Influence of water vapour on autoignition of air-methane mixtures

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Abstract

A reactor with a volume of 20 liters was set up using Cantera in Python. Maximal temperatures, pressures and maximal pressure rise were calculated as a function of initial methane volume fraction, temperature and pressure. Calculations were performed for three molar fractions of water in the mixture (0, 15.97% and 27.54%). Maximum rate of pressure rise was too far away from experimental data to be taken into consideration.

1 Mathematical model

Mixture consisting of: 1 mole air (defined as 78% N_2 21% O_2 and 1%Ar), $ch4_mol$ moles of CH_4 and $water_mol$ moles of H_2o was set up in a Cantera reactor with a volume of 20l. Autoignition process occurs and explosion maximum pressures (defined as $maximal\ pressure\ -initial\ pressure\ in\ the\ reactor$) and temperatures are calculated. Maximum rate of pressure rise was also calculated but the results were too far away from experimental data.

Calculations were performed for three molar fractions of water in the mixture: 0, 1 and 2 moles, (coresponding to 0%, 15.97% and 27.54% of water vapour vol. in the mixture respectively).

2 Python 3.6 program code

2.1 Preparing the program

Necessary modules are imported.

```
import csv
import cantera as ct
import numpy as np
import matplotlib.pyplot as plt
```

2.2 Creating the 'airm' function

2.2.1 Preparing the function

Next a function airm was created. It would take initial temperature (temp) in K, initial pressure (pressure) in Pa, H_2O mole fraction $(water_mol)$ and CH_4 mole fraction $(ch4_mol)$ as arguments. Additionally plot could be set to either 0, 1 or 2 for printing information abut the simulation to the console to a different extent of details.

```
def airm(temp, pressure, water_mol, ch4_mol, plot):
```

This part of code is calculating stoichiometric conditions and allowing to set up CH_4 and H_2O mole fractions

Creating mixture to autoignite

```
gas = ct.Solution('gri30.xml')
gas.TPX = temp, pressure, d #setting gas temperature as 'temp', pressure as '
    pressure' and molar fractions as in 'd'
gas.name = "Methane-air-water_mixture"
if plot==2: #additional information about the mixture to be printed if 'plot'
    was set to '2'
    print (gas())

#Creating a reactor, filled up with 'gas' and with a volume of 0.02 cubic
    meters
r = ct.Reactor(contents=gas, name='reactor', volume=0.02)

print ('Water_mass_fraction_=_%10.3f_%%\n' % (r.thermo['H2O'].Y*100))
print ('Stoichiometry__index_(phi)_=_%10.3f\n' % ((r.thermo['CH4'].X/r.thermo['O2'].X)/(0.5)))
```

2.2.2 Preparing simulation

```
#Preparing space for data
times = np.zeros(size)
data = np.zeros((size,7))
time = 0.0 \# starting time
counter=size #setting 'counter' to 'size' (number of the loop iterations)
#different basic time steps for different initial temperatures
if temp>1400:
     current step = 1.e-5 #shorter timestep for high temperatures
elif temp>1100:
     current_step = 1.e-4 #shorter timestep for high temperatures
else:
     current\_step = 1.e-2 \#basic time step
dP=0
f=open('data.txt', 'a') #preparing file for appending data
sim = ct.ReactorNet([r]) #simulation
size = 20000 #number of iterations in the simulation advancing loop
stepchange=0
#different shorter time steps for different initial temperatures
if temp > 1400:
     short_step=1.e-6
elif temp>1100:
     {\tt short\_step} = 2.5 \! * \! 1.e \! - \! 6
else:
     short_step=1.e-4 #shorter time step [s]
itafex = ((1.e-1)/short\_step) #going through this many iterations at specified #timestep='short_step', should be equal to advancing the simulation by 0.1
 \begin{array}{l} print (\ '\%10s \_\%10s \_\%10s \_\%14s \ '\ \% \ (\ 't \_[s] \ '\ , \ 'T \_[K] \ '\ , \ 'P \_[Pa] \ '\ , \ 'u \_[J/kg] \ ')) \\ f.\ write (\ ''Initial \_temperature \_ is \_\%10.3 \ f \ n \ '' \ \% \ (temp)) \end{array} 
f.write ('%10s_%10s_%10s_%10s_%10s_%10s_%10s' % ('t_[s]', 'step_[s]', 'dT_[K
     ]','T_[K]', 'dP_[Pa]', 'P_[Pa]', 'licznik', 'iteration\n'))
```

