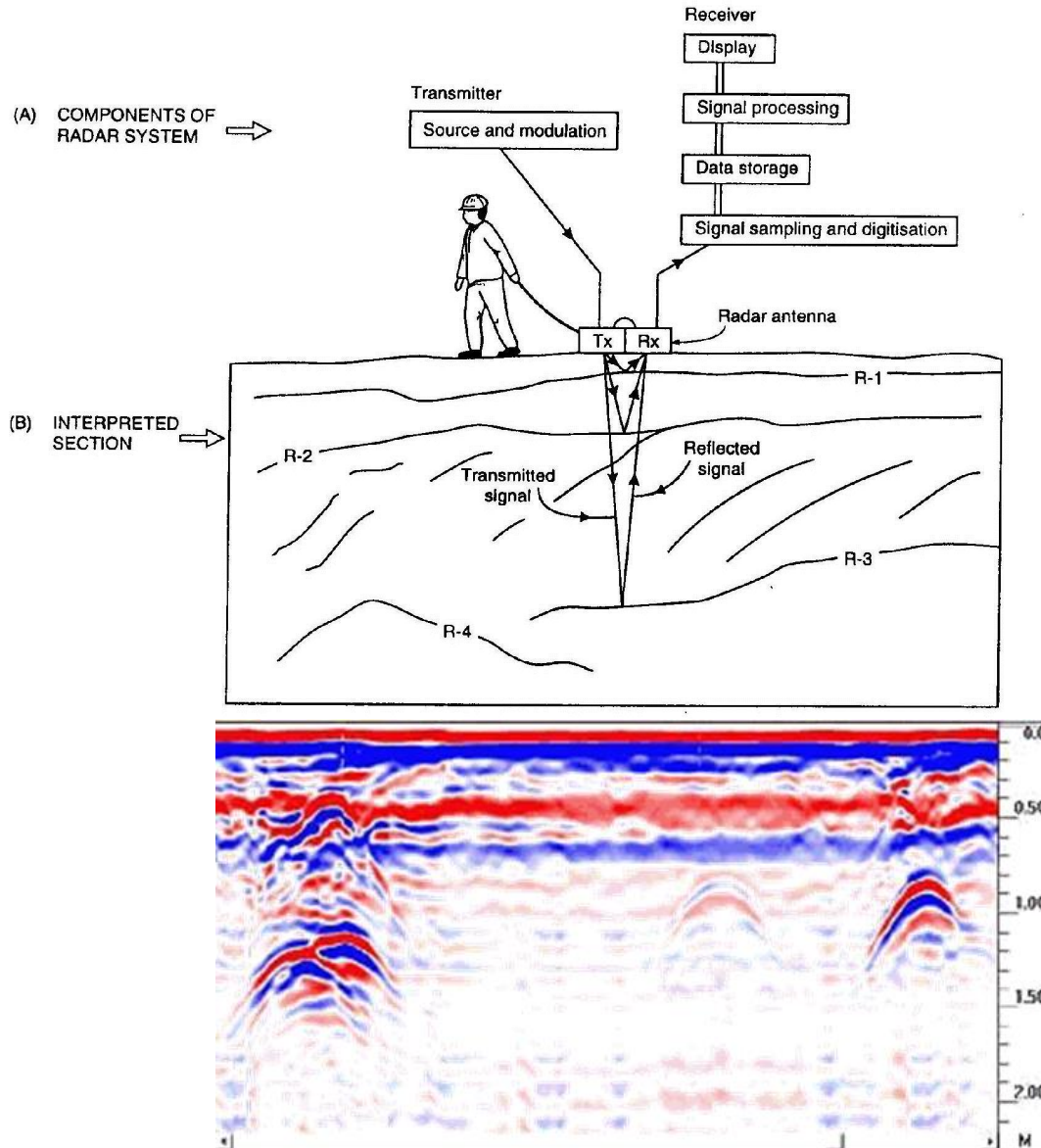


# Ground Penetrating Radar (day 1)

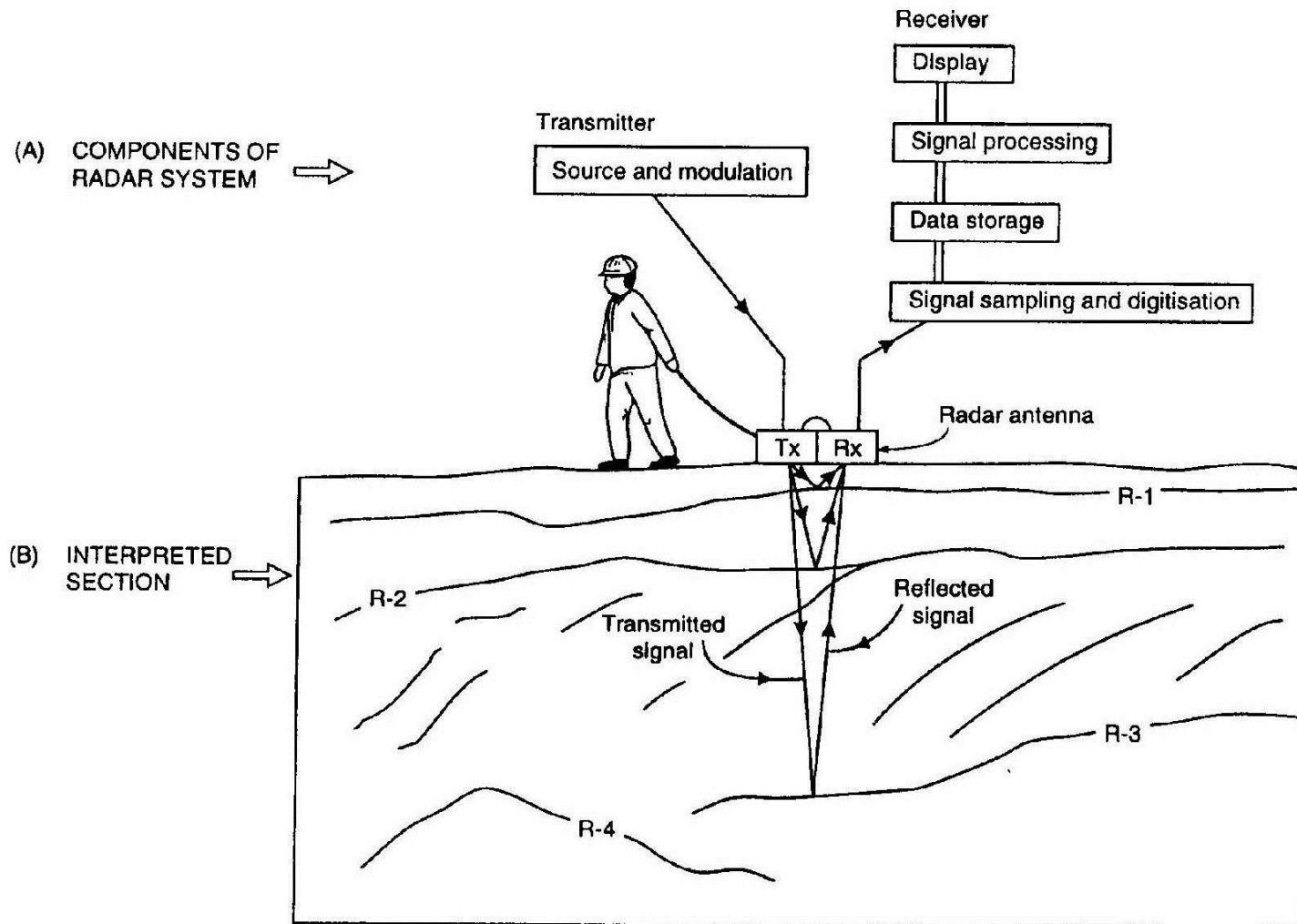


# Today's Topics

- Introduction to GPR
- Setup: Motivational Problems
- Physical Properties
  - Dielectric Permittivity and Radiowaves
  - Microwave Example
- Basic Principles:
  - Propagation of Radiowaves
  - Attenuation
  - Reflection and Refraction

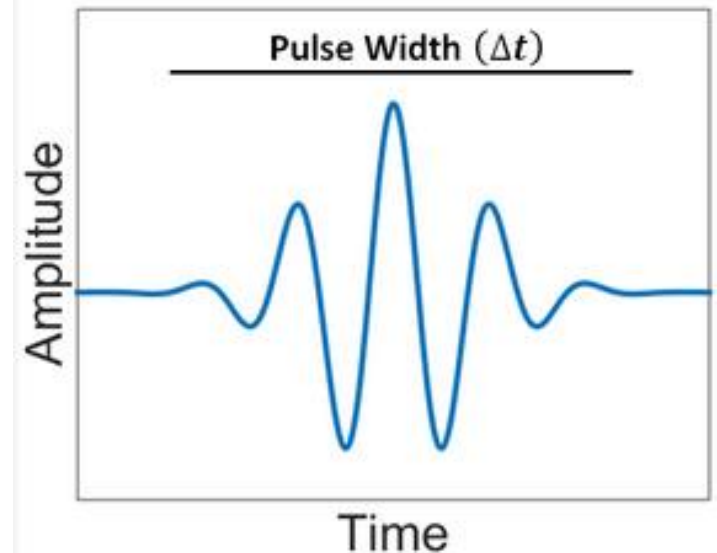
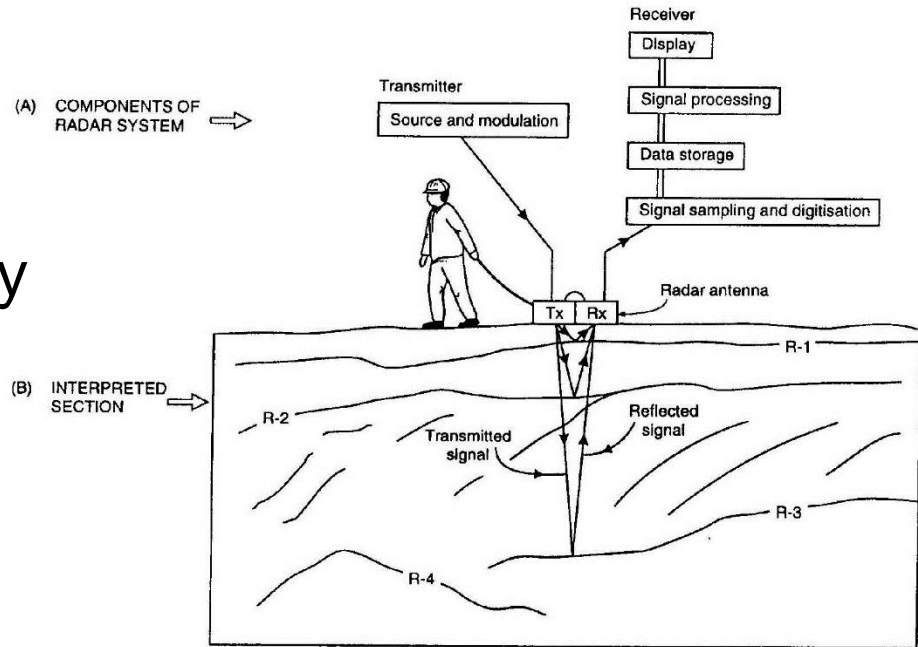
*\*See GPG introduction, physical properties  
and basic principles pages*

# Introduction to GPR



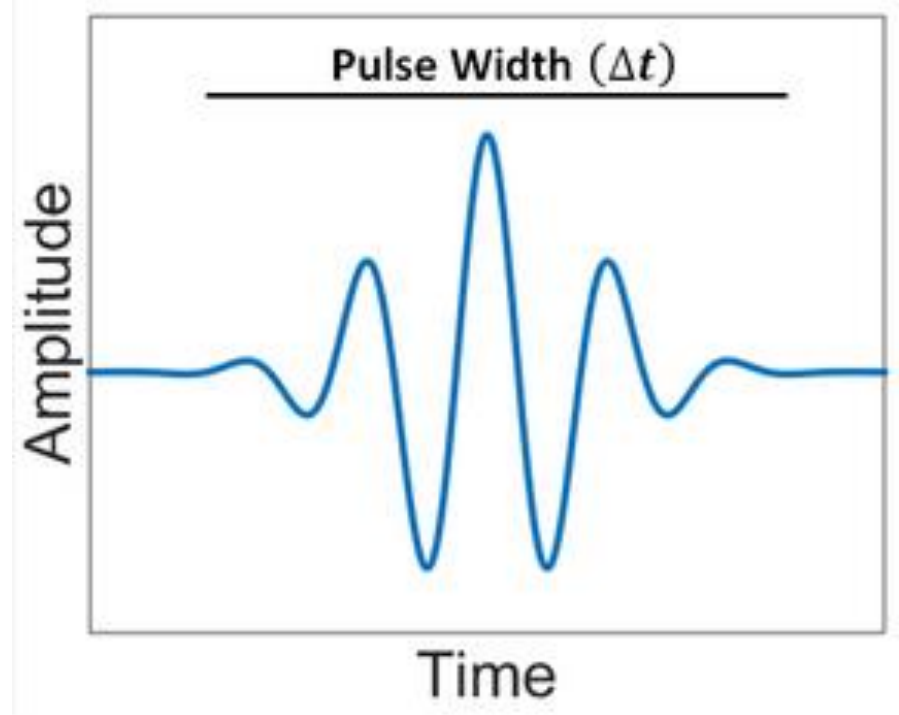
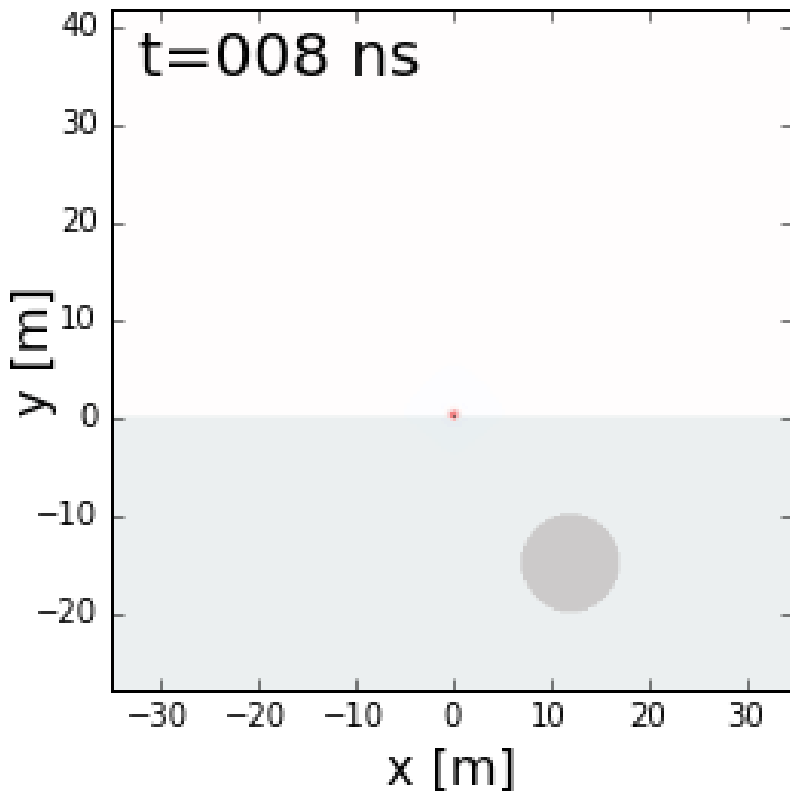
# Introduction to GPR

