

Digit Recognizer

Terris Becker, Travis Barton

June 28, 2018

1 Abstract

The attempt to classify hand written digits is a traditional beginning to machine learning techniques, much like “hello world” is for coding. This is an exploratory analysis into how 3 different techniques perform in their base forms with and without Principal Component Analysis. While there are many modifications that can be implemented to each technique that outperform their base counterparts, we will be mainly focused on their simplest forms. The main focus of this project will be the use of Support Vector Machines, K-Nearest Neighbor algorithms, and Random Forest algorithms, to analyze the Kaggle data science competition for digit recognition. [1]. We will also attempt to combine these three machine learning algorithms to form a structure named the BeckerBarton Device (BBD).

2 Data Description

The data comes from the Kaggle ‘Digit Recognizer’ data challenge utilizing the MNIST hand written digit database [2], which describes each observational unit as a picture of a handwritten digit “28 pixels in height and 28 pixels in width, for a total of 784 pixels in total. Each pixel has a single pixel-value associated with it, indicating the lightness or darkness of that pixel, with higher numbers meaning darker. This pixel-value is an integer between 0 and 255, inclusive.” Our data was in grey scale, we did not need to be concerned with the color of the digit, only with the shape. Since our algorithms do not care if the data is structured in a matrix or not, each observation will take the form of a row with 784 variables (one for each pixel). In order to determine which pixel corresponds to which variable, Kaggle provides the following description: “Each pixel column in the training set has a name like pixel_x , where x is an integer between 0 and 783, inclusive. To locate this pixel on the image, suppose that we have decomposed x as $x = i * 28 + j$, where i and j are integers between 0 and 27, inclusive. Then pixel_x is located on row i and column j of a 28×28 matrix, (indexing by zero)” [2]. Picture this as what you get after pulling a thread at the top of each picture and unraveling it pixel by pixel. The unraveled ‘thread’ is what will be fed into the BBD and other algorithms.

3 Methods

The BBD utilizes the decision making power of 3 different machine learning techniques, Support Vector Machines, K Nearest Neighbors, and Random Forest. Each one is able to distinguish certain numbers better than others. Through repeated sampling, we were able to establish a rough empirical distribution of which numbers each technique predicts best. The heart of the BBD is the utilization of each algorithms' strengths. Before describing the algorithm in detail, we will give a high level summary of each method. Although these techniques can be used for regression or categorization, we will only be looking at the classification techniques, as those are the only ones that pertain to our goal.

