

# STAT 242b/542b THEORY OF STATISTICS: COURSE SYLLABUS

**GRADING:** Weekly homework 40%, First test 30%, Second test 30%

**DISCUSSION SESSION:** Monday 8:00pm-9:00pm, 24 Hillhouse Ave.

**OFFICE HOURS:** MWF: In Classroom 10:15 to 10:25am (after class), then Stat Dept, Dana House (10:30am to 11am)

**TFs:** Xinyuan Chen, Xin Xu, Mingrui Zhang. Basement of Dana House.

## **WEEK 1: January 18,20. PROBABILITY REVIEW**

- \* Probability models and the situations in which they arise (Ch. 1,2,3).
- \* Expected values and variances of sample means. Use of the Central Limit Theorem. Normal approximation. Delta method. (Ch. 4,5).

## **WEEK 2: Jan 23,25,27. DISTRIBUTIONS BASED ON NORMAL**

- \* SOME MORE PROBABILITY FOR STATISTICS  
Normal, Chi-square, t, and F distributions for statistics based on the normal. (Ch. 6).
- \* METHOD OF MOMENTS and the Delta method (Ch. 8.3, 8.4)

## **WEEK 3: Jan 30. Feb 1,3. ESTIMATION (Ch. 8)**

- \* METHOD OF MAXIMUM LIKELIHOOD (Sections 8.3, 8.4, 8.5)

## **WEEK 4: February 6, 8,10. SAMPLING DISTRIBUTIONS, LARGE SAMPLE APPROXIMATIONS, RELATIVE EFFICIENCY (Sections 8.3, 8.4, 8.5).**

- \* Comparison of sampling distributions of MLE and other estimators. Relative efficiency.
- \* Notions of consistency, asymptotic normality, asymptotic variance and standard error.
- \* Consistency of the MLE.
- \* Asymptotic Normality of the MLE.

## **WEEK 5: February 13,15,17,20. SUFFICIENCY, RISK, AND BAYES PROCEDURES (Sec. 8.6-8.8).**

- \* Sufficiency and Likelihood factorization
- \* Mean Squared error. Bias and variance tradeoff.
- \* Unbiased estimators. Cramer-Rao inequality.
- \* Bayes estimators.

## **WEEK 6: February 22,24. TESTING STATISTICAL HYPOTHESES (Ch.9).**

- \* *Bayes' Formulation, Significance and Power, Neyman-Pearson Formulation.*
- \* Notions of simple and composite hypotheses concerning distributions and their parameters.
- \* Neyman-Pearson Lemma for optimal tests in simple versus simple cases.
- \* Generalized likelihood ratios for composite cases (not necessarily optimal).  
Simplifying the form of generalized likelihood ratios.
- \* Choosing the threshold of a test statistic according to the desired significance level.

**WEEK 7: February 27, March 1,3. MORE ON TESTING HYPOTHESES AND REVIEW**

- \* Tests for a specific value of a parameter.
  - one-sided alternatives. Uniformly most powerful tests made easy.
  - two-sided alternatives. Relationship with confidence intervals.
  - examples.
- \* Tests for goodness of fit of an estimated model.
  - Chi-square test statistic
  - Generalized likelihood ratio test statistic  
(both approximately Chi-square distributed under the null hypothesis.)
  - Accounting for degrees of freedom.
  - Example.
- \* Review of Inference
  - Selecting probability models.
  - Estimating parameters in the model.
  - Testing statistical hypotheses.

**WEEK 8: March 6,8,10. FIRST EXAM AND SUMMARIZING DATA**

**\* March 6. FIRST TEST**

Covering chapters 8, 9 and any additional material presented.

- \* March 8,10. **SUMMARIZING DATA** (a sampling of ch. 10).
  - Plotting and interpreting empirical distributions,
  - quantile-quantile plots, histograms, densities, stem & leaf, and box-plots.

**March 11-26. SPRING BREAK**

**WEEK 9: March 27,29,31. HYPOTHESIS TESTS: LOCATIONS IN 2 SAMPLES (Ch. 11).**

- \* Tests for location in independent samples
  - various tests do about the same thing.
  - specifics for tests of location depend on assumptions about the variances.
- \* Tests for paired samples
  - Reduces to a one-sample test regarding differences.
  - Easier and more accurate than with independent samples.
- \* Issues in the design of experiments.

**WEEK 10: April 3,5,7. HYPOTHESIS TESTS: LOCATIONS IN MANY SAMPLES (Ch. 12).**

- \* One-way layout
  - plots of means or medians (with box-plots).
  - multiple comparisons.
  - analysis of variance.
- \* Two-way layout
  - superimposed plots of mean response for each value of a second factor.
  - the additive model and its graphical interpretation.
  - tests for additive and interaction models.
  - analysis of variance.

**WEEK 11: April 10,12,14. LEAST SQUARES FITS OF LINES/CURVES (Ch. 14.1,14.2).**

- \* Solving and interpreting the least squares problem in linear regression.
  - Graphical interpretation (best fitting line)
  - Solution in terms of standardized variables (slope = correlation coefficient  $r$ )
  - Solution in terms of original variables
  - Pythagorean identity for sum of squared errors and its geometrical interpretation.
  - least squares projection yields residual vector which is orthogonal to the vector of the explanatory variable.
  - residual plots.
- \* Statistical Properties of the estimated parameters.
  - standard linear model with homoscedastic errors.
  - means, variances, and distribution of estimated parameters.
  - estimated variances, standard errors, confidence intervals.
  - heteroscedastic errors and non-linearities revealed through residual plots.
  - uses of transformations. Transforming inputs to correct for non-linearities.
  - Transforming outputs to correct for heteroscedasticity.
- \* Galton and the "regression" interpretation of least squares.

**WEEK 12: April 17,19,21. LINEAR LEAST SQUARES WITH MANY VARIABLES.**

- \* Iterative Projection Interpretation
- \* Matrix Interpretation
- \* Statistical Properties
  - Standard statistical model
  - Mean and covariance matrix of least squares estimates.
  - Estimation of  $\sigma^2$ .
  - Standard errors of coefficients.
  - Confidence intervals for coefficients.
  - Hypothesis tests concerning values of coefficients.
  - t-values and interpreting regression output (testing whether a coefficient is zero, when the others are not).
  - standard errors and confidence intervals for regression fits.
- \* Practice with multiple regression, tests and confidence intervals.

**WEEK 13: April 24,26. MODEL SELECTION.**

- \* Step-size selection by examination of largest magnitude t-value (merits and difficulties).
- \* Prediction error criterion (merits and difficulties).
- \* Practice with model selection by either method.

\* **April 28: SECOND TEST**