- GPR is an EM method (depends on  $\epsilon$ ,  $\sigma$ , and  $\mu$ )
- Uses a pulse of high-frequency radiowaves (10s MHz to GHz)
- Generally shallow surveys (10s of metres or less)
- Radiowaves reflect and refract at boundaries  
→ Theory very similar to seismic
- Radiowave propagation depends on Earth's EM properties



# Introduction to GPR: 2D Example

- Sends a **pulse** of waves **not** continuous waves
- What features/behaviours do you see?

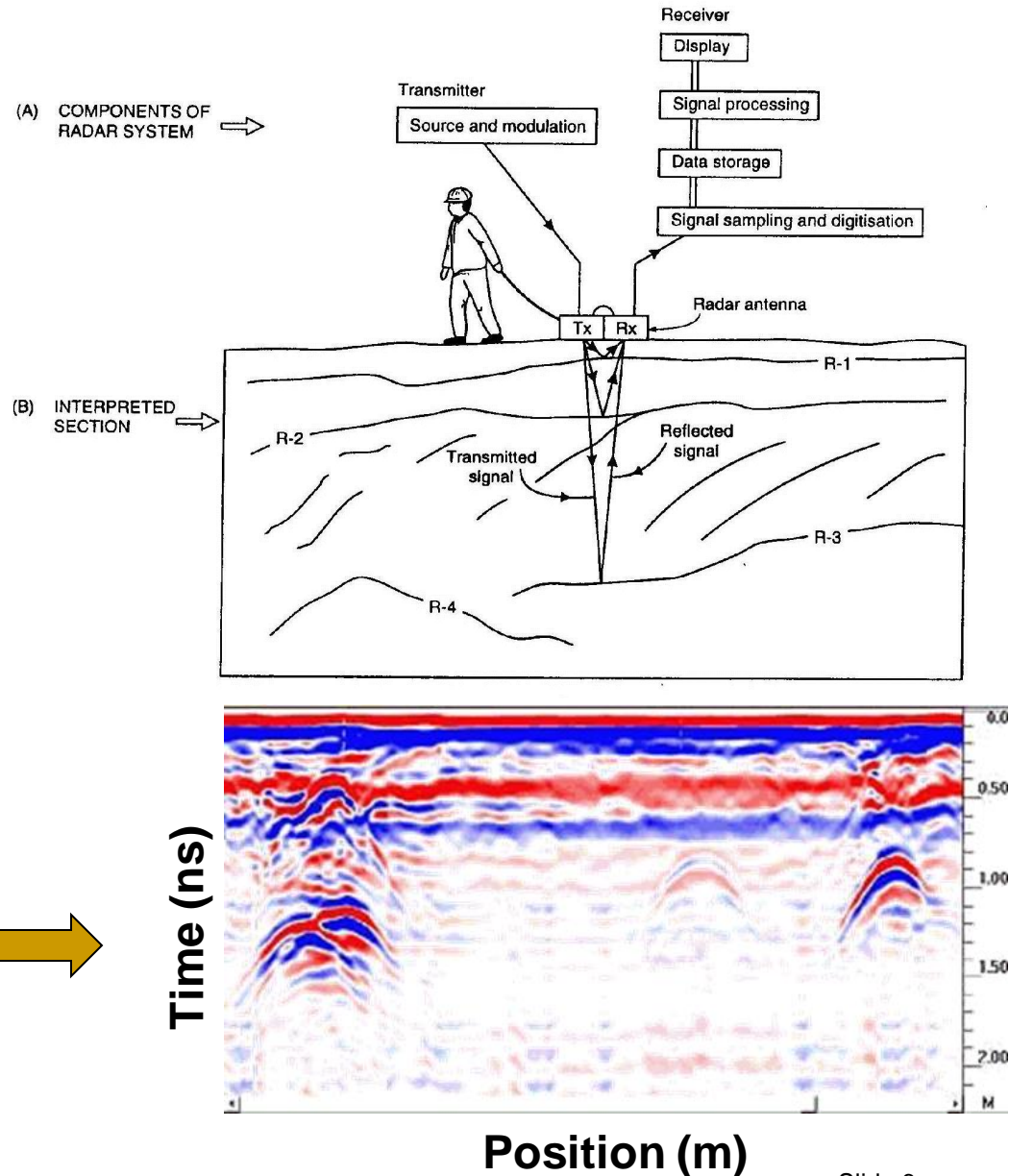




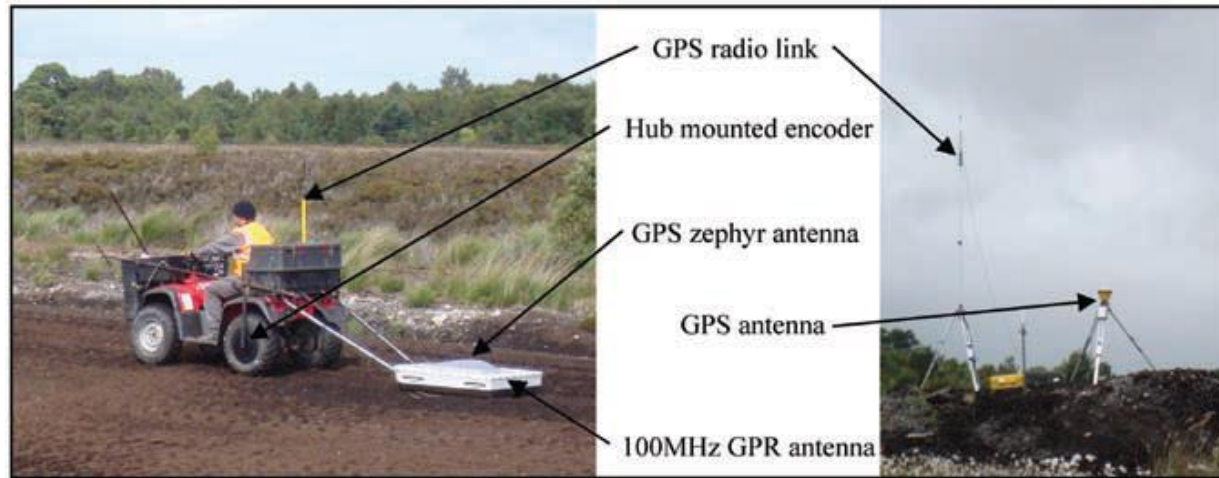
# Introduction to GPR

- Returning radiowave signals are measured
- These signals are represented using a **radargram**
- Radargrams essentially seismograms for GPR

**Radargram example**



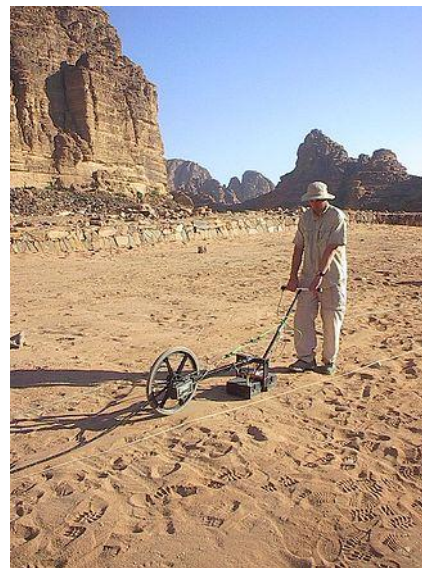
# Some Motivational Problems



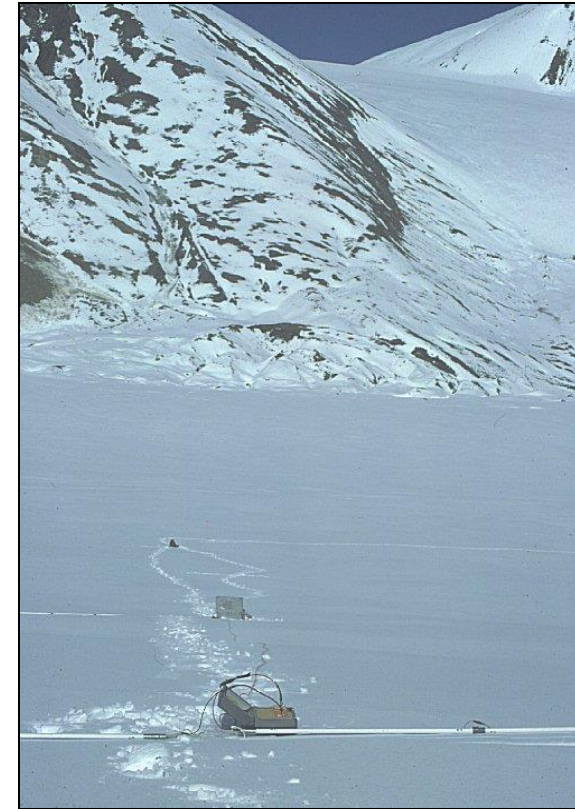
**Mapping Peat Thickness (Ireland)**



**Urban Geotechnical Problems**



**Archaeology (Jordan)**



**Mapping Ice Thickness (Antarctica)**

# Some Motivational Problems

- Looking for buried pipes, objects
- Investigating concrete structures, roads
- Ice/snow: avalanche, search and rescue
- Near surface soil conditions: salinity, saturation
- Geotechnical work (tunnels)
- Forensics
- Archaeology

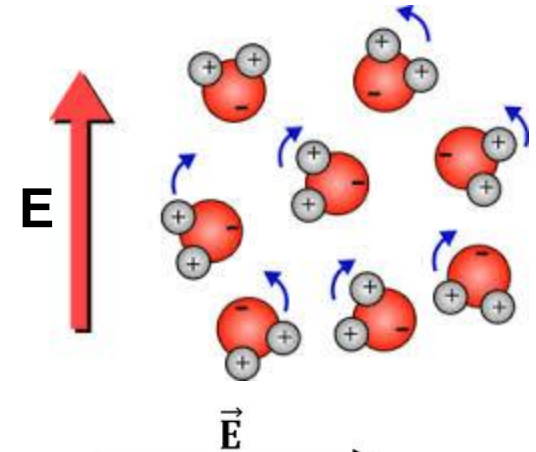
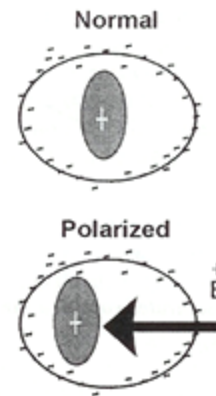
<http://sensoft.ca/>



# Physical Properties

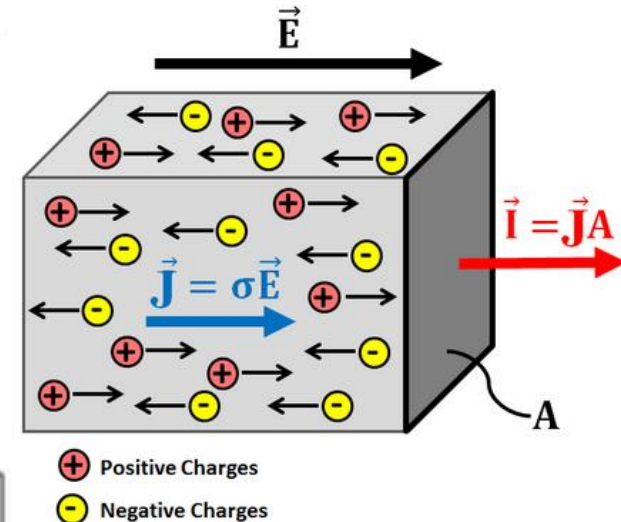
## Dielectric Permittivity ( $\epsilon$ ):

How easily a material is electrically polarized



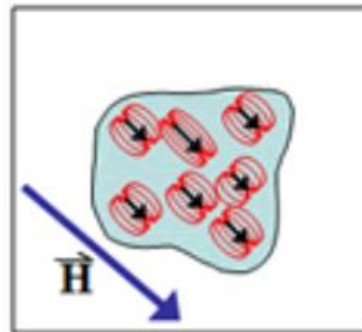
## Electrical Conductivity ( $\sigma$ ):

How easily electrical charges flow through a material



## Magnetic Permeability ( $\mu$ ):

How strongly a material supports magnetism



# Physical Properties

## Dielectric Permittivity ( $\epsilon$ ):

- Considered the **diagnostic physical** property for GPR
- Impacts velocity and reflection/refraction of radiowaves
- Significantly impacted by water content ( $\epsilon_r = 80$ )

## Electrical Conductivity ( $\sigma$ ):

- Impacts attenuation (amplitude loss) of GPR signals

## Magnetic Permeability ( $\mu$ ):

- Only important if things are very susceptible (generally ignored)

# Physical Properties

Dielectric Permittivity:  $\epsilon$

Relative Permittivity:  $\epsilon_r = \frac{\epsilon}{\epsilon_0}$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$1 \leq \epsilon_r \leq 80$$

Magnetic Permeability:  $\mu$

Relative Permeability:  $\mu_r = \frac{\mu}{\mu_0}$

$$\mu_0 = 1.26 \times 10^{-6} \text{ H/m}$$

# Physical Properties

Dielectric Permittivity:  $\epsilon$

Relative Permittivity:

$$\epsilon_r = \frac{\epsilon}{\epsilon_0}$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$1 \leq \epsilon_r \leq 80$$

Magnetic Permeability:  $\mu$

Relative Permeability:  $\mu_r = \frac{\mu}{\mu_0}$

$$\mu_0 = 1.26 \times 10^{-6} \text{ H/m}$$

$$\mu_r = 1$$

# Dielectric Permittivity and Radiowaves

- Water has strongest effect on  $\epsilon$  in geologic materials.
- **Velocity** of radar signals is (usually) most affected by  $\epsilon$ .

