



**wada**



# **Practice Exercise Solutions**



# wada



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## Exercise 1

```
{-  
  
1- Write a program that takes as input two numbers and return the greatest  
  
-}  
  
-- first solution  
theGreaterBetween1 x y  
  | x < y = y  
  | otherwise = x  
  
-- second solution  
theGreaterBetween2 x y =  
  if x < y  
  then y  
  else x  
  
-- third solution  
theGreaterBetween3 x y = max x y
```

## Exercise 2

```
{-  
  
2- Write a program that takes an integer number and return the string "EVEN" if the number is  
even or "ODD" if the number is odd  
  
-}  
  
-- first solution
```



```
evenOrOdd1 n =  
  if mod n 2 == 0  
  then "EVEN"  
  else "ODD"  
  
-- second solution  
evenOrOdd2 n  
  | (mod n 2) == 0 = "EVEN"  
  | otherwise = "ODD"
```

## Exercise 3

```
{-  
  
3- Write a program that returns the team of a student given its matricula number.  
There are three possible teams: RED, GREEN and BLUE. The assignment takes place  
with the following criterion: the student with matricula 1 goes to RED team,  
the one with matricula 2 in the GREEN, the one with matricula number 3 in the BLUE,  
the one with matricula number 4 in the RED, that one with 5 in GREEN etc.  
(Note: you can use case construction)  
  
-}  
  
teamDetermination mat =  
  case (mod mat 3) of  
    0 -> "BLUE"  
    1 -> "RED"  
    2 -> "GREEN"
```



## Exercise 4

```
{-  
4- Write a program that takes as input an integer corresponding to the score of a student  
and returns "Insufficient" if it is less than 18, "Just enough" (if the score is 18),  
"Low" (if the score is between 19-20), "Medium" (if the score is between 21-23),  
"Good" (if the score is between 24-26), "High" (if the score is between 27-29),  
"Maximum" (if the score is 30) "Impossible" (in others cases) (Note: you can use guard)  
-}  
  
scoreAppreciation score  
| score < 18 = "Insufficient"  
| score == 18 = "Just enough"  
| score >= 19 && score <= 20 = "Low"  
| score >= 21 && score <= 23 = "Medium"  
| score >= 24 && score <= 26 = "Good"  
| score >= 27 && score <= 29 = "High"  
| score == 30 = "Maximum"  
| otherwise = "Impossible"
```

## Exercise 5

```
{-  
5- Write a program that takes three coefficients a, b and c of a second degree equation,  
and returns the solutions if these are real; if they are not, it must simply return  
"Non-real values".  
-}
```



```
data SolutionData =
  RealSolution Double Double
| NonRealValues
deriving (Eq, Show)

solveEquationSecondDegree a b c =
  let delta = b * b - 4*a*c
  in if delta >= 0
    then RealSolution ((-b - sqrt delta)/(2*a)) ((-b + sqrt delta)/(2*a))
    else NonRealValues
```

## Exercise 6

```
{-
6- A secular year (divisible by 100) is a leap year if it is divisible by 400, a non-secular
year is a leap year if it is divisible by 4. For example, the year 1900 was not a leap, 1996 was
a leap, 2000 was, 2002 was not a leap. Write a program that takes a year as input and indicates
whether it is a leap year or not.
-}
```

```
isLeapYear year
  | (mod year 100) == 0 =
    if (mod year 400) == 0
    then True
    else False
  | otherwise =
    if (mod year 4) == 0
    then True
    else False
```



## Exercise 7

```
{-  
  
7- Write a program that takes as input a list of integers and returns the average of the number  
in the list.  
  
-}  
  
average xs = realToFrac (sum xs)/realToFrac (length xs)
```

## Exercise 8

```
{-  
  
8- Write a program that takes a list of integers as input,  
and returns a list consisting first of all the even values  
in the order in which they are in the input list and then  
all the odd values in the reverse order.  
Example: given the values: 8 1 3 2 8 6 5, the  
program will return: 8 2 8 6 5 3 1  
  
-}  
  
evenOrdOddReverse :: Integral a => [a] -> [a]  
evenOrdOddReverse xs =  
    let pair = filter (\x -> (mod x 2) == 0) xs  
        impair = filter (\x -> (mod x 2) == 1) xs  
    in pair ++ reverse impair
```



