Task 1 - Grid Game

January 1, 2023

1 Task 1 - Grid Game

```
[1]: # Import libraries
     import matplotlib.pyplot as plt
     import numpy as np
     # Set the seed for the random integer generators
     np.random.seed(46853)
[2]: # Prompt the player to enter the grid size
     grid_width = int(input("Enter the grid width: "))
     # Prompt the player to enter the grid size
     grid_height = int(input("Enter the grid height: "))
     # Prompt the player to enter the distribution parameters
     distribution_mean = float(input("Enter the distribution mean: "))
     distribution_stddev = float(input("Enter the distribution standard deviation:
      "))
    Enter the grid width: 15
    Enter the grid height: 11
    Enter the distribution mean: 4
    Enter the distribution standard deviation: 5
[3]: # Generate a grid with random cell values using a normal distribution based on
     ⇔the user input
     # and generate the integers to be between 0 and 9
     grid = [[np.around(np.clip(np.random.normal(distribution_mean,_
      ⇔distribution_stddev), 0, 9)).astype(int)
              for _ in range(grid_height)] for _ in range(grid_width)]
     # Define the start and goal positions
     start = (0, 0)
     goal = (grid_width - 1, grid_height - 1)
[4]: |# Simple Heuristic Algorithm - Not used but developed into the Dijkstra_
     →algorithm below
```

```
def heuristic_algorithm(beginning, end):
         # Create a set to store the visited nodes
         visited_nodes = set()
         # Create a queue for the nodes to visit and add the start node to the queue
         queue = [beginning]
         # Create a dictionary to store the came_from values of the nodes
         came_from_dict = {beginning: None}
         # While the queue is not empty
         while queue:
             # Get the next node in the queue
             current_node = queue.pop(0)
             # If the current node is the goal, return the came from dictionary
             if current_node == end:
                 return came_from_dict
             # Add the current node to the visited set
             visited_nodes.add(current_node)
             # For each neighbour of the current node
             for dx, dy in [(1, 0), (-1, 0), (0, 1), (0, -1)]:
                 # Calculate the position of the neighbour
                 x_pos, y_pos = current_node
                 neighbour = (x_pos + dx, y_pos + dy)
                 # If the neighbour is out of bounds or has been visited, skip it
                 if not (0 <= x_pos + dx < grid_width) or not (0 <= y_pos + dy <__

→grid_height) or neighbour in visited_nodes:
                     continue
                 # Set the came_from value of the neighbour to the current node
                 came_from_dict[neighbour] = current_node
                 # Add the neighbour to the queue
                 queue.append(neighbour)
[7]: # Dijkstra Algorithm developed from the Heuristic Algorithm
     def dijkstra(beginning, end):
         # Create a set to store the visited nodes
         visited_nodes = set()
```

→to the queue with a priority of 0

queue = [(0, beginning)]