Table of relative dielectric permittivity ( $\epsilon_R$ ), electrical conductivity ( $\sigma$ ), and velocity.			
Material	$\epsilon_R$		V avg (m/ns)
Air	1		.3
Distilled water	80		0.033
Fresh water	80		0.033
Sea water	80		0.01
Dry sand	3-5		0.15
Saturated sand	20-30		0.06
Limestone	4-8		0.12
Shales	5-15		0.09
Silts	5-30		0.07
Clays	5-40		0.06
Granite	4-6		0.13
Dry salt	5-6		0.13
Ice	3-4		0.16

$$v = \frac{c}{\sqrt{\epsilon_r}}$$

$$c = 3 \times 10^8 m/sec$$

$$c = 0.3m/ns$$

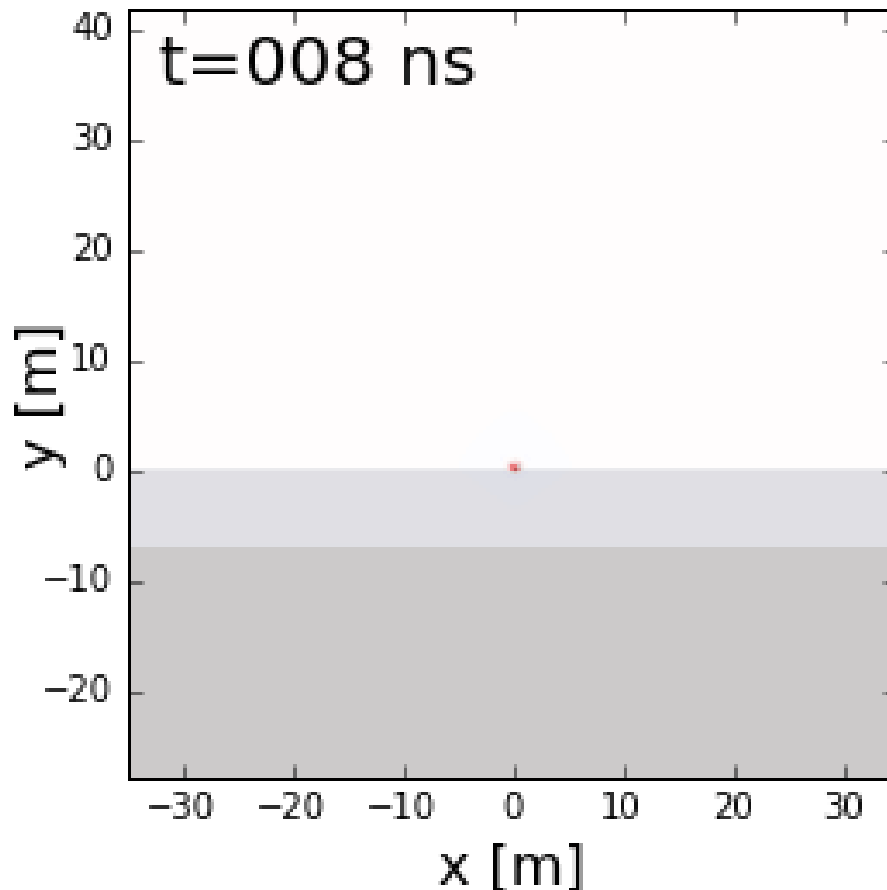
$$\epsilon_r = \frac{\epsilon}{\epsilon_0}$$



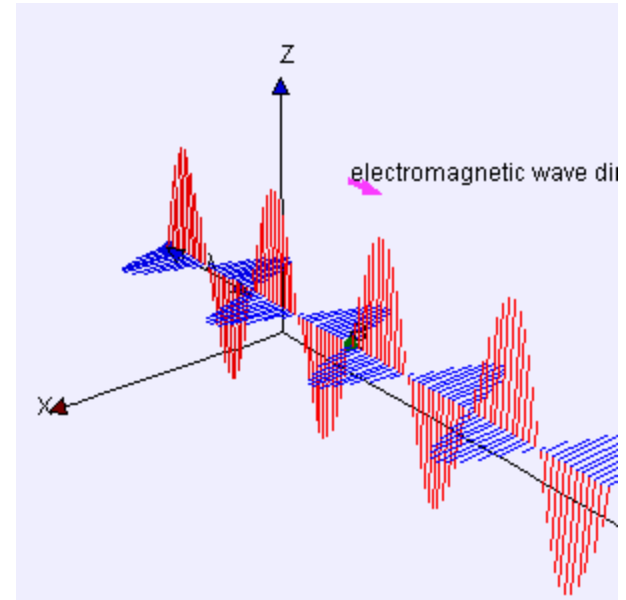
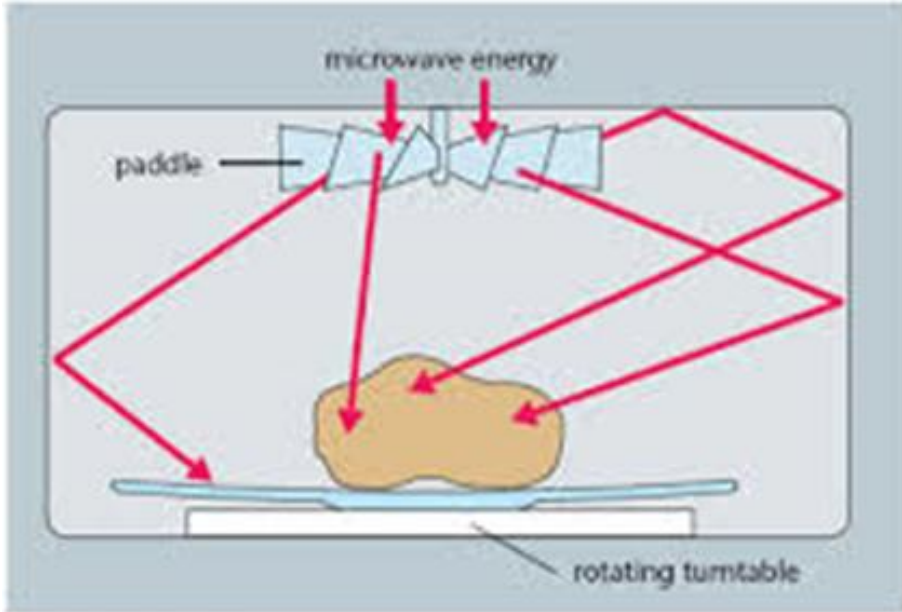
# Introduction to GPR: 2D Example

- What has faster propagation velocity?
- What has larger dielectric permittivity?

$$v = \frac{c}{\sqrt{\epsilon_r}}$$

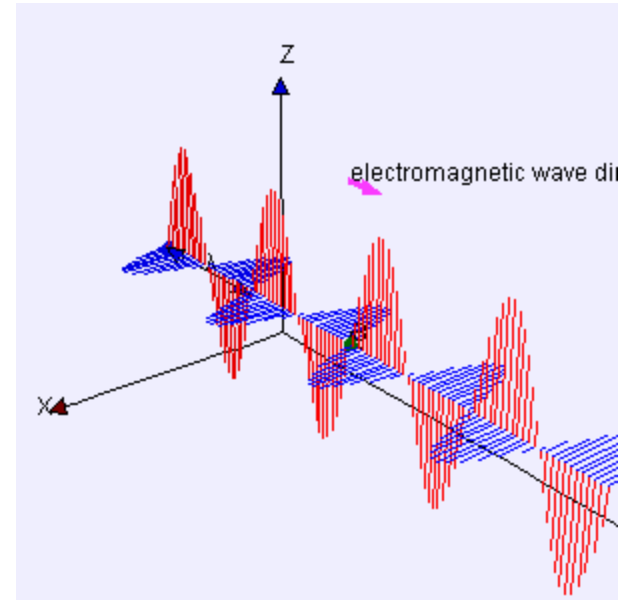
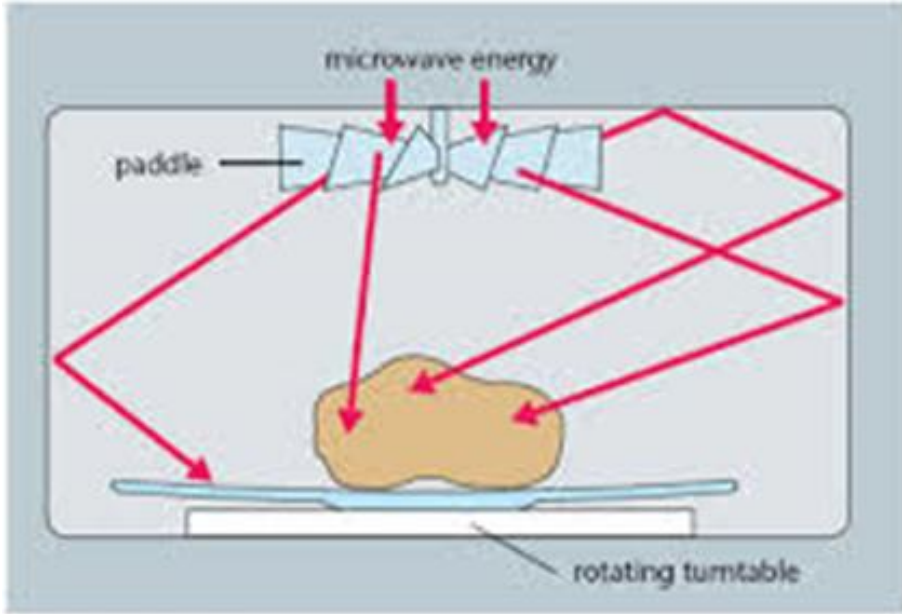


# Microwave Oven Example



- Radiowaves and microwaves support oscillating electric and magnetic fields (why  $\epsilon$ ,  $\sigma$  and  $\mu$  are all significant)
- Microwaves use very high frequencies (  $\sim 2.45$  GHz)
- Wavelength: 
$$L = \frac{c}{f} = \frac{3.00 \times 10^8 \text{ m/s}}{2.45 \times 10^9 \text{ s}} \approx 12 \text{ cm}$$

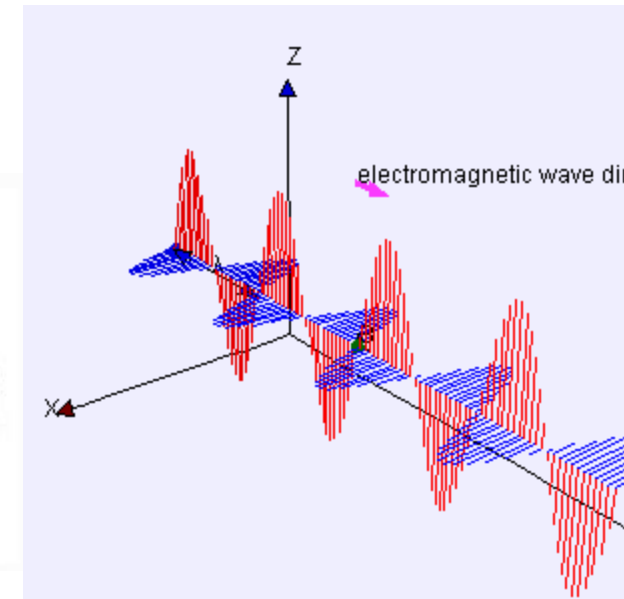
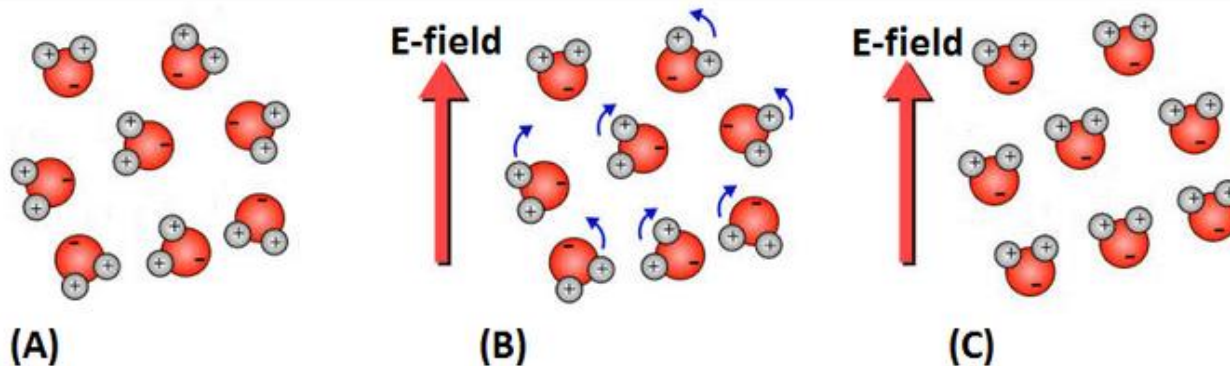
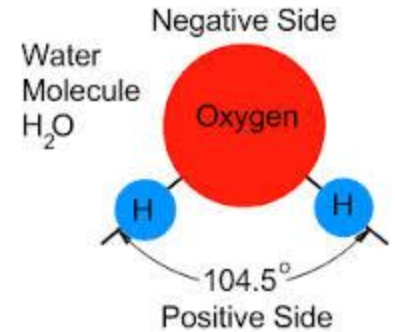
# Microwave Oven Example



- Microwaves (and radiowaves) reflect off conductive walls
- Microwaves (and radiowaves) don't interact with plastic turntable
- Microwaves energy absorbed by water in food

# Microwave Oven Example

- Water molecules are naturally polarized
- Water molecules align strongly with electric fields (large permittivity)
- Reorientation of water molecules happens at the frequency of the microwaves (2.45 GHz is 2.45 billion times per second!!!)



