Manipulating Tabular Data

Lesson 5 with Benoit Parmentier

Lesson Objectives

- · Review what makes a dataset tidy.
- · Meet a complete set of functions for most table manipulations.
- Learn to transform datasets with split-apply-combine procedures.
- Understand the basic join operation.

Specific Achievements

- · Reshape data frames with pandas
- · Summarize data by groups with pandas
- Combine multiple data frame operations with method chaining (piping with pandas ".")
- Combine multiple data frames with "joins" (merge)

Data frames occupy a central place in Python data analysis pipelines. The pandas package provides the objects and most necessary tools to subset, reformat and transform data frames. The key functions in the package have close counterparts in SQL (Structured Query Language), which provides the added bonus of facilitating translation between python and relational databases.

Tidy Concept

Most time is spent on cleaning and wrangling data rather than analysis. In 2014, Hadley Wickam (R developer at RStudio) published a paper that defines the concepts underlying tidy datasets. Hadley Wickam defined tidy datasets as those where:

- each variable forms a column (also called field)
- · each observation forms a row
- · each type of observational unit forms a table

These guidelines may be familiar to some of you—they closely map to best practices for "normalization" in database design. It correspond to the 3rd normal form's described by Codd 1990 but uses the language of statical analysis rather than relationtional database.

Consider a data set where the outcome of an experiment has been recorded in a perfectly appropriate way:

bloc	drug	control	placebo
1	0.22	0.58	0.31
2	0.12	0.98	0.47
3	0.42	0.19	0.40

The response data are present in a compact matrix, as you might record it on a spreadsheet. The form does not match how we think about a statistical model, such as:

$$response \sim block + treatment$$

In a tidy format, each row is a complete observation: it includes the response value and all the predictor values. In this data, some of those predictor values are column headers, so the table needs to be reshaped. The pandas package provides functions to help re-organize tables.

The third principle of tidy data, one table per category of observed entities, becomes especially important in synthesis research. Following this principle requires holding tidy data in multiple tables, with associations between them formalized in metadata, as in a relational database.

Datasets split across multiple tables are unavoidable in synthesis research, and commonly used in the following two ways (often in combination):

- two tables are "un-tidied" by joins, or merging them into one table
- statistical models conform to the data model through a hierarchical structure or employing "random effects"

The pandas package includes several functions that all perform variations on table joins needed to "un-tidy" your tables, but there are only two basic types of table relationships to recognize:

- One-to-one relationships allow tables to be combined based on the same unique identifier (or "primary key") in both tables.
- Many-to-one relationships require non-unique "foreign keys" in the first table to match the primary key of the second.

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Wide to Long

The pandas package's melt function reshapes "wide" data frames into "long" ones.

```
worksheet-5.ipynb
import pandas as pd
import numpy as np
trial_df = pd.DataFrame({"block": [1,2,3],
              "drug": [0.22,0.12,0.42],
              "control": [0.58,0.98,0.19],
              "placebo": [0.31,0.47,0.40]})
trial_df.head()
   block control drug placebo
0
      1
            0.58 0.22
                           0.31
                           0.47
1
      2
            0.98 0.12
            0.19 0.42
2
                           0.40
       3
                                                                                                  worksheet-5.ipynb
tidy_trial_df = pd.melt(trial_df,
                  id_vars=['block'],
                  var_name='treatment',
                  value_name='response')
tidy_trial_df.head()
   block treatment response
0
      1 control
                      0.58
1
      2
          control
                       0.98
2
                       0.19
      3 control
3
      1
             drug
                       0.22
4
      2
             drug
                       0.12
```

All columns, accept for "block", are stacked in two columns: a "key" and a "value". The key column gets the name treatment and the value column receives the name response. For each row in the result, the key is taken from the name of the column and the value from the data in the column.

Long to Wide

Data can also fail to be tidy when a table is too long. The Entity-Attribute-Value (EAV) structure common in large databases distributes multiple attributes of a single entity/observation into separate rows.

