

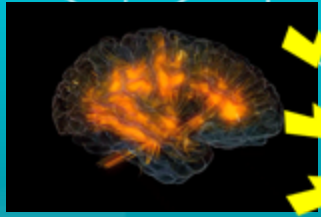


Biosignal Processing

July 28, 2022

Accurate Biosignal Representation Starts with Processing

Physiological
Energy



Measuring Equipment

Transducer

Amplifier

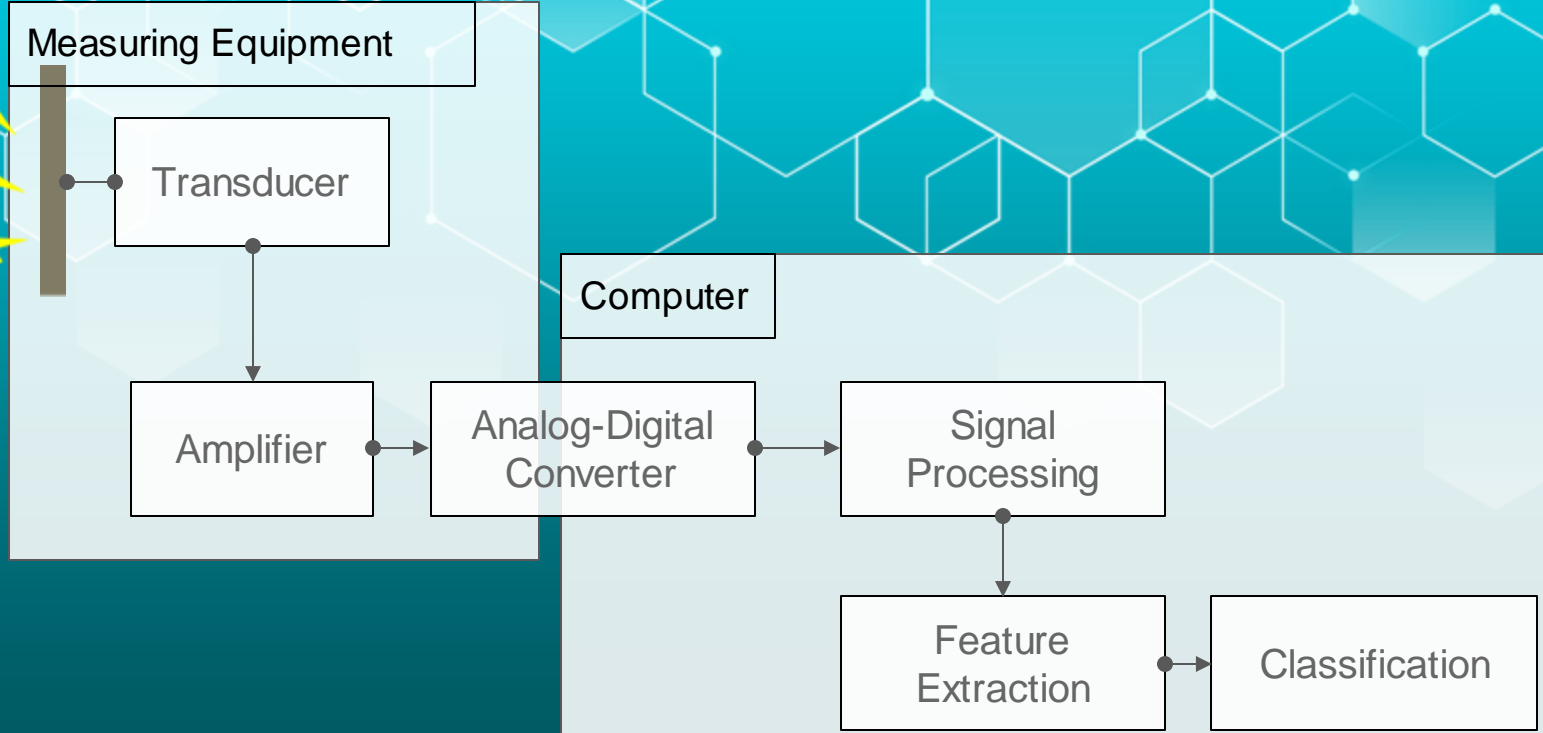
Analog-Digital
Converter

Computer

Signal
Processing

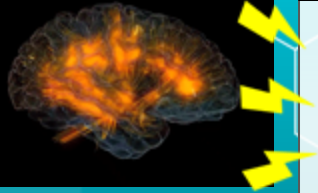
Feature
Extraction

Classification



Accurate Biosignal Representation Starts with Processing

Physiological
Energy



Measuring Equipment

Transducer

Amplifier

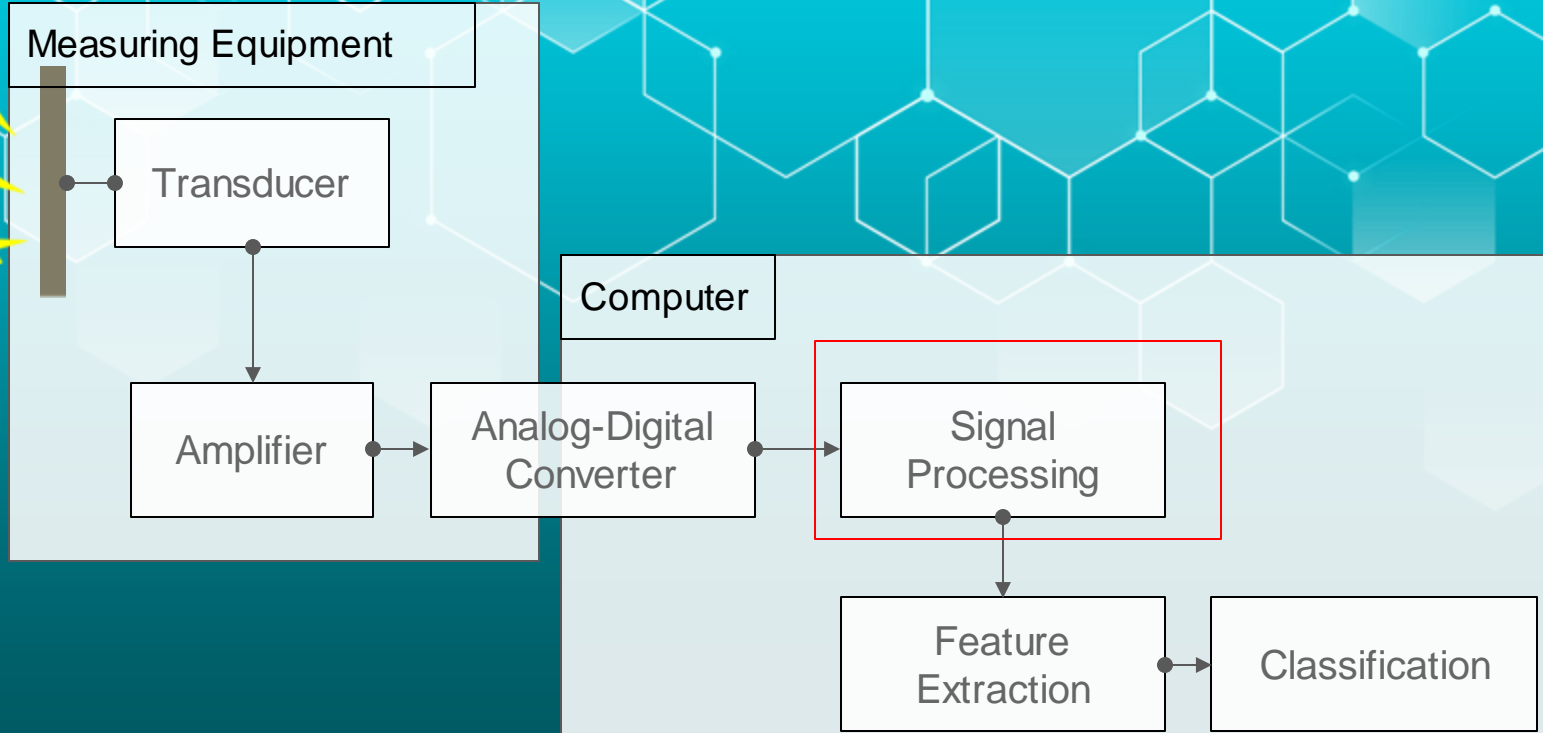
Analog-Digital
Converter

Computer

Signal
Processing

Feature
Extraction

Classification



Workshop Objectives

01
Signal
Sampling

02
Time and
Frequency Domains

03
Noise

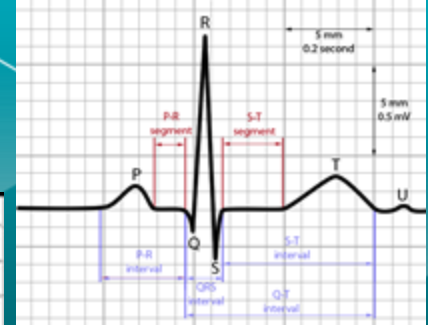
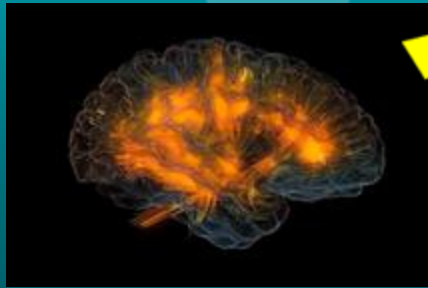
04
Filtering



Part 1: Signal Sampling

Continuous System

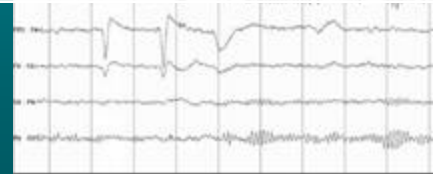
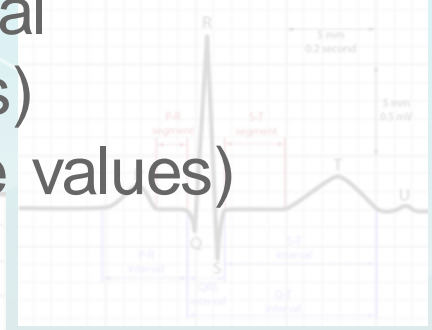
Discrete Representation



