# CSE 599B-SP24: Reinforcement Learning Homework 3 - Model Based RL

Due Wednesday May 31 @ 11:59pm PST

The goal of this homework is to get a basic understanding of MBRL. In particular, you will be implementing random MPC with shooting, MPPI and ensemble MPPI. Please refer to the git link for the assignment https://github.com/WEIRDLabUW/cse542-sp24-hw3

Related Lectures: This homework largely involves knowledge from Lecture 10 and Lecture 11 on Model Based RL.

Collaboration: Students can discuss questions, but each student MUST write up their own solution, and code their own solution. We will be checking code/PDFs for plagiarism.

Late Policy: This assignment may be handed in up to 5 days late. If you have used up your 10 late days this quarter, there will be a penalty of 10% of the maximum grade per day.

### 1 Code Overview

The starter code is written in Python and depends on NumPy and Matplotlib as well as Pytorch. If you are new to Pytorch, please refer to the following tutorial [Link]. The README describes how to install packages in a conda environment to solve this assignment. We also provide a link to a Google Colab notebook below that can be used for cloud execution. We recommend either using a Linux machine or using the Colab, rather than Windows. This section gives a brief overview and the README provides detailed instructions.

- main.py overall launcher with environment creation and policy alternation [DO NOT MODIFY]
- environment.yml Conda env file to install dependencies [DO NOT MODIFY]
- utils.py functions for data collections and networks. [DO NOT MODIFY]
- evaluate.py Evaluating learned policy reward and success rate [DO NOT MODIFY]
- planning\_mbrl.py implementation of single and ensemble mbrl [TODO]
- train\_model.py training networks [TODO]

Environment Details This is the same conda environment as in HW1, so feel free to reuse that environment. Otherwise, to get started, you must install the correct dependencies for the code to run. There are several ways to do this - if you have a Linux machine, install a conda environment (install Anaconda from here https://docs.anaconda.com/free/anaconda/install/index.html) with the correct dependencies from the provided environment.yml file using the following command

conda env create -f environment.yml conda activate cse542a1

This should give you an environment with all the necessary dependencies, and you can run the code by running main.py as described in each section below.

If you do not have a Linux machine, it is advisable for you to use Google Colab instead. This will provide you with a single GPU instance that should be sufficient to run this code. The Colab instance can be found https://colab.research.google.com/drive/100eyKIKSaOfctpCb9ei8-HOOldogqn2M, and all the installs are completed by just running the initial cells inline. Please come talk to the course staff if you are having environment setup issues!

The reacher environment is the same as in homework 1, which is 2D environment where a double-jointed arm aims to move its end effector to a target location. You may refer to this follow link for further details: [Link].

# 2 Random MPC with Shooting [30 points]

```
$ python main.py --task policy_gradient
```

Model Predictive Control (MPC) is a method that optimizes a sequence of actions and achieves the best performance according to the reward function. It predicts the future states or observations of the system and adjusts its actions based on the prediction. In this part, you will implement one common technique in MPC: random MPC with shooting. In particular, instead of using a deterministic optimization method to find the best action, you sample N trajectory randomly from the action space. Each trajectory is evaluated by calculating the total rewards from the predicted observation of the network. The trajectory that yields the highest total reward is selected and its first action will be your action. This process is repeated at each step, and we can use the model prediction to keep updating the action using the current observation.

## 2.1 Random MPC with Shooting Pseudocode

```
def plan_model_random_shooting(env, state, ac_size, horizon, model, reward_fn, n_samples_mpc=100):
   #Initialize state and sample random_actions
   state_repeats = repeat(state, n_samples_mpc)
   random_actions = sample_uniform_random_actions(n_samples_mpc, horizon, ac_size, env.action_space)
   # Roll out based on the sampled random actions
   all_states, all_rewards = rollout_model(model, state_repeats, random_actions, horizon, reward_fn)
   # Compute the total rewards for each trajectory
   total_rewards = sum(all_rewards, axis=-1)
   # Select the trajectory with the highest total reward
   best_ac_idx = argmax(total_rewards)
   # use the first action from the best trajectory
   best_ac = random_actions[best_ac_idx, 0]
def rollout_model(model, initial_states, actions, horizon, reward_fn):
   all_states = []
   all_rewards = []
   curr_state = initial_states
   for j in range(horizon):
       curr_ac = actions[:, j]
       next_s = model(curr_state, curr_ac)
       next_r = reward_fn(next_s, curr_ac)
```

```
all_states.append(next_s)
all_rewards.append(next_r)
curr_state = next_s
return all_states, all_rewards
```