Create a min-priority queue for the nodes to visit and add the start node,

```
# Create a dictionary to store the costs of the nodes
  cost_dict = {beginning: 0}
  # Create a dictionary to store the came from values of the nodes
  came_from_dict = {beginning: None}
  # While the queue is not empty
  while queue:
      # Sort the queue in ascending order by cost
      queue.sort(key=lambda x_sort: x_sort[0])
      # Get the node with the lowest priority
      cost, current_node = queue.pop(0)
      # If the current node is the goal, return the came from dictionary
      if current_node == end:
          return came_from_dict
      # Add the current node to the visited set
      visited_nodes.add(current_node)
      # For each neighbour of the current node
      for dx, dy in [(1, 0), (-1, 0), (0, 1), (0, -1)]:
          # Calculate the position of the neighbour
          x_pos, y_pos = current_node
          neighbour = (x_pos + dx, y_pos + dy)
          # If the neighbour is out of bounds or has been visited, skip it
          if not (0 <= x_pos + dx < grid_width) or not (0 <= y_pos + dy <__
→grid_height) or neighbour in visited_nodes:
              continue
          # Calculate the cost to reach the neighbour
          cost = cost_dict[current_node] + grid[x_pos][y_pos]
          # If the cost is lower than the current cost of the neighbour
          if cost < cost_dict.get(neighbour, float('inf')):</pre>
              # Update the cost of the neighbour
              cost_dict[neighbour] = cost
              # Add the neighbour to the queue with the calculated cost
              queue.append((cost, neighbour))
              # Set the came from value of the neighbour to the current node
              came_from_dict[neighbour] = current_node
```

```
[11]: # Find the shortest path using Dijkstra's algorithm
      came_from = dijkstra(start, goal)
      # Create a figure with a specified size
      fig = plt.figure(figsize=(grid_width, grid_height))
      # Rotate the grid to correct the position of the grid
      grid = np.rot90(grid, k=-1)
      # Display the grid as an image with no shading
      plt.imshow(grid, cmap=None, alpha=0)
      # Rotate the grid back to correct the position of the path
      grid = np.rot90(grid)
      # Display the numbers in the center of each grid square
      for i in range(grid_width):
          for j in range(grid_height):
              plt.text(i, j, grid[i][j], ha="center", va="center", color="black", u
       ⇔fontsize=20)
      # Reconstruct the path from the came_from dictionary
      path = []
      current = goal
      while current != start:
          path.append(current)
          current = came_from[current]
      path.append(start)
      # Get the coordinates of the points on the path
      x, y = zip(*path)
      # Draw the path on the grid
      plt.plot(x, y, c="green", linewidth=3, alpha=0.8)
      # Turn off the x-axis tick marks and labels
      plt.tick_params(axis='x', which='both', bottom=False, top=False,__
       →labelbottom=False)
      # Turn off the y-axis tick marks and labels
      plt.tick_params(axis='y', which='both', left=False, right=False,_
       ⇔labelleft=False)
      # Show the plot
      plt.show()
```