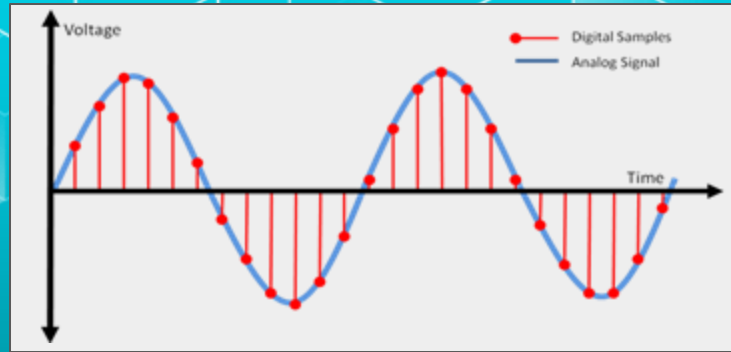
Continuous System

Discrete Representation

Reconstruct the continuous signal
(with infinite # of possible values)
using digital signals (finite # of possible values)

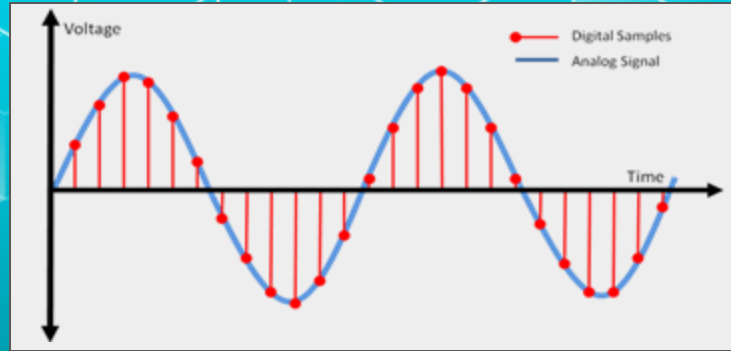


Sampling Rate



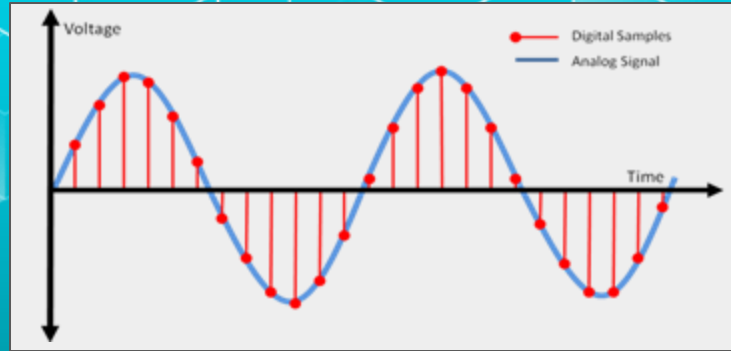
- Sample the continuous signal at discrete time points at a constant rate (sampling frequency)
- Connect the discrete voltage values at the sampled times to reconstruct/represent continuous signal

Sampling Rate



How do we know if our sampling rate accurately represents our measured signal?

Sampling Rate



How do we know if our sampling rate accurately represents our measured signal?

The Nyquist Theorem!

Nyquist Theorem

We must sample a signal at a rate that is at least 2x higher than the highest frequency in the signal

Nyquist Theorem

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Let's practice choosing our sampling frequency!

Nyquist Theorem

We must sample a signal at a rate that is at least 2x higher than the highest frequency in the signal

Example 1: We want to measure a Human ECG signal (heart activity). The clinically defined signal bandwidth is 0.05-100 Hz. What should our sampling frequency be?

Nyquist Theorem

We must sample a signal at a rate that is at least 2x higher than the highest frequency in the signal

Example 2: We want to measure the alpha wave activity in an EEG signal. What is the signal bandwidth? What is the minimum sampling frequency to accurately represent the signal?

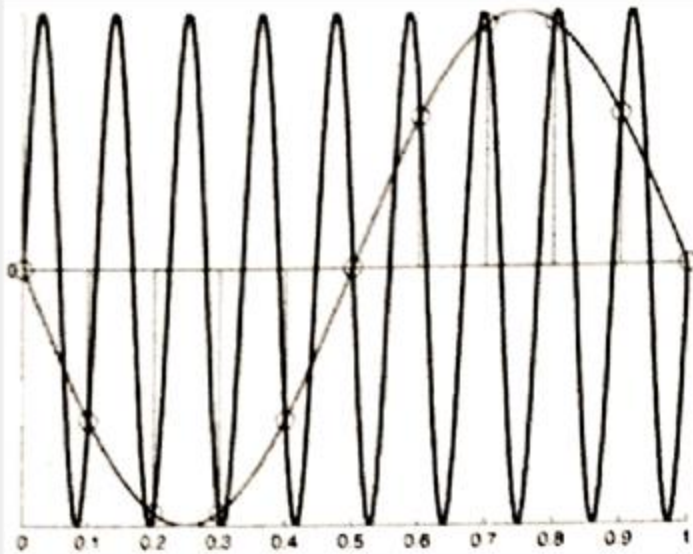
Nyquist Theorem

We must sample a signal at a rate that is at least 2x higher than the highest frequency in the signal

What happens if we sample below the Nyquist frequency?

Aliasing and the Nyquist Theorem

Aliasing!



- 9 Hz sinusoid (black) sampled every 0.1 s (10 Hz)
- Sampled signal appears as 1 Hz sinusoid ($F_s - f_0$)

Practical biomedical signal analysis using Matlab, KJ Blinowska and J Zygliewicz,
Boca Raton: CRC Press, 2012

Aliasing and the Nyquist Theorem

Aliasing!

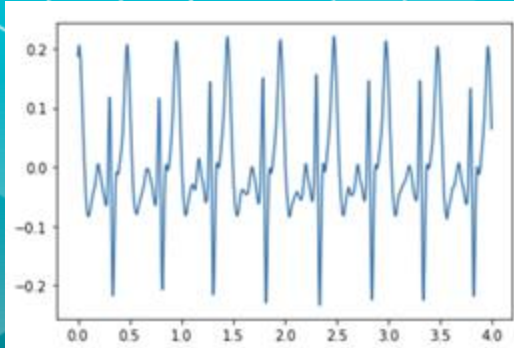
<https://www.youtube.com/watch?v=yr3ngmRuGUc>



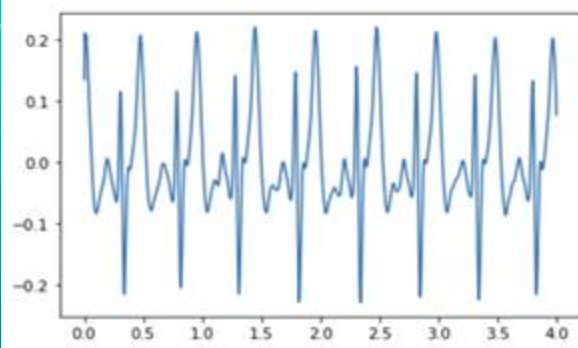
Activity 1: ECG signal and Aliasing

Activity 1: ECG signal and Aliasing

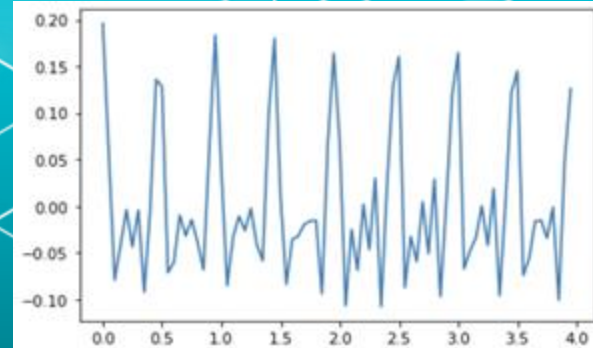
2000 Hz



200 Hz



200 Hz



Why not always have a high sampling frequency?



Can reconstruct the original signal accurately



Have to store a lot of data (Need more storage space)

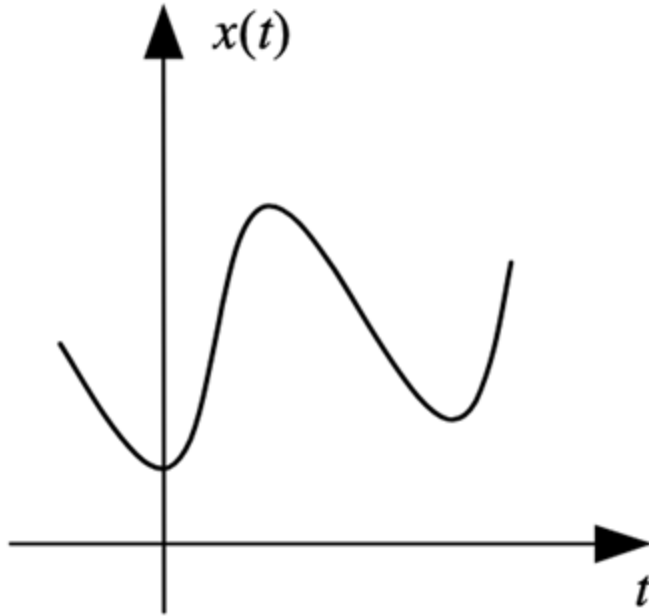


Have to collect & save the data quickly
(Need high processing power)