Remember that the exact state of "tidy" may depend on the analysis: the key is knowing what counts as a complete observation. For example, the community ecology package vegan requires a matrix of species counts, where rows correspond to species and columns to sites. This may seem like too "wide" a format, but in the packages several multi-variate analyses, the abundance of a species across multiple sites is considered a complete observation.

Consider survey data on participant's age and income stored in a EAV structure.

```
df2 = df2.reset_index()
df2.columns
Index(['block', 'control', 'drug', 'placebo'], dtype='object', name='treatment')
worksheet-5.ipynb
                                                                                                df2.reset_index()
treatment index block control drug placebo
0
              0
                   1
                           0.58 0.22
                                          0.31
1
                           0.98 0.12
                                          0.47
              1
                     2
2
                    3 0.19 0.42
              2
                                          0.40
                                                                                                worksheet-5.ipynb
df2
treatment block control drug placebo
              1
                   0.58 0.22
                                  0.31
1
              2
                    0.98 0.12
                                   0.47
2
              3
                    0.19 0.42
                                   0.40
Consider survey data on participant's age and income stored in a EAV structure.
                                                                                                worksheet-5.ipynb
from io import StringIO, BytesIO
```

```
text_string = StringIO("""
participant, attr, val
1, age, 24
2,age,57
3,age,13
1, income, 30
2, income, 60
""")
survey_df = pd.read_csv(text_string, sep=",")
survey_df
   participant
                   attr val
0
             1
                          24
                    age
1
             2
                    age
                          57
2
             3
                          13
                    age
3
             1 income
                          30
4
             2 income
                          60
```

Transform the data with the pivot function, which "reverses" a melt. These are equivalent to spread and gather in the dplyr r package.

```
worksheet-5.ipynb
tidy_survey = survey_df.pivot(index='participant',
                          columns='attr',
                          values='val')
print(tidy_survey.head())
attr
             age income
participant
1
            24.0
                     30.0
2
             57.0
                     60.0
3
            13.0
                     NaN
```

```
worksheet-5.ipynb
tidy_survey = tidy_survey.reset_index()
tidy_survey.columns
Index(['participant', 'age', 'income'], dtype='object', name='attr')
                                                                                                worksheet-5.ipynb
tidy_survey.reset_index()
attr index participant
                              income
                          age
0
         0
                      1 24.0
                                 30.0
1
         1
                      2 57.0
                                 60.0
2
         2
                      3 13.0
                                  NaN
                                                                                                worksheet-5.ipynb
tidy_survey
attr participant
                   age
                        income
0
                  24.0
                          30.0
               1
1
                  57.0
                          60.0
2
               3 13.0
                           NaN
```

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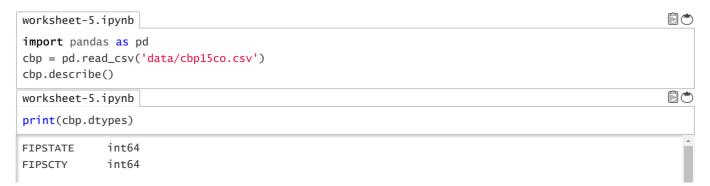
Sample Data



Credit: US Census Bureau

To learn about data transformation with pandas, we need more data. The Census Bureau collects subnational economic data for the U.S., releasing annual County Business Patterns (CBP) datasets including the number of establishments, employment, and payroll by industry. They also conduct the American Community Survey (ACS) and publish, among other demographic and economic variables, estimates of median income for individuals working in different industries.

- County Business Patterns (CBP)
- American Community Survey (ACS)



```
NAICS
            object
            object
EMPFLAG
EMP_NF
            object
             int64
EMP
            object
QP1_NF
             int64
QP1
AP_NF
            object
ΑP
              int64
              int64
EST
              int64
```

See the CBP dataset documentation for an explanation of the variables we don't discuss in this lesson.