Task 2 - MNIST Dataset Neural Network

January 1, 2023

1 Task 2 - MNIST Dataset Neural Network

```
[1]: # Import libraries
import numpy as np
from keras.datasets import mnist
from matplotlib import pyplot as plt
```

```
[2]: # Load the MNIST dataset
     (X_train, y_train), (X_test, y_test) = mnist.load_data()
     # Preprocess the data
     X_train = X_train.reshape(60000, 784)
     X_test = X_test.reshape(10000, 784)
     X_train = X_train.astype('float32')
     X_test = X_test.astype('float32')
     X_train /= 255
     X_test /= 255
     # Convert the labels to categorical variables
     y_train = np.eye(10)[y_train]
     y_test = np.eye(10)[y_test]
     # Initialize the weights and biases
     weights = {}
     biases = {}
     # Initialize the input layer weights and biases
     weights['w1'] = np.random.randn(784, 512)
     biases['b1'] = np.zeros((1, 512))
     # Initialize the hidden layer weights and biases
     weights['w2'] = np.random.randn(512, 512)
     biases['b2'] = np.zeros((1, 512))
     # Initialize the output layer weights and biases
     weights['w3'] = np.random.randn(512, 10)
     biases['b3'] = np.zeros((1, 10))
```

```
# Set the learning rate
learning_rate = 0.01
# Set the dropout rate
dropout_rate = 0.5
# Set the number of epochs
num_epochs = 100
# Set the batch size
batch_size = 8
# Set the number of batches
num_batches = X_train.shape[0] // batch_size
# Create arrays for the accuracy and loss measurements
mean accuracies = []
mean_losses = []
def sigmoid(z):
    return 1 / (1 + np.exp(-z))
# Define the SGD optimiser
def sgd_optimiser(grad_w1, grad_b1, grad_w2, grad_b2, grad_w3, grad_b3,__
```

```
[4]: # Define the test for the sigmoid function
def test_sigmoid_layer():
    # Test 1: Check that the sigmoid function returns the expected output
    z = np.array([[-2, -1, 0, 1, 2]])
    expected_output = np.array([[0.119203, 0.268941, 0.5, 0.731059, 0.880797]])
    output = sigmoid(z)
```

```
[5]: # Train the model
     for epoch in range(num_epochs):
         # Shuffle the training data
         permutation = np.random.permutation(X_train.shape[0])
         X_train = X_train[permutation]
         y_train = y_train[permutation]
         # Loop over the batches
         for batch in range(num batches):
             # Get the batch data
             start = batch * batch size
             end = start + batch_size
             X batch = X train[start:end]
             y_batch = y_train[start:end]
             # Forward propagation
             z1 = X_batch.dot(weights['w1']) + biases['b1']
             a1 = sigmoid(z1)
             # Implement dropout
             mask = np.random.binomial(1, 1 - dropout_rate, size=a1.shape)
             a1 *= mask
             z2 = a1.dot(weights['w2']) + biases['b2']
             a2 = sigmoid(z2)
             # Implement dropout
             mask = np.random.binomial(1, 1 - dropout_rate, size=a2.shape)
             a2 *= mask
             z3 = a2.dot(weights['w3']) + biases['b3']
             a3 = sigmoid(z3)
```

```
# Calculate the loss
      loss = cross_entropy_loss(y_batch, a3)
      # Backward propagation
      grad_z3 = a3 - y_batch
      grad_w3 = a2.T.dot(grad_z3) / batch_size
      grad_b3 = np.sum(grad_z3, axis=0, keepdims=True) / batch_size
      grad_a2 = grad_z3.dot(weights['w3'].T)
      # Scale the gradients by the inverse of the dropout rate
      grad_a2 *= 1.0 / (1.0 - dropout_rate)
      grad_z2 = grad_a2 * sigmoid(z2) * (1 - sigmoid(z2))
      grad_w2 = a1.T.dot(grad_z2) / batch_size
      grad_b2 = np.sum(grad_z2, axis=0, keepdims=True) / batch_size
      grad_a1 = grad_z2.dot(weights['w2'].T)
      # Scale the gradients by the inverse of the dropout rate
      grad_a1 *= 1.0 / (1.0 - dropout_rate)
      grad_z1 = grad_a1 * sigmoid(z1) * (1 - sigmoid(z1))
      grad_w1 = X_batch.T.dot(grad_z1) / batch_size
      grad_b1 = np.sum(grad_z1, axis=0, keepdims=True) / batch_size
      # Update the weights and biases
      sgd_optimiser(grad_w1, grad_b1, grad_w2, grad_b2, grad_w3, grad_b3,_u
→learning_rate, weights, biases)
      # print statistics
      if batch % 1000 == 999: # print every 2000 mini-batches
          print("Batch: " + str(batch))
          running loss = 0.0
  print("Epochs:", epoch + 1)
  # Calculate the accuracy on the test set
  z1 = X_test.dot(weights['w1']) + biases['b1']
  a1 = sigmoid(z1)
  z2 = a1.dot(weights['w2']) + biases['b2']
  a2 = np.maximum(z2, 0) # ReLU activation function
  z3 = a2.dot(weights['w3']) + biases['b3']
  # Shift the input values down to prevent overflow
  z3_shift = z3 - np.max(z3, axis=1, keepdims=True)
```

```
# Calculate the softmax activations
a3 = np.exp(z3_shift) / np.sum(np.exp(z3_shift), axis=1, keepdims=True)
loss = cross_entropy_loss(y_test, a3)
mean_loss = loss / len(y_test)
mean_losses.append(mean_loss)
# Calculate the predictions
predictions = a3.argmax(axis=1)
# Calculate the number of correct predictions
num_correct = (predictions == y_test.argmax(axis=1)).sum()
# Calculate the mean accuracy
accuracy = num_correct / len(predictions)
# Store the accuracy in a list
mean_accuracies.append(accuracy)
# Print the accuracy
print(f'Accuracy: {accuracy:.4f}')
```

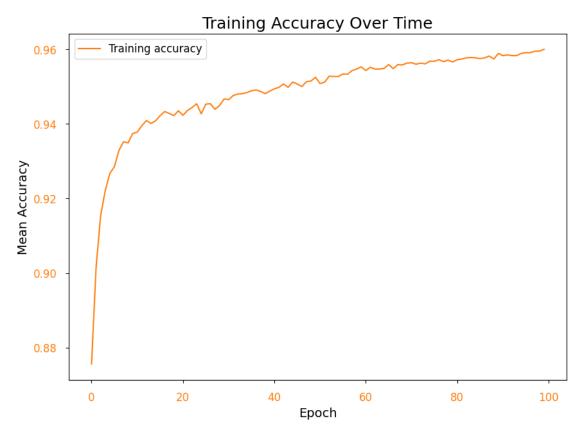
Batch: 999 Batch: 1999 Batch: 2999 Batch: 3999 Batch: 4999 Batch: 5999 Batch: 6999 Epochs: 1 Accuracy: 0.8756