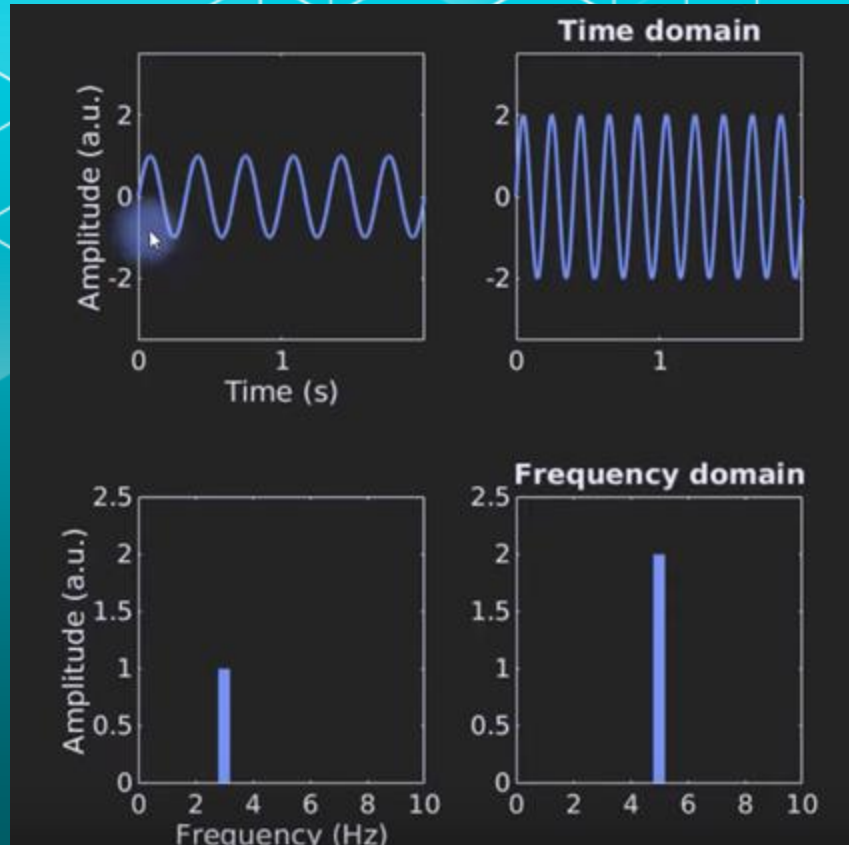


Part 2: Time and Frequency Domain

Time and Frequency Domains



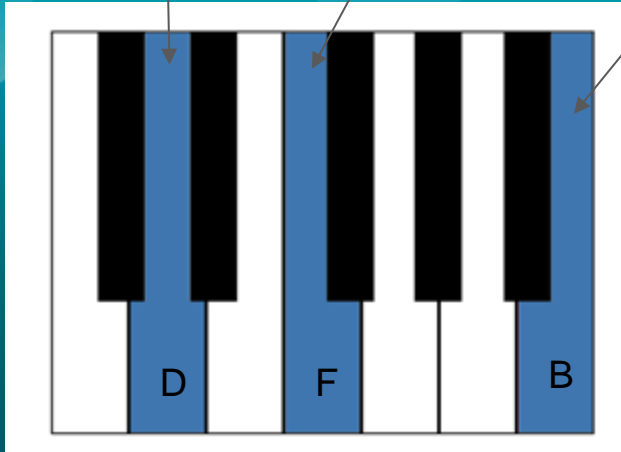
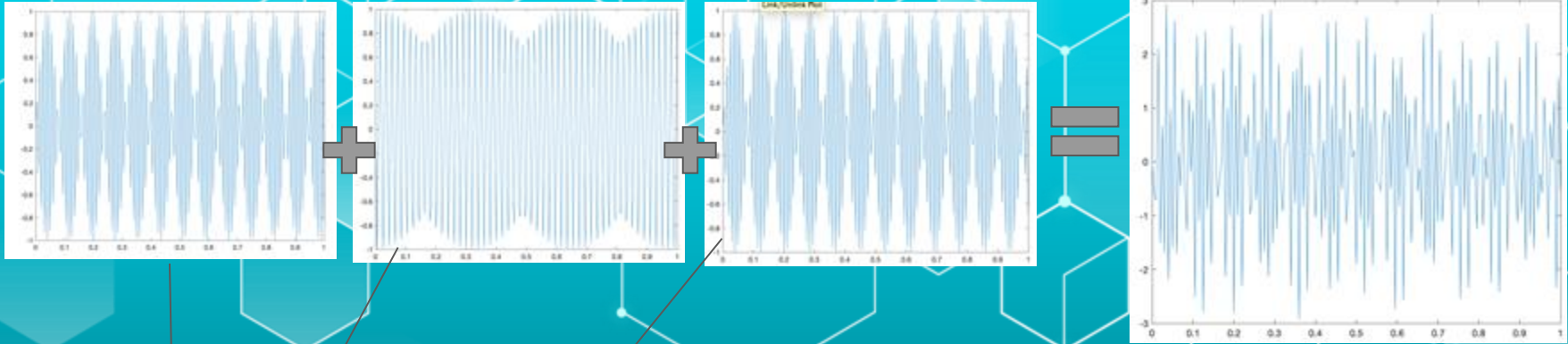
Time and Frequency Domains



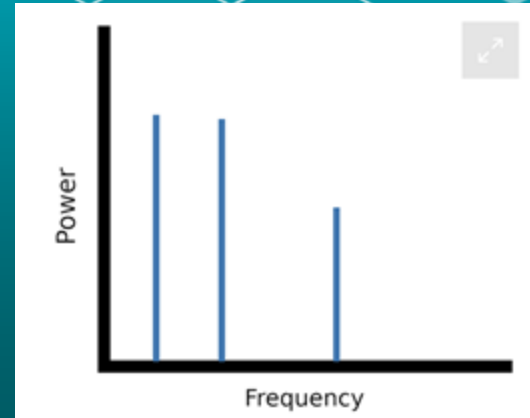
Time and Frequency Domains

How do we interpret complex signals in the frequency domain?

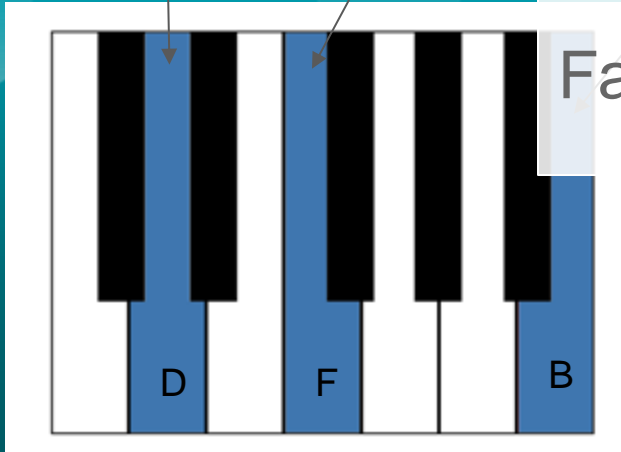
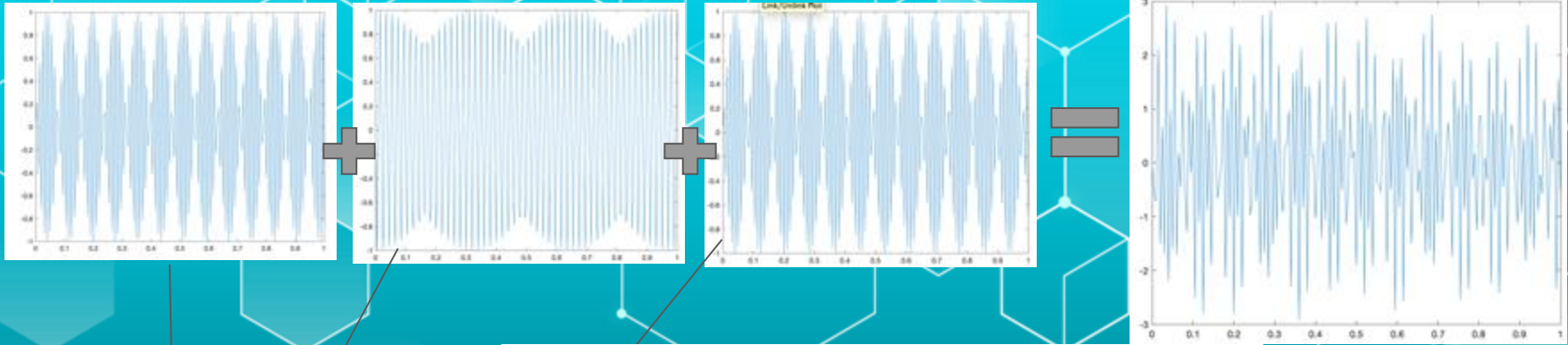
Time vs. Frequency Domain



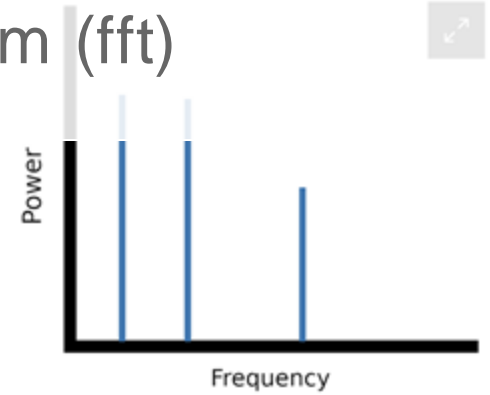
=



Time vs. Frequency Domain



Fast Fourier Transform (fft)

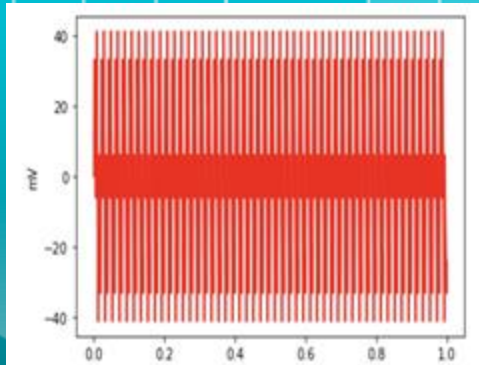




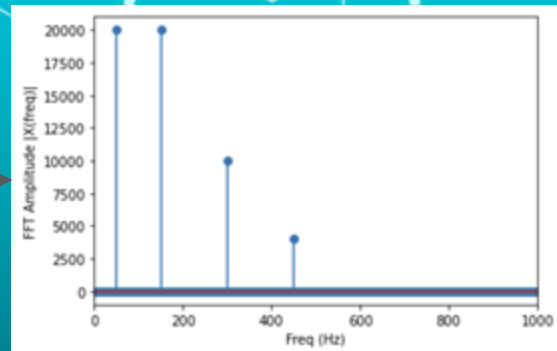
Activity 2: Identify Frequency Components using `fft()`

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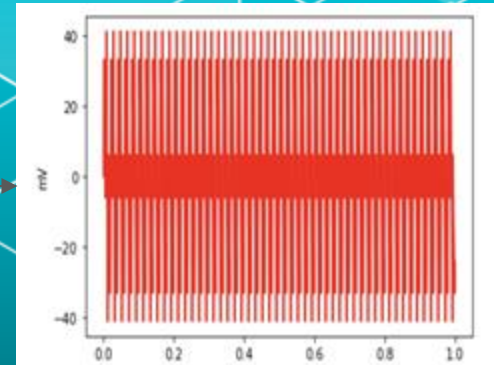
Time Domain



Frequency Domain



Time Domain



Aliasing in the Frequency Domain?

