

# Sardar Vallabhbhai Patel Institute of Technology, Vasad

## Digital Fundamentals

### Assignment 3

#### Simplification of Boolean Expression

1. Implement the Boolean functions. (a)  $xyz + x'y + xyz'$  (b)  $(A+B)'(A'+B)'$  and

$$F = xy + xy' + y'z \text{ with logic gates.}$$

2. Obtain the simplified expression in sum of product for the following Boolean functions.

(a)  $F = \Sigma(0,1,4,5,10,11,12,14)$  and (b)  $F = \Sigma(11,12,13,14,15)$ .

3. Implement the functions  $F = \Sigma(1,3,7,11,15)$  with don't care conditions  $d = \Sigma(0,2,5)$  Discuss the effect of don't care conditions

4. Find the complement of the following Boolean function and reduce to a minimum number of literals.

$$B'D + A'BC' + ACD + A'BC$$

5. Obtain the simplified expressions in sum of products using K-map:

$$x'z + w'xy' + w(x'y + xy')$$

6. Given Boolean function

$$F = x y + x' y' + y' z$$

1. Implement it with only OR & NOT gates

2. Implement it with only AND & NOT gates

7. Determine the Prime Implicants of following Boolean Function using Tabulation Method.

$$F(A,B,C,D,E,F,G) = \Sigma(20,28,38,39,52,60,102,103,127)$$

8. Simplify the following Boolean function using K-Map.

$$F = A'B'C' + B'CD' + A'BCD' + AB'C'$$

9. Simplify the following Boolean function by using K-Map.

$$F = \Sigma(0,1,2,8,10,11,14,15)$$

10. Simplify Boolean function  $F(w,x,y,z) = \Sigma(0,1,2,4,5,6,8,9,12,13,14)$  using K-map and Implement it using (i) NAND gates only (ii) NOR gates only.

11. Simplify the following Boolean function using K-Map and draw logic diagram using NOR gates only.  $F(w,x,y,z) = \Sigma(0,1,2,8,10,11,14,15)$

12. Simplify the Boolean function:

$$(1) F(w,x,y,z) = \Sigma(0,1,2,4,5,6,8,9,12,13,14)$$

$$(2) F(w,x,y) = \Sigma(0,1,3,4,5,7)$$

13. Explain with figures how NAND gate and NOR gate can be used as Universal gate.

14. Simplify the Boolean function:

$$(1) F = A'B'C' + B'CD' + A'BCD' + AB'C'$$

$$(2) F = A'B'D' + A'CD + A'BC$$

$d = A'BC'D + ACD + AB'D'$  Where "d" indicates Don't care conditions.

15. Obtain the simplified expressions in sum of products for the following Boolean functions:

(i)  $F(A,B,C,D,E) = \sum(0,1,4,5,16,17,21,25,29)$

(ii)  $A'B'CE' + A'B'C'D' + B'D'E' + B'CD$

16. The Boolean expression  $BE + B'DE'$  is a simplified version of expression  $A'BE + BCDE + BC'D'E + A'B'DE' + B'C'DE'$ . Are there any don't care condition? If so what are they?

17. Simplify the Boolean functions using K-map

$$F(A,B,C,D,E,F) = \sum(6,9,13,18,19,25,27,29,41,45,57,61).$$

$$F(A,B,C,D,E,F,G) = \sum(20,28,52,60)$$

18. Implement the following Boolean functions using Don't care conditions.

a)  $F(A,B,C,D) = \sum(0,1,2,9,11)$   $d(A,B,C,D) = \sum(8,10,14,15)$

b)  $F = B'D + B'C + ABCD$   $d = A'BD + AB'C'D'$