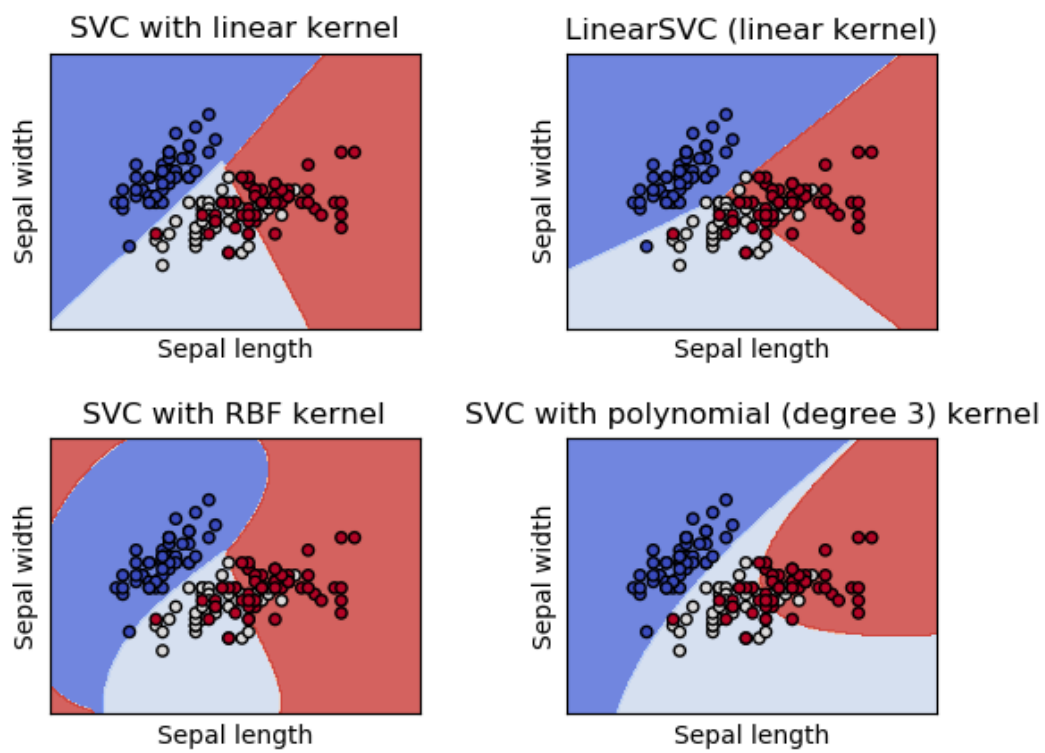
3.1 Principal Component Analysis

PCA is a method of dimensionality reduction that takes advantage of the correlation between the given variables to create new variables that are linear combinations of the old ones. This has several perks, including the fact that the new variables are guaranteed to be linearly independent of each other and that, often, a fraction of the new variables can explain almost all of the variability in that data. [3]

3.2 SVM

Support Vector Machines, or SVM, attempts to analyze data by creating m , n -dimensional hyperplanes planes that reduce the residual error as much as possible **Needs Citation**. These hyperplanes attempt to act as borders, separating the response into categories. Since we have 10 response values (digits 0-9) and a total of 784 pixel values, we need $m = 9$, 784-dimensional planes to separate them. The number of dimensions for each plane depends on how many predictors we use. Our "unraveled thread" contained the information from a 28x28 pixel image, so our planes each have $n = 784$ dimensions. For the purposes of explanation, we will look at the following 2 dimensional example. If one were to attempt draw a line that separates the red dots from the blue dots from the white dots, it would be impossible to do so perfectly with a strait line, no matter how it is rotated (figure 1). Luckily, SVM allows for planes to have varying degrees of "curviness" based on the γ parameter. Adjusting gamma can allow the model to be more or less stringent, too little and the model will not perform well, too much and the model will be overfit. Tuning the parameter to the perfect amount is difficult, but can be approximated via bootstrapping/sampling techniques. Another parameter to consider is the 'cost'. When drawing the planes that separate the data, SVM first finds the space between different regions where each response category is centered. The space can carry in its 'emptiness' depending on the value of the cost. When no points are allowed in between each region, the model is called 'hard' and the cost parameter is 0. As the cost parameter is increased, more and more points are allowed to reside in the space between regions. Strict models rarely perform optimally, with many packages defaulting the cost value to 1. After tuning

Figure 1: Example of Support Vector Classification using different kernels



our model with the `linear.svc` function from the `sklearn` package, we used a cost parameter of .01. For a more in-depth look at SVM and the underlying math check out (INSERT HERE).(CITE) To further improve the accuracy of our SVM model within the BBD, we created 100 SVM models from different randomly subsetting training sets, then decided the category of new data via a vote from our 100 different models. This is done in the hopes that diversifying our selection process will aid in classifying borderline data points, and help us identify the structure of difficult to classify numbers.

3.3 KNN

That is the essence of KNN, training data is fit to a model, and the response of a new data point is determined by the responses of the k nearest points to the new point. in our case, nearest means smallest Euclidean distance, but other metrics can be used. The points that make up the k -nearest neighbors are called the neighborhood, and can be processed in different ways. The default way is to take the mode category of the neighborhood. Each point inside the neighborhood is asked what its response category is, and the category with the most points determines the prediction of the new point. This way, all points have an equal say in the decision, regardless of how far away they are from C . We decided that the distance between the point in the neighborhood and the new point should have an impact, so our voting scheme is weighted with a gaussian curve. Thus, closer points to the new point have a vote that is worth more than points that are farther away. KNN has some advantages over SVM, one of which is that the only parameter that needs to be tuned is the number of points inside of each neighborhood, k . To find the optimal k , we used the `tune` function from the `FNN` package. [4] Another is that model fitting and predictions can be done simultaneously, decreasing total run time. For a more in-depth look into KNN and the underlying math behind it, check out *Elements of Statistical Learning*, section 13.1. [5]