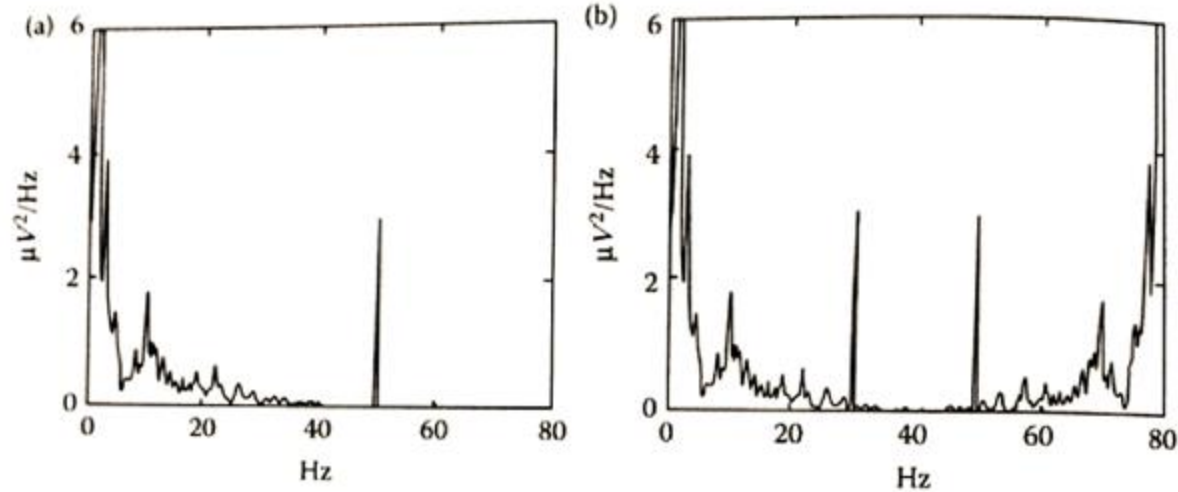
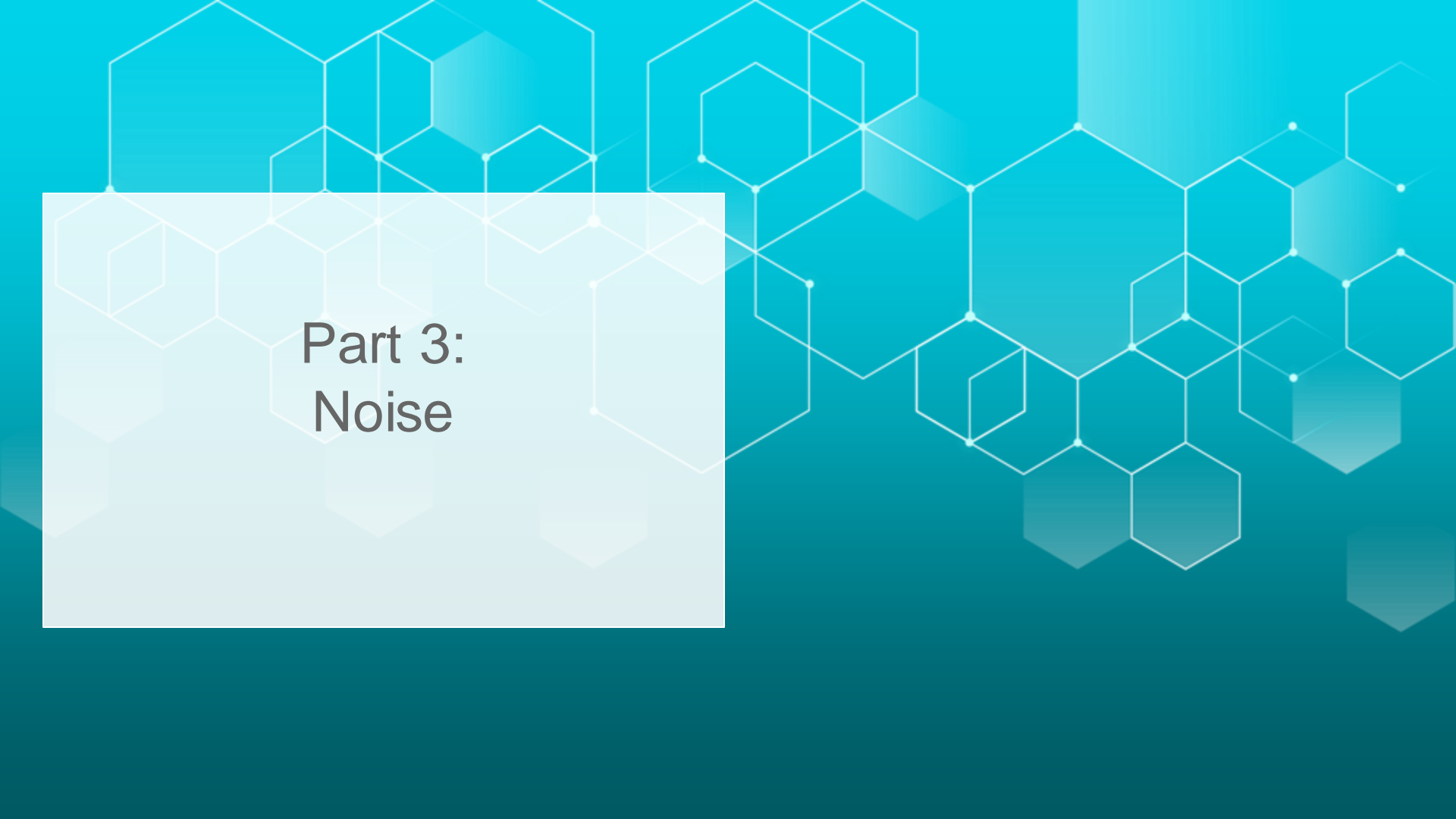
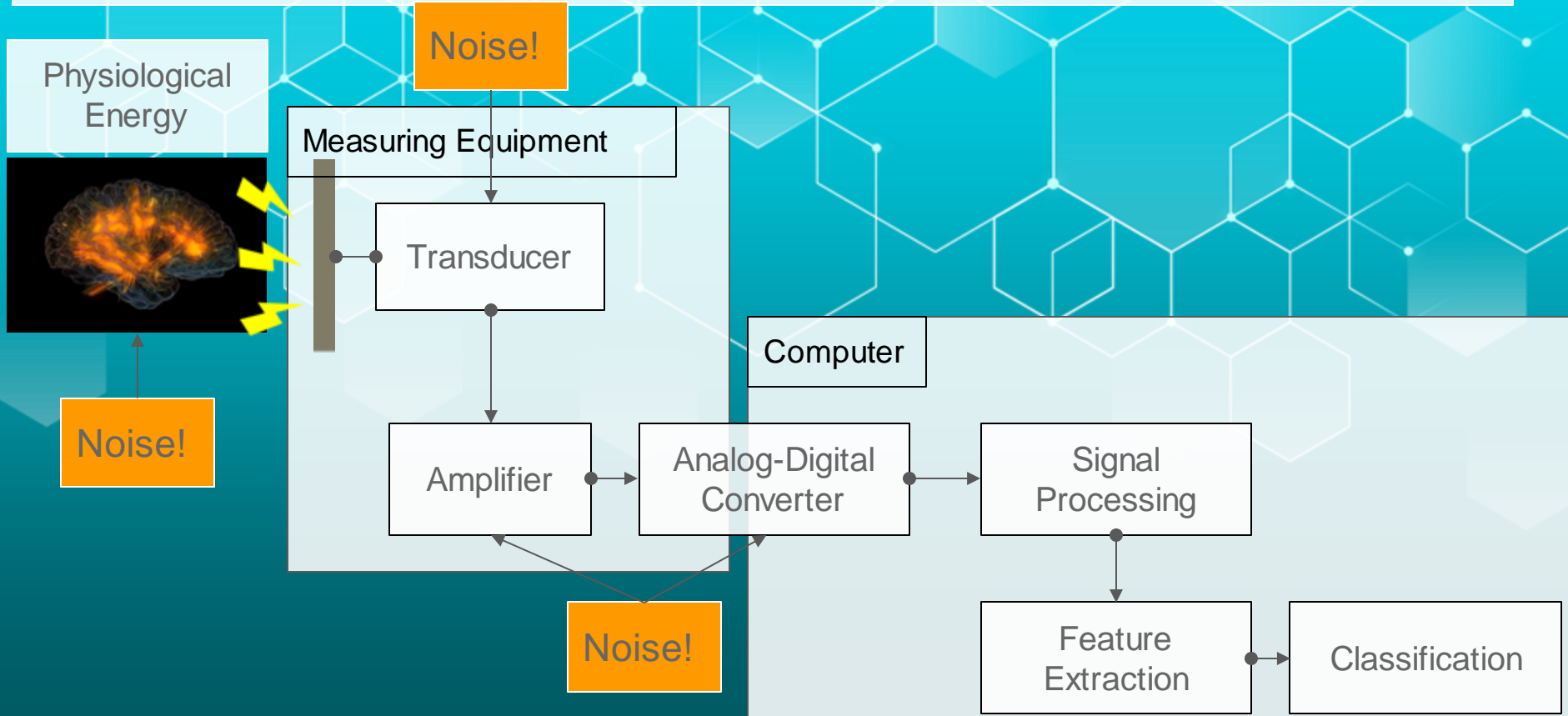


FIGURE 1.3 Power spectrum of an EEG signal (originally bandlimited up to 40 Hz). The presence of 50 Hz mains noise (a) causes aliasing error in the 30 Hz component (i.e., in the β diagnostic band) in the sampled signal (b) if $f_s = 80$ Hz.



