errors in encoded data can propagate, making it more sensitive to transmission errors.
- **Patented Implementation**: Some implementations may be restricted by patents, limiting open-source usage.

# III. LZW Coding (Lempel-Ziv-Welch)

#### **Pros**:

- **Dictionary-Based**: Builds a dictionary dynamically, which can efficiently compress repetitive data without prior knowledge of symbol frequencies.
- Widely Used in Image Formats: Integral to GIF and TIFF formats and suitable for compressing both text and image files.
- Lossless Compression: No data is lost, making it suitable for exact reproduction.

#### Cons:

- **Not Optimal for Small Files**: Performance gains depend on data length, as the dictionary needs time to adapt to data patterns.
- **Limited Compression with High-Variability Data**: Less effective for data with little repetition, as the dictionary grows without compressing efficiently.
- **Potential Memory Usage**: Can consume considerable memory if the dictionary grows too large, especially with high variability in data.

#### IV. Transform Coding (e.g., Discrete Cosine Transform, DCT)

#### **Pros**:

- **Effective for Image and Audio Compression**: Especially useful in JPEG and MP3 formats, as it effectively reduces spatial and temporal redundancies.
- **Frequency-Based Compression**: Encodes data in the frequency domain, making it possible to selectively discard less perceptible details (e.g., psycho-visual redundancy).
- **High Compression Ratios**: Achieves substantial reduction in file size by focusing on essential frequency components.

#### Cons:

- **Lossy Compression**: Often discards data, which may lead to quality loss, especially at high compression rates.
- **Computational Complexity**: Requires significant processing power, particularly for large data sets like high-resolution images or audio.
- Not Suitable for All Data Types: Works best for continuous data (e.g., images, audio) and is not generally effective for text or other discrete data types.

# V. Run-Length Encoding (RLE)

### **Pros**:

- **Simple and Fast**: Easy to implement and performs very fast encoding and decoding, requiring minimal computation.
- **Highly Effective for Repetitive Data**: Works best with data that has long runs of identical values (e.g., simple graphics, logos).
- **Lossless Compression**: Retains original data integrity, making it suitable for applications requiring exact reproduction.

#### Cons:

- **Ineffective for Complex Data**: Performs poorly on data with high variability or frequent changes, as the compression ratio decreases.
- **Not Optimal for Photographic Images**: Not suitable for images with high color variation (like photos) since runs of identical pixels are rare.
- **Limited Application**: Primarily used in specific image types and basic file formats (e.g., BMP, TIFF) rather than complex multimedia files.

#### **Summary Table**

Algorithm	Pros	Cons		
Huffman	Lossless, efficient for frequent	Inefficient for small data sets, static		
Coding	symbols, simple	scheme, suboptimal for rare symbols		
Arithmetic	High compression ratio, adaptive,   Complex, error-sensitive, potent			
Coding	flexible patent issues			
LZW Coding	Builds a dictionary dynamically,	Less effective on small files, high-		
	effective for repetitive data,	ta, variability data, memory usage ca		
	lossless	increase		
Transform	High compression for multimedia,	Lossy, complex, unsuitable for		
Coding	effective frequency compression	discrete data		
<b>Run-Length</b>	Simple, fast, effective for	Ineffective for complex or high-		
Encoding	repetitive data, lossless variability data, limited applications			

Each of these algorithms has its specific strengths, making them ideal for different types of data compression, depending on the redundancy, data patterns, and fidelity requirements.

# 8. Perform Huffman coding on a given set of pixel values. Show the step-bystep process and calculate the compression ratio achieved.

#### Ans:

To demonstrate Huffman coding, let's go through a sample set of pixel values. I'll create a hypothetical example where each pixel value occurs with a specific frequency, then show the steps to create a Huffman tree and calculate the compression ratio.