Modify the import to clean up this read: consider the data type for FIPS codes along with what string in this CSV file represents NAs, a.k.a. data that is not-available or missing.

```
import numpy as np
import pandas as pd

cbp = pd.read_csv(
   'data/cbp15co.csv',
   na_values = "NULL",
   keep_default_na=False,
   dtype = {"FIPSTATE": np.str,
   "FIPSCTY": np.str}
   )
```

Question

What changed?

Answer

Using dtypes() shows that the character string "" in the CSV file is no longer read into R as missing data (an NA) but as an empty string. The two named "FIPS" columns are now correctly read as strings.

```
worksheet-5.ipynb
import pandas as pd
import numpy as np
acs = pd.read_csv(
   'data/ACS/sector_ACS_15_5YR_S2413.csv',
   dtype = {"FIPS": np.str}
   )
```

Now let's display the data types

```
worksheet-5.ipynb

#acs.dtypes
print(acs.dtypes)

FIPS object
County object
Sector object
median_income float64
dtype: object
```

The two datasets both contain economic variables for each U.S. county and specified by different categories of industry. The data could potentially be manipulated into a single table reflecting the follow statistical model.

Key Functions

Function	Returns
query	keep rows that satisfy conditions
assign	apply a transformation to existing [split] columns
['col1', 'col2']	select and keep columns with matching names
merge	merge columns from separate tables into one table
groupby	split data into groups by an existing factor
agg	summarize across rows to use after groupby [and combine split groups]

The table above summarizes the most commonly used functions in pandas, which we will demonstrate in turn on data from the U.S. Census Bureau.

Filter and pattern matching

The cbp table includes character NAICS column. Of the 2 million observations, lets see how many observations are left when we keep only the 2-digit NAICS codes, representing high-level sectors of the economy.

```
worksheet-5.ipynb
                                                                                       #import pandas as pd
cbp2 = cbp[cbp['NAICS'].str.contains("----")]
cbp2 = cbp2[~cbp2.NAICS.str.contains("----")]
cbp2.head()
  FIPSTATE FIPSCTY NAICS EMPFLAG ... N1000_3 N1000_4 CENSTATE CENCTY
       01 001 11---- ...
                                                 0
1
                                        0
                                                        63
                                                                1
10
       01
            001 21----
                                         0
                                                 0
                                                        63
                                                                1
17
       01
             001 22----
                                         0
                                         0
                                                 0
                                                        63
                                                                1
                                . . .
             001 23----
                                                 0
27
       01
                                                        63
                                                                1
                                . . .
93
       01
             001 31----
                                                        63
                                                                1
[5 rows x 26 columns]
```

Note that a logical we used the function contains from pandas to filter the dataset in two steps. The function contains allows for pattern matching of any character within strings. The \sim is used to remove the rows that contains specific patterns.

Filtering string often uses pattern matching by regular expressions which may be a bit more manageable, and streamlines the operations.

```
worksheet-5.ipynb
                                                                                      cbp3 = cbp[cbp['NAICS'].str.contains('[0-9]{2}----')]
cbp3.head()
  FIPSTATE FIPSCTY NAICS EMPFLAG ... N1000_3 N1000_4 CENSTATE CENCTY
1
       01
             001 11----
                                ... 0
                                                 0
                                                        63
                                                                1
       01
             001 21----
                                                 0
                                                        63
10
                                         0
                                                                1
                                . . .
             001 22----
                                               0
17
       01
                                        0
                                                        63
                                                                1
                                . . .
27
             001 23----
       01
                                        0
                                                 0
                                                        63
                                                                1
93
       01
           001 31----
                                                        63
[5 rows x 26 columns]
```

Altering, updating and transforming columns

The assign function is the pandas answer to updating or altering your columns. It performs arbitrary operations on existing columns and appends the result as a new column of the same length.