Part 3: Noise

Noise affects all parts of acquisition



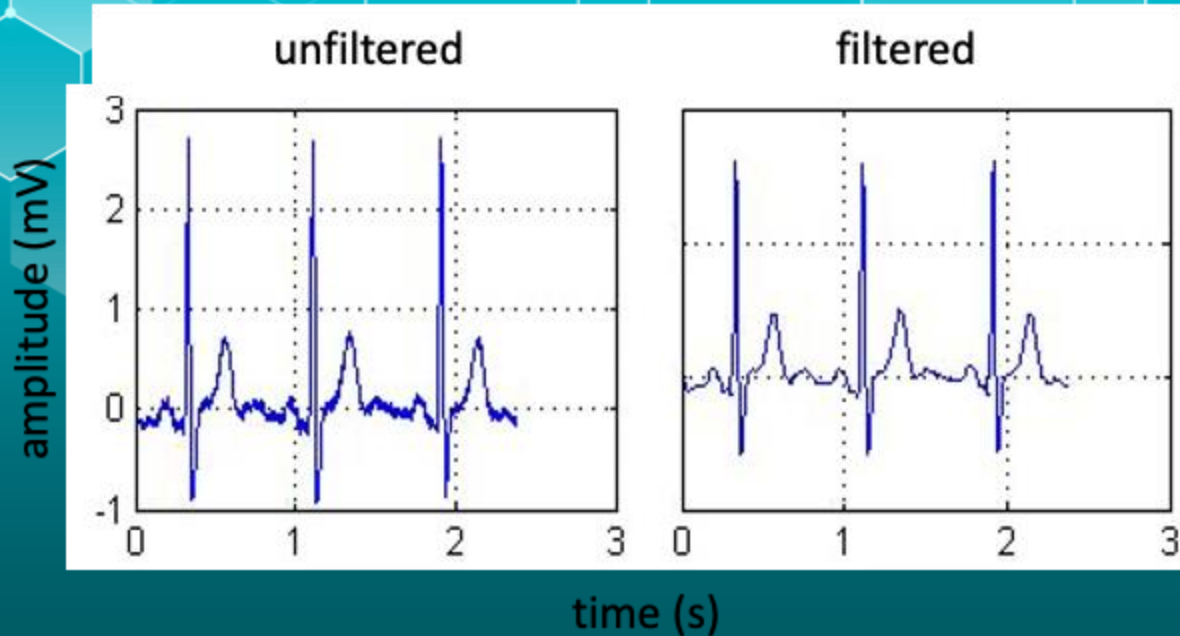
Sources of Noise

Measurement noise from:

- **Electrodes**
 - Movement, coupling to skin changes
 - Thermal noise caused by thermal agitation of electrons in a conductor
- **Electronic components in the measurement circuit**
 - Amplifiers, resistors, *etc* each contribute some noise to the signal
- **Electrical sources in the surrounding environment**
 - *e.g.* 60 Hz AC noise from power lines, fluorescent lights

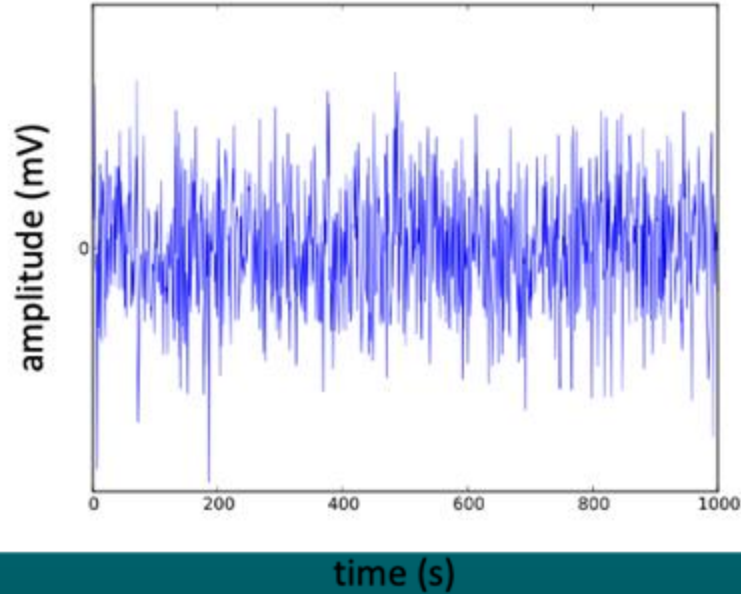
Sources of Noise

60Hz noise (Mains Hum)



Sources of Noise

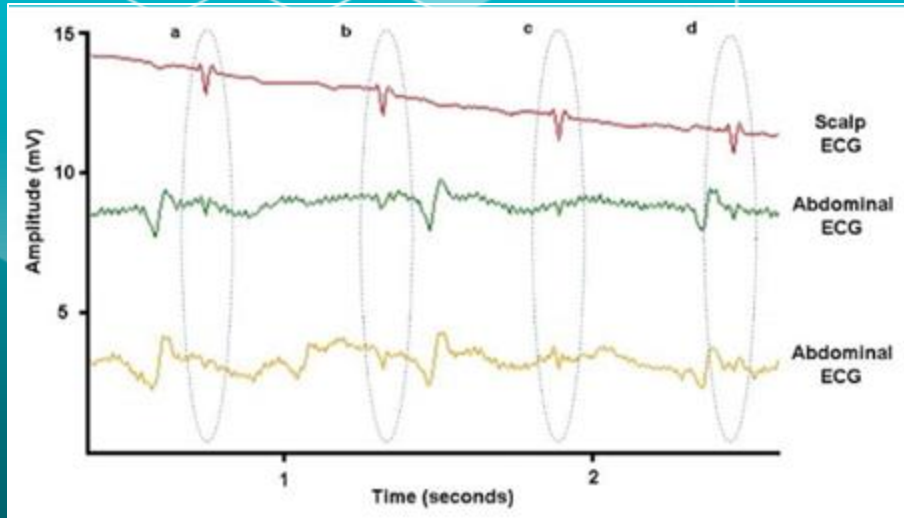
White noise



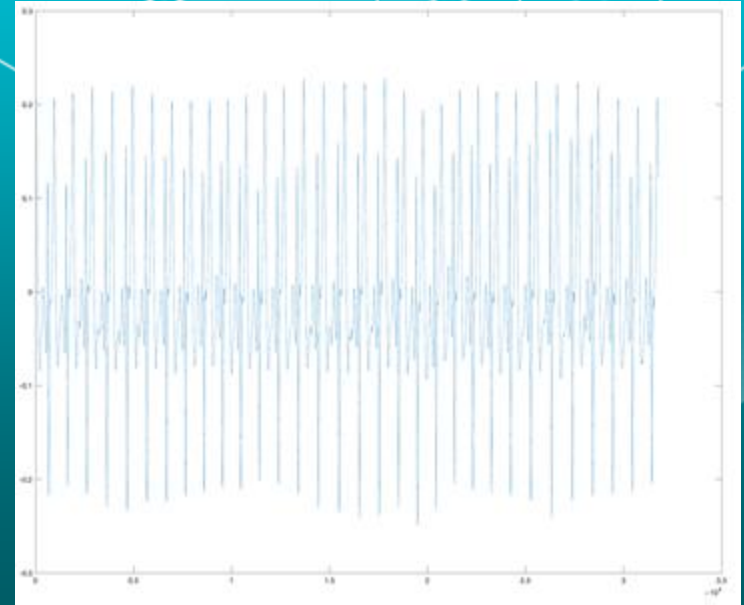
Sources of Noise

Physiological Noise

e.g. heart rate or respiration in MRI

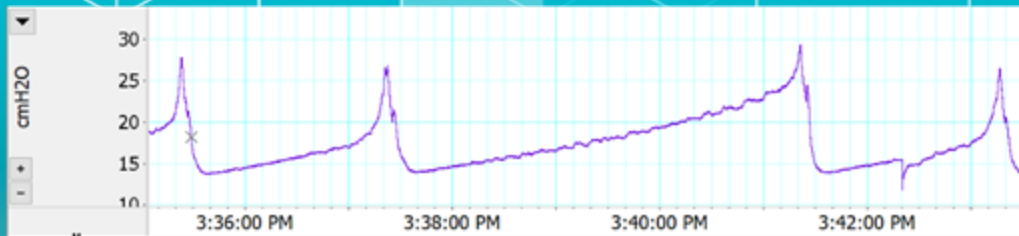


Sameni, et al. A Review of Fetal ECG Signal Processing; Issues and Promising Directions, 2010

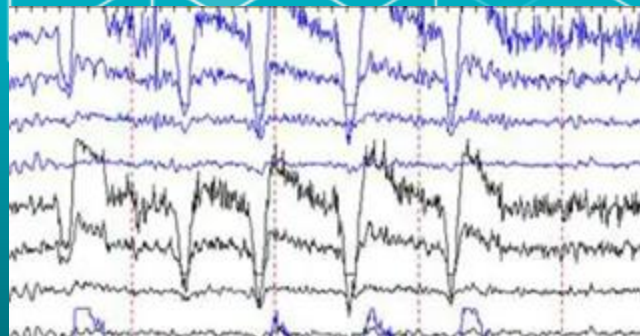


Sources of Noise

Motion Artifact



Franz, Karly S., CMG Data in Rat

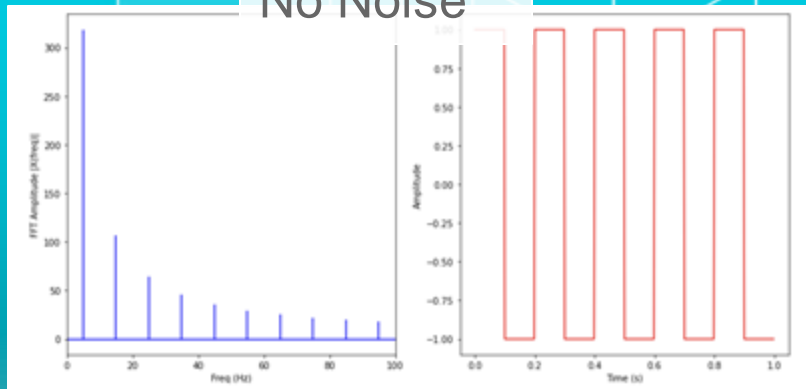




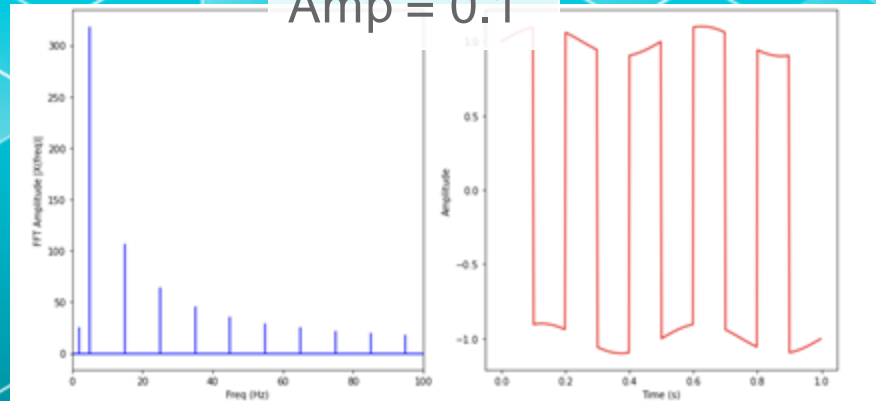
Activity 3: How does noise affect our signal in time and frequency domains?