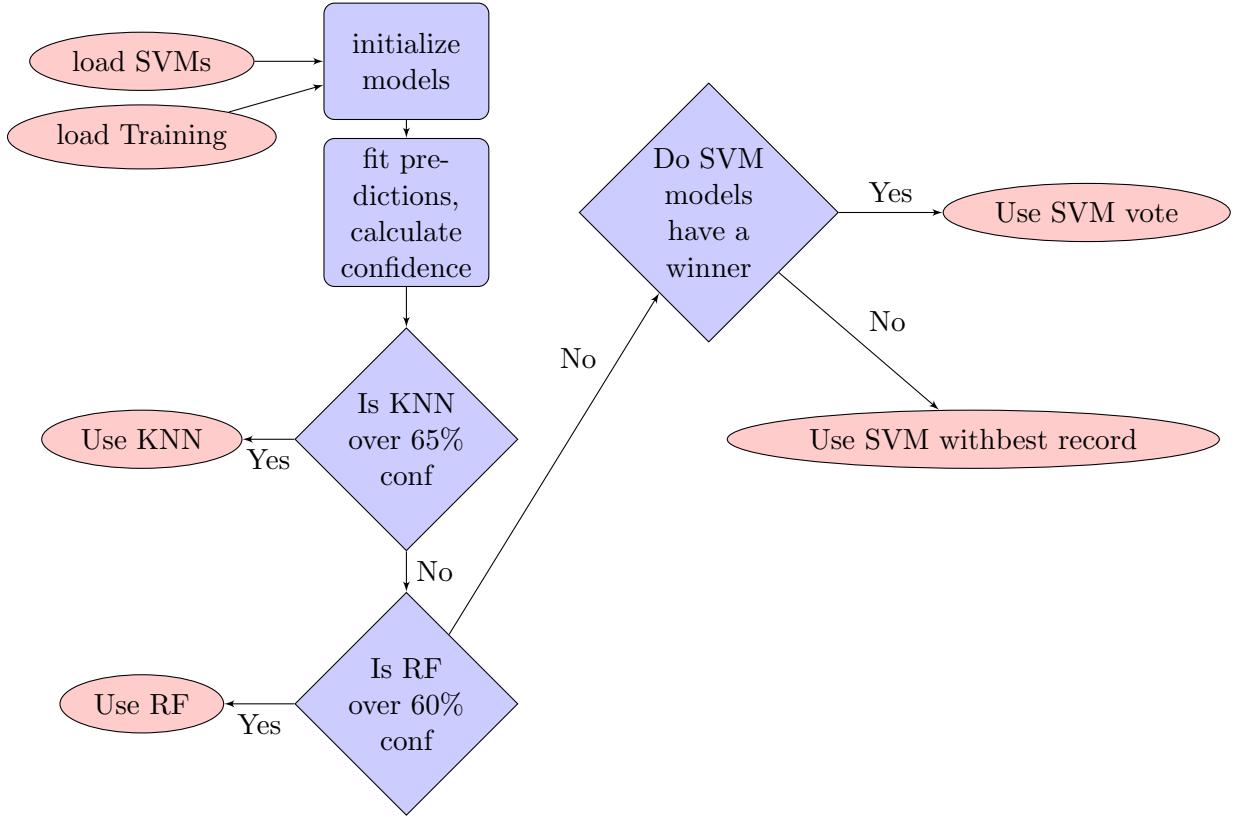
3.4 Random Forest Algorithm

The Random Forest Algorithm is the only one of the three utilized machine learning techniques that does not take into account all of the predictors all of the time. The principle behind the Random Forest Algorithm is to create N decision trees, and make a decision based on the winner of a vote where every tree gets an equal say. For more information on decision trees, check out *Elements of Statistical Learning*. [6] The number of trees used in each forest is determined based on computing power and possible subsets of the predictors. Decision trees can be overfit if too many predictors are fed through them, but ignoring large swathes of predictors underutilizes the information. The random forest algorithm solves this trade off by randomly subsetting M of the predictors and creating a decision tree based on those predictors, then repeating this process N times. This way, no individual tree is over fit, and all of the predictors are utilized. The number of trees that can