# **Step 1: Define Pixel Values and Their Frequencies**

Suppose we have the following pixel values and frequencies:

Pixel Value	Frequency
A	10
В	15
С	30
D	16
Е	29

**Step 2: Build the Huffman Tree** 

# 1. Sort Pixels by Frequency:

- Initially, sort pixel values by their frequencies in ascending order.
- Order: A (10), B (15), D (16), E (29), C (30)

# 2. Combine the Two Lowest-Frequency Nodes:

- Combine A (10) and B (15) to create a new node with frequency 25.
- Tree:

25

/\

A B

• New order: D (16), 25 (A+B), E (29), C (30)

## 3. Repeat Combination:

- Combine **D** (16) and 25 (A+B) to create a new node with frequency 41.
- Tree:

• New order: E (29), C (30), 41 (D+A+B)

# 4. Combine Again:

- Combine E (29) and C (30) to create a new node with frequency 59.
- Tree:

• New order: 41 (D+A+B), 59 (E+C)

#### 5. Final Combination:

- Combine **41** (**D**+**A**+**B**) and **59** (**E**+**C**) to form the root node with frequency **100**.
- Complete Huffman Tree:

**Step 3: Assign Binary Codes to Each Pixel Value** 

Assign 0 to the left branches and 1 to the right branches to determine each pixel's binary code:

Pixel Value	Code
A	001
В	000
С	11
D	01
E	10

Step 4: Calculate Total Bit Usage with Huffman Coding

Using Huffman coding, the total number of bits required to encode each pixel value is calculated by multiplying the length of each code by its frequency:

Total Huffman Bits= $(3\times10)+(3\times15)+(2\times30)+(2\times16)+(2\times29)=30+45+60+32+58=225$  bits.

# **Step 5: Calculate Original Bit Usage (Fixed-Length Encoding)**

If each pixel value were encoded with a fixed-length binary code, we would need

[log5]=3 bits per pixel value (since we have 5 unique values).

Total Fixed-Length Bits= $3\times(10+15+30+16+29)=3\times100=300$  bits.

#### **Step 6: Calculate Compression Ratio**

The compression ratio achieved by Huffman coding is:

Compression Ratio = Original Bits / Huffman Bits = 300/225 = 1.33:1

This means that Huffman coding reduces the file size by about 33%, achieving a compression ratio of 1.33:1.

# 9. Explain the concept of arithmetic coding and how it differs from Huffman coding. Why is arithmetic coding considered more efficient in some cases?

#### Ans:

**Arithmetic coding** is an advanced form of entropy coding used in data compression. Unlike Huffman coding, which assigns fixed-length codes to symbols, arithmetic coding represents an entire message as a single fractional number in the range [0, 1).

# **Concept of Arithmetic Coding**

- 1. **Representation of Data**: In arithmetic coding, the entire message is represented as a single number, which is derived from the cumulative probabilities of the symbols in the message.
- 2. **Precision**: The more bits you allocate to the fractional representation, the more precise the representation of the message becomes, allowing for efficient compression.
- 3. **Encoding Process**: The encoder subdivides the interval [0, 1) into segments whose sizes correspond to the probabilities of the symbols. As symbols are processed, the interval narrows down to a smaller subinterval, and the final number represents the encoded message.

### **Differences Between Arithmetic Coding and Huffman Coding**

Here is a comparison presented in table form:

Feature	Arithmetic Coding	Huffman Coding	
Encoding Method	Represents entire messages as a single number based on cumulative probabilities.	Assigns fixed-length binary codes to individual symbols based on their frequencies.	
Efficiency	More efficient for small alphabets and large messages, as it can	1	

Code Length	Produces a variable-length code that can be arbitrarily precise, depending on the number of bits used.	Produces fixed-length codes for each symbol based on its frequency, leading to a bounded maximum code length.
Handling of Symbols	Can encode an entire sequence of symbols in one go, leading to potentially better compression.	Encodes symbols one at a time, which may result in less efficient use of bits.
Complexity	More complex to implement and requires more computational resources, especially for encoding and decoding.	Simpler to implement and faster for encoding and decoding, as it uses a straightforward tree structure.
Probability Table	Utilizes a cumulative probability table for continuous intervals, leading to more flexible compression.	Requires a fixed probability table based on the frequencies of symbols before encoding.
Use Cases	Commonly used in contexts requiring high compression ratios, such as image and video coding (e.g., JPEG2000).	Widely used in data formats like ZIP and PNG, where simplicity and speed are advantageous.

### Why is Arithmetic Coding Considered More Efficient in Some Cases?

- **Adaptability**: Arithmetic coding adapts better to varying symbol probabilities, making it particularly effective in scenarios where certain symbols occur much more frequently than others.
- **Higher Compression Ratios**: It can achieve better compression ratios than Huffman coding, especially for sources with high entropy or when dealing with long sequences of symbols.
- **Finer Granularity**: The ability to represent probabilities with more precision allows for more efficient encoding, especially when working with large datasets where the frequency of occurrence varies significantly.