# The Magic of Microwave Ovens

1. Microwaves reach food
2. Microwaves cause rapid re-orientation of water molecules in food (because of  $\epsilon_r$ )
3. 2.45 GHz is the resonance frequency for water  
→ Energy absorbed and turned into kinetic energy (heat)
4. Water molecules transfer heat to the rest of the food



# Microwave Oven Recap

- Microwaves (and radiowaves) are high-frequency, short wavelength waves
- Conductive objects reflect microwaves (and radiowaves) very efficiently.
- The operating frequency has a significant impact on how microwaves (and radiowaves) interact with materials.
- Materials containing water are strongly polarized by microwaves (and radiowaves)

# Questions: Recap

**Q:** What geophysical survey is most comparable to GPR?

**Q:** What is the scale of GPR surveys? Applications?

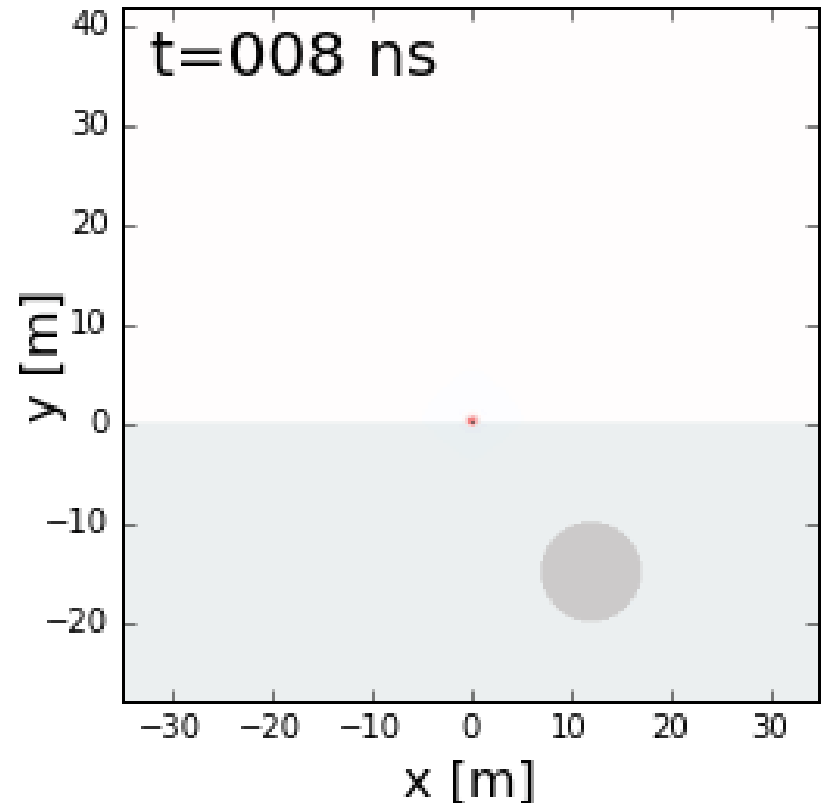
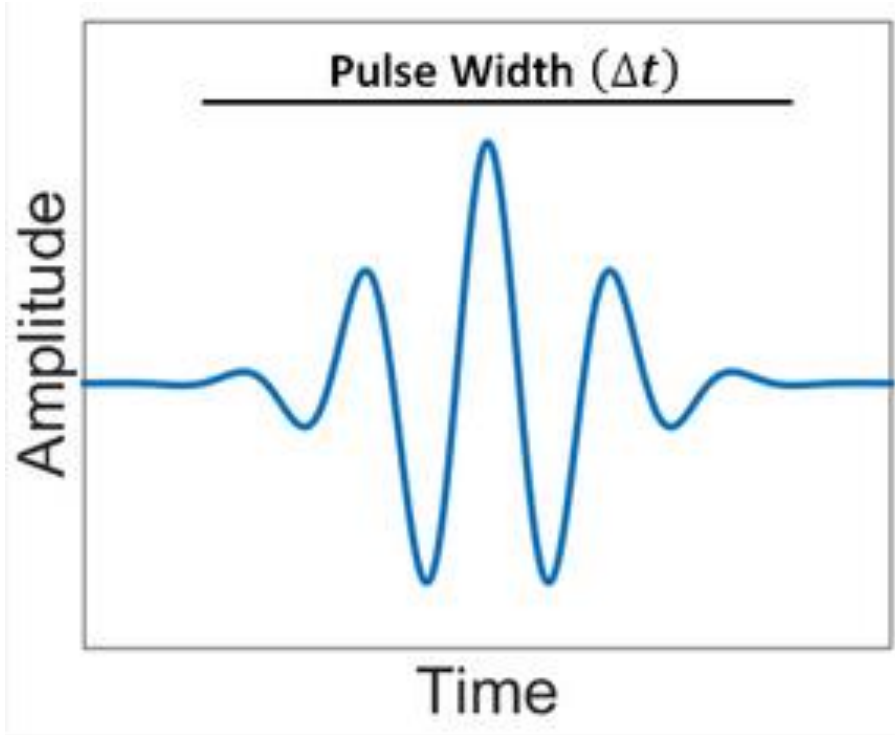
**Q:** What is the diagnostic physical property for GPR?

**Q:** What impacts this physical property the most?

**Q:** What is the signal that GPR sends into the ground? Is it continuous or a pulse?

# Radiowave Propagation

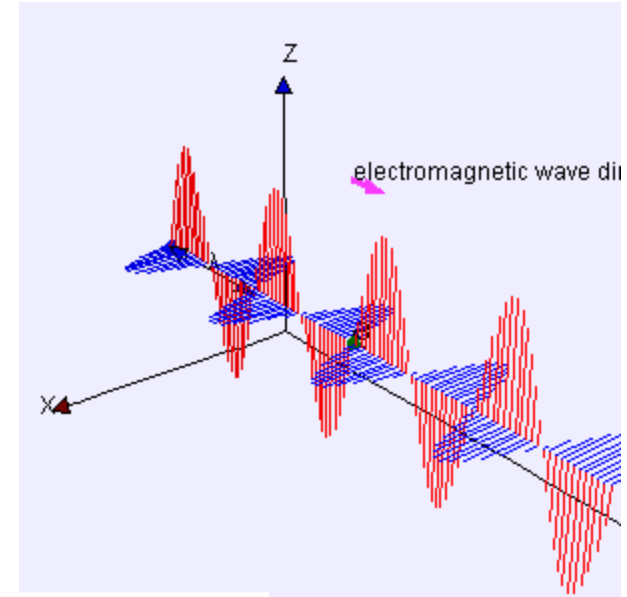
- GPR sends a **pulse** of EM waves. **Not continuous!**



- GPR is 100s MHz to GHz which are **radiowaves**

# Radiowave Propagation

- EM waves carry oscillating electric and magnetic fields at a particular frequency
- EM waves move through different materials at different speeds



- In general: 
$$V = \sqrt{\frac{2}{\mu\epsilon} \left[ \left( 1 + \left( \frac{\sigma}{\omega\epsilon} \right)^2 \right)^{1/2} + 1 \right]^{-1/2}}$$

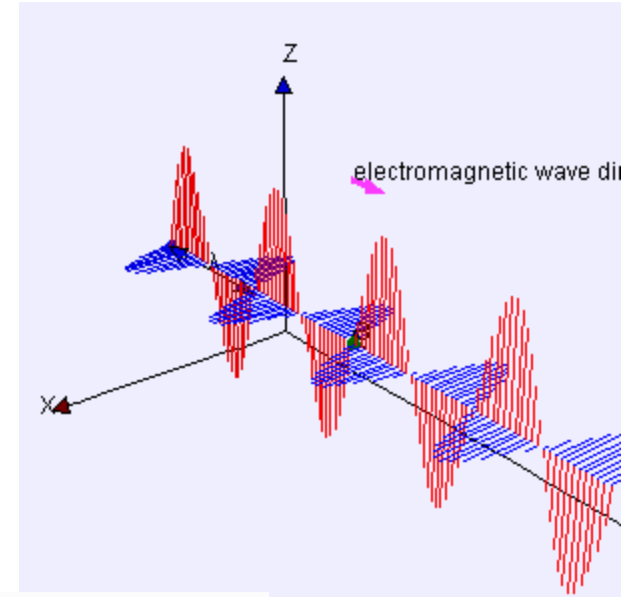
- Wave regime ( $\sigma \ll \omega\epsilon$ ): 
$$V = \frac{1}{\sqrt{\mu\epsilon}} = \frac{c}{\sqrt{\mu_r \epsilon_r}}$$

- Non-magnetic approximation ( $\mu_r = 1$ ):

$$V = \frac{c}{\sqrt{\epsilon_r}}$$

# Radiowave Propagation

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# Radiowave Propagation

Table of relative dielectric permittivity ( $\epsilon_R$ ), electrical conductivity ( $\sigma$ ), and velocity.			
Material	$\epsilon_R$	$\sigma$ (mSeimens/m)	V avg (m/ns)
Air	1	0	.3
Distilled water	80	0.01	0.033
Fresh water	80	0.5	0.033
Sea water	80	3000	0.01
Dry sand	3- 5	0.01	0.15
Saturated sand	20-30	0.1-1.0	0.06
Limestone	4-8	0.5-2.0	0.12
Shales	5-15	1-100	0.09
Silts	5-30	1-100	0.07
Clays	5-40	2- 1000	0.06
Granite	4-6	0.01-1.0	0.13
Dry salt	5-6	0.01-1.0	0.13
Ice	3-4	0.01	0.16

# Radiowave Propagation

- Velocity decreases as  $\epsilon_r$  increases:

$$V = \frac{c}{\sqrt{\epsilon_r}}$$

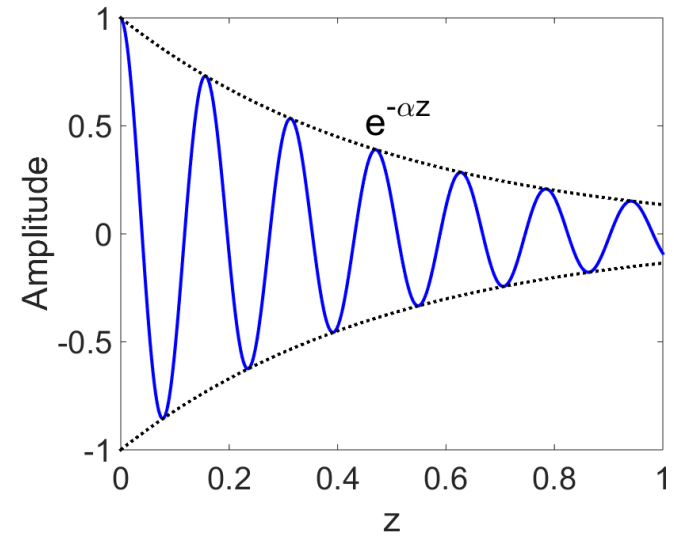
- Radiowaves always travel faster in the air than in the Earth.
- Radiowaves travel slower in water saturated sediments ( $\epsilon_r = 80$  for water)

# Wave Attenuation

- Defines the rate of amplitude loss a wave experiences as it travels:

$$\frac{|\mathbf{A}|}{|\mathbf{A}_0|} = e^{-\alpha z}$$

- EM waves experience an exponential amplitude loss as they travel.



$$\alpha = \omega \sqrt{\frac{\mu\epsilon}{2}} \left[ \left( 1 + \left( \frac{\sigma}{\omega\epsilon} \right)^2 \right)^{1/2} - 1 \right]^{1/2} \approx \begin{cases} \sqrt{\frac{\omega\mu\sigma}{2}} & \text{for } \omega\epsilon \ll \sigma \\ \frac{\sigma}{2} \sqrt{\frac{\mu}{\epsilon}} & \text{for } \sigma \ll \omega\epsilon \end{cases}$$