2.2.3 Advancing simulation

The simulation is then advanced in a loop

```
for n in range(size):
    time+= current_step
    sim.advance(time)
```

Data is stored in *times* and *data* arrays

```
\frac{\mathrm{data[n,6]}}{\mathrm{rise\ in\ [Mpa/s]}} = \frac{\mathrm{dP/current\_step/1.e+6}}{\mathrm{dP/dt}} - \mathrm{maximum\ rate\ of\ pressure}
```

Writing to file for the itafex number of **it**erations **af**ter the **ex**plosion, that is equal to 0.1 seconds passing, so as to catch the rapid rise of pressure and temperature and then going back to 1.e-2 time step.

```
if r.T>temp*1.5 and n<counter+itafex and stepchange==4: #for the itafex
                number of interations
#between explosion and going back to 1.e-2 tstep, that is equal to 0.0225 [
                  f.write('%10.7f_%10.3e_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f\n' % (
                                     sim.time.
                  current step, data[n,0]-data[n-1,0], r.T, dP, r.thermo.P, counter, n)
 elif r.T>temp*1.5 and n>=counter+itafex: #setting time step back to 1.e-2,
                  0.00225 seconds after the explosion
                   f.write('%10.7f_%10.3e_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10.3f_\%10
                                     sim.time,
                    \operatorname{current\_step}, \operatorname{data}[n,0] - \operatorname{data}[n-1,0], r.T, \operatorname{dP}, r.thermo.P, counter, n)
                    if stepchange==4:
                                      f.write('setting_step_back_to_1.e-2\n')
                                     current step=1.e-2
                                     stepchange=2
                                      break #optional, will make the simulation stop at 0.1 seconds after
                                                            the ignition.
 if r.T = temp *1.5: #writing to file reactor state at each iteration before
                    the explosion
                   f.write('%10.7f_{\sim}%10.3e_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_{\sim}%10.3f_
                                    \operatorname{sim}.\ \operatorname{time}\ ,
                  \texttt{current\_step}\ ,\ \mathtt{data}\,[\,n,0\,]\,-\,\mathtt{data}\,[\,n-1\,,0\,]\,,\ r\,.\,T,\ dP,\ r\,.\,\mathsf{thermo}\,.\,P,\ \mathtt{counter}\,\,,\ n\,)\,)
 elif r.T>temp*1.5 and counter=size: #during the peak, one iteration where
                   counter is still set as size
                   f.write('%10.7f_%10.3e_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f_%10.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f_%0.3f
                                    sim.time,
                  current step, data[n,0]-data[n-1,0], r.T, dP, r.thermo.P, counter, n)
                   f.write('Setting_current_step_to_5.e-4\n')
                   current_step=short_step
                  counter=n
                  stepchange=4
 if n==0: #prints the state of reactor at the beginning of sumiulaton
                    print('%10.3e_%10.3f_%10.3f_%14.6e' % (sim.time, r.T, r.thermo.P, r.
                                     thermo.u))
 if plot == 2: #if argument 'plot' of function "airm" is set to 2, state of
                   the reactor will be printed once a 1000 iterations
                    if n % 1000 == 3:
                                      print('%10.3e_%10.3f_%10.3f_%14.6e' % (sim.time, r.T, r.thermo.P, r
                                                        .thermo.u))
```

2.2.4 Calculating 'airm' function output

After the loop maximal temperature, pressure and rate of pressure rise are calculated

```
#extracing maximal values out of data tables
Tmax=max(data[:,0]) #maximal temperature
Tend=data[n,0] #temperature at the end of simulation
Pmax=max(data[:,1]) #maximal pressure (pressure computed - initial pressure)
dPmax=max(data[:,6]) #maximum rate of pressure rise
index_max = np.argmax(data[:,6])
adt=times[index_max]
if Pmax<(pressure*1.05-pressure):
    adt=None
print ('Tmax_=_%s_[K]\nTend_=_%s_[K]' % (Tmax, Tend))
print ('Explosion_Pmax_=_%s_[Pa]\n' % (Pmax))
print ('Explosion_dP/dt_max_=_%s_[MPa/s]\n' % (dPmax))
print ('Autoignition_delay_time_=_%s_[s]\n' % (adt))
output=[Tmax, Pmax, dPmax, adt] #this is what this function ("airm") returns at</pre>
```