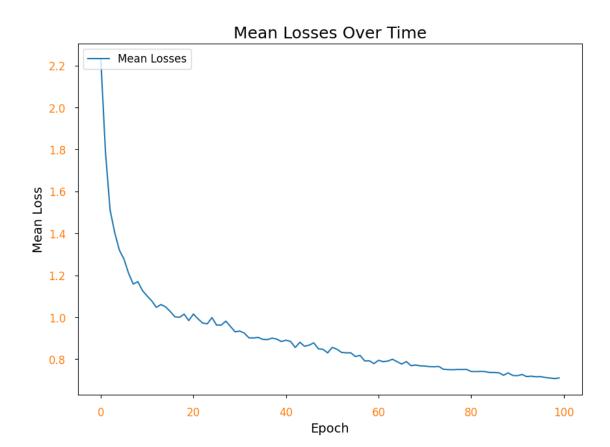
Batch: 999 Batch: 1999 Batch: 2999 Batch: 3999 Batch: 4999 Batch: 5999 Batch: 6999 Epochs: 2

Accuracy: 0.9016

Batch: 999 Batch: 1999 Batch: 2999 Batch: 3999 Batch: 4999 Batch: 5999 Batch: 6999 Epochs: 3

```
Accuracy: 0.9595
    Batch: 999
    Batch: 1999
    Batch: 2999
    Batch: 3999
    Batch: 4999
    Batch: 5999
    Batch: 6999
    Epochs: 100
    Accuracy: 0.9600
[6]: # Calculate the overall accuracy
     overall accuracy = sum(mean accuracies) / len(mean accuracies)
     # Print the overall accuracy
     print(f'Overall accuracy: {overall_accuracy:.3f}')
     # Calculate the overall loss
     overall_loss = sum(mean_losses) / len(mean_losses)
     # Print the overall accuracy
     print(f'Overall mean loss: {overall_loss:.3f}')
    Overall accuracy: 0.949
    Overall mean loss: 0.900
[7]: # Set the figure size
    plt.figure(figsize=(10, 7))
     # Plot the training accuracy
     plt.plot(mean_accuracies, color='tab:orange', label='Training accuracy')
     # Add a title and axis labels
     plt.title('Training Accuracy Over Time', fontsize=18)
     plt.xlabel('Epoch', fontsize=14)
     plt.ylabel('Mean Accuracy', fontsize=14)
     # Set the font size and style of the tick labels
     plt.tick_params(axis='both', which='major', labelsize=12, labelcolor='tab:
      ⇔orange', pad=10)
     # Add a legend
     plt.legend(loc='upper left', fontsize=12)
     # Show the plot
     plt.show()
     # Set the figure size
```