Here are two ways to create a new column using assign and the [] operators.

```
worksheet-5.ipynb
cbp3["FIPS"] = cbp3["FIPSTATE"]+cbp3["FIPSCTY"]
/usr/bin/python3:1: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead
See the caveats in the documentation: http://pandas.pydata.org/pandas-docs/stable/indexing.html#indexir
                                                                                                   worksheet-5.ipynb
cbp3.assign(FIPS2=lambda x: x['FIPSTATE']+x['FIPSCTY'])
                                         ... CENSTATE
        FIPSTATE FIPSCTY
                          NAICS EMPFLAG
                                                        CENCTY
                                                                 FIPS FIPS2
1
              01
                     001 11----
                                                    63
                                                             1
                                                                01001
                                                                       01001
                                          . . .
                     001 21----
10
              01
                                                                01001 01001
                                                    63
                                                             1
17
              01
                     001 22----
                                                                01001
                                                    63
                                                             1
                                                                       01001
                                          . . .
27
              01
                     001 23----
                                                    63
                                                             1
                                                                01001
                                                                       01001
                                          . . .
93
                     001 31----
                                                             1 01001 01001
              01
                                                    63
163
              01
                     001 42----
                                                             1
                                                                01001 01001
                                                    63
                                          . . .
                     001 44----
218
              01
                                                    63
                                                             1
                                                                01001 01001
351
              01
                     001 48----
                                                    63
                                                             1 01001 01001
381
              01
                     001 51----
                                                    63
                                                             1 01001 01001
                                          . . .
401
              01
                     001 52----
                                                             1 01001 01001
                                                    63
429
              01
                     001 53----
                                                    63
                                                             1
                                                                01001 01001
                                          . . .
465
              01
                     001 54----
                                                    63
                                                             1 01001 01001
                                          . . .
worksheet-5.ipynb
                                                                                                   cbp3.shape
(58901, 27)
                                                                                                   worksheet-5.ipynb
cbp3.head()
   FIPSTATE FIPSCTY
                      NAICS EMPFLAG ... N1000_4
                                                  CENSTATE CENCTY
                                                                    FIPS
         01
                                                                1 01001
1
                001 11----
                                               0
                                                        63
10
         01
                001 21----
                                               0
                                                        63
                                                                1 01001
                                     . . .
17
         01
                001 22----
                                               0
                                                        63
                                                                1 01001
                                     . . .
27
                001 23----
                                                                1 01001
         01
                                               0
                                                        63
                001 31----
                                                                1 01001
93
         01
                                                        63
                                     . . .
[5 rows x 27 columns]
```

Select

To keep particular columns of a data frame (rather than filtering rows), use the filter or [] functions with arguments that match column names

One way to "match" is by including complete names, each one you want to keep:

```
cbp3 = cbp3[['FIPS','NAICS','N1_4', 'N5_9', 'N10_19']]
cbp3.head()
     FIPS
           NAICS N1_4 N5_9 N10_19
    01001 11----
                     5
                           1
                                   0
1
10 01001 21----
                     0
                           1
                                   1
17 01001 22----
                   2
                          1
                                   2
   01001 23----
                    51
                          13
                                   7
93 01001 31----
                     9
                           4
                                   4
```

Alternatively, we can use the filter function to select all columns starting with N or matching with 'FIPS' or 'NAICS' pattern. The filter command is useful when chaining methods (or piping operations).

```
worksheet-5.ipynb
cbp4= cbp.filter(regex='^N|FIPS|NAICS',axis=1)
cbp4.head()
                    NAICS N1_4 ...
 FIPSTATE FIPSCTY
                                      N1000_1 N1000_2
                                                        N1000_3
                                                                 N1000_4
0
       01
              001 -----
                            430
                                 . . .
                                            0
                                                     0
                                                              0
                                                                       0
       01
                              5 ...
                                            0
                                                     0
                                                              0
                                                                       0
1
              001 11----
2
       01
              001 113///
                              4 ...
                                            0
                                                     0
                                                              0
                                                                       0
3
                                                     0
       01
              001 1133//
                              4 ...
                                            0
                                                              0
                                                                       0
       01
                                            0
                                                     0
                                                              0
                                                                       0
4
              001 11331/
                              4 ...
[5 rows x 16 columns]
```