Optionally plotting graphs showing temperature, pressure, CH_4 and H_2O mole fractions as a function of time.

```
#plotting graphs if argument 'plot' of "airm" function is set to 1 or 2
if plot==1 or plot==2:
    n=n+1 #because "0:n" means "from 0 to n-1"
    plt.clf()
     plt.figure(figsize=(6,6))
     plt.subplot(2, 2, 1)
    plt.plot(times[:], data[:,0])
     plt.xlabel('Time_[s]')
plt.ylabel('Temperature_(K)')
     plt.subplot (2, 2, 2)
    plt.plot(times[0:n], data[0:n,1]/1.e+6)
plt.xlabel('Time_[s]')
plt.ylabel('Pressure_(MPa)')
     plt.subplot(2, 2, 3)
     plt.plot(times[0:n], data[0:n,2])
plt.xlabel('Time_[s]')
     plt.ylabel('O2_mole_fraction_[%]')
     plt.subplot(2, 2, 4)
     plt.plot(times[0:n], data[0:n,4])
     plt.xlabel('Time_[s]')
     plt.ylabel('CH4_mle_fraction_[%]')
     plt.tight layout()
     plt.show()
```

Figure 1 shows example of plots printed by the function for input:

```
airm(temp=850, pressure=ct.one atm, water mol=1, ch4 mol=0.5, plot=2)
```

This corresponds to mixture consisting of 0.5 moles of methane, 1 mole of air, and 1 mole of water with initial temperature of 850K and initial pressure of 1 atm.

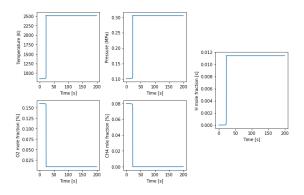


Figure 1: Example data.

2.3 Using the 'airm' function

The function 'airm' defined earlier is used in three loops.

2.3.1 The first loop

In the first loop maximal pressures and temperatures are calculated as a function of CH_4 molar fractions, with addition of 0, 1 and 2 moles of water, that is $water_mol$ is set as 0, 1 and 2. This coresponds to 0%, 15.97% and 27.54% of H_2O in the mixture (volumetric). CH_4 range tested is from 0 to 2 moles, in 41 iterations with an increase of 0.05 moles each.

```
lp=41 #number of iterations for 1st loop #preparing space for data pdata = np.zeros((lp,3)) #without water ch4m_data = np.zeros(lp) #without water ch4m_w_data = np.zeros(lp) #with water ch4m_2w_data = np.zeros(lp) #with water ch4m_2w_data = np.zeros(lp) #with water pdata_w = np.zeros((lp,3)) #with 1 mol of water pdata_2w = np.zeros((lp,3)) #with 2 moles of water o2=1 n2=0.78/0.21 ar=0.01/0.21
```

```
wt=1 #mole fraction of water in mixture
#in this loop CH4 mole fraction is changing from 0 to lp*i/2, with and without
              addition of water
 for i in range(lp):
              pdata [i : ] = airm(temp = 850, pressure = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = ct.one\_atm, water mol = 0, ch4 mol = i/2, plot = i/2,
                            =0) #without water
              pdata w[i,:]=airm(temp=850, pressure=ct.one atm, water mol=wt, ch4 mol=i/2,
                            plot=0) #with water
              pdata_2w[i,:]=airm(temp=850, pressure=ct.one_atm, water_mol=2*wt, ch4_mol=i/2,
                           plot=0) #with water
              ch4m_data[i]=(i/20)/(i/20+o2+n2+ar)*100
                                                                                                                                                                          #molar/volume fraction of CH4 in
                                                         when there is no water
              mixture, when there is 1 mole water
              ch4m_2w_data[i]=(i/20)/(i/20+o2+n2+ar+2*wt)*100 #molar/volume fraction of CH4
                            in mixture, when there are 2 moles of water
```