## Exercise 9

```
{-
9- Write a program that takes a list of doubles as input,
and returns a list of 3-value moving averages of these numbers.
The program must check that the number of values in the list
is at least equal to 3. The moving average is an arithmetic average
over only a part of the values (in this case 3),
for example if the sequence of values is given:
2.1, 4.2, 1.3, 6.7, 3.1, 5.5, 2.1, 4.9, 3.0, 5.4, 3.9
the program has to calculate the average of 2.1, 4.2 and 1.3 and record it,
then the average of 4.2, 1.3 and 6.7 and record it,
then 1.3, 6.7 and 3.1 and record it,
etc. up to 3.0, 5.4 and 3.1

-}

-- first solution
mobileThreeAvarage1 :: Fractional a => [a] -> [a]
mobileThreeAvarage1 xs
  | length xs < 3 = error "List too small"
  | otherwise = fst $ foldl f ([], 0) xs
    where f (yx, ind) x =
      if (length xs - ind) >= 3
      then let mobileAvg = (x + xs!!(ind + 1) + xs!!(ind + 2))/3
           in (yx ++ [mobileAvg], ind + 1)
      else (yx, ind + 1)

--second solution
mobileThreeAvarage2 :: Fractional a => [a] -> [a]
mobileThreeAvarage2 [] = error "List too small"
mobileThreeAvarage2 (_,[]) = error "List too small"
mobileThreeAvarage2 (_,_:[]) = error "List too small"
mobileThreeAvarage2 (x:y:z:[]) = [(x + y + z)/3]
mobileThreeAvarage2 (x:y:z:xs) = ((x + y + z)/3): mobileThreeAvarage2 (y:z:xs)
```





## Exercise 10

```
{-  
  
10- Write a program that takes a list of integer values as input and identifies the longest sequence  
of consecutive equal numbers. If several sequences of the same length are identified, consider only  
the first one identified. The program must indicate the repeated value and the number of repetitions  
of that value.  
Example:  
  Inputs: [19, 3, 15, 15, 7, 9, 9, 9, 9, 12, 3, 3, 3]  
  Output: number: 9, occurrences: 4  
  
-}  
  
import Data.List  
  
longestConsSequence :: (Eq a, Show a) => [a] -> String  
longestConsSequence [] = []  
longestConsSequence xs =  
  let gprs = group xs  
      res = foldr step [] gprs  
      where  
        step :: [a] -> [a] -> [a]  
        step xs ys =  
          if length xs >= length ys  
          then xs  
          else ys  
  
in case res of  
  [] -> "Empty"  
  (x:_) -> "Output: number: " ++ show x ++ ", occurrences: " ++ show (length res)
```

## Exercise 11

```
{-
```



11- Write a program that takes as input a matrix of integers and returns the maximum, the minimum, the sum and the average.

-}

```
maxMatrix :: [[Integer]] -> (Integer, Integer, Integer, Double)
maxMatrix [] = error "empty list"
maxMatrix xs =
    let max = maximum lineraMatrix
        min = foldr step matr00 xs
            where
                matr00 = head $ head xs
                step :: [Integer] -> Integer -> Integer
                step ys y =
                    if y <= l1
                    then y
                    else l1
                    where
                        l1 = minimum ys
        summ = foldr step 0 xs
            where
                step :: [Integer] -> Integer -> Integer
                step line acc = sum line + acc
        aver = fromIntegral (sum lineraMatrix) / fromIntegral (length lineraMatrix)
    in (max, min, summ, aver)
    where lineraMatrix = concat xs
```

## Exercise 12

{-

12- Write a program that takes a matrix of integer values as input and returns how many values are even and how many are odd.