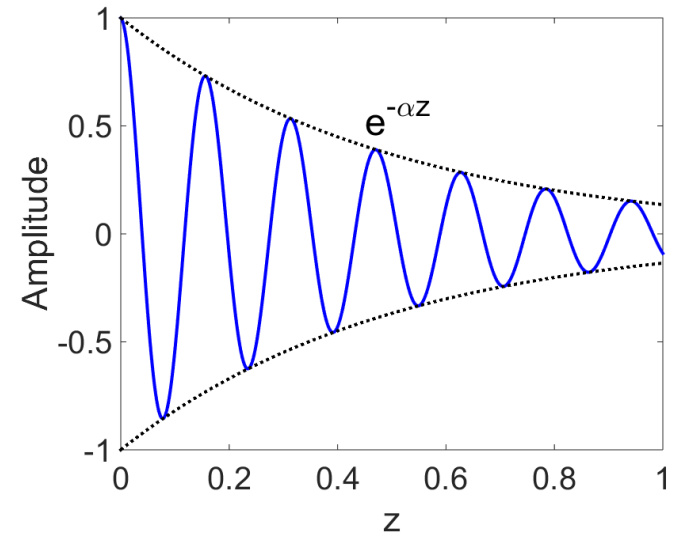
- Quasi-Static ( $\omega\epsilon \ll \sigma$ ): Conductive/Low-frequency
- Wave Regime ( $\sigma \ll \omega\epsilon$ ): Resistive/High-frequency

# Wave Attenuation

- Defines the rate of amplitude loss a wave experiences as it travels:

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$$\alpha = \omega \sqrt{\frac{\mu \epsilon}{2}} \left[ \left( 1 + \left( \frac{\sigma}{\omega \epsilon} \right)^2 \right)^{1/2} - 1 \right]^{1/2} \approx \begin{cases} \sqrt{\frac{\omega \mu \sigma}{2}} & \text{for } \omega \epsilon \ll \sigma \\ \frac{\sigma}{2} \sqrt{\frac{\mu}{\epsilon}} & \text{for } \sigma \ll \omega \epsilon \end{cases}$$

- Quasi-Static ( $\omega \epsilon \ll \sigma$ ): Conductive/Low-frequency
- Wave Regime ( $\sigma \ll \omega \epsilon$ ): Resistive/High-frequency

# Radiowave Attenuation

Table of relative dielectric permittivity ( $\epsilon_R$ ), electrical conductivity ( $\sigma$ ), and velocity.

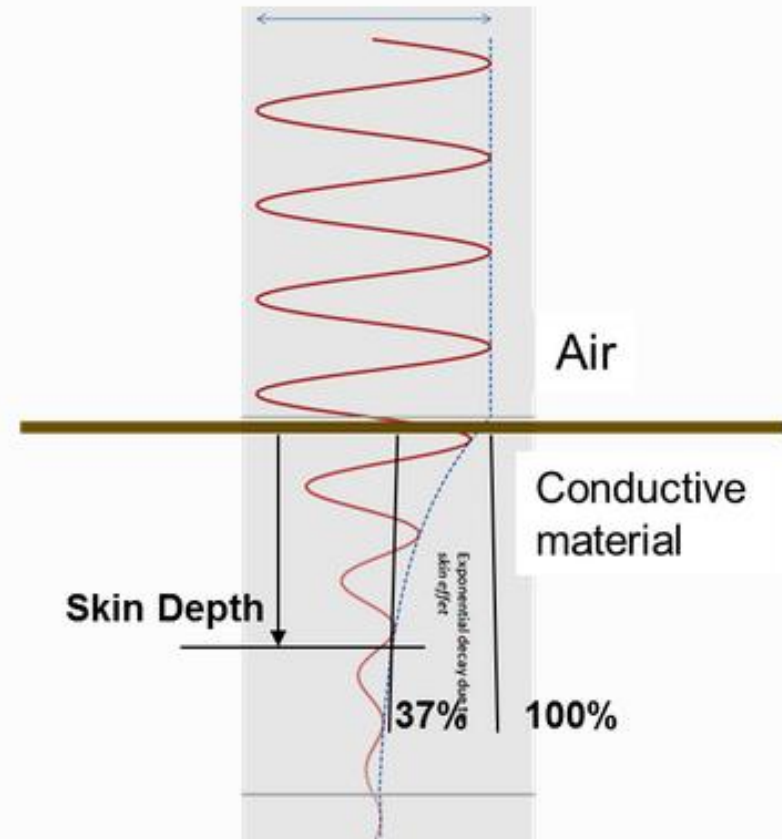
Material	$\epsilon_R$	$\sigma$ (mSeimens/m)	V avg (m/ns)
Air	1	0	.3
Distilled water	<b>80</b>	<b>0.01</b>	0.033
Fresh water	80	0.5	0.033
Sea water	80	<b>3000</b>	<b>0.01</b>
Dry sand	<b>3</b> - 5	0.01	0.15
Saturated sand	20-30	0.1-1.0	0.06
Limestone	4-8	0.5-2.0	0.12
Shales	5-15	1-100	0.09
Silts	5-30	1-100	0.07
Clays	5-40	2- 1000	0.06
Granite	4-6	0.01-1.0	0.13
Dry salt	5-6	0.01-1.0	0.13
Ice	3-4	0.01	<b>0.16</b>

- Radiowaves attenuate quickly if conductivity is large

# Radiowave Attenuation: Skin Depth

- **Skin Depth:** Distance at which a wave is reduced to 37% of its original amplitude
- Assuming Earth is non-magnetic ( $\mu_r = 1$ ):

$$\delta \approx \begin{cases} 503 \sqrt{\frac{1}{\sigma f}} & \text{for } \omega\epsilon \ll \sigma \\ 0.0053 \frac{\sqrt{\epsilon_r}}{\sigma} & \text{for } \sigma \ll \omega\epsilon \end{cases}$$



- The skin depth is smaller if the frequency of the radiowaves is higher.
- The skin depth is larger in materials with lower conductivities.
- The skin depth is larger in materials with higher dielectric permittivities.

# Questions: Recap

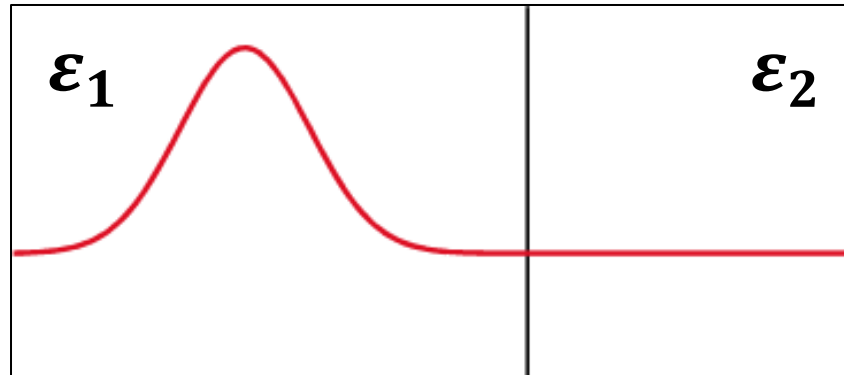
**Q:** What happens to wave amplitude as it propagates?

**Q:** Is the wave velocity higher/lower in water saturated sediments?

$$V = \frac{c}{\sqrt{\epsilon_r}}$$

**Q:** What happens to skin depth at higher frequencies?

# Reflection and Transmission



$$R = \frac{\text{Reflected Amplitude}}{\text{Incident Amplitude}} = \frac{\sqrt{\epsilon_1} - \sqrt{\epsilon_2}}{\sqrt{\epsilon_1} + \sqrt{\epsilon_2}} \quad -1 < R < 1$$

$$T = \frac{\text{Transmitted Amplitude}}{\text{Incident Amplitude}} = \frac{2\sqrt{\epsilon_2}}{\sqrt{\epsilon_1} + \sqrt{\epsilon_2}}$$

- If  $\epsilon_1 \approx \epsilon_2$ , most of the wave is transmitted
- If  $\epsilon_1 \ll \epsilon_2$  or  $\epsilon_1 \gg \epsilon_2$ , most of the wave is reflected



# Reflection and Transmission

$$R = \frac{\text{Reflected Amplitude}}{\text{Incident Amplitude}} = \frac{\sqrt{\epsilon_1} - \sqrt{\epsilon_2}}{\sqrt{\epsilon_1} + \sqrt{\epsilon_2}} \quad -1 < R < 1$$

Material	$\epsilon_R$
Air	1
Distilled water	80
Fresh water	80
Sea water	80
Dry sand	3-5
Saturated sand	20-30
Limestone	4-8
Shales	5-15
Silts	5-30
Clays	5-40
Granite	4-6
Dry salt	5-6
Ice	3-4

**Example:**

Dry Sand

----- R ~ 0.101

Limestone

**Example:**

Dry Sand

----- R ~ 0.429

Wet Sand

**Example:**

Air

----- R ~ 0.799

Sea Water

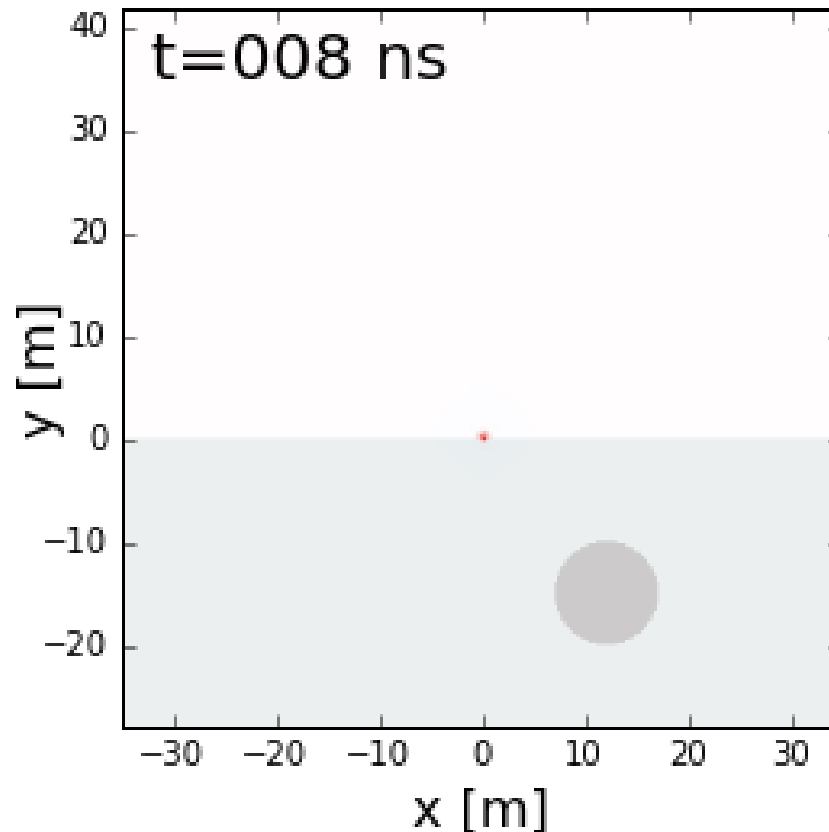
# Reflection from Conductors

$$V = \sqrt{\frac{2}{\mu\epsilon}} \left[ 1 + \left( 1 + \left( \frac{\sigma}{\omega\epsilon} \right)^2 \right)^{1/2} \right]^{-1/2}$$

- Shows  $V \rightarrow 0$  as  $\sigma \rightarrow \infty$
- Thus radiowaves don't propagate in perfect conductors
- Waves get completely reflected

# Reflection and Transmission

- What can we said about  $\epsilon_1$  and  $\epsilon_2$ ?
- Does wave go through conductor or reflect?

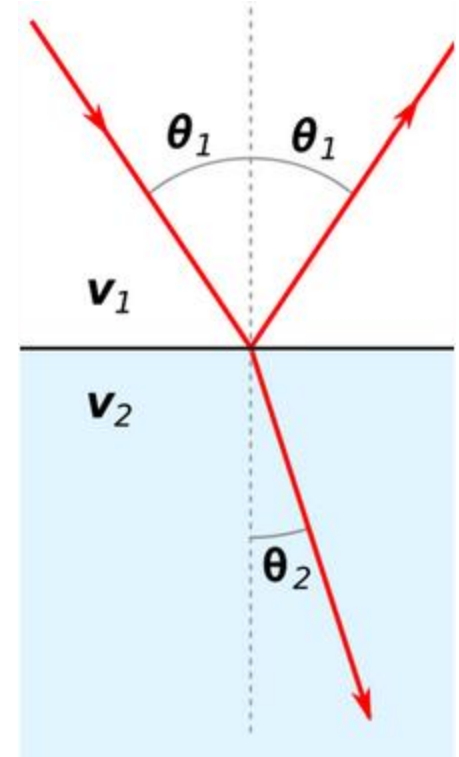


# Refraction

- Snell's Law: 
$$\frac{\sin\theta_1}{V_1} = \frac{\sin\theta_2}{V_2}$$

$$V = c/\sqrt{\epsilon_r}$$

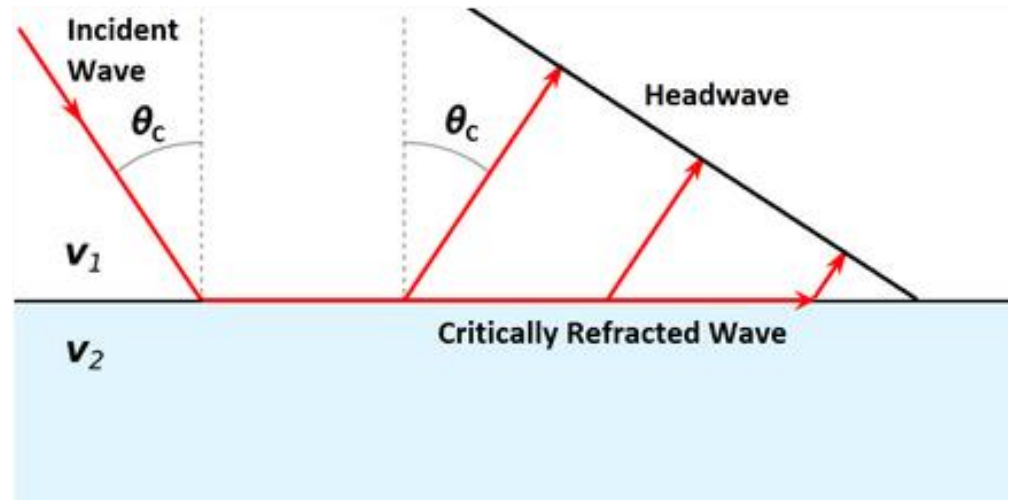
$$\sqrt{\epsilon_1} \sin\theta_1 = \sqrt{\epsilon_2} \sin\theta_2$$