2.3.2 The second loop

In the second loop maximal pressures and temperatures are calculated as a function of initial temperatures. The range of temperatures tested is 850 - 2100 K, in 26 iterations with an increase of 50 K in each. The CH_4 fraction is constant, equal to $0.5 \ moles$.

```
12p=26 #number of iterations for 2nd loop
#preparing space for data
pdata2 = np.zeros((l2p,3)) #without water
pdata2_w = np.zeros((l2p,3)) \#with 1 moles of water
pdata2_2w = np.zeros((l2p,3)) #with 2 moles of water
temps = np. zeros(12p)
 #loop through initial temperatures
for j in range(l2p):
                  \texttt{current\_temp} {=} 850 {+}\, j * 50
                  pdata2[j,:]=airm(temp=current_temp, pressure=ct.one_atm, water_mol=0, ch4_mol
                                    =5, plot=0)
                  pdata2_w[j,:] = airm(temp=current_temp, pressure=ct.one_atm, water_mol=wt,
                                    ch4 mol=5, plot=0)
                  pdata2\_\overline{2}w[j,:] = airm(temp=current\_temp, pressure=ct.one\_atm, water\_mol=2*wt, pdata2\_\overline{2}w[j,:] = airm(temp=current\_temp, pressure=ct.one\_atm, press
                                    ch4_mol=5, plot=0)
                  temps [j]=current temp
```

2.3.3 The third loop

In the third loop maximal pressures and temperatures are calculated as a function of initial pressures. The range of pressures tested is 0.5 - 25.5 atm (0.051 - 2.584MPa), in 26 iterations with an increase of 0.5 atm (0.101325 MPa) in each. The CH_4 fraction is constant, equal to 0.5 moles.

```
13p=26 #number of loop iterations
#preparing space for data
pdata3 = np.zeros((13p,3)) \#without water
pdata3_w = np.zeros((13p,3)) \#with 1 mole of water
pdata3_2w = np.zeros((13p,3)) #with 2 moles of water
press = np. zeros(13p)
#wt=1 #mole fraction of water in mixture
#loop through start pressures
for j in range(l3p):
    \texttt{current\_press} = (0.5*\texttt{ct.one\_atm}) + \texttt{ct.one\_atm*j} \ \#\texttt{current\_start\_pressure\_in\_[Pa]}
    pdata3[j,:]=airm(temp=850, pressure=current_press, water_mol=0, ch4_mol=5, plot
        =0)
    pdata3_w[j,:]=airm(temp=850, pressure=current_press, water_mol=wt, ch4_mol=5,
         plot = 0
    pdata3\_2w\,[\,j\,\,,:\,] = airm\,(\,temp = 850\,,\ pressure = current\,\_\,press\,\,,\ water\,\_\,mol = 2*wt\,,\ ch4\_\,mol\,\_\,press\,\,,
         =5, plot=0)
    press[j]=current press #in [Pa]
```

2.4 Plotting and saving the data

2.4.1 The first loop

Data acquired in the first loop is then plotted:

```
plt.figure(figsize=(20,20)) #setting size of figures
plt.subplot(2, 2, 1)
plt.plot(ch4m\_data,\ pdata[:,1]/1.e+6,\ label='without\_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel('P_max_[Mpa]')
plt.subplot(2, 2, 2)
plt.plot(ch4m_data, pdata[:,0], label='without_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel('T_max_[K]')
#with 1 mole of water
plt.subplot(2, 2, 1)
plt.plot(ch4m_w_data, pdata_w[:,1]/1.e+6, label='15.97%_of_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel('P_max_[Mpa]')
plt.subplot(2, 2, 2)
plt.plot(ch4m\_data, pdata\_w[:,0], label='15.97\%\_of\_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel ('T_max_[K]')
#with 2 moles of water
plt.subplot(2, 2, 1)
plt.plot(ch4m_2w_data, pdata_2w[:,1]/1.e+6, label='27.54%_of_water')
plt.xlabel('CH4_(%vol)
plt.ylabel('P_max_[Mpa]')
plt.legend()
plt.subplot(2, 2, 2)
plt.plot(ch4m_data, pdata_2w[:,0], label='27.54%_of_water') plt.xlabel('CH4_(%vol)')
plt.ylabel('T max_[K]')
plt.legend()
plt.tight_layout()
plt.show()
plt.clf()
plt. figure (figsize = (10,10))
plt.subplot(1, 1, 1)
plt.plot(ch4m_data, pdata[:,3]*1.e+3, label='without_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel ('Autoign_delay_[ms]')
plt.subplot(1, 1, 1)
plt.plot(ch4m_data, pdata_w[:,3]*1.e+3, label='15.97%_of_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel('Autoign_delay_[ms]')
plt.subplot (1, 1, 1)
plt.plot(ch4m_data, pdata_2w[:,3]*1.e+3, label='27.54%_of_water')
plt.xlabel('CH4_(%vol)')
plt.ylabel('Autoign_delay_[ms]')
plt.legend()
plt.grid()
plt.tight layout()
plt.show()
csv\_file = 'graphdata.csv'
with open(csv_file, 'w') as outfile:
     writer = \overline{csv}.writer(outfile)
    writer.writerow(['The_first_loop'])
writer.writerow(['Without_water'])
     writer.writerow(['CH4_[%]', 'Tmax_[K]', 'Pmax_[MPa]', 'dP/dt_max_[MPa/s]', 'adt
         _[s]'])
     for i in range(lp):
           writer.writerow([ch4m\_data[i], pdata[i,0], pdata[i,1]/1.e+6, pdata[i,2], \\
               pdata[i,3]])
    writer.writerow(['With_1_mole_of_water'])
writer.writerow(['CH4[%]', 'Tmax_[K]', 'Pmax_[MPa]', 'dP/dt_max_[MPa/s]', 'adt_
         [s]'])
    for i in range(lp):
          writer.writerow([ch4m_w_data[i], pdata_w[i,0], pdata_w[i,1]/1.e+6, pdata_w
               [i,2], pdata_w[i,3]])
    writer.writerow(['With_2_moles_of_water'])
writer.writerow(['CH4[%]', 'Tmax_[K]', 'Pmax_[MPa]', 'dP/dt_max_[MPa/s]', 'adt_
         [s]'])
     for i in range(lp):
```

```
 \begin{array}{lll} writer.\,writerow\,(\,[ch4m\_2w\_data\,[\,i\,]\,,\,\,pdata\_2w\,[\,i\,\,,0\,]\,,\,\,pdata\_2w\,[\,i\,\,,1\,]\,/\,1\,.\,e+6\,,\\ pdata\_2w\,[\,i\,\,,2\,]\,,\,\,\,pdata\_2w\,[\,i\,\,,3\,]\,]\,) \end{array}
```

