

### Question 6 [1 Marks]

Consider the following function

```
int unknown(int n) {  
  
    int i, j, k = 0;  
  
    for (i = n/2; i <= n; i++)  
  
        for (j = 2; j <= n; j = j * 2)  
  
            k = k + n/2;  
  
    return k;  
  
}
```

What is the returned value of the above function? (GATE CS 2013)

- (A)  $\Theta(n^2)$
- (B)  $\Theta(n^2 \log n)$
- (C)  $\Theta(n^3)$
- (D)  $\Theta(n^3 \log n)$

A

A

☒

B

C

C

D

D

### Explanation

In the below explanation, '^' is used to represent exponent:

The outer loop runs  $n/2$  or  $\Theta(n)$  times.

The inner loop runs  $(\log n)$  times (Note that  $j$  is multiplied by 2 in every iteration).

So the statement " $k = k + n/2;$ " runs  $\Theta(n \log n)$  times.

The statement increases value of  $k$  by  $n/2$ .

So the value of  $k$  becomes  $n/2 * \Theta(n \log n)$  which is  $\Theta((n^2) * \log n)$ .