### 2.2 Expected Results

We provide an example below which serves as a reference for the expected output; You are expected to get a success rate higher than 0.25. please note that the success rate and reward may fluctuate:

```
$ python main.py --model_type single --plan_mode random_mpc
using device cuda
Episode: 0, reward: -44.39803820644873, max path length: 50
Episode: 1, reward: -17.73652850726456, max path length: 50
Episode: 2, reward: -16.54873229390969, max path length: 50
Episode: 3, reward: -17.09515906142727, max path length: 50
Episode: 4, reward: -13.370320994343928, max path length: 50
Episode: 5, reward: -16.10938280377134, max path length: 50
Episode: 6, reward: -15.057747536611572, max path length: 50
Episode: 7, reward: -15.66250521516793, max path length: 50
Episode: 8, reward: -16.894985734482116, max path length: 50
Episode: 9, reward: -16.185416048796206, max path length: 50
Episode: 10, reward: -16.945894300410362, max path length: 50
Episode: 11, reward: -15.591242310833053, max path length: 50
Episode: 12, reward: -14.094809423579566, max path length: 50
Episode: 13, reward: -13.313228855386575, max path length: 50
Episode: 14, reward: -14.6755356699752, max path length: 50
Success rate: 0.28
Average reward (success only): -13.936932248085684
Average reward (all): -15.29830527289742
```

#### 2.3 Execution

- 1. Fill in the blanks in the code marked with TODO in the plan\_model\_random\_shooting function in planning\_mbrl.py.
- 2. Fill in the blanks in the code marked with TODO in the rollout\_model function in planning\_mbrl.py.
- 3. Plot the reward during the training with default hyperparameters. Report the success rate and average reward using the evaluate function that is provided to you.

# 3 MPPI [30 points]

```
$ python main.py --model_type single --plan_mode mppi
```

Random MPC with shooting provides a simple yet effective way to handle control problems by randomly sampling action sequences and selecting the best one based on predicted rewards, but it may not be the best method for more complex environments.

Model Predictive Path Integral (MPPI) Control is a more efficient approach compared to MPC. Unlike random MPC that samples actions uniformly from the action space, MPPI optimizes action sequences using importance sampling, focusing on trajectories with higher rewards rather than sampling uniformly. This method provides a more efficient exploration of the action space, helping us to converge faster to optimal actions. In particular, the idea of a standard MPPI is to sample action sequences according to their weights computed by the exponential of their returns. This helps to focus on trajectories with higher expected rewards and its faster to find the optimal actions.

### 3.1 MPPI Pseudocode

```
def plan_model_mppi(env, state, ac_size, horizon, model, reward_fn,
                      n_samples_mpc=100, n_iter_mppi=10,
                      gaussian_noise_scales):
   #Initialize state and sample random_actions
   state_repeats = repeat(state, n_samples_mpc)
   random_actions = sample_uniform_random_actions(n_samples_mpc, horizon, ac_size, env.action_space)
   # Compute initial rollout using the model
   all_states, all_rewards = rollout_model(model, state_repeats, random_actions, horizon, reward_fn)
   all_returns = sum(all_rewards along the last axis)
   # Iterate through a few iterations of MPPI
     for iter in range(n_iter_mppi):
       # Weight trajectories by exponential of returns
       weights = compute_expotential_return(all_return)
       # Compute weighted sum of actions
       weighted_sum = sum(random_actions * weights, axis=0)
       # compute mean and std of the best trajectories
       action_mean = weighted_sum.flatten()
       action_std = ones(weighted_sum.shape) * gaussian_noise_scales[iter]
       # Sample new actions
       random_actions = sample_actions(action_mean, action_std, n_samples_mpc)
       # Perform rollout with new actions using the model
       all_states, all_rewards = rollout_model(model, state_repeats, random_actions, horizon,
           reward fn)
       all_returns = sum(all_rewards)
   # Identify the best action based on final rollouts
   # Select the trajectory with the highest total reward
   best_ac_idx = argmax(total_rewards)
   # use the first action from the best trajectory
   best_ac = random_actions[best_ac_idx, 0]
   return best_ac, random_actions[best_ac_idx]
```