2.4.2 The second loop

Data acquired in the second loop is then plotted:

```
plt.clf()
plt. figure (figsize = (20,20))
11=plt.subplot(2, 2, 1)
plt.plot(temps, pdata2[:,1]/1.e+6, label='without\_water')
plt.xlabel('Temperature_[K]')
plt.ylabel('P_max_[MPa]')
plt.subplot(2, 2, 2)
plt.plot(temps, pdata2[:,0], label='without_water')
plt.xlabel('Temperature_[K]')
plt.ylabel('T_max_[K]')
#with water
plt.subplot(2, 2, 2)
{\tt plt.plot(temps, pdata2\_w[:,0], label='15.97\%\_of\_water')}
plt.xlabel('Temperature_[K]')
plt.ylabel('T_max_[K]')
plt.subplot(2, 2, 1)
plt.plot(temps, pdata2_w[:,1]/1.e+6, label='15.97%_of_water')
plt.xlabel('Temperature_[K]')
plt.ylabel('P_max_[MPa]')
#with 2 moles of water
plt.subplot(2, 2, 2)
plt.plot(temps, pdata2_2w[:,0], label='27.54%_of_water')
plt.xlabel('Temperature_[K]')
plt.ylabel ('T max_[K]')
plt.legend()
plt.subplot(2, 2, 1)
plt.plot(temps, pdata2_2w[:,1]/1.e+6, label='27.54%_of_water')
plt.xlabel('Temperature_[K]')
plt.ylabel('P_max_[MPa]')
plt.legend()
plt.tight_layout()
plt.show()
plt.clf()
plt.figure(figsize = (10,10))
plt.subplot(1, 1, 1)
plt.plot(1000/temps, pdata2[:,3]*1.e+3, label='without\_water')
plt.xlabel('1000/T_[1/K]')
plt.yscale('log')
plt.ylabel ('Autoign_delay_[ms]')
plt.subplot(1, 1, 1)
plt.plot(1000/temps, pdata2_w[:,3]*1.e+3, label='15.97%_of_water')
plt.xlabel('1000/T_[1/K]')
plt.yscale('log')
plt.ylabel('Autoign_delay_[ms]')
plt.subplot(1, 1, 1)
plt.\ plot\ (1000/\ temps\ ,\ \ pdata2\_2w\ [:\ ,3]*1.\ e+3,\ \ label='27.54\%\_of\_water')
plt.xlabel('1000/T_[1/K]')
plt.yscale('log')
plt.ylabel ('Autoign_delay_[ms]')
plt.legend()
plt.grid()
plt.tight_layout()
plt.show()
csv_file = 'graphdata.csv'
with open(csv file, 'a') as outfile:
     writer = \overline{csv}.writer(outfile)
     writer.writerow(['The_second_loopr'])
writer.writerow(['Without_water'])
writer.writerow(['TO_[K]', 'Tmax_[K]', 'Pmax_[MPa]', 'dP/dt_max_[MPa/s]', 'adt_
          [s]'])
     for i in range(12p):
           writer.writerow([temps[i], pdata2[i,0], pdata2[i,1]/1.e+6, pdata2[i,2],
                pdata2[i,3]])
```