#### **Conclusion**

Arithmetic coding is a powerful compression technique that provides a more flexible and potentially more efficient alternative to Huffman coding in certain situations. While it may involve increased complexity and computational overhead, its adaptability and superior compression capabilities make it an attractive choice for various applications in data compression.

# 10. Provide an example of LZW coding on a simple sequence of image pixel values.

#### Ans:

LZW is a dictionary-based compression algorithm that builds a dictionary dynamically based on patterns in the data.

### **Example Sequence of Pixel Values**

Consider the following simple sequence of pixel values:

#### ABABABABA

# **Step-by-Step LZW Coding Process**

#### 1. **Initialize the Dictionary**:

- Start with a dictionary containing each unique symbol in the sequence.
- Assign an index to each symbol:

$$A \to 0$$
  
$$B \to 1$$

• The initial dictionary:

### 2. **Encoding Process**:

- Begin scanning the sequence and build the dictionary as you go.
- Look for the longest sequence (or "phrase") that matches an entry in the dictionary.
- Output the index for the phrase and add the new phrase (current phrase + next symbol) to the dictionary with a new index.

Step	<b>Current Phrase</b>	Next Symbol	<b>Dictionary Output</b>	New Dictionary Entry	Index
1	A	В	0	AB	2
2	В	A	1	BA	3
3	A	В	0	Already exists	
4	AB	A	2	ABA	4
5	A	В	0	Already exists	
6	AB	(End)	2	N/A	

### 4. Final Encoded Output

The LZW encoding for the sequence A B A B A B A B A is 0, 1, 0, 2, 0, 2

#### **Explanation of Steps**

• **Step 1**: The current phrase is A, and the next symbol is B. A is in the dictionary with index 0, so output 0 and add the new phrase AB to the dictionary with index 2.

- **Step 2**: The current phrase is B, and the next symbol is A. B is in the dictionary with index 1, so output 1 and add the new phrase BA to the dictionary with index 3.
- **Step 3**: The current phrase is A, and the next symbol is B. A is in the dictionary with index 0, so output 0. AB already exists in the dictionary, so there's no need to add it.
- **Step 4**: The current phrase is AB, and the next symbol is A. AB is in the dictionary with index 2, so output 2 and add the new phrase ABA with index 4.
- **Step 5**: The current phrase is A, and the next symbol is B. Output 0 as A is in the dictionary.
- **Step 6**: The current phrase is AB, and there are no more symbols in the sequence. Output 2.

#### **Final Dictionary**

After encoding, the dictionary looks like this:

A: 0,

B: 1,

AB: 2,

BA: 3,

ABA: 4

#### **Decoding the Output**

To reconstruct the original sequence from the encoded output 0, 1, 0, 2, 0, 2, use the dictionary created during encoding to retrieve each pattern and reconstruct the sequence accurately.

#### **Summary**

The LZW encoded sequence 0, 1, 0, 2, 0, 2 provides a compressed representation of the original pixel sequence A B A B A B A B A B A. This example demonstrates how LZW builds a dictionary dynamically, allowing it to identify and store repeating patterns, thus achieving compression on repetitive data.

# 11. What is transform coding? Explain how it helps in compressing image data by reducing redundancies in the frequency domain.

#### Ans:

**Transform Coding** is a technique used in image and audio compression that converts data from the spatial (or time) domain into the frequency domain. This transformation enables more efficient data representation and compression by leveraging the different perceptual properties of the human visual and auditory systems.

#### **Key Concepts of Transform Coding**

- 1. **Transformation**: In transform coding, the original data is subjected to a mathematical transformation that converts it into a set of coefficients representing different frequency components. Common transforms used in image coding include:
  - **Discrete Cosine Transform (DCT)**: Most widely used in image compression formats like JPEG.
  - **Discrete Wavelet Transform** (**DWT**): Employed in more advanced compression schemes, such as JPEG2000.
- 2. **Frequency Domain Representation**: After transformation, the image is represented as a sum of sine and cosine functions (in the case of DCT), each with a corresponding coefficient. These coefficients represent the amount of each frequency present in the image.
- 3. **Redundancy Reduction**: The frequency domain representation often reveals that most of the image information is concentrated in a small number of coefficients, while the higher frequency components (which generally correspond to fine details) can be less significant for human perception.