# Critical Refraction

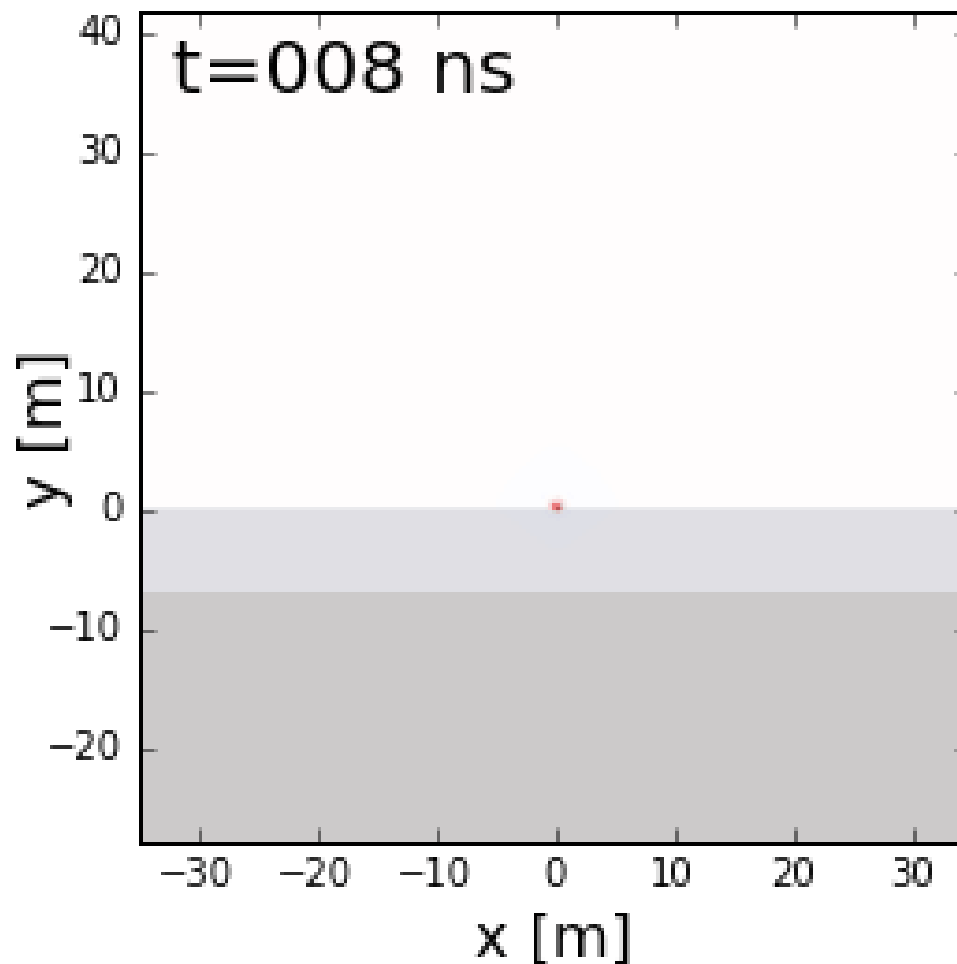
$$\sin\theta_c = \frac{V_1}{V_2}$$

Requires  $V_1 < V_2$



# Refraction

- Can we see any refraction?



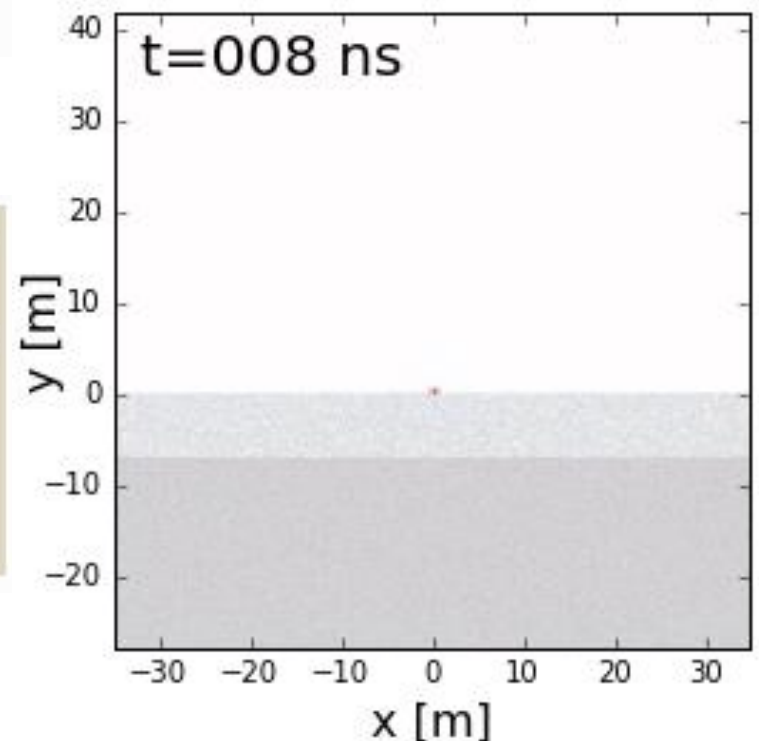
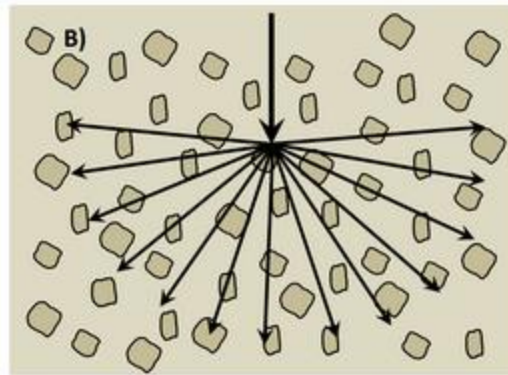
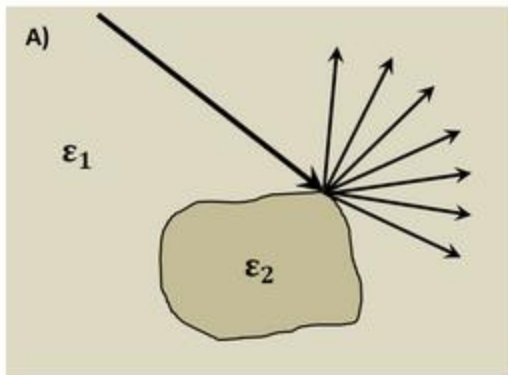
# Scattering

Deviations in ray paths due to localized non-uniformities.

→ leads to noisy data.

→ decreases amplitude of usable signal

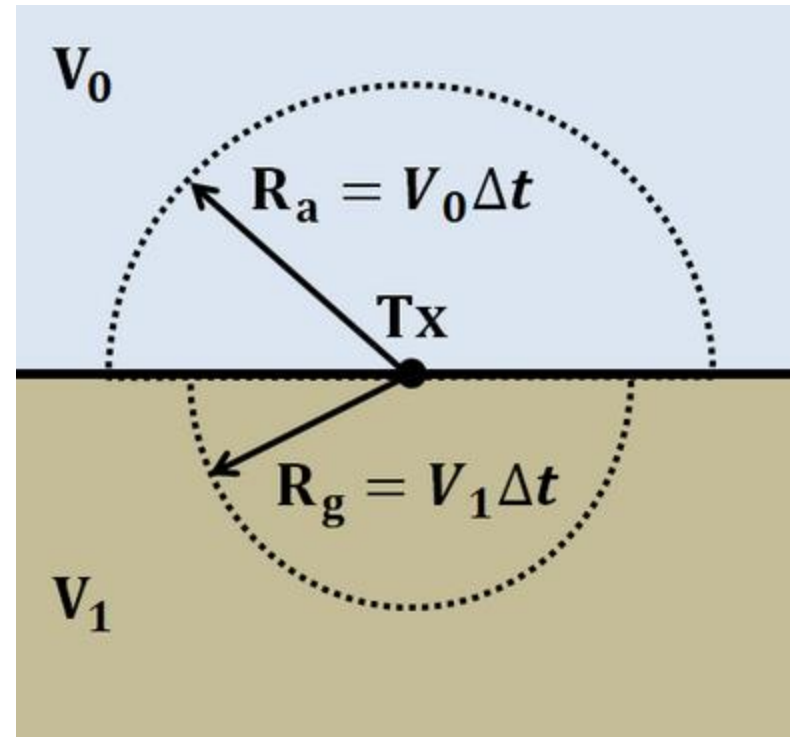
- Irregular surface shape of larger buried objects (below left).
- Rocky soils, which are a large contributor to the scattering of GPR signals (below right).
- Gas bubbles trapped in ice.
- Clutter made up of small buried objects



# Geometrical Spreading

- As the wave front travels, it spreads geometrically
- The rate of geometrical spreading depends on the velocity
- Spreading causes the radiowave to lose amplitude

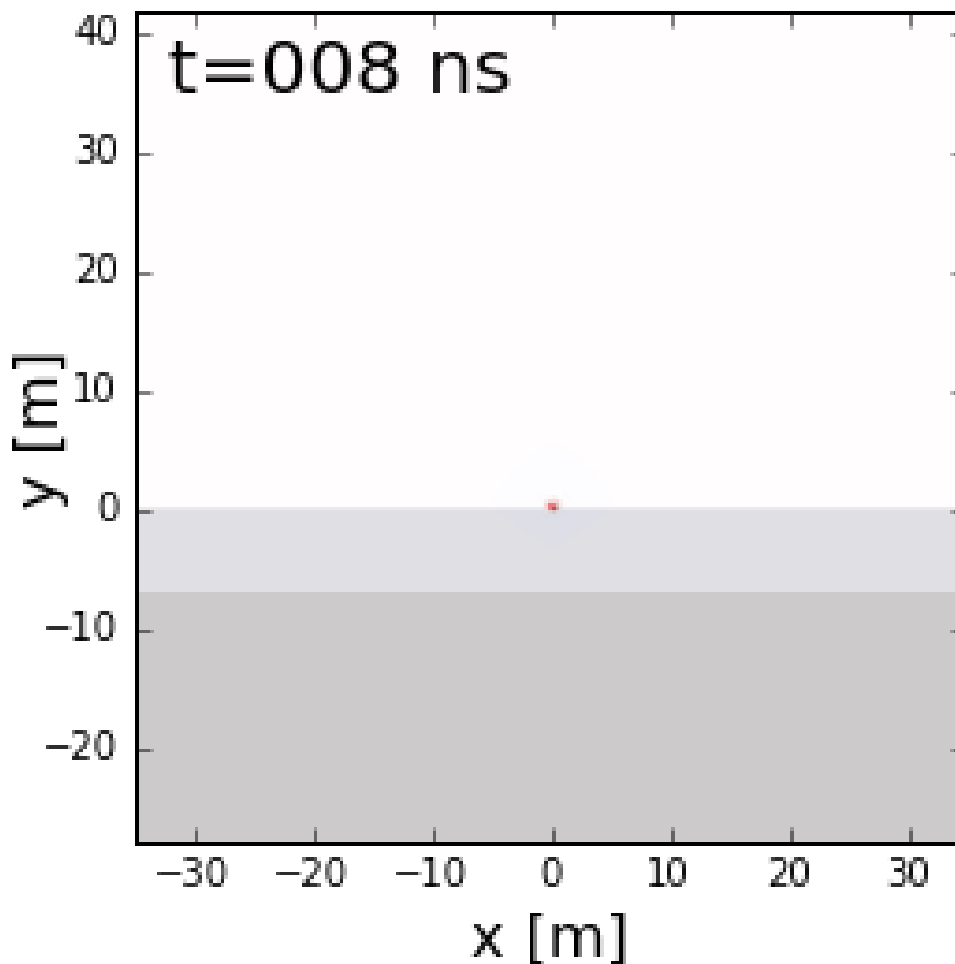
$$\frac{|A|}{|A_0|} \propto \frac{1}{R}$$





# Geometrical Spreading

- Can we see geometrical spreading?