2.4.3 The third loop

Data acquired in the third loop is then plotted:

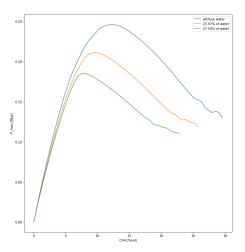
```
plt.clf() #clear the current figure
plt.figure(figsize = (20,20))
plt.subplot(2, 2, 1)
plt.plot(press/1.e+6, pdata3[:,1]/1.e+6, label='without_of_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('P_max_[MPa]')
plt.subplot(2, 2, 2)
plt.plot(press/1.e+6,\ pdata3[:,0],\ label='without_of_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('T_max_[K]')
#with 1 mole of water
plt.subplot(2, 2, 1)
plt.plot(press/1.e+6, pdata3_w[:,1]/1.e+6, label='15.97%_of_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('P_max_[MPa]')
plt.subplot(2, 2, 2)
plt.plot(press/1.e+6, pdata3_w[:,0], label='15.97%_of_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('T_max_[K]')
with 2 moles of water
plt.subplot(2, 2, 1)
plt.plot(press/1.e+6, pdata3_2w[:,1]/1.e+6, label='27.54\%_of_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('P_max_[MPa]')
plt.legend()
plt.subplot(2, 2, 2)
plt.plot(press/1.e+6, pdata3\_2w[:,0], label='27.54\%\_of\_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('T_max_[K]')
plt.legend()
plt.tight_layout()
plt.show()
plt.clf()
plt. figure (figsize = (10,10))
plt.subplot(1, 1, 1)
plt.plot(press/1.e+6, pdata3[:,3]*1.e+3, label='without_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel('Autoign_delay_[ms]')
plt.subplot(1, 1, 1)
plt.plot(press/1.e+6, pdata3_w[:,3]*1.e+3, label='15.97\%\_of\_water')
plt.xlabel('Pressure_[MPa]')
plt.ylabel ('Autoign_delay_[ms]')
plt.subplot(1, 1, 1)
plt.plot(press/1.e+6, pdata3 2w[:,3]*1.e+3, label='27.54%_of_water')
plt.xlabel('Pressure_[MPa]')
plt.yscale('log')
plt.ylabel('Autoign_delay_[ms]')
plt.legend()
plt.tight_layout()
plt.show()
csv file = 'graphdata.csv'
with open (csv file, 'a') as outfile:
    writer = \overline{csv}.writer(outfile)
```

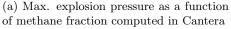
```
writer.writerow(['The_third_loop'])
 writer.writerow([[","without"]")
  writer.writerow([''p0_[MPa]', 'Tmax_[K]', 'Pmax_[MPa]', 'dP/dt_max_[MPa/s]', '
                           adt_[s]'])
 for i in range(13p):
                                     writer . writerow ([press[i]/1.e+6, pdata3[i,0], pdata3[i,1]/1.e+6, pdata3[i
                                                               ,2], pdata3[i,3]])
writer.writerow(['With_1_mole_of_water'])
writer.writerow(['p0_[MPa]', 'Tmax_[K]', 'Pmax_[MPa]', 'dP/dt_max_[MPa/s]', '
                           adt_[s]'])
 for i in range(13p):
                                   writer.\,writerow\,([\,press\,[\,i\,]/\,1.\,e+6,\,\,pdata3\_w\,[\,i\,\,,0\,]\,,\,\,pdata3\_w\,[\,i\,\,,1\,]/\,1.\,e+6,
                                                             pdata3_w[i,2], pdata3_w[i,3]])
 writer.writerow(['With_2_moles_of_water'])
 writer.writerow([\ 'p0\_[MPa]\ ',\ 'Tmax\_[K]\ ',\ 'Pmax\_[MPa]\ ',\ 'dP/dt\_max\_[MPa/s]\ ',\ 'pnax\_[MPa/s]\ '
                           adt_[s]'])
                       i in range(13p):
                                    writer.writerow ([press[i]/1.e+6, pdata3\_2w[i,0], pdata3\_2w[i,1]/1.e+6, pdata3\_2w[i,0], pdata3\_2w[i,1]/1.e+6, pdata3\_2w[i,0], pdata3_2w[i,0], pdata3_2w[i,0]
                                                              pdata3_2w[i,2], pdata3_2w[i,3]])
```