-}

```
helper :: [Integer] -> (Int, Int)
```



```
helper xs = foldl f (0, 0) xs
    where f (evenAcc, oddAcc) x =
        if (mod x 2) == 0
        then (evenAcc + 1, oddAcc)
        else (evenAcc, oddAcc + 1)

-- first solution
countEvenAndOdd1 :: [[Integer]] -> (Int, Int)
countEvenAndOdd1 mx = helper $ concat mx

-- second solution
countEvenAndOdd2 :: [[Integer]] -> (Int, Int)
countEvenAndOdd2 mx = foldl f (0, 0) (map helper mx)
    where f (evenAcc, oddAcc) (e, o) = (evenAcc + e, oddAcc + o)
```

## Exercise 15

```
{-
15- Write a program that takes as input two matrices and returns the product of the two.
The program must verify that the matrices are valides and if they can be multiplied.
Two matrices can be multiplied if the number of columns of the first matrix is equal to
the number of lines of the second.
-}

import Data.List

isMatrix :: [[a]] -> Bool
isMatrix [[]] = True
isMatrix matrix = foldl f True matrix
    where --f :: Bool -> [a] -> Bool
          f acc line = acc && (length line == length (matrix !! 0))

canBeMultiply :: (Num a) => [[a]] -> [[a]] -> Bool
canBeMultiply a b
```



```
| isMatrix a == False || isMatrix b == False = False
| length (a !! 0) /= length b = False
| otherwise = True
```

```
matrixProduct :: (Num a) => [[a]] -> [[a]] -> [[a]]
matrixProduct a b
  | canBeMultiply a b == False = error "The matrixs can not be multiplied"
  | otherwise = foldl f [] a
    where f ac alineOfa = ac ++ [row]
          where row = foldl ff [] (transpose b)
                where ff acc alineOfbTranspose = acc ++ [res]

where res = sum $ zipWith (*) alineOfa alineOfbTranspose
```

## Exercise 16

```
{-
16- Write a function that divides two integral numbers using recursive subtraction.
The type should be (Integral a) => a -> a -> a.
Redo this exercise using the type (Integral a) => a -> a -> (a, a)
where (a, a) represents the quotient and the rest of the division.
-}

-- first solution
divideWithRecursiveSubtraction1 :: (Integral a) => a -> a -> a
divideWithRecursiveSubtraction1 0 0 = error "Unknown Result"
divideWithRecursiveSubtraction1 _ 0 = error "Infinity quotient"
divideWithRecursiveSubtraction1 dividende divisor =
  if dividende < divisor
  then 0
  else 1 + divideWithRecursiveSubtraction1 (dividende - divisor) divisor

-- second solution
divideWithRecursiveSubtraction2 :: (Integral a) => a -> a -> (a, a)
```



```
divideWithRecursiveSubtraction2 0 0 = error "Unknown Result"
divideWithRecursiveSubtraction2 _ 0 = error "Infinity quotient"
divideWithRecursiveSubtraction2 dividende divisor =
  if dividende < divisor
  then (0, dividende)
  else let res = divideWithRecursiveSubtraction2 (dividende - divisor) divisor
       in (1 + fst res, snd res)
```

## Exercise 17

```
{-
17- Write a function that recursively sums all numbers from 1 to n,
n being the argument. So that if n was 5, you'd add 1 + 2 + 3 + 4 + 5 to get 15. The type
should be (Eq a, Num a) => a -> a.
-}

sumInterval :: (Eq a, Num a) => a -> a
sumInterval 0 = 0
sumInterval n = n + sumInterval (n - 1)
```

## Exercise 18

```
{-
18- Write a function that multiplies two integral numbers using recursive summation.
The type should be (Integral a) => a -> a -> a.
-}

multiplyRecurAdd :: (Integral a) => a -> a -> a
multiplyRecurAdd 0 _ = 0
```



```
multiplyRecurAdd _ 0 = 0
multiplyRecurAdd x y = x + multiplyRecurAdd x (y - 1)
```

## Exercise 19

```
{-
19- Write a program that takes two strings as input and returns the longest.
The first if they are of equal length.
-}

longestString :: String -> String -> String
longestString xs ys =
    if (length xs) >= (length ys)
    then xs
    else ys
```

## Exercise 20

```
{-
20- Write a program that takes two strings as input and returns the greater one.
-}

greatestString :: String -> String -> String
greatestString xs ys = if xs >= ys then xs else ys
```



