

# Multi Party Computation - Active Adversaries

## Computer Science Lab

### July 9, 2015

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**Abstract.** This project aimed at implementing a secure MPC protocol against active adversaries.

We implemented a protocol called SPDZ that belongs to the family of protocols in the preprocessing model. This protocol pushes all the expensive public-key machinery to the preprocessing phase. Then, in the online phase, it only uses cheap primitives, which gives us extremely efficient computations. In addition, this phase is actively secure against a dishonest majority of corrupted players.

This work is focused on the online phase.

**Keywords:** multi party computation, SPDZ

## 1 Introduction

Although secure multiparty computation was invented almost thirty years ago, only in the recent years these protocols were implemented and tested in practice. They can be divided in two camps essentially: based on Yao circuits or based on secret sharing. The ones based on Yao circuits are mainly focused on two party computations, but the ones based on secret sharing can be applied to a more general number of players.

The protocols based on secret sharing can be divided on those which consider only honest-but-curious adversaries and those which consider active adversaries. The latter are often presented in the preprocessing model in which is possible to produce random data that will be consumed during the online phase. SPDZ fits this model and provides full active security against a dishonest majority.

The goal of this project is to implement the online phase of SPDZ assuming a trusted dealer. This dealer provides the preprocessed data that would be generated in the offline phase.

**Report structure.** Bearing this in mind, this report will firstly address the theory behind this work in section 2; It will then in 3 explain the system's architecture and implementation choices; And, in section 4 a final appreciation of the work will be made, together with some suggestions for improvement.

## 2 SPDZ

As stated before, SPDZ is divided in two phases: offline and online. One key aspect of the offline phase is that it can occur without knowing neither the function to be computed

nor the inputs. This is good because both may not be known until the online phases starts. This asynchrony allows us to have very efficient and secure computations.

The protocol also supports full reactive computations: after one function is evaluated, another can be executed depending on the output of the first. This can go forever until the preprocessed data runs out.

Before we proceed, we shall first introduce some notations. Let  $n$  be the number of players and  $\mathbb{F}_q$  the finite field over which we will perform computations. Each player  $P_i$  has a share  $\alpha_i \in \mathbb{F}_q$  of a secret shared value  $\alpha = \alpha_1 + \dots + \alpha_n$ . This  $\alpha$  is known as the fixed MAC key. Each player  $P_i$  has also a secret key  $\beta_i$ .

**[a]**  $a \in \mathbb{F}_q$  is  $[\cdot]$ -shared if  $P_i$  holds a tuple  $(a_i, \gamma(a)_i)$  where  $a_i$  is an additive secret sharing of  $a$ , i.e.  $a = a_1 + \dots + a_n$ , and  $\gamma(a)_i$  is an additive secret sharing of  $\gamma(a) := \alpha \cdot a$ , i.e.

$$\gamma(a) = \gamma(a)_1 + \dots + \gamma(a)_n$$

**[[a]]**  $a \in \mathbb{F}_q$  is  $[[\cdot]]$ -shared if  $P_i$  holds a tuple  $(a_i, \gamma_1(a)_i, \dots, \gamma_n(a)_i)$  where  $a_i$  is an additive secret sharing of  $a$  and  $\forall j \in [1, n] : \gamma_j(a)_i$  is an additive secret sharing of  $\gamma_j(a) := \beta_j \cdot a$ , i.e.

$$\gamma_j(a) = \gamma_j(a)_1 + \dots + \gamma_j(a)_n$$

## 2.1 Offline Phase

The goal of this phase is to produce raw material to the online phase. With this, functions in the online phase can be computed more efficiently. In our implementation, this phase is replaced by a dealer that provides the data needed.

If  $rnd(x)$  returns a random  $y \in \mathbb{F}_q$ , then given an arbitrary  $x$ , the dealer can generate a tuple with shares of  $x$  with

$$(rnd(x), rnd(x), \dots, x - \sum_{i=1}^{n-1} x_i)$$

In order to multiply secret shared values during the online phase we will use Beaver's multiplication triples, i.e. shares of random values  $[a]$ ,  $[b]$ ,  $[c]$  such that  $a \cdot b = c$ . As we will see further in the document, to achieve commitment functionalities and to do batch-MAC-check of opened values, the dealer will have to deliver  $[[\cdot]]$ -shared values to players.

## 2.2 Online Phase

## 3 Implementation

## 4 Conclusions and Future Work

## References