Task 3 - PyTorch

January 1, 2023

1 Task 3 - PyTorch

```
[1]: # Import libraries
     import torch
     import torchvision
     import torch.nn as nn
     import torch.nn.functional as F
     import torchvision.transforms as transforms
     import matplotlib.pyplot as plt
[2]: # Download and load the CIFAR-10 dataset
     # dataset = torchvision.datasets.CIFAR10(root='data/', download=True,,,
     ⇔transform=transforms.ToTensor())
     # Download and load the FASHION-MNIST dataset
     # dataset = torchvision.datasets.FashionMNIST(root='data/', download=True,_
     ⇔transform=transforms.ToTensor())
     # Download and load the KMNIST dataset
     dataset = torchvision.datasets.KMNIST(root='data/', download=True, __
      →transform=transforms.ToTensor())
     # Split the dataset into a training set and a test set
     num_train = int(0.8 * len(dataset))
     num test = len(dataset) - num train
     train_dataset, test_dataset = torch.utils.data.random_split(dataset,__
     →[num train, num test])
     # Create data loaders for the training and test sets
     batch_size = 8
     train_loader = torch.utils.data.DataLoader(train_dataset,__
      ⇒batch_size=batch_size, shuffle=True)
     test_loader = torch.utils.data.DataLoader(test_dataset, batch_size=batch_size,_u
      ⇔shuffle=False)
```

```
[3]: # # Network for CIFAR-10 # class CNN(nn.Module):
```

```
#
               self.conv1 = nn.Conv2d(3, 6, 5)
     #
               self.batch_norm1 = nn.BatchNorm2d(6) # Batch normalization layer
               self.pool = nn.MaxPool2d(2, 2)
     #
               self.conv2 = nn.Conv2d(6, 16, 5)
     #
               self.batch norm2 = nn.BatchNorm2d(16) # Batch normalization layer
     #
               self.fc1 = nn.Linear(16 * 5 * 5, 120)
     #
               self.dropout = nn.Dropout(p=0.5)
               self.fc2 = nn.Linear(120, 128)
     #
               self.batch norm3 = nn.BatchNorm1d(128) # Batch normalization layer
               self.fc3 = nn.Linear(128, 84)
               self.batch_norm4 = nn.BatchNorm1d(84) # Batch normalization layer
     #
               self.fc4 = nn.Linear(84, 10)
     #
           def forward(self, x):
               x = self.pool(F.relu(self.batch_norm1(self.conv1(x)))) # Batch_
      →normalization on the output of the first convolutional layer
               x = self.pool(F.relu(self.batch norm2(self.conv2(x)))) # Batch
      ⇔normalization on the output of the second convolutional layer
               x = x.view(-1, 16 * 5 * 5)
     #
               x = F.relu(self.fc1(x))
     #
               x = self.dropout(x)
               x = F.relu(self.batch norm3(self.fc2(x))) # Batch normalization on
      → the output of the second fully connected layer
               x = F.relu(self.batch_norm4(self.fc3(x))) # Batch normalization on #
      → the output of the third fully connected layer
               x = self.fc4(x)
               return x
[4]: # # Network for FASHION-MNIST
     # class CNN(nn.Module):
           def __init__(self):
               super(CNN, self).__init__()
     #
               self.conv1 = nn.Conv2d(1, 6, 3, stride=1, padding=1) # Change the_{\sqcup}
      →input channels and kernel size
               self.batch_norm1 = nn.BatchNorm2d(6)
     #
               self.pool = nn.MaxPool2d(2, 2)
     #
               self.conv2 = nn.Conv2d(6, 16, 3, stride=1, padding=1)
     #
               self.batch_norm2 = nn.BatchNorm2d(16)
               self.fc1 = nn.Linear(16 * 7 * 7, 120) # Change the input size to_{\square}
      →match the new feature map size
               self.dropout = nn.Dropout(p=0.5)
     #
               self.fc2 = nn.Linear(120, 128)
     #
               self.batch_norm3 = nn.BatchNorm1d(128)
     #
               self.fc3 = nn.Linear(128, 84)
               self.batch_norm4 = nn.BatchNorm1d(84)
```

def __init__(self):