### 3.2 Expected Results

We provide an example below which serves as a reference for the expected output; You are expected to get a success rate higher than 0.25. please note that the success rate and reward may fluctuate:

```
$ python main.py --model_type single --plan_mode mppi
using device cuda
Episode: 0, reward: -45.0685292711599, max path length: 50
Episode: 1, reward: -8.028816349416811, max path length: 50
Episode: 2, reward: -11.181899229796787, max path length: 50
Episode: 3, reward: -10.187376193755673, max path length: 50
Episode: 4, reward: -7.974100628605427, max path length: 50
Episode: 5, reward: -12.418430370016777, max path length: 50
Episode: 6, reward: -9.837710231454908, max path length: 50
Episode: 7, reward: -8.775532875691537, max path length: 50
Episode: 8, reward: -10.247916344380988, max path length: 50
Episode: 9, reward: -9.131945952749149, max path length: 50
Episode: 10, reward: -5.747245489228223, max path length: 50
Episode: 11, reward: -8.331408758062988, max path length: 50
Episode: 12, reward: -8.474610788412223, max path length: 50
Episode: 13, reward: -7.870262004116912, max path length: 50
Episode: 14, reward: -9.202479269493242, max path length: 50
Success rate: 0.53
Average reward (success only): -5.447100768498477
Average reward (all): -7.627708552630046
```

### 3.3 Execution

- 1. Fill in the blanks in the code marked with TODO START-MPPI in the plan\_model\_mppi function in planning\_mbrl.py.
- 2. Plot the reward during the training with default hyperparameters. Report the success rate and average reward using the evaluate function that is provided to you.

## 4 Ensemble MPPI [30 points]

```
$ python main.py --model_type ensemble --plan_mode mppi
```

So far, you've implemented the standard single MPPI method, we can further improve this by introducing model ensembles. In environments especially with stochastic dynamics, single MPPI might be less accurate. Ensemble MPPI is simply using multiple networks instead of just one network. By leveraging multiple network predictions, Ensemble MPPI can better capture the dynamics of the environment and reduce the risk of overfitting to any single model's inaccuracies. Ensuring diversity is important for implementing an effective Ensemble MPPI. For example, each model can have their separate optimizer, batch size and learning rate, or using different architectures. The diversity helps the predictions are not overly biased by the single network, leading to a more stable and accurate policy.

## 4.1 Expected Results

When you execute the code, you may get similar outputs as below. You are expected to get a success rate higher than 0.4. Please note that the success rate and reward may fluctuate.

```
Episode: 0, reward: -43.46004802481881, max path length: 50
Episode: 1, reward: -10.8674283885565, max path length: 50
Episode: 2, reward: -12.883924277131664, max path length: 50
Episode: 3, reward: -8.933863638550225, max path length: 50
Episode: 4, reward: -8.313068222586896, max path length: 50
Episode: 5, reward: -7.589171558519515, max path length: 50
Episode: 6, reward: -9.222474745213445, max path length: 50
Episode: 7, reward: -7.393583362317796, max path length: 50
Episode: 8, reward: -6.579779976928853, max path length: 50
Episode: 9, reward: -7.697173480373474, max path length: 50
Episode: 10, reward: -6.232915190180099, max path length: 50
Episode: 11, reward: -8.142131283083632, max path length: 50
Episode: 12, reward: -5.390735122525843, max path length: 50
Episode: 13, reward: -6.648134272343903, max path length: 50
Episode: 14, reward: -5.465611595751769, max path length: 50
Success rate: 0.62
Average reward (success only): -5.194262059586056
Average reward (all): -6.475862579254006
```

\$ python main.py --model\_type ensemble --plan\_mode mppi

#### 4.2 Execution

- 1. Add Ensemble MPPI in the plan\_model\_mppi function in planning\_mbrl.py.
- 2. fill in TODO in the train\_model function in train\_model.py.
- 3. Plot the return during the training with default hyperparameters. Report the success rate and average reward using the evaluate function that is provided to you.

# 5 Discussion [10 points]

- 1. Compare Random MPC with shooting, MPPI and Ensemble MPPI. Discuss the strengths and weaknesses of each method.
- 2. Why is diversity important in an ensemble model? What techniques did you use to improve diversity in the ensemble MPPI?

### 6 Submission

We will be using the Canvas for submission of the assignments. Please submit the written assignment answers as a PDF. For the code, submit a zip file of the entire working directory.