## Exercise 21

```
{-  
  
21- Write a program that takes as input a string  
and returns the number of characters it is composed of  
  
-}  
  
-- first solution  
numChar1 :: String -> Int  
numChar1 = length  
  
-- second solution  
numChar2 :: String -> Int  
numChar2 "" = 0  
numChar2 (_:xs) = 1 + numChar2 xs
```

## Exercise 22

```
{-  
  
22- Write a program that takes a string as input, and returns the same string converted to all  
uppercase.  
  
-}
```



```
import Data.Char (toUpper)

toUpperCase :: [Char] -> [Char]
toUpperCase = map toUpper

toUpperCaseRec :: [Char] -> [Char]
toUpperCaseRec [] = []
toUpperCaseRec (x:xs) = toUpper x : toUpperCaseRec xs
```

## Exercise 23

```
{-
23- Write a program that takes a string as input and checks
if it contains at least one 'A' among the first 10 characters.
-}
```

```
checkAInFirstTen :: String -> Bool
checkAInFirstTen str =
    if (length str) <= 10
    then 'A' `elem` str
    else 'A' `elem` take 10 str
```

## Exercise 24





```
{-  
  
24- Write a program that takes a string as input and counts how many digits it contains.  
Example "Hello2022! C6? " must give 5.  
  
-}
```

```
import Data.Char  
  
countDigitsRec :: [Char] -> Integer  
countDigitsRec [] = 0  
countDigitsRec (x:xs) =  
    if isDigit x  
    then 1 + countDigitsRec xs  
    else countDigitsRec xs  
  
countDigitsFold :: [Char] -> Integer  
countDigitsFold = foldr (\ x acc -> if isDigit x then 1 + acc else acc) 0
```

## Exercise 25

```
{-  
  
25- Write a program that takes a string as its input and counts  
how many uppercase letters, lowercase letters, digits and other characters it consists of  
Example  
    "Hello2022! C6? " must give:  
    uppercase: 2, lowercase: 4, digits: 5, others: 4.  
  
-}
```

```
import Data.Char  
  
countThem :: [Char] -> [Char]  
countThem xs =  
    let (uc,lc,dc,oc) =  
        foldr step (0,0,0,0) xs  
    where
```



```
step :: Char -> (Int, Int, Int, Int) -> (Int, Int, Int, Int)
step c (upp, low, dig, oth)
  | isUpper c = (upp + 1, low, dig, oth)
  | isLower c = (upp, low + 1, dig, oth)
  | isDigit c = (upp, low, dig + 1, oth)
  | otherwise = (upp, low, dig, oth + 1)
in "uppercase: " ++ show uc ++
  ", lowercase: " ++ show lc ++
  ", digits: " ++ show dc ++
  ", others: " ++ show oc
```

## Exercise 26

```
{-
26- Write a program that takes two strings of different lengths as input
and indicates whether the shortest is contained only once in the longest.
-}
```

```
import Data.List

removeAllBeforeOccurrence :: String -> String -> String
removeAllBeforeOccurrence smallone bigone =
  let occ = dropWhile (\x -> (smallone!!0 /= x)) bigone
      sm = take (length smallone) occ
  in if sm == smallone
     then drop (length smallone) occ
     else removeAllBeforeOccurrence smallone occ

myContains :: String -> String -> Bool
myContains "" _ = False
```



```
myContains smallone bigone =
  if not (isInfixOf smallone bigone)
  then False
  else
    let occ = removeAllBeforeOccurence smallone bigone
    in if  isInfixOf smallone occ
        then False
        else True

contains :: String -> String -> Bool
contains first second =
  if (length first) > (length second)
  then myContains second first
  else myContains first second
```

## Exercise 27

```
{-
27- Write a function that tells you whether or not a given String (or list) is a palindrome.
Here you'll want to use a function called reverse,
a predefined function that does what it sounds like.
reverse :: [a] -> [a]
reverse "blah" is "halb"
  Example:
  radar, rotor, madam, kayak, anilina, otto, elle

-}

-- first solution
isPalindrome :: Ord a => [a] -> Bool
isPalindrome xs = xs == reverse xs

-- second solution
```



```
isPalindromeRec :: Ord a => [a] -> Bool
isPalindromeRec [] = True
isPalindromeRec (x:xs) =
    x == last xs && isPalindrome (init xs)
```

## Exercise 32



```
{-
```

32- Given a number, determine whether or not it is valid per the Luhn formula. The Luhn algorithm is a simple checksum formula used to validate a variety of identification numbers, such as credit card numbers and Canadian Social Insurance Numbers. The task is to check if a given string is valid.