### **How Transform Coding Helps in Compressing Image Data**

Transform coding reduces redundancies in image data through the following mechanisms:

# 1. Energy Compaction:

- The transformation tends to concentrate the image energy (information) into fewer coefficients. In many images, most of the significant information can be captured by a small number of low-frequency coefficients.
- For instance, in DCT, the first few coefficients often represent the majority of the image's perceptible information, allowing for compression by retaining these coefficients while discarding the less significant high-frequency coefficients.

#### 2. Quantization:

- Once the image is transformed, quantization can be applied to the coefficients. This process involves reducing the precision of the less significant coefficients, leading to data loss that is often imperceptible to the human eye.
- For example, in JPEG compression, quantization tables are used to determine how much precision to retain for each coefficient, favoring lower frequencies where more detail is visible.

#### 3. Reducing Spatial Redundancy:

• In the spatial domain, adjacent pixels can exhibit strong correlation (redundancy). Transform coding takes advantage of this by transforming blocks of pixels, breaking the strong correlation in the spatial domain and converting it into frequency components.

• This separation allows for better exploitation of the perceptual characteristics of images, where the human eye is less sensitive to high-frequency variations.

# 4. Efficient Coding:

- After quantization, the remaining significant coefficients can be efficiently encoded using techniques like Huffman coding or arithmetic coding. This results in a further reduction of the data size.
- The combination of quantization and efficient coding allows for significant data compression.

#### **Example of Transform Coding Process (JPEG)**

- 1. **Block Division**: The image is divided into blocks (e.g., 8x8 pixels).
- 2. **DCT Transformation**: Each block is transformed using the DCT to convert it from the spatial to the frequency domain.
- 3. **Quantization**: The DCT coefficients are quantized, reducing the precision of high-frequency components.
- 4. **Zig-Zag Scanning and Encoding**: The quantized coefficients are scanned in a zig-zag order, grouping low-frequency components together, followed by encoding using entropy coding methods.

#### **Summary**

Transform coding is a powerful method for image compression because it effectively reduces redundancies by representing image data in the frequency domain. By concentrating information into fewer significant coefficients, allowing for quantization and efficient encoding, transform coding enables substantial reductions in file size while maintaining perceptual quality. This technique is foundational in popular image compression formats, enabling efficient storage and transmission of image data.

# 12. Discuss the significance of sub-image size selection and blocking in image compression. How do these factors impact compression efficiency and image quality?

#### Ans:

The selection of sub-image size and the use of blocking are critical components in image compression techniques. They significantly influence both the compression efficiency and the quality of the resulting images. Below are the key points that highlight their significance:

#### **Significance of Sub-Image Size Selection**

#### 1. Balancing Compression Efficiency and Quality:

• Optimal Size: The size of the blocks (sub-images) used in compression algorithms, such as JPEG, affects how well redundancies are exploited. Smaller

- blocks may capture more localized variations, while larger blocks can better utilize global patterns but may overlook local details.
- Adaptive Size: In some advanced compression schemes, adaptive block sizes can be used, which allows for a balance between preserving fine details and achieving higher compression rates.

# 2. Impact on Transform Coding:

- The chosen sub-image size directly affects the effectiveness of transform coding (e.g., DCT). For instance, standard 8x8 blocks in JPEG allow for efficient frequency representation, capturing both low and high frequencies effectively.
- If the block size is too large, it may average out important details in areas with significant variation. Conversely, if it's too small, the overhead of managing many blocks can increase.

# 3. Edge and Feature Preservation:

• Smaller block sizes can help preserve edges and fine features in images, which are crucial for visual quality. However, using excessively small blocks can lead to artifacts due to insufficient averaging of pixel values.

#### **Importance of Blocking in Image Compression**

#### 1. Segmentation:

• Blocking helps segment the image into manageable pieces, allowing the compression algorithm to analyze and process each block independently. This segmentation facilitates the application of transformation and quantization techniques to local areas of the image.

#### 2. Local Redundancy Exploitation:

Blocking enables the algorithm to exploit local spatial redundancy more
effectively. Each block can be analyzed for redundancy, and similar pixel values
within a block can be compressed more efficiently than across the entire image.

