

A complex geometric diagram illustrating a construction involving multiple circles and points. The diagram features several circles of different sizes. Points are labeled with letters: A , B , C , D , E , E' , G , H , K , M , S , T , X , Y , and Z . Lines connect various points, forming a network of geometric relationships. A prominent blue line segment connects points B , M , and C . Other lines connect points like A to Z , A to H , A to M , Z to G , Z to X , Z to H , G to X , G to H , X to H , H to K , H to M , K to M , M to C , C to E' , E' to D , D to B , B to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H to T , T to B , B to X , X to Y , Y to H , H to T , T to D , D to M , M to S , S to E , E to G , G to Z , Z to A , A to D , D to H , H

Consider an inversion about a circle at M with radius MB . It sends $Y \mapsto X$, $A \mapsto K$, $E \mapsto D$ therefore it sends $(YAE) \mapsto (XKD)$. Since $DX = DK$ and $DE \parallel XK$ we get (XKD) is tangent to BC at D therefore (YAE) is tangent to BC at E .

Hence the claim is proved. \square

The problems will be equivalent to (w) pass through T or proving 3 circles (ZHS) , (ZXD) and (ZGM) are coaxial. (*)

It sends $Z \mapsto Y$, $H \mapsto A$, $S \mapsto E$, $X \mapsto G$, $M \mapsto E'$ therefore it sends $(ZHS) \mapsto (YAE)$, $(ZXD) \mapsto GY$, $(ZGM) \mapsto (YXE')$.

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A geometric diagram illustrating a construction involving circles and lines. A horizontal line contains points S, E, D, N, E', M from left to right. Above this line, a series of overlapping circles are drawn. Point A is the topmost point of the largest circle. Other points labeled include T, X, K, Y, H, G on the circles and X', I in the interior. Lines connect various points: S to T, E, D, N, E', M ; A to X, K, Y, H, D ; X to T, G, H, Y, K ; K to X, Y, H, D, M ; E to G, H, Y, D ; N to H, Y, D ; and M to K, Y, H, D . Several lines are highlighted in blue: AX , AK , EX , EN , EM , and AY .