#

super(CNN, self).__init__()

```
[5]: # Network for KMNIST
     class CNN(nn.Module):
         def __init__(self):
             super(CNN, self).__init__()
             self.conv1 = nn.Conv2d(1, 6, 3, stride=1, padding=1)
             self.batch_norm1 = nn.BatchNorm2d(6)
             self.pool = nn.MaxPool2d(2, 2)
             self.conv2 = nn.Conv2d(6, 16, 3, stride=1, padding=1)
             self.batch norm2 = nn.BatchNorm2d(16)
             self.fc1 = nn.Linear(16 * 7 * 7, 120)
             self.dropout = nn.Dropout(p=0.5)
             self.fc2 = nn.Linear(120, 128)
             self.batch norm3 = nn.BatchNorm1d(128)
             self.fc3 = nn.Linear(128, 84)
             self.batch_norm4 = nn.BatchNorm1d(84)
             self.fc4 = nn.Linear(84, 10)
         def forward(self, x):
             x = self.pool(F.relu(self.batch_norm1(self.conv1(x))))
             x = self.pool(F.relu(self.batch_norm2(self.conv2(x))))
             x = x.view(-1, 16 * 7 * 7) # Change the shape of the feature maps
             x = F.relu(self.fc1(x))
             x = self.dropout(x)
             x = F.relu(self.batch_norm3(self.fc2(x)))
             x = F.relu(self.batch_norm4(self.fc3(x)))
             x = self.fc4(x)
             return x
```

```
[6]: # Define the model
model = CNN()
criterion = nn.CrossEntropyLoss()
optimiser = torch.optim.SGD(model.parameters(), lr=0.0066)
# Define lists to store the training loss and accuracy
```

```
train_losses = []
mean_accuracies = []
```

```
[7]: # Train the CNN
     for epoch in range(50): # loop over the dataset multiple times
         running loss = 0.0
         running_accuracy = 0.0
         num batches = 0
         for i, data in enumerate(train_loader, 0):
             # get the inputs; data is a list of [inputs, labels]
             inputs, labels = data
             # zero the parameter gradients
             optimiser.zero_grad()
             # forward + backward + optimize
             outputs = model(inputs)
             loss = criterion(outputs, labels)
             loss.backward()
             optimiser.step()
             # Calculate the accuracy for this mini-batch
             accuracy = (outputs.argmax(dim=1) == labels).float().mean().item()
             # Adds this to the running accuracy
             running_accuracy += accuracy
             num_batches += 1
             # print statistics
             running_loss += loss.item()
             if i % 500 == 499: # print every 2000 mini-batches
                 print('[%d, %5d] loss: %.3f' %
                       (epoch + 1, i + 1, running_loss / 2000))
                 train_losses.append(running_loss / 2000)
                 print("Accuracy: " + str(accuracy))
                 running_loss = 0.0
         # Calculate the mean accuracy for the epoch
         mean_accuracy = running_accuracy / num_batches
         mean_accuracies.append(mean_accuracy)
```

```
[1, 500] loss: 0.463
Accuracy: 0.375
[1, 1000] loss: 0.313
Accuracy: 0.75
[1, 1500] loss: 0.246
Accuracy: 0.875
```

```
[49, 2000] loss: 0.019
    Accuracy: 1.0
    [49, 2500] loss: 0.012
    Accuracy: 1.0
    [49, 3000] loss: 0.015
    Accuracy: 1.0
    [49, 3500] loss: 0.015
    Accuracy: 1.0
    [49, 4000] loss: 0.017
    Accuracy: 0.875
    [49, 4500] loss: 0.013
    Accuracy: 1.0
    [49, 5000] loss: 0.015
    Accuracy: 0.875
    [49, 5500] loss: 0.019
    Accuracy: 1.0
    [49, 6000] loss: 0.017
    Accuracy: 1.0
    [50, 500] loss: 0.013
    Accuracy: 1.0
    [50, 1000] loss: 0.016
    Accuracy: 1.0
    [50, 1500] loss: 0.014
    Accuracy: 0.875
    [50, 2000] loss: 0.015
    Accuracy: 1.0
    [50, 2500] loss: 0.012
    Accuracy: 1.0
    [50, 3000] loss: 0.015
    Accuracy: 1.0
    [50, 3500] loss: 0.017
    Accuracy: 1.0
    [50, 4000] loss: 0.015
    Accuracy: 1.0
    [50, 4500] loss: 0.016
    Accuracy: 0.875
    [50, 5000] loss: 0.016
    Accuracy: 1.0
    [50, 5500] loss: 0.014
    Accuracy: 0.875
    [50, 6000] loss: 0.015
    Accuracy: 0.875
[8]: # Evaluate the CNN on the test set
     correct = 0
     total = 0
     with torch.no_grad():
```

```
for data in test_loader:
    images, labels = data
    outputs = model(images)
    _, predicted = torch.max(outputs.data, 1)
    total += labels.size(0)
    correct += (predicted == labels).sum().item()

print('Accuracy of the network on the test images: %d %%' % (
    100 * correct / total))
```

Accuracy of the network on the test images: 96 %

```
[9]: # Set the figure size
    plt.figure(figsize=(10, 7))
     # Set the colors for the lines and markers
     train_color = 'tab:blue'
     test_color = 'tab:orange'
     lr_color = 'tab:green'
     # Plot the training loss
     plt.plot(train_losses, color=train_color, label='Training loss')
     # Add a title and axis labels
     plt.title('Training Loss Over Time', fontsize=18)
     plt.xlabel('Epoch', fontsize=14)
     plt.ylabel('Loss', fontsize=14)
     # Set the font size and style of the tick labels
     plt.tick_params(axis='both', which='major', labelsize=12,__
      ⇒labelcolor=train_color, pad=10)
     # Add a legend
     plt.legend(loc='upper right', fontsize=12)
     # Show the plot
     plt.show()
     # Set the figure size
     plt.figure(figsize=(10, 7))
     # Plot the training accuracy
     plt.plot(mean_accuracies, color=test_color, label='Training accuracy')
     # Add a title and axis labels
     plt.title('Training Accuracy Over Time', fontsize=18)
     plt.xlabel('Epoch', fontsize=14)
```

