

⑤

$$f(x) = \begin{cases} 0, & x \leq -a \\ b(x+a)/a, & -a \leq x \leq 0 \\ be^{-\lambda x}, & x \geq 0 \end{cases}$$

$$F(x) = \begin{cases} \int_{-\infty}^x 0 \cdot dx, & x \leq -a \\ \int_{-a}^x b(x+a)/a \cdot dx, & -a \leq x \leq 0 \\ \frac{ab}{2} + \int_0^x be^{-\lambda x} dx, & x \geq 0 \end{cases}$$

$$F(x) = \begin{cases} 0, & x \leq -a \\ \frac{b(x+a)^2}{2a}, & -a \leq x \leq 0 \\ \frac{ab}{2} + \frac{b(1-e^{-\lambda x})}{\lambda}, & x \geq 0 \end{cases}$$

$$F(x) = R$$

$$x \leq -a: 0 = R$$

$$-a \leq x \leq 0: \frac{b(x+a)^2}{2a} = R$$

$$\Rightarrow (x+a)^2 = \frac{2aR}{b}$$

$$\Rightarrow (x+a) = \sqrt{\frac{2aR}{b}}$$

$$\Rightarrow x = -a + \sqrt{\frac{2aR}{b}}$$

$$x \geq 0: \quad \frac{ab}{2} + \frac{b(1-e^{-\lambda x})}{\lambda} = R$$

$$\Rightarrow 1 - e^{-\lambda x} = \left(R - \frac{ab}{2}\right) \times \frac{\lambda}{b}$$

$$\Rightarrow e^{-\lambda x} = 1 - \left(\left(R - \frac{ab}{2}\right) \times \frac{\lambda}{b}\right)$$

$$\Rightarrow -\lambda x = \ln\left(1 - \left(R - \frac{ab}{2}\right) \times \frac{\lambda}{b}\right)$$

$$\Rightarrow x = -\frac{1}{\lambda} \ln\left(1 - \frac{\lambda}{b}\left(R - \frac{ab}{2}\right)\right)$$

$$X = \begin{cases} -a + \sqrt{\frac{2aR}{b}}, & 0 \leq R \leq \frac{ab}{2} \\ -\frac{1}{\lambda} \ln\left(1 - \frac{\lambda}{b}\left(R - \frac{ab}{2}\right)\right), & R \geq \frac{ab}{2} \end{cases}$$

$$\begin{aligned} E(X) &= \int_{-a}^0 x \cdot f(x) \cdot dx + \int_0^{\infty} x \cdot f(x) \cdot dx \\ &= \int_{-a}^0 x \cdot \frac{b(x+a)}{a} \cdot dx + \int_0^{\infty} x \cdot be^{-\lambda x} \cdot dx \end{aligned}$$

$$= -\frac{a^2 b}{6} + \frac{b}{\lambda^2}$$

$$a=1, b=1, \lambda=2 \Rightarrow -\frac{1}{6} + \frac{1}{4}$$

$$= -0.166 + 0.25$$