

## Functional Dependency

1. Consider a relation scheme  $R = (A, B, C, D, E, H)$  on which the following functional dependencies hold:  $\{A \rightarrow B, BC \rightarrow D, E \rightarrow C, D \rightarrow A\}$ . What are the candidate keys of  $R$ ?

Closure of  $AEH$ , i.e.  $AEH^+ = \{ABCDEH\}$

Closure of  $BEH$ , i.e.  $BEH^+ = \{ABCDEH\}$

Closure of  $DEH$ , i.e.  $DEH^+ = \{ABCDEH\}$

Candidate keys of  $R$  ( $AEH, BEH, DEH$ )

2. Consider schema  $R = (A, B, C, G, H, I)$  and the set  $F$  of functional dependencies  $\{A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H\}$ . Prove that  $AG \rightarrow I$  Holds.

$R = (A, B, C, G, H, I)$

$F = \{A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H\}$

- some members of  $F^+ - A \rightarrow H$
- by transitivity from  $A \rightarrow B$  and  $B \rightarrow H - AG \rightarrow I$
- by augmenting  $A \rightarrow C$  with  $G$ , to get  $AG \rightarrow CG$  and then transitivity with  $CG \rightarrow I$

3. Consider the relation scheme  $R = \{E, F, G, H, I, J, K, L, M, N\}$  and the set of functional dependencies  $\{E, F \rightarrow G, F \rightarrow I, J, E, H \rightarrow K, L, K \rightarrow M, L \rightarrow N\}$  on  $R$ . What is the key for  $R$ ?

$\{E, F, H\}^+ = \{E, F, H, G, I, J, K, L, M, N\}$

$\therefore$  it is a key

Key for  $R$  is  $\{E, F, H\}$ .

4. Compute the closure of the following set  $F$  of functional dependencies for relation schema  $R = (A, B, C, D, E)$ .  $A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A$ . List the candidate keys for  $R$ .

$A \rightarrow BC, B \rightarrow D$  so  $A \rightarrow D$  so  $A \rightarrow DC \rightarrow E$   
therefore  $A \rightarrow ABCDE$

$E \rightarrow A, A \rightarrow ABCDE$ , so  $E \rightarrow ABCDE$   
 $CD \rightarrow E$ , so  $CD \rightarrow ABCDE$   
 $B \rightarrow D, BC \rightarrow CD$ , so  $BC \rightarrow ABCDE$

Attribute closure:

$A \rightarrow ABCDE$   
 $B \rightarrow BD$   
 $C \rightarrow C$   
 $D \rightarrow D$   
 $E \rightarrow ABCDE$   
 $AB \rightarrow ABCDE$   
 $AC \rightarrow ABCDE$   
 $AD \rightarrow ABCDE$   
 $AE \rightarrow ABCDE$   
 $BC \rightarrow ABCDE$   
 $BD \rightarrow BD$   
 $BE \rightarrow ABCDE$

CD -> ABCDE  
CE -> ABCDE  
DE -> ABCDE  
ABC -> ABCDE  
ABD -> ABCDE  
ABE -> ABCDE  
ACD -> ABCDE  
ACE -> ABCDE  
ADE -> ABCDE  
BCD -> ABCDE  
BDE -> ABCDE  
CDE -> ABCDE  
ABCD -> ABCDE  
ABCE -> ABCDE  
ABDE -> ABCDE  
ACDE -> ABCDE  
BCDE -> ABCDE

The candidate keys are A, E, CD, and BC

5. Write a PL/SQL program that fetches records of all students and insert record as students having CPI > 4 in ELIGIBLE table and students having CPI <= 4 in NOT\_ELIGIBLE table from student\_master table.