

⑥ The histogram suggests that it may be an exponential distribution.

$$F(X_{(k)}) = \frac{k - 1/2}{N}$$

$$1 - e^{-\lambda X_{(k)}} = \frac{k - 1/2}{N}$$

$$y_k = X_{(k)} = -\frac{1}{\lambda} \ln\left(1 - \frac{k - 1/2}{N}\right)$$

From the excel sheet,  $\frac{1}{\lambda} = \text{mean} = 9.459$

Looking at the diagram given by sir,

$$\begin{array}{ccc} N & & n \\ 20 < N \leq 50 & & 5 < n \leq 10 \end{array}$$

I would prefer to use a value of "n" which is closer to 10 corresponding to the "n/2" residing in the right half.

value of  $\chi^2$

I choose  $n=8$  with  $df = 8-1-1=6$ .

From the notes, we have,

$$\begin{aligned} p &= 1 - F_v(\chi^2) \\ &= 1 - \frac{1}{2^{v/2} \Gamma(v/2)} \int_0^{\chi^2} z^{v/2-1} e^{-z/2} dz \\ &= 1 - \frac{1}{2^{6/2} \Gamma(6/2)} \int_0^{\chi^2} z^{6/2-1} e^{-z/2} dz \\ &= 1 - \frac{1}{2^3 \cdot 2} \int_0^{\chi^2} z^2 e^{-z/2} dz \\ &= 1 - \frac{1}{2^4} \int_0^{1.84} z^2 e^{-z/2} dz \end{aligned}$$

From excel, I computed  $\chi^2 = 1.84$ .

$$p = 1 - \frac{1}{16} (1.05904)$$

- 1 - 0.0619

$$-1 \quad 0.000$$

$$= 0.93381$$

Therefore, we are confident that our hypothesis of the distribution being exponential is true.