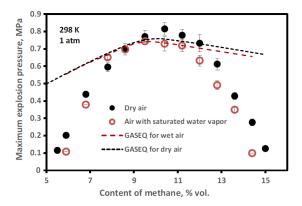
3 Results

3.1 Results from the first loop

Maximal explosion pressure is highest for 12% of CH_4 in the mixture when there is no water, for 9.43% when there is 1 mole of water and for 7.52 when there are 2 moles of water. The maximal pressure is getting lower the more water is in the mixture and occurs at lower fraction of methane. Those results were compared to those acquired by Shen et al.[2], but because of Cantera's zero dimensionality, spark ignition couldn't been simulated, thus minimal temperature tested was 850K in comparison to 298K in aforementioned paper. In Cantera simulation, maximal pressure without addition of water was determined to occur at higher vol. fraction of CH_4 (12% vs 10.5%) than in experiment. The maximal pressure was 0.2461MPa, which is 3.33 times lower than in Shen's experiment. Like in Shen's experiment, the point of maximal pressure was moving towards lower CH_4 vol. fractions when water was added and was lower with water than than when there was no water added. The discrepancy in results may be due to different phenomenons tested, that is ignition instead of autoignition. Figure 2 shows comparison of acquired maximal pressures as a function of methane vol. fraction in the mixture.







(b) Max. temperature as a function of methane fraction from [2]

Figure 2: Results comparison

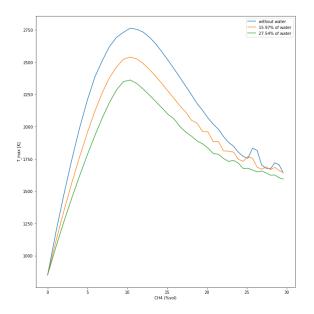


Figure 3: Maximum temperatures as a function of methane vol. fractions acquired in Cantera

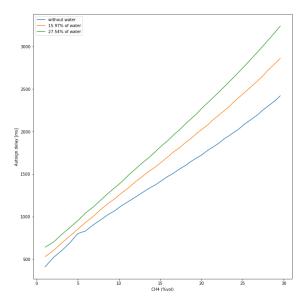


Figure 4: Autoiginition delay times acquired in Cantera

3.2 Results from the second loop

Maximal explosion pressures are getting lower the higher the temperature. Without water the drop between 850 and 2100 degrees is 75%, with 15% of water 76.6% and 77.4%. Maximal temperature is increasing with the increase of initial temperature. Relative maximal temperature for initial 850K is 1880 K and drops on average by 75.3K every 100K more for the initial temperature. The drop is 70.7/100 for 15.97% of water and 65.1/100 for 27.64% of water in the mixture (vol.). Results are shown on Figures 5 and 6.

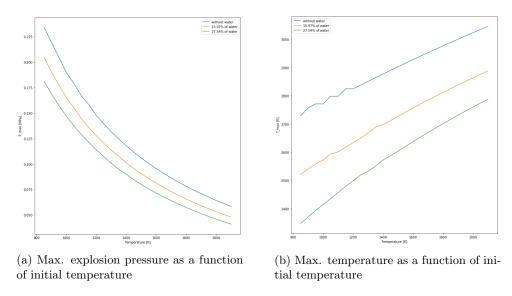


Figure 5: Results from the second loop

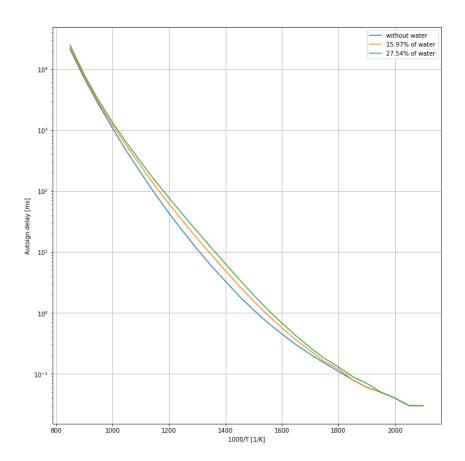


Figure 6: Autoiginition delay times acquired in Cantera

Additional computations were performed for no water nad 8% of water in the mixture (vol.) at the pressure of 10 atm to compare it to results reported by Goy et al.[1], they are shown together with Cantera results on Figure 7