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Join

The CBP dataset uses FIPS to identify U.S. counties and NAICS codes to identify types of industry. The ACS dataset also uses FIPS but their data may aggregate across multiple NAICS codes representing a single industry sector.

```
worksheet-5.ipynb
sector = pd.read_csv(
  'data/ACS/sector_naics.csv',
  dtype = {"NAICS": np.int64})
print(sector.dtypes)
Sector
          object
           int64
NAICS
dtype: object
                                                                                                    worksheet-5.ipynb
print(cbp.dtypes)
FIPSTATE
            object
            object
FIPSCTY
NAICS
            object
EMPFLAG
            object
EMP_NF
            object
EMP
            int64
            object
QP1_NF
             int64
QP1
AP_NF
            object
             int64
AΡ
EST
             int64
             int64
N1_4
```

```
worksheet-5.ipynb
cbp.head()
  FIPSTATE FIPSCTY
                   NAICS EMPFLAG ... N1000_3 N1000_4 CENSTATE CENCTY
0
       01
              001 -----
                                           0
                                                     0
                                                             63
                                                                      1
        01
              001 11----
                                                     0
1
                                             0
                                                             63
                                                                      1
                                   . . .
2
        01
              001 113///
                                   . . .
                                             0
                                                     0
                                                             63
                                                                      1
3
        01
              001 1133//
                                             0
                                                     0
                                                             63
                                                                      1
        01
              001 11331/
                                                             63
                                                                      1
                                   . . .
[5 rows x 26 columns]
                                                                                                worksheet-5.ipynb
cbp.dtypes
FIPSTATE
           object
FIPSCTY
           object
           object
NAICS
EMPFLAG
           object
EMP_NF
           object
EMP
            int64
QP1_NF
           object
            int64
QP1
AP_NF
           object
AP
            int64
            int64
EST
N1 4
            int64
N5_9
            int64
                                                                                                worksheet-5.ipynb
cbp.head()
 FIPSTATE FIPSCTY NAICS EMPFLAG ... N1000_3 N1000_4 CENSTATE CENCTY
       01
              001 -----
                                                    0
                                                             63
0
                                           0
                                                                      1
        01
              001 11----
                                             0
                                                     0
                                                             63
                                                                      1
1
2
        01
              001 113///
                                             0
                                                      0
                                                             63
                                                                      1
                                   . . .
3
        01
              001 1133//
                                             0
                                                     0
                                                             63
                                                                      1
                                   . . .
       01
              001 11331/
                                                             63
                                                                      1
[5 rows x 26 columns]
                                                                                                worksheet-5.ipynb
print(sector.dtypes)
Sector
         object
NAICS
          int64
dtype: object
worksheet-5.ipynb
                                                                                                print(sector.shape) #24 economic sectors
(24, 2)
                                                                                                worksheet-5.ipynb
sector.head()
                                       Sector NAICS
0
      agriculture forestry fishing and hunting
                                                  11
1 mining quarrying and oil and gas extraction
                                                  21
```

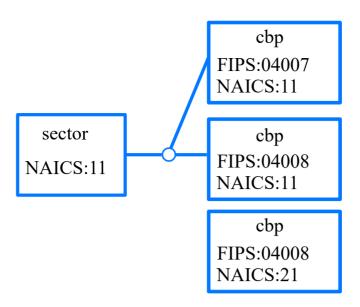
```
2 utilities 22
3 construction 23
4 manufacturing 31
```

Probably the primary challenge in combining secondary datasets for synthesis research is dealing with their different sampling frames. A very common issue is that data are collected at different "scales", with one dataset being at higher spatial or temporal resolution than another. The differences between the CBP and ACS categories of industry present a similar problem, and require the same solution of reaggregating data at the "lower resolution".