# Material Recap

- Radiowaves reflect at boundaries where the velocity/dielectric permittivity changes:

$$R = \frac{\text{Reflected Amplitude}}{\text{Incident Amplitude}} = \frac{\sqrt{\epsilon_1} - \sqrt{\epsilon_2}}{\sqrt{\epsilon_1} + \sqrt{\epsilon_2}}$$

- Conductors are large reflectors of radiowaves
- Snell's law applies to GPR:

$$\frac{\sin\theta_1}{V_1} = \frac{\sin\theta_2}{V_2}$$

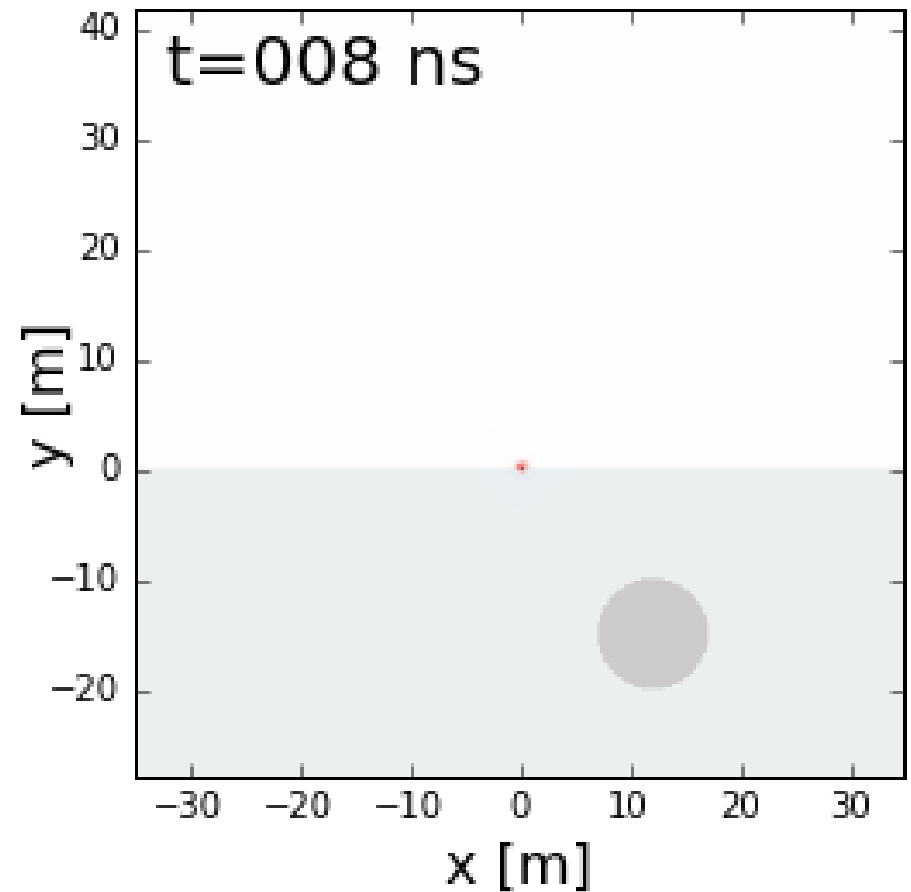
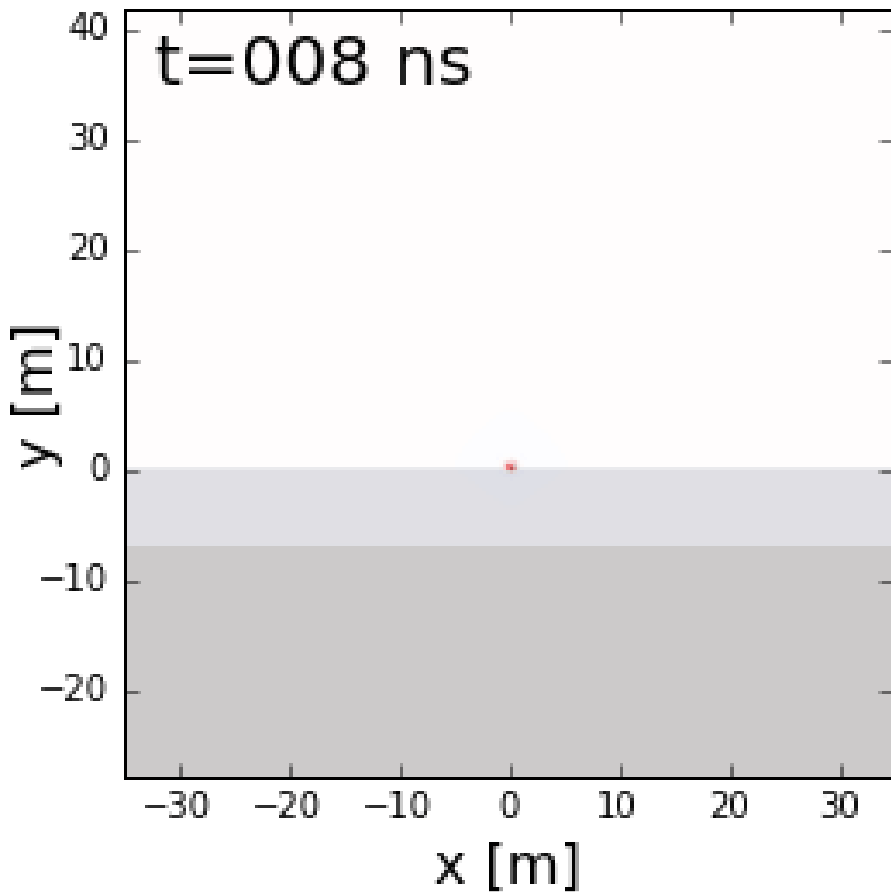
$$\sqrt{\epsilon_1} \sin\theta_1 = \sqrt{\epsilon_2} \sin\theta_2$$

# Questions Recap

**Q:** What happens to a wave that undergoes geometrical spreading?

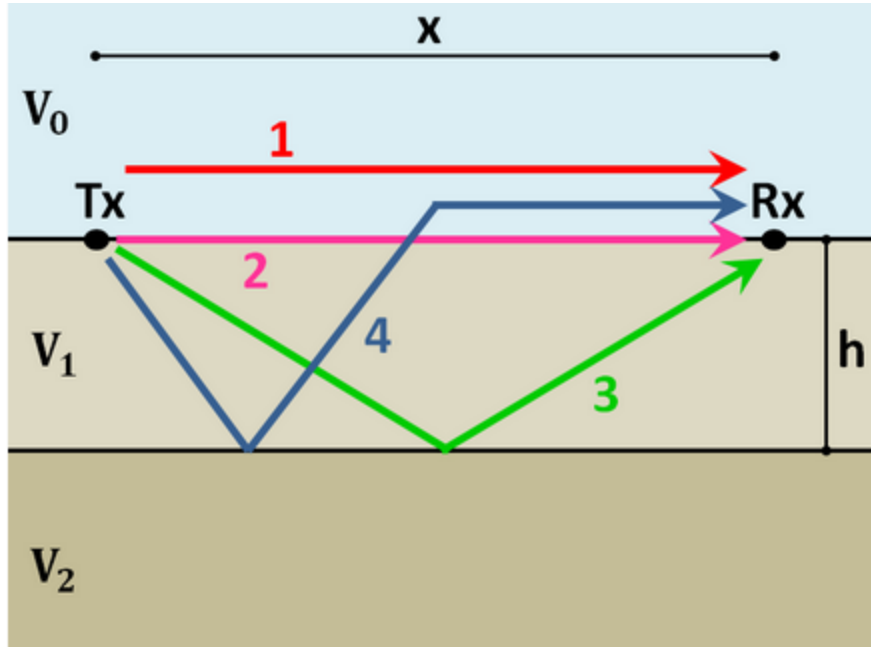
**Q:** Why is scattering an issue?