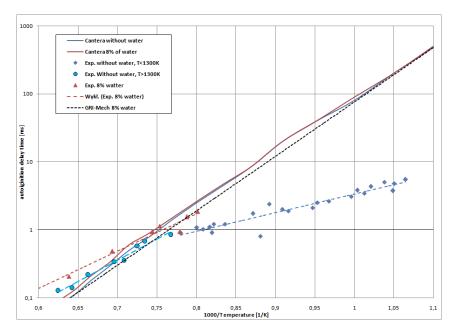


Figure 7: Comarison of results from Cantera and [1]

Data from Cantera simulation is fairly consistent (relative error of 4.84% for 900K, 37% for 1300K and 27% for 1500K) with the data calculated using also GRI 3.0 mechanism from Goy paper, but diverges greatly from experimental data for temperatures below 1300K (small relative error of 34.5% for 1500K, 27.86% for 1300K and a massive error of 8581.3% for 900K). Slopes for exponential trend lines for experimental data for temperatures below and above 1300K are different. This is because Version 3.0 of the GRI kinetic mechanism is validated only for temperatures above 1350 K.[1]. Goy et al. states, that this may be due to change in activation energy at low temperature.

3.3 Results from the third loop

Maximal explosion pressure is changing linearly with initial pressure. The increase of 1MPa of initial pressure corresponds to increase of 1.886, 1.507 and 1.337 for no water, 15.67% and 27.54% of CH_4 fraction in the mixture (vol.) respectively (see Figure 8a). Maximal temperature for initial pressure of 0.5 atm is 7.33% lower for 15.67% of water in the mixture and 13.37% for 27.64% if water in the mixture (vol.) than when there was no water added. For initial pressure of 25.5 atm maximal temperature is 9.71% lower for 15.67% of water in the mixture and 17.18% for 27.64% of water in the mixture (vol.) than hen there was no water added (see Figure 8b).

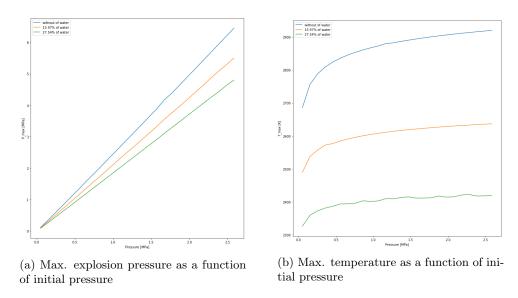


Figure 8: Results from the third loop

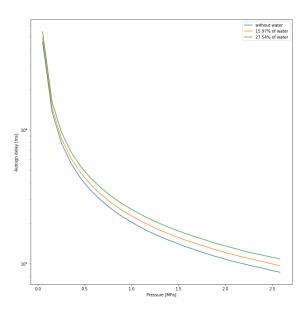


Figure 9: Autoiginition delay times acquired in Cantera

3.4 Maximal rate of pressure rise

The maximal rate of pressure rise $(dP/dt)_{\ell}(max)$ was calculated, but results were too far away from experimental data and varied greatly with the change time step, as seen on Figure 11. Because of that they were not analysed in this report.

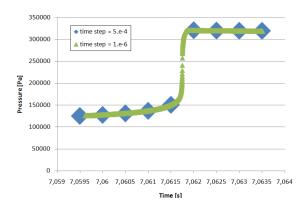


Figure 10: Pressure as a function of time

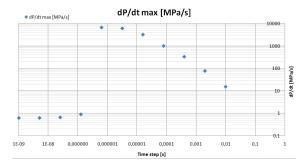


Figure 11: Maximal rate of pressure rise as a function of simulation time step

3.5 Conclusions

In each case addition of water vapour lowers maximal explosion pressure and maximal temperature, and also makes the autoignition delay time longer.

References

- [1] C. J. Goy, A. J. Moran, and G. O. Thomas. Autoignition characteristics of gaseous fuels at representative gas turbine conditions. (78514):V002T02A018, 2001.
- [2] Xiaobo Shen, Bo Zhang, Xiaoliang Zhang, and Sizhe Wu. Explosion behaviors of mixtures of methane and air with saturated water vapor. *Fuel*, 177:15–18, 2016.