Validating a Number

Strings of length 1 or less are not valid. Spaces are allowed in the input, but they should be stripped before checking. All other non-digit characters are disallowed.

Example 1: valid credit card number

4539 3195 0343 6467

The first step of the Luhn algorithm is to double every second digit, starting from the right. We will be doubling

4\_3\_ 3\_9\_ 0\_4\_ 6\_6\_

If doubling the number results in a number greater than 9 then subtract 9 from the product. The results of our doubling:

8569 6195 0383 3437

Then sum all of the digits:

$8+5+6+9+6+1+9+5+0+3+8+3+3+4+3+7 = 80$

If the sum is evenly divisible by 10, then the number is valid. This number is valid!

Example 2: invalid credit card number

8273 1232 7352 0569

Double the second digits, starting from the right

7253 2262 5312 0539

Sum the digits

$7+2+5+3+2+2+6+2+5+3+1+2+0+5+3+9 = 57$

57 is not evenly divisible by 10, so this number is not valid.

```
-}
```

```
import Data.Char

isValidateCCNumber :: [Char] -> Bool
isValidateCCNumber [] = error "invalid number"
isValidateCCNumber [x] = error "invalid number"
isValidateCCNumber xs =

    let cleanxs = filter isDigit xs
        dgs = map digitToInt cleanxs
        dxs = doubleSndDigits dgs
        sm = sum dxs
    in sm `mod` 10 == 0
```



```
where
  doubleSndDigits :: [Int] -> [Int]
  doubleSndDigits xs =
    fst $
      foldr step ([], 0) xs
      where
        step x (ys, ind) =
          if even ind
          then (x:ys, ind + 1)
          else
            let xTime2 = 2*x
            in if xTime2 > 9
               then ((xTime2 - 9):ys, ind + 1)
               else (xTime2 :ys, ind + 1)
```

## Exercise 34

```
{-
34- Implement run-length encoding and decoding.
Run-length encoding (RLE) is a simple form of data compression, where runs (consecutive data
elements) are replaced by just one data value and count.
For example we can represent the original 53 characters with only 13.
"WWWWWWWWWWWWBWWWWWWWWWWWWBBBWWWWWWWWWWWWWWWWWWWWWWB" -> "12WB12W3B24WB"
RLE allows the original data to be perfectly reconstructed from the compressed data, which makes
it a lossless data compression.
"AABCCCDEEEE" -> "2AB3CD4E" -> "AABCCCDEEEE"
For simplicity, you can assume that the unencoded string will only contain the letters A through Z
(either lower or upper case) and whitespace. This way data to be encoded will never contain any
numbers and numbers inside data to be decoded always represent the count for the following character.
-}
```

```
import Data.List
import Data.Char

runLenght :: [Char] -> [Char]
```



```
runLenght [] = []
runLenght xs =
  let grouped = group xs
      grouped' = map countGroups grouped
  in concat grouped'
where
  countGroups :: [Char] -> [Char]
  countGroups ys =
    if size == 1
    then ys
    else show size ++ [head ys]
    where size = length ys

unRunLenght :: [Char] -> [Char]
unRunLenght [] = []
unRunLenght xs =
  let grouped = groupBy (\x y -> isDigit x && isDigit y) xs
      original = expand grouped
  in original
where
  expand :: [[Char]] -> [Char]
  expand [] = []
  expand (xs:xss) =
    if all isTrue $ fmap isDigit xs
    then replicate n (head $ head xss) ++ expand (tail xss)
    else xs ++ expand xss
    where
      n = toDigit xs
      toDigit :: [Char] -> Int
      toDigit x = read x :: Int
      isTrue :: Bool -> Bool
      isTrue = (== True)
```