Many-to-One

Before performing the join operation, some preprocessing is necessary to extract from the NAICS columns the first two digits matching the sector identifiers.

```
worksheet-5.ipynb
logical_idx = cbp['NAICS'].str.match('[0-9]{2}----') #boolean index
cbp = cbp.loc[logical_idx]
cbp.head()
   FIPSTATE FIPSCTY
                     NAICS EMPFLAG ... N1000_3
                                                  N1000_4 CENSTATE
                                                        0
1
        01
                001 11----
                                               0
                                                                63
                                                                         1
                                                        0
10
        01
                001 21----
                                               0
                                                                63
                                                                         1
                                                        0
                                                                         1
17
        01
                001 22----
                                               0
                                                                63
                                     . . .
27
        01
                001 23----
                                               0
                                                        0
                                                                63
                                                                         1
93
        01
                001 31----
                                                                63
                                                                         1
[5 rows x 26 columns]
                                                                                                   worksheet-5.ipynb
cbp.shape
(58901, 26)
                                                                                                   worksheet-5.ipynb
cbp['NAICS'] = cbp.NAICS.apply(lambda x: np.int64(x[0:2])) # select first two digits
                                                                                                   worksheet-5.ipynb
#Many to one to join economic sector code to NAICS
cbp_test = cbp.merge(sector, on = "NAICS", how='inner')
cbp_test.head()
  FIPSTATE FIPSCTY
                        CENCTY
                                                                   Sector
0
        01
               001
                              1 agriculture forestry fishing and hunting
1
        01
               003
                                 agriculture forestry fishing and hunting
                    . . .
2
        01
               005
                              5 agriculture forestry fishing and hunting
3
        01
               007
                              7 agriculture forestry fishing and hunting
4
        01
               009
                              9 agriculture forestry fishing and hunting
[5 rows x 27 columns]
                                                                                                   worksheet-5.ipynb
print(cbp_test.shape)
(56704, 27)
```



The NAICS field in the cbp table can have the same value multiple times, it is not a primary key in this table. In the sector table, the NAICS field is the primary key uniquely identifying each record. The type of relationship between these tables is therefore "many-to-one".

Question

Note that we lost a couple thousand rows through this join. How could cop have fewer rows after a join on NAICS codes?

Answer

The CBP data contains an NAICS code not mapped to a sector—the "error code" 99 is not present in sector. The use of "error codes" that could easily be mistaken for data is frowned upon.

Group By

A very common data manipulation procedure know as "split-apply-combine" tackles the problem of applying the same transformation to subsets of data while keeping the result all together. We need the total number of establishments in each size class *aggregated within* each county and industry sector.

The pandas function groupby begins the process by indicating how the data frame should be split into subsets.

```
worksheet-5.ipynb

cbp["FIPS"] = cbp["FIPSTATE"]+cbp["FIPSCTY"]
cbp = cbp.merge(sector, on = "NAICS")

cbp_grouped = cbp.groupby(['FIPS','Sector'])
cbp_grouped

<pandas.core.groupby.generic.DataFrameGroupBy object at 0x7f5974d485f8>
```

At this point, nothing has really changed:

```
worksheet-5.ipynb
cbp_grouped.dtypes
                                                       FIPSTATE ... CENCTY
FIPS Sector
01001 accommodation and food services
                                                                 ... int64
                                                         object
     administrative and support and waste management...
                                                         object ... int64
     agriculture forestry fishing and hunting
                                                         object ... int64
     arts entertainment and recreation
                                                         object ... int64
     construction
                                                         object ... int64
     educational services
                                                         object ... int64
     finance and insurance
                                                         object ... int64
                                                         object ... int64
     health care and social assistance
```

```
information object ... int64
management of companies and enterprises object ... int64
```