# Ray Path vs. Wavefront

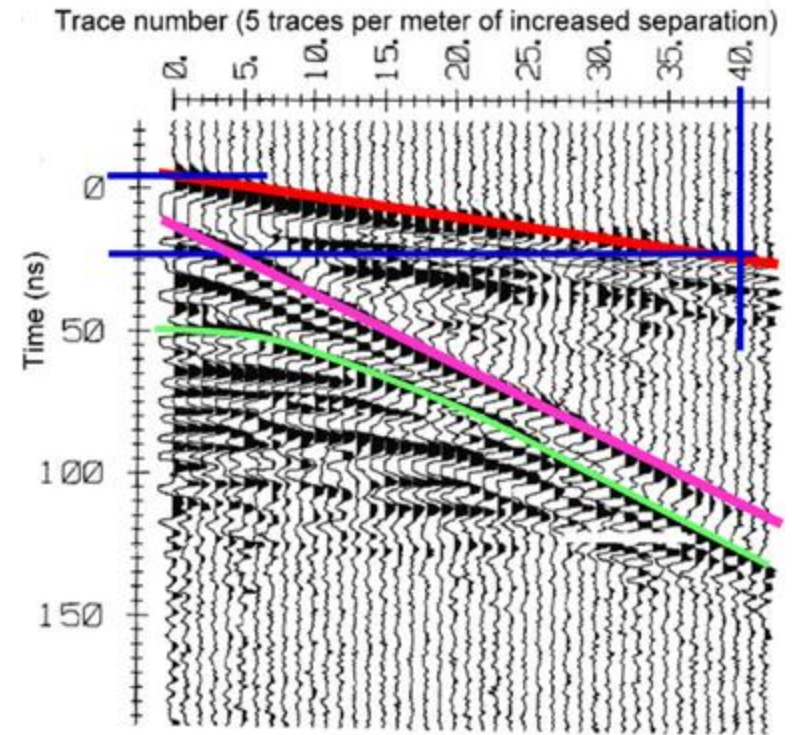


# 2-Layer Example

Model

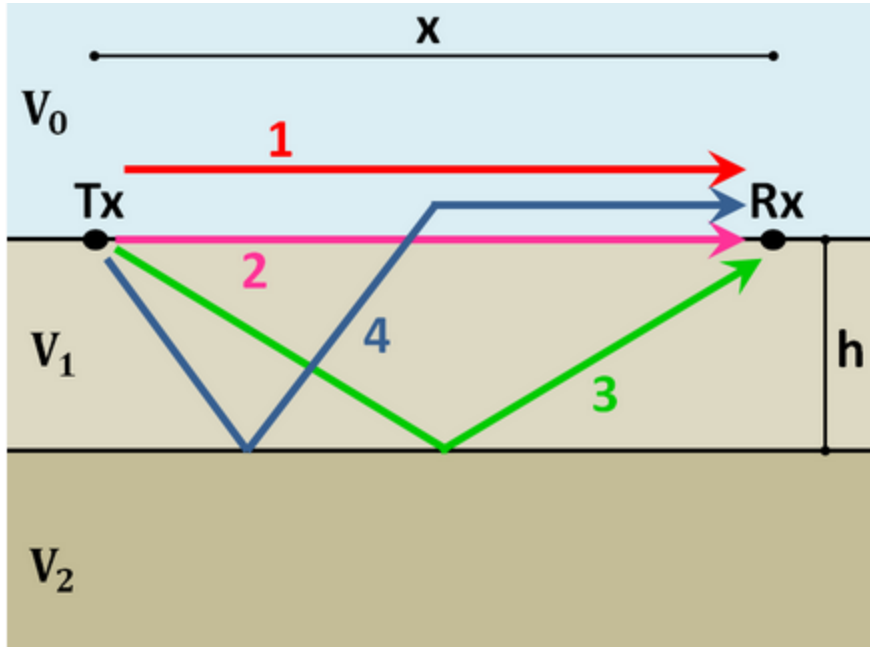


Radargram

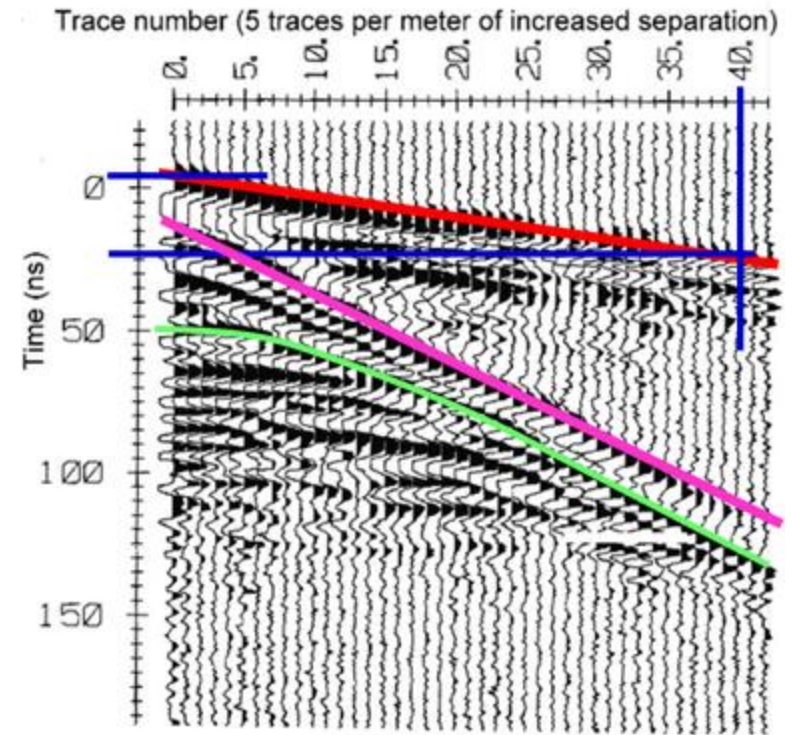


# 2-Layer Example

Model



Radargram



## 1) Direct Air Wave

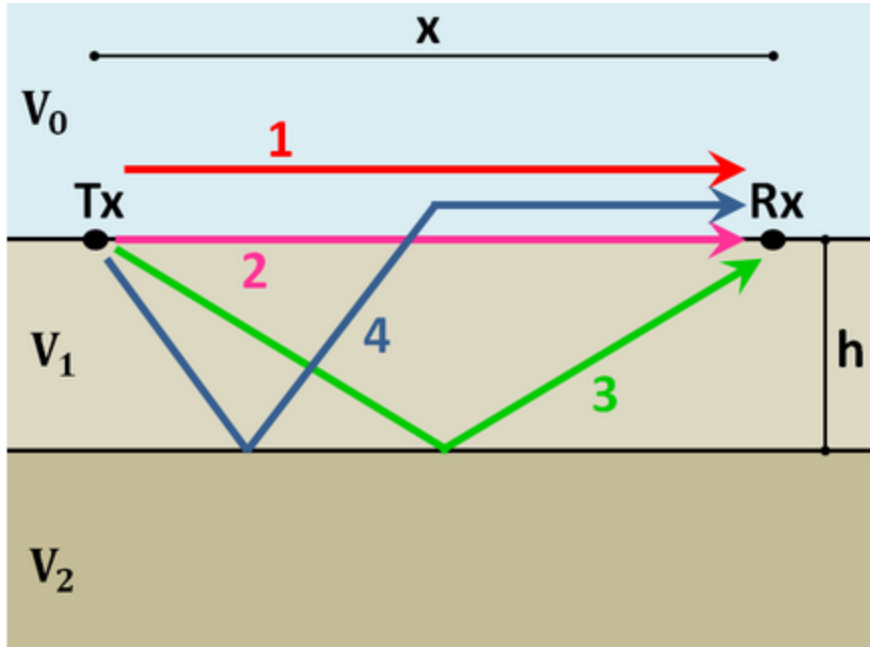
Travel Time:  $t_{air} = \frac{x}{c}$

$$V = c / \sqrt{\epsilon_r}$$

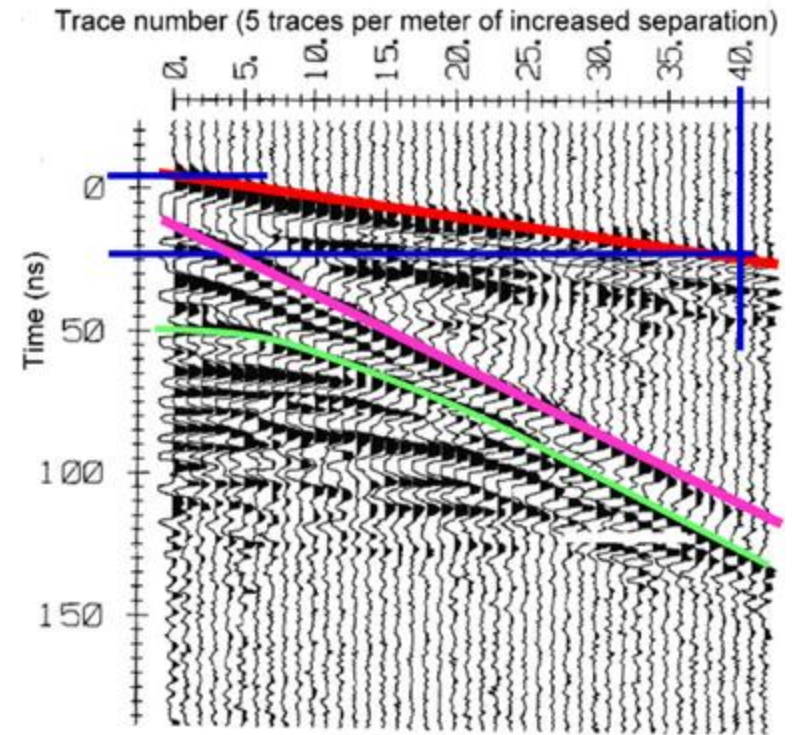
$$c = 3.00 \times 10^8 \text{ m/s}$$

# 2-Layer Example

Model



Radargram



## 2) Direct Ground Wave

Travel Time: 
$$t_{ground} = \frac{x}{V_1}$$

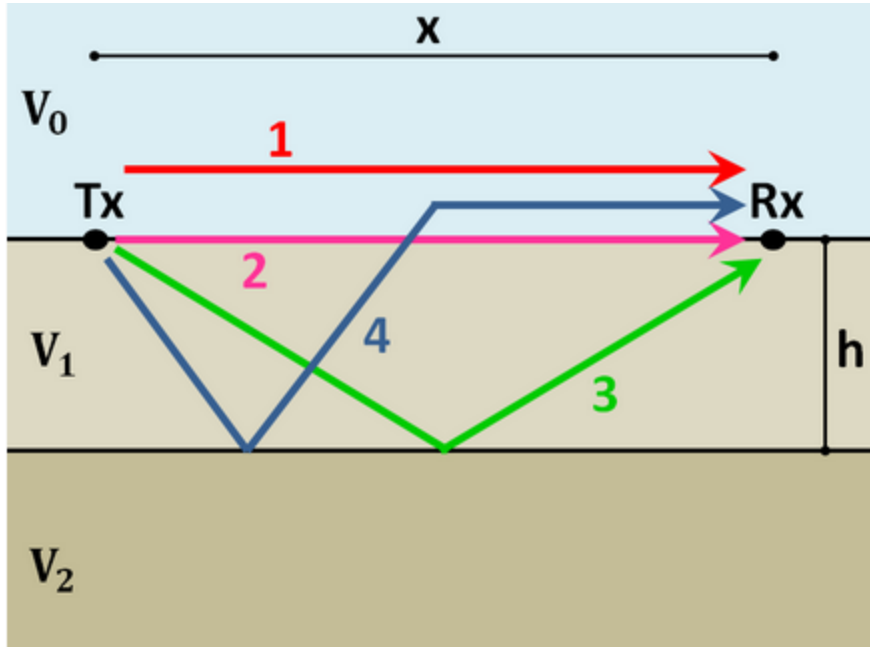
$$V = c/\sqrt{\epsilon_r}$$

$$V_1 < c$$

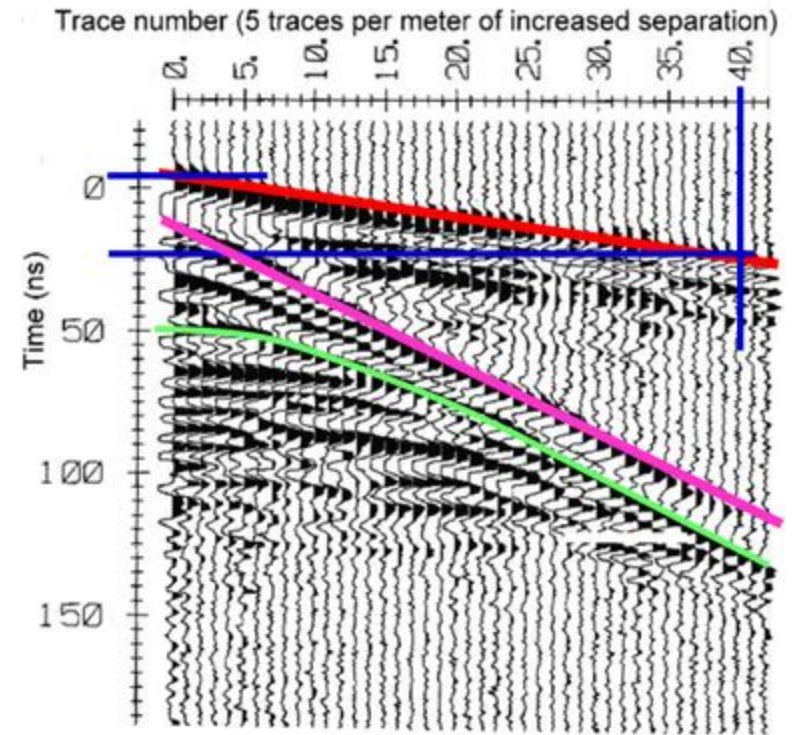


# 2-Layer Example

Model



Radargram



## 3) Reflected Wave

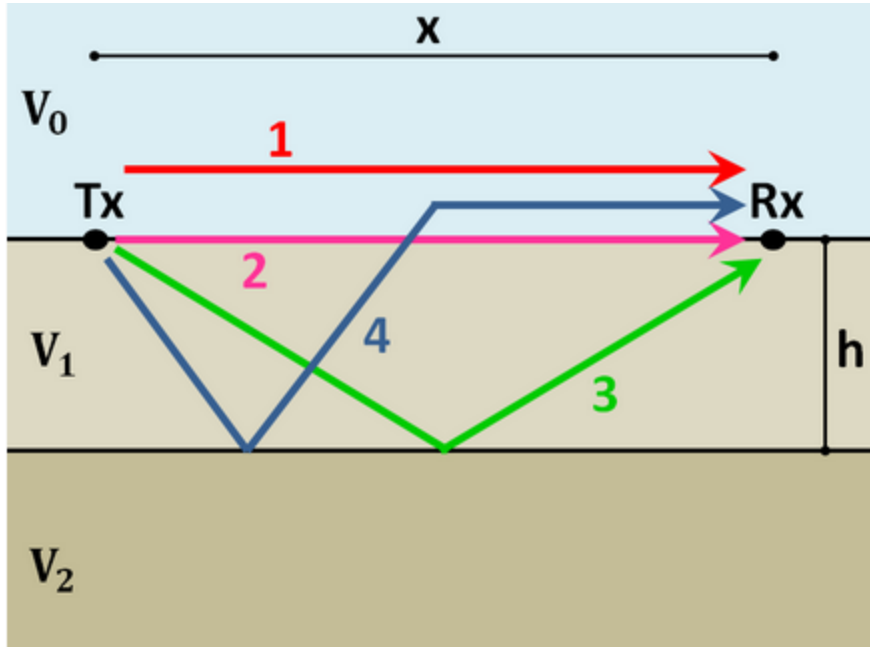
Travel Time:

$$t_{ref} = \frac{\sqrt{x^2 + 4h^2}}{V_1}$$

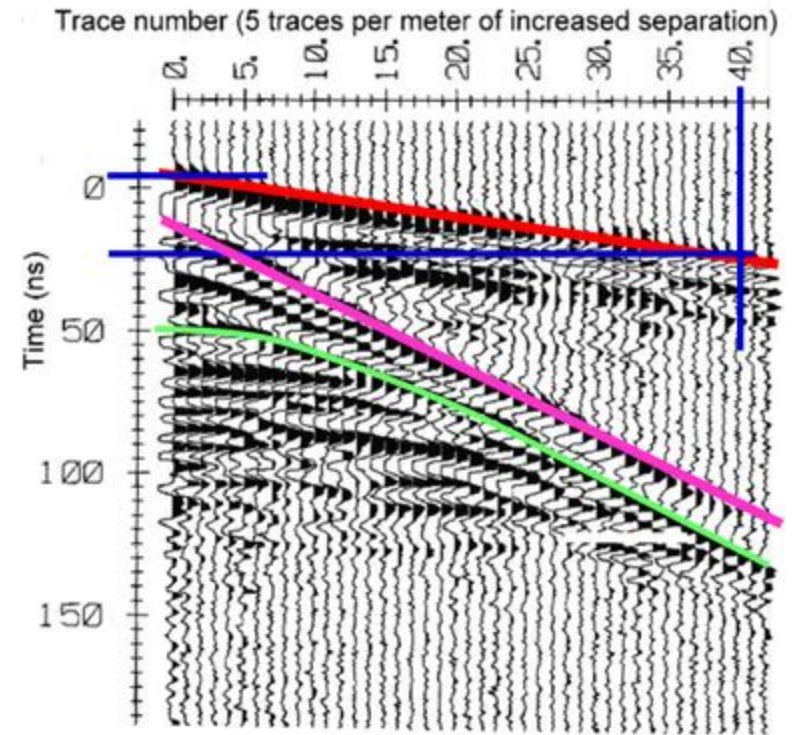


# 2-Layer Example

Model



Radargram

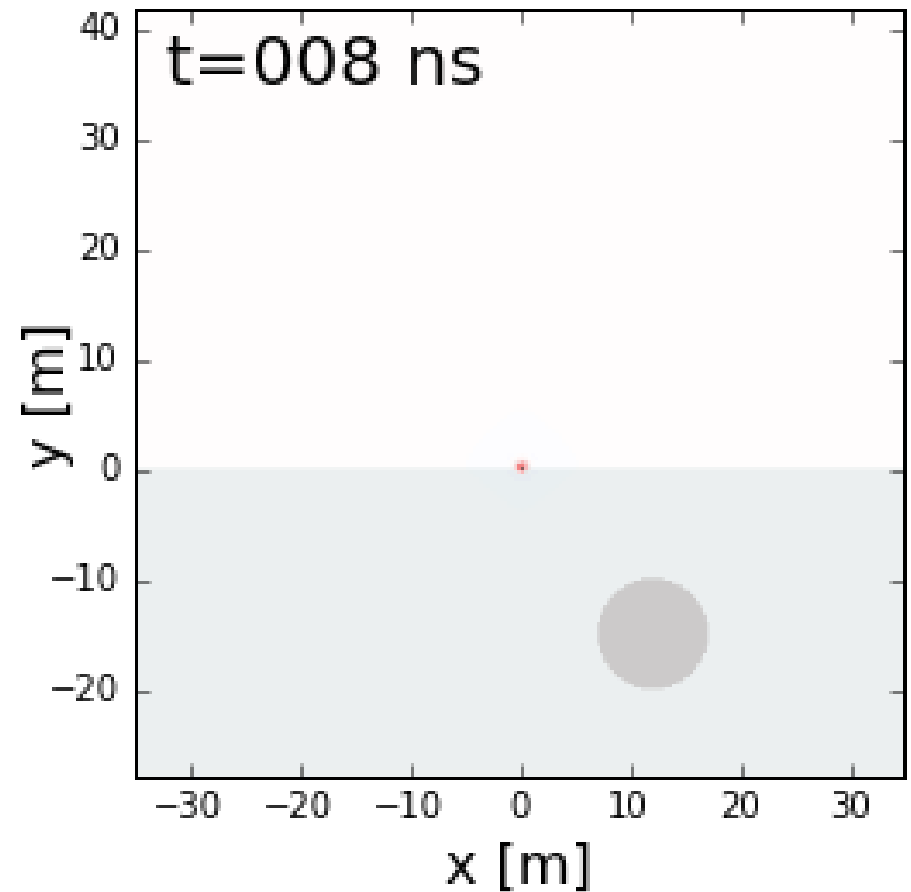