#### 3. Artifact Introduction:

- **Blocking Artifacts**: If the block size is not well chosen, it can lead to visible artifacts, especially at boundaries. When blocks are too large, transitions between different blocks can create noticeable lines or edges in the compressed image (often referred to as blocking artifacts).
- **Seamless Transition**: Properly selecting block sizes can help ensure that transitions between blocks are smooth, minimizing visible artifacts.

#### **Impact on Compression Efficiency and Image Quality**

#### 1. Compression Efficiency:

- Smaller blocks can lead to higher efficiency in terms of capturing local details but may increase the complexity of encoding due to a higher number of blocks. Conversely, larger blocks can simplify the encoding process but might not compress the image as efficiently.
- Efficient compression techniques exploit the correlations and redundancies in small regions. An optimal balance in block size contributes to better compression ratios without excessively compromising image quality.

#### 2. Image Quality:

- The choice of sub-image size affects how well the compression preserves the visual quality of the image. Overly aggressive compression can lead to noticeable artifacts, loss of detail, and poor representation of edges.
- If the block size is chosen correctly, it can help maintain the essential features and details in the image, ensuring that the compressed version remains visually acceptable to the viewer.

# 3. Adaptive Techniques:

• Some modern compression algorithms employ adaptive techniques that change block sizes based on image content, enabling better handling of both smooth areas and regions with high detail or complexity.

#### Conclusion

In summary, the selection of sub-image size and blocking in image compression plays a crucial role in determining both compression efficiency and image quality. A careful balance must be struck to optimize the trade-offs between file size reduction and the preservation of essential visual characteristics. Advances in adaptive techniques continue to enhance how these factors are managed, leading to improved outcomes in various applications, from digital photography to streaming video.

# 13. Explain the process of implementing Discrete Cosine Transform (DCT) using Fast Fourier Transform (FFT). Why is DCT preferred in image compression?

#### Ans:

The **Discrete Cosine Transform (DCT)** is a widely used transform in image compression, especially in the JPEG format. It transforms spatial domain data (pixel values) into the frequency domain, allowing for the separation of image components based on frequency. The **Fast Fourier Transform (FFT)** is an efficient algorithm for computing the Discrete Fourier Transform (DFT), and it can also be adapted to compute the DCT.

#### **Implementing DCT Using FFT**

The DCT can be computed efficiently using the FFT due to the mathematical relationship between DCT and DFT. Here's a step-by-step explanation of how to implement the DCT using the FFT:

#### 1. Understanding DCT and Its Relation to FFT:

- The DCT can be thought of as a specialized case of the DFT, where it utilizes only cosine functions. This property allows it to represent real-valued signals without generating complex numbers.
- The DCT can be derived from the DFT by evaluating it at specific points and then transforming the resulting coefficients.

#### 2. **Preprocessing**:

- For an NNN-point sequence, the DCT can be derived by manipulating the input data:
  - Preprocess the input signal by applying a windowing function (optional) to mitigate edge effects, but it's not always required for basic DCT.
  - Extend the signal appropriately to ensure it meets the periodic conditions of the DFT.

#### 3. Computing the FFT:

- Use the FFT algorithm to compute the DFT of the preprocessed signal.
- This involves recursively breaking down the DFT into smaller DFTs, allowing for a significant reduction in computational complexity from  $O(N^2)$  to  $O(N\log N)$ .

#### 4. **Post-processing**:

- After computing the DFT, extract the real part of the result. The DCT outputs real coefficients, so the imaginary parts are discarded.
- Apply appropriate scaling factors to the output coefficients to match the DCT definition, as DCT includes specific normalization.

# **5. Finalizing the DCT**:

• The output of the FFT is adjusted and combined appropriately to yield the final DCT coefficients, which represent the frequency content of the original image block.

#### **Example of Implementing DCT Using FFT**

To implement the DCT of an N×N image block using FFT, you would typically:

- 1. Reshape the image data block into a 1D array.
- 2. Perform the FFT on the array to obtain frequency coefficients.
- 3. Scale and adjust the coefficients to conform to the DCT properties.
- 4. Reshape the output back into a 2D array if necessary.