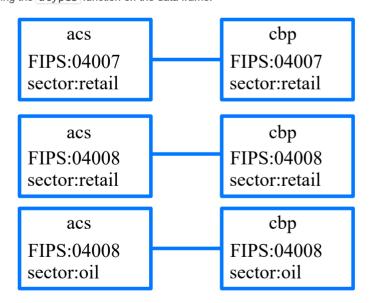
The groupby statement generates a groupby data frame. You can add multiple variables (separated by commas) in groupby; each distinct combination of values across these columns defines a different group.

Summarize

The operation to perform on each group is summing: we need to sum the number of establishments in each group. Using pandas functions, the summaries are automically combined into a data frame.

```
worksheet-5.ipynb
grouped_df = (cbp)
.groupby(['FIPS', 'Sector'])
.agg('sum')
.filter(regex='^N')
.drop(columns=['NAICS'])
)
grouped_df.head(5)
                                                          N1_4 ... N1000_4
FIPS Sector
01001 accommodation and food services
                                                            23
                                                                           0
                                                                . . .
                                                                           0
     administrative and support and waste management...
                                                            18 ...
     agriculture forestry fishing and hunting
                                                            5 ...
                                                                           0
     arts entertainment and recreation
                                                            5
                                                                           0
                                                            51 ...
     construction
                                                                           0
[5 rows x 13 columns]
```

The "combine" part of "split-apply-combine" occurs automatically, when the attributes introduced by groupby are dropped. You can see attributes by running the dtypes function on the data frame.



There is now a one-to-one relationship between cbp and acs, based on the combination of FIPS and Sector as the primary key for both tables.

```
worksheet-5.ipynb
print(grouped_df.shape)

(56704, 13)
```

```
worksheet-5.ipynb
print(acs.shape)

(59698, 4)

worksheet-5.ipynb
acs_cbp = grouped_df.merge(acs,on='FIPS',)
print(acs_cbp.shape)

(1061416, 17)
```

Again, however, the one-to-one relationship does not mean all rows are preserved by the join. The specific nature of the inner_join is to keep all rows, even duplicating rows if the relationship is many-to-one, where there are matching values in both tables, and discarding the rest.

The acs_cbp table now includes the median_income variable from the ACS and appropriatey aggregated establishment size information (the number of establishments by employee bins) from the CBP table.

WC	rksheet	-5.ipy	'nb					
acs_cbp.head()								
	FIPS	N1_4		Sector	median_income			
0	01001	23		agriculture forestry fishing and hunting	27235.0			
1	01001	23		mining quarrying and oil and gas extraction	102722.0			
2	01001	23		construction	31632.0			
3	01001	23		manufacturing	40233.0			
4	01001	23		wholesale trade	41656.0			
[5	[5 rows x 17 columns]							

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Additional Resources

The following cheat sheets and tutorials repeat much of this lesson, but also provide information on additional functions for "data wrangling".

- Data Wrangling Cheat Sheet
- Tidyverse In Pandas
- String and Text With Pandas

The first is a set of cheat sheets created by pydata.org, and provides a handy, visual summary of all the key functions discussed in this lesson. It also lists some of the auxiliary functions that can be used within each type of expression, e.g. aggregation functions for summarize, "moving window" functions for mutate, etc. For those familiar with the tidyverse univers, please consult the second link.

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If you need to catch-up before a section of code will work, just squish it's $\stackrel{\bigstar}{}$ to copy code above it into your clipboard. Then paste into your interpreter's console, run, and you'll be ready to start in on that section. Code copied by both $\stackrel{\bigstar}{}$ and $\stackrel{\textcircled{}}{}$ will also appear below, where you can edit first, and then copy, paste, and run again.

```
# Nothing here yet!
```