be created in our model is bounded by 784 choose M . It is important to note that many of the predictors in our data set were completely empty, and were thus removed prior to utilizing the model. The parameters to tune in a random forest model are the number of trees (N) and the number of predictors inside each tree (M). Using the `estimators` function inside the `sklearn.RandomForestClassifier` package, we decided on a $M = 10$ and an $N = 100$. For a more in-depth look into the Random Forest Algorithm and the underlying math behind it, check out *Elements of Statistical Learning*, chapter 15. [7]

3.5 Becker-Barton Device

The thought behind the Becker-Barton Device (BBD) is that the aggregate decisions of many algorithms each playing to their strengths should be more accurate than the algorithms on their own. The structure works by evaluating the certainty of each prediction. Within each algorithm, there are means of evaluating how certain it is about any given prediction. In Random Forest and KNN, this is The thought behind the Becker-Barton Device (BBD) is that the aggregate decisions of many algorithms each playing to their strengths should be more accurate than the algorithms on their own. The structure works by evaluating the certainty of each prediction. Within each algorithm, there are means of evaluating how certain it is about any given prediction. In Random Forest and KNN, this is decided by the ratio of votes, in SVM it is decided by its proximity to the different hyperplanes. The BBD starts with loading in the training data, as well as the 100 SVM models that were pre-trained on subsets of the training data. The other models are then initialized, their predictions are made, and their certainties are calculated. After that, the model looks first to KNN, if it is confident, then it trusts its prediction. It does the same for the Random Forest algorithm. If neither are confident, it turns to the different SVM models where it will go with the decision with the highest votes. Confidence cutoffs were decided if there is a tie, it chooses the number with the best track record thus far in our experiments. Below is a visualization of that process. decided by the ratio of votes, in SVM it is decided by its proximity to the different hyperplanes. The BBD starts with loading in the training data, as well as the 100 SVM models that were pre-trained on subsets of the training data. The other models are then initialized, their predictions are made, and their certainties are calculated. After that, the model looks first to KNN, if it is confident, then it trusts its prediction. It does the same for the Random Forest algorithm. If neither are confident, it turns to the different SVM models where it will go with the decision with the highest votes. Confidence cutoffs were decided by finding the minimum percent where the algorithm achieves its maximum accuracy (figure 4, 5). If there is a tie, it chooses the number with the best track record thus far in our experiments. ?Track record? was decided by empirical testing on the training data. Below is a visualization of that process.



4 Results

The performances of the 3 techniques and the BBD varied to some degree, but all preformed above 96% accuracy. While this may not compare to some neural network or XGboosting techniques, it is still noteworthy that their most baseline performance was so high. The results are chronicled by the table below:

Model	PCA Prior	Accuracy	Run Time
KNN	No		
Random Forest	No		
SVM	No		
BBD	No		
KNN	Yes		
Random Forest	Yes		
SVM	Yes		
BBD	Yes		

5 Future Work

6 Conclusion

References

- [1] <https://www.kaggle.com/c/digit-recognizer>, *kaggle*, 2018 ©
- [2] Kaggle. (1998). Digit Recognizer. Retrieved from <https://www.kaggle.com/c/digit-recognizer/data>
- [3] The Elements of Statistical Learning, Springer, 2017
- [4] Alina Beygelzimer, Sham Kakade, John Langford, Sunil Arya, David Mount and Shengqiao Li (2013). FNN: Fast Nearest Neighbor Search Algorithms and Applications. R package version 1.1.
- [5] "13.3 Nearest Neighbor Classifiers." The Elements of Statistical Learning, Springer, 2017, pp. 463-485.
- [6] "Decision Trees" The Elements of Statistical Learning, Springer, 2017, pp. 305-315.
- [7] "13.3 Nearest Neighbor Classifiers." The Elements of Statistical Learning, Springer, 2017, pp. 463-485.