### Why DCT is Preferred in Image Compression

# 1. Energy Compaction:

• The DCT is particularly effective at concentrating the energy of an image into a small number of low-frequency coefficients. Most of the visually significant information tends to be represented by these low-frequency components, which can be efficiently retained while discarding higher-frequency components that contribute less to perceived image quality.

#### 2. Perceptual Relevance:

• The human visual system is more sensitive to low frequencies and less sensitive to high frequencies. The DCT aligns well with this characteristic, allowing for more aggressive quantization of high-frequency coefficients without significantly affecting perceived image quality.

#### 3. Lossy Compression Capability:

 DCT enables lossy compression techniques, as it allows for the quantization of coefficients based on their importance. This is crucial in formats like JPEG, where file size reduction is prioritized while maintaining acceptable visual fidelity.

# 4. Computational Efficiency:

• The ability to compute DCT using FFT algorithms means that it can be calculated efficiently even for larger images. This efficiency is vital for real-time image processing applications, such as video encoding and streaming.

#### 5. Standardization:

• DCT is standardized in several compression standards (e.g., JPEG, MPEG), making it widely accepted and implemented in various software and hardware solutions.

#### **Conclusion**

The implementation of DCT using FFT leverages the efficiency of the FFT algorithm to compute DCT coefficients effectively, allowing for rapid image transformation. The DCT's ability to compact energy, align with human visual perception, and support efficient lossy compression makes it a preferred choice in image compression applications, ensuring high-quality results with manageable file sizes.

14. Describe how run-length coding is used in image compression, particularly for images with large areas of uniform color. Provide an example to illustrate your explanation.

#### Ans:

**Run-Length Coding (RLE)** is a simple yet effective method for compressing data, particularly useful for images with large areas of uniform color, such as bitmap graphics and certain types of medical images. RLE works by reducing the amount of data needed to represent consecutive pixels of the same value (color) in an image.

#### **How Run-Length Coding Works**

- 1. **Identification of Runs**: RLE identifies sequences of the same pixel value that occur consecutively in the image. A "run" is defined as a sequence of identical pixels.
- 2. **Encoding Runs**: Instead of storing each pixel value individually, RLE encodes the run by storing the pixel value followed by the number of times it is repeated. The encoded format typically looks like:
  - (value, count), where value is the pixel color and count is the number of consecutive pixels with that color.
- 3. **Storage Efficiency**: This method is particularly efficient for images where there are long runs of the same color, as it significantly reduces the amount of data that needs to be stored.

#### **Example of Run-Length Coding**

Consider the following simple example of a 1D pixel array representing a row of an image:

#### In this array:

- The value 255 (white) appears three times consecutively.
- The value 0 (black) appears twice consecutively.
- The value 255 appears five times consecutively.
- Finally, the value 0 appears three times consecutively.

#### **Step-by-Step Encoding with RLE**

- 1. **Identify Runs**:
  - **Run 1**: 255 appears **3 times**.
  - Run 2: 0 appears 2 times.
  - **Run 3**: 255 appears **5 times**.
  - Run 4: 0 appears 3 times.

# 2. **Encoding**:

- The original pixel sequence can be encoded as follows:
- 3 255 (for the first run)
- 2 0 (for the second run)
- 5 255 (for the third run)
- 3 0 (for the fourth run)

Thus, the RLE encoded representation of the original sequence would be:

[(3, 255), (2, 0), (5, 255), (3, 0)]

#### **Advantages of Run-Length Coding**

- Compression: RLE can significantly reduce the file size of images with large areas of uniform color. For example, in the above case, instead of storing 13 values, RLE represents the same information in just 4 pairs.
- **Simplicity**: The algorithm is easy to implement and requires minimal computational resources, making it suitable for environments with limited processing capabilities.

#### **Limitations of Run-Length Coding**

- **Inefficiency on Complex Images**: RLE is not efficient for images with high variability, as it may not achieve significant compression compared to the original size. In cases where pixel values change frequently, the encoded data could actually be larger than the original.
- **Data Representation**: RLE is typically more effective with monochrome images or images with large contiguous color regions, such as simple graphics or images generated by computer graphics.

#### Conclusion

Run-Length Coding is a straightforward and efficient method for compressing images, especially those with large areas of uniform color. By encoding consecutive pixels of the same color as a single value and a count, RLE significantly reduces the amount of data that needs to be stored. While it has limitations in handling complex images, it remains a valuable tool in specific applications where uniformity is prevalent.