“Respiration” (Physiological) noise

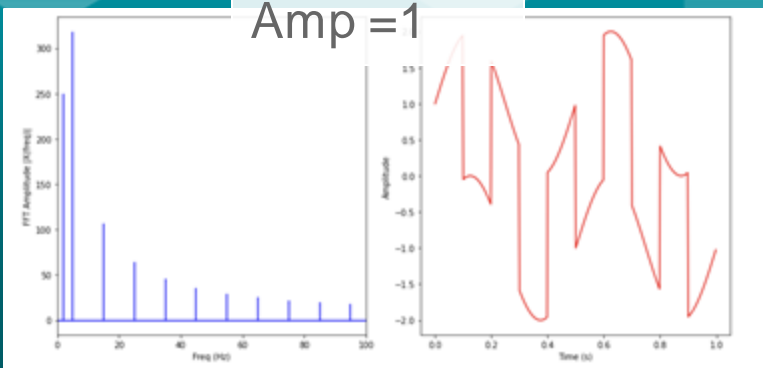
No Noise



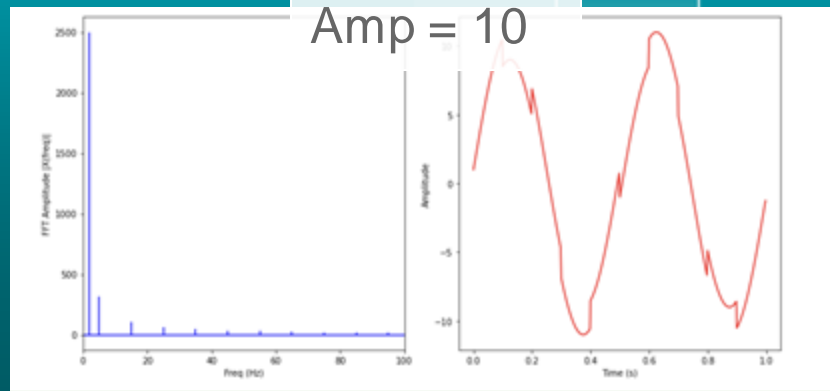
Amp = 0.1



Amp = 1

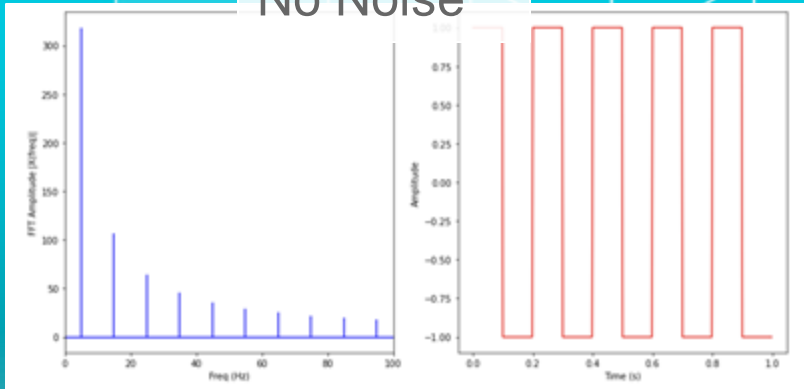


Amp = 10

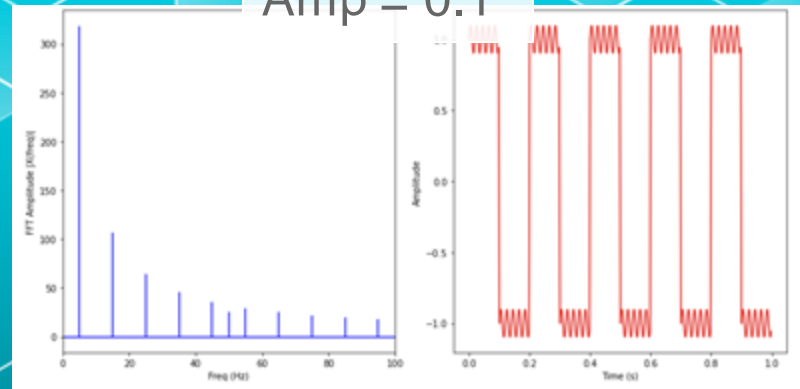


Mains Hum

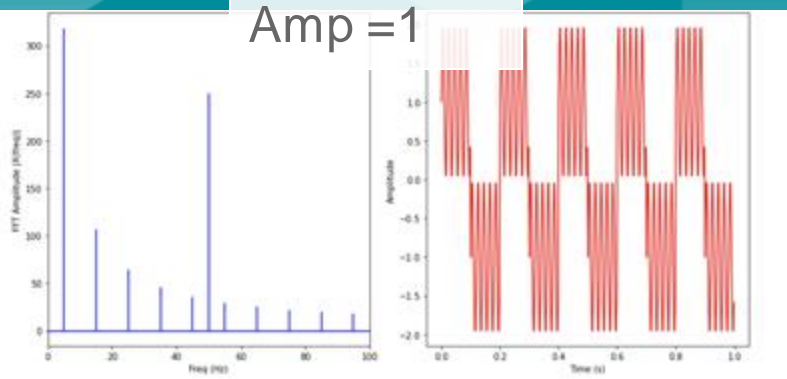
No Noise



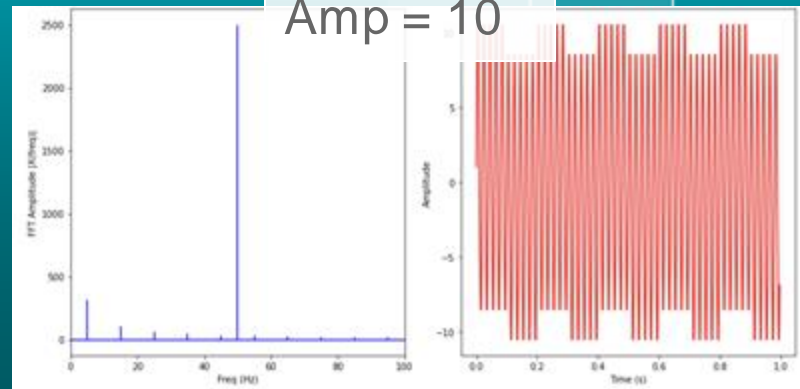
Amp = 0.1



Amp = 1

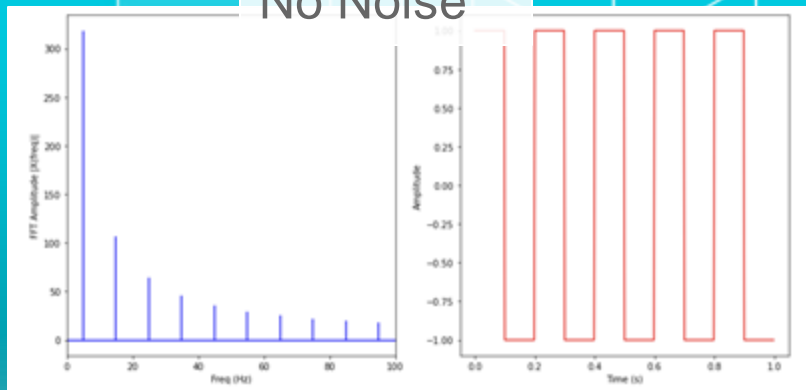


Amp = 10

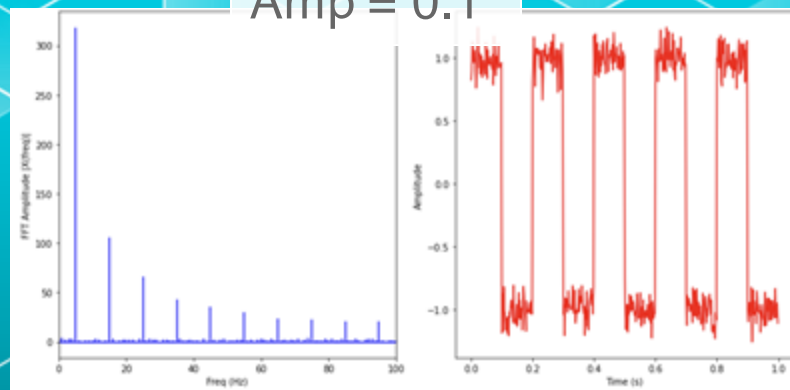


White Noise

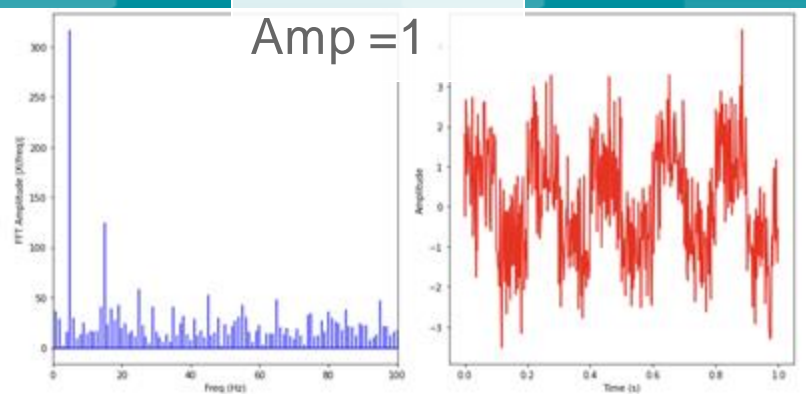
No Noise



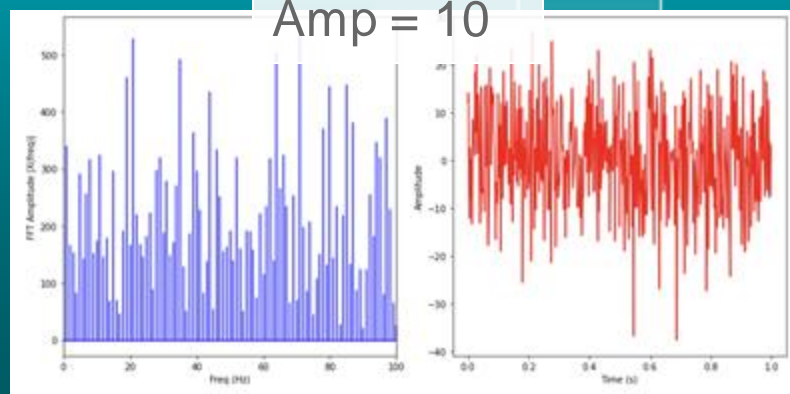
Amp = 0.1



Amp = 1



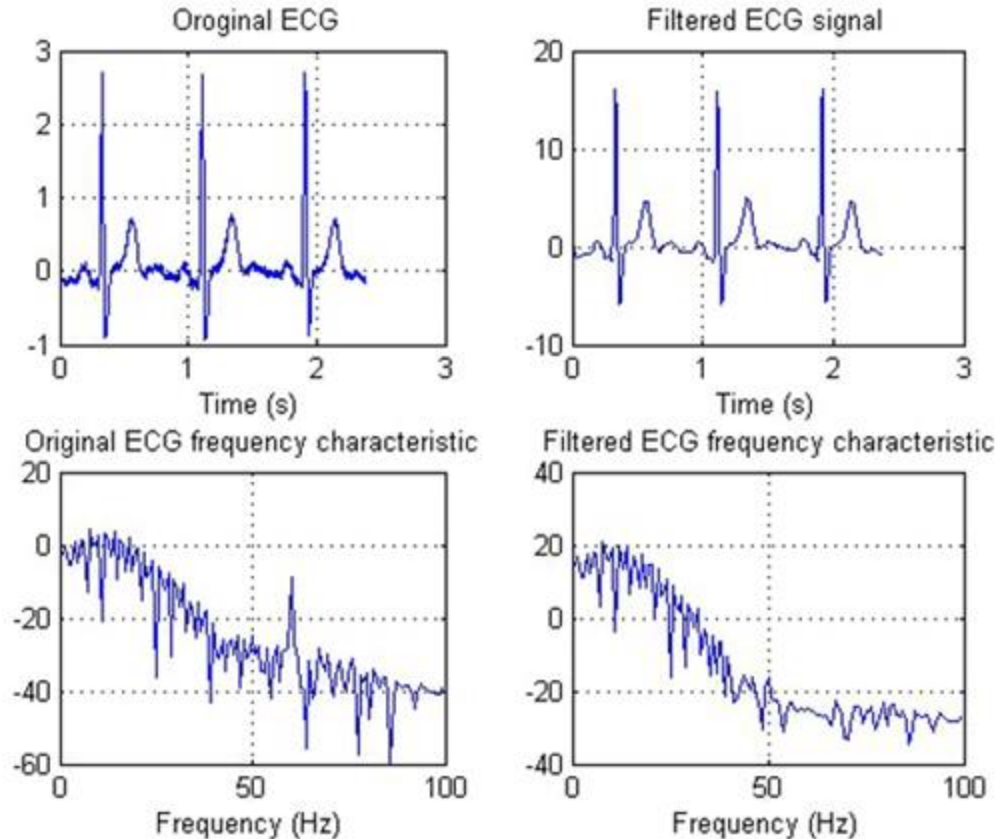
Amp = 10





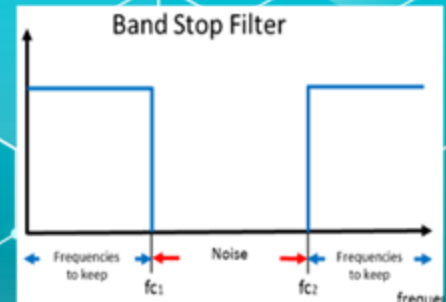
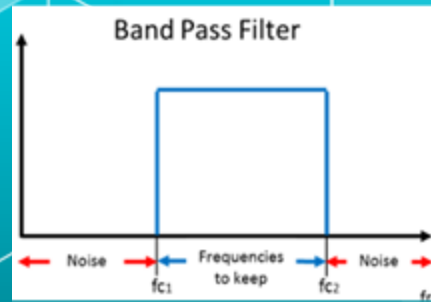
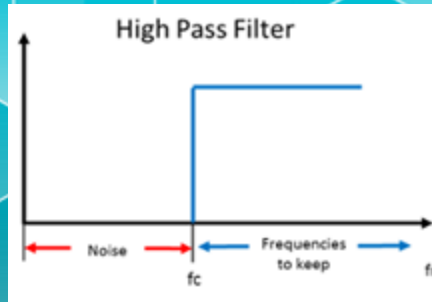
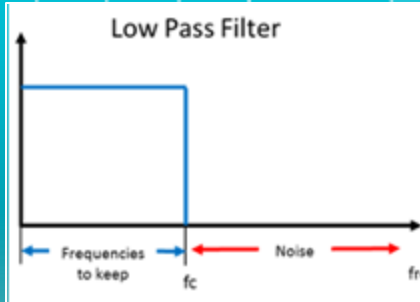
Part 4: Filtering

Noise can easily be identified in the frequency domain

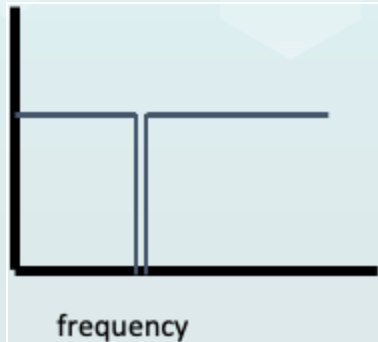


How can we remove noise?

Digital Filters can be used to eliminate noise

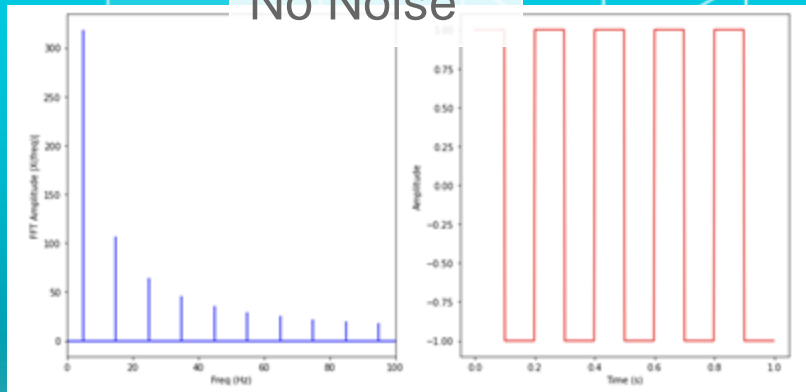


Notch filter....

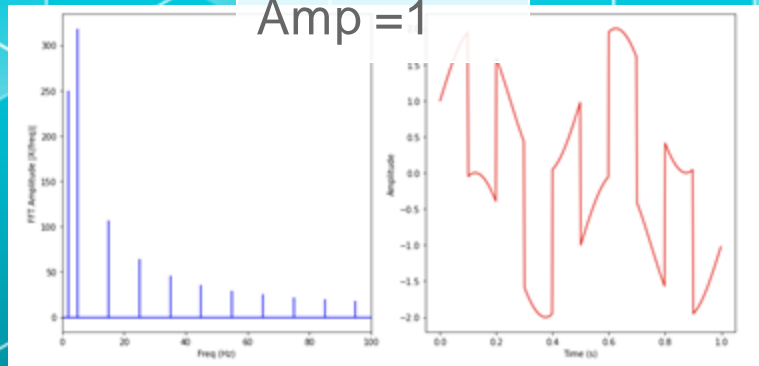


Example: "Respiration" (Physiological) noise

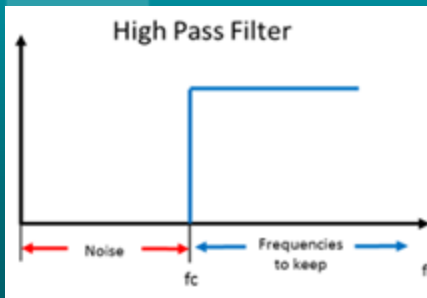
No Noise



Amp = 1

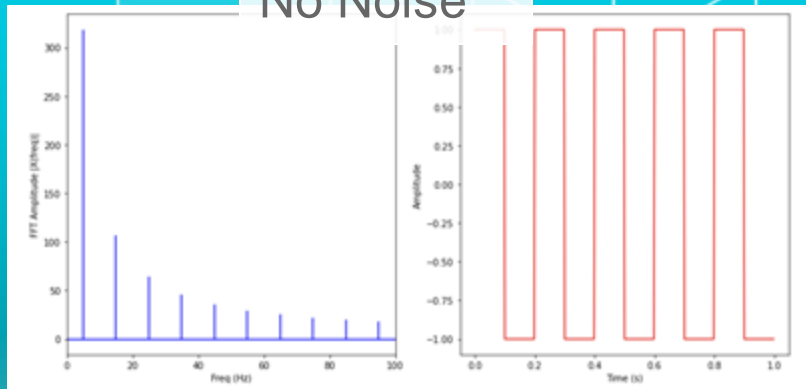


High Pass Filter

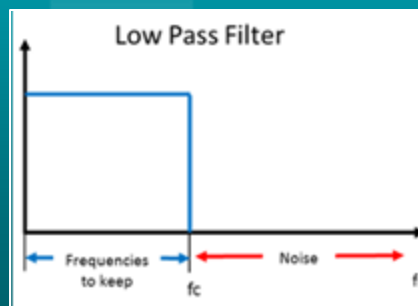
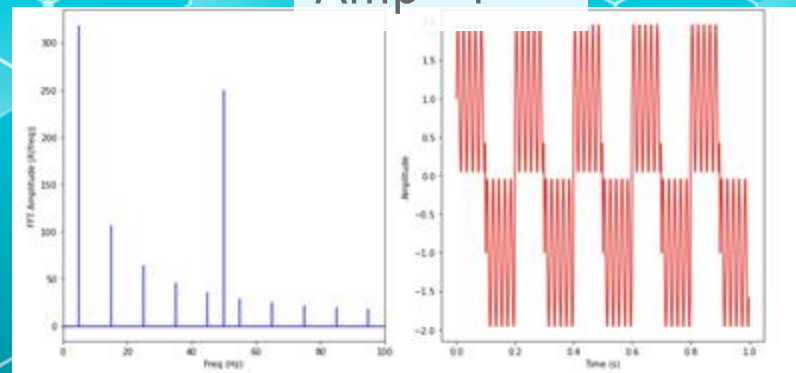


Example: Mains Hum

No Noise

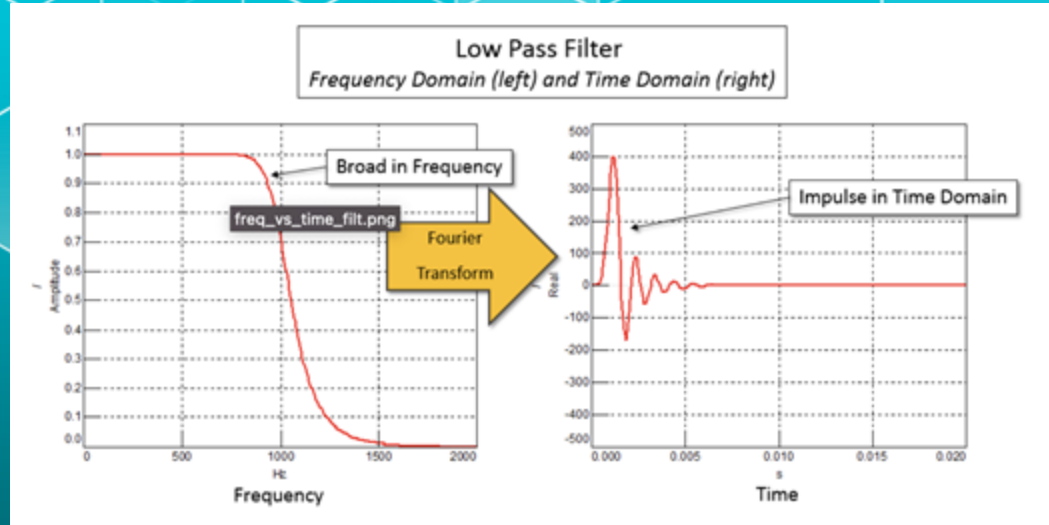


Amp = 1



How do Filters work?

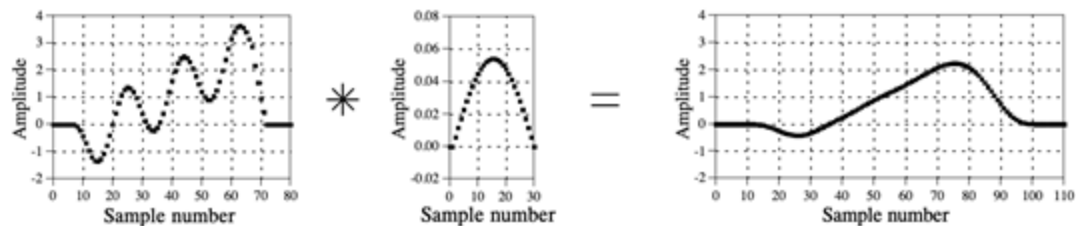
Impulse response is the filter response in the time domain



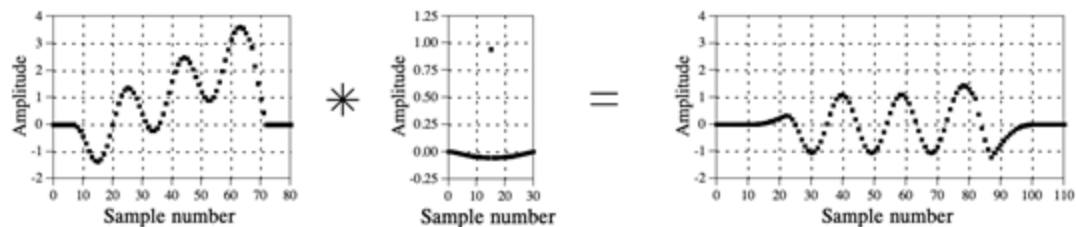
How do Filters work?

Convolution

a. Low-pass Filter



b. High-pass Filter



Input Signal

Impulse Response

Output Signal

How do Filters work?

FIR and IIR filters

$$\text{FIR Filter Equation: } y(n) = \sum_{k=0}^N a(k)x(n-k)$$

$$\text{IIR Filter Equation: } y(n) = \sum_{k=0}^N a(k)x(n-k) + \sum_{j=0}^P b(j)y(n-j)$$

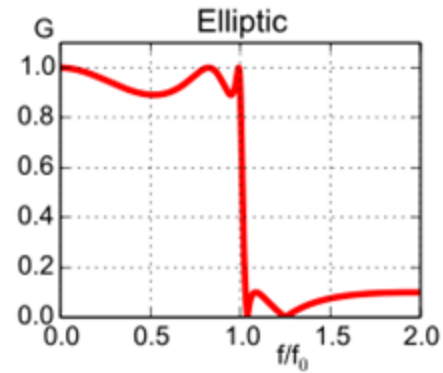
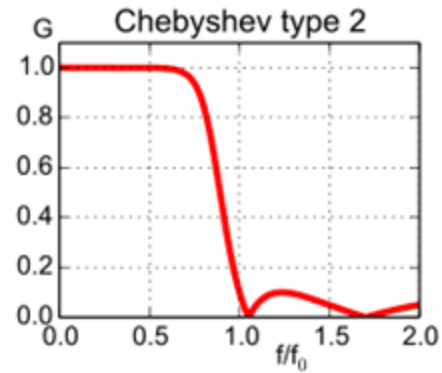
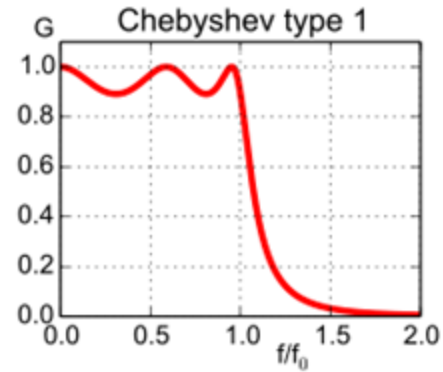
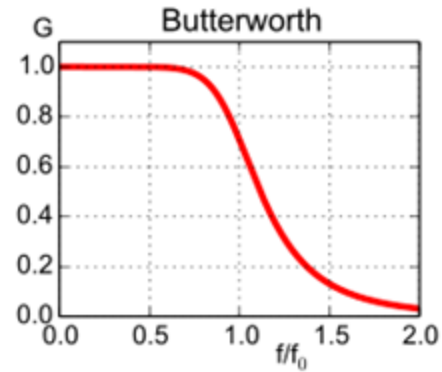
Output used recursively



	IIR	FIR
Computational Speed	Fast – Low Order	Slow – High Order
Phase / Delay	Not constant	Constant
Stability	Sometimes	Always

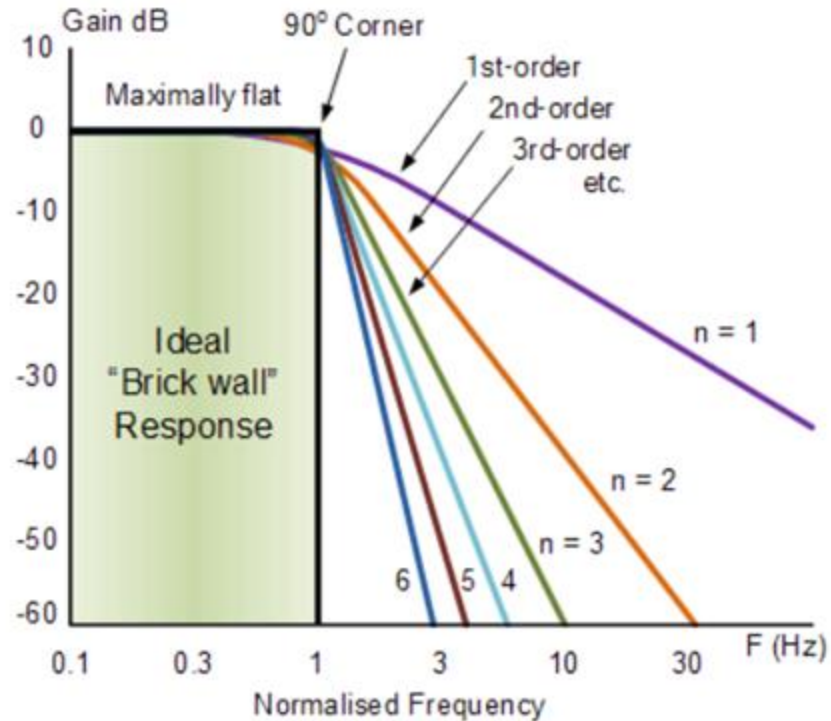
<https://community.sw.siemens.com/s/article/introduction-to-filters-fir-versus-iir>

Filter Design Considerations: Filter Types



Filter Design Considerations: Filter Order

Ideal Frequency Response for a Butterworth

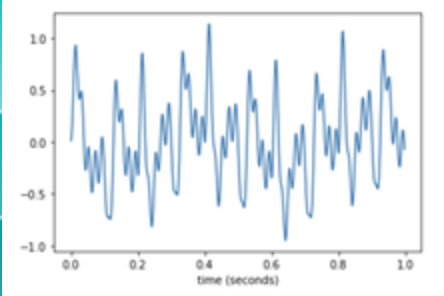
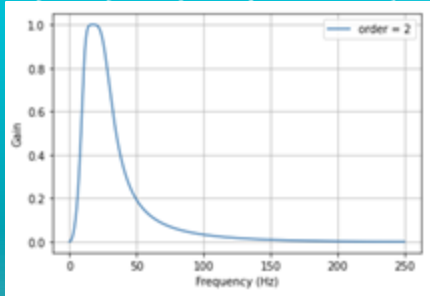




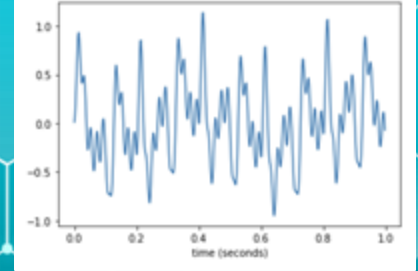
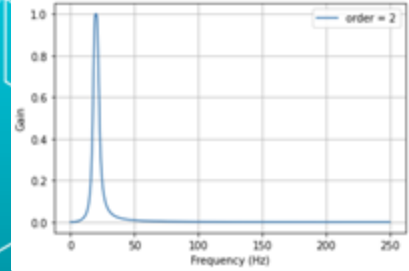
Activity 4: Let's build filters and apply them!

Activity 4: Let's build filters and apply them!

$Fc1 = 10 \text{ Hz}$; $fc2 = 30 \text{ Hz}$; order = 2



$Fc1 = 18 \text{ Hz}$; $fc2 = 22 \text{ Hz}$; order = 2



$Fc1 = 18 \text{ Hz}$; $fc2 = 22 \text{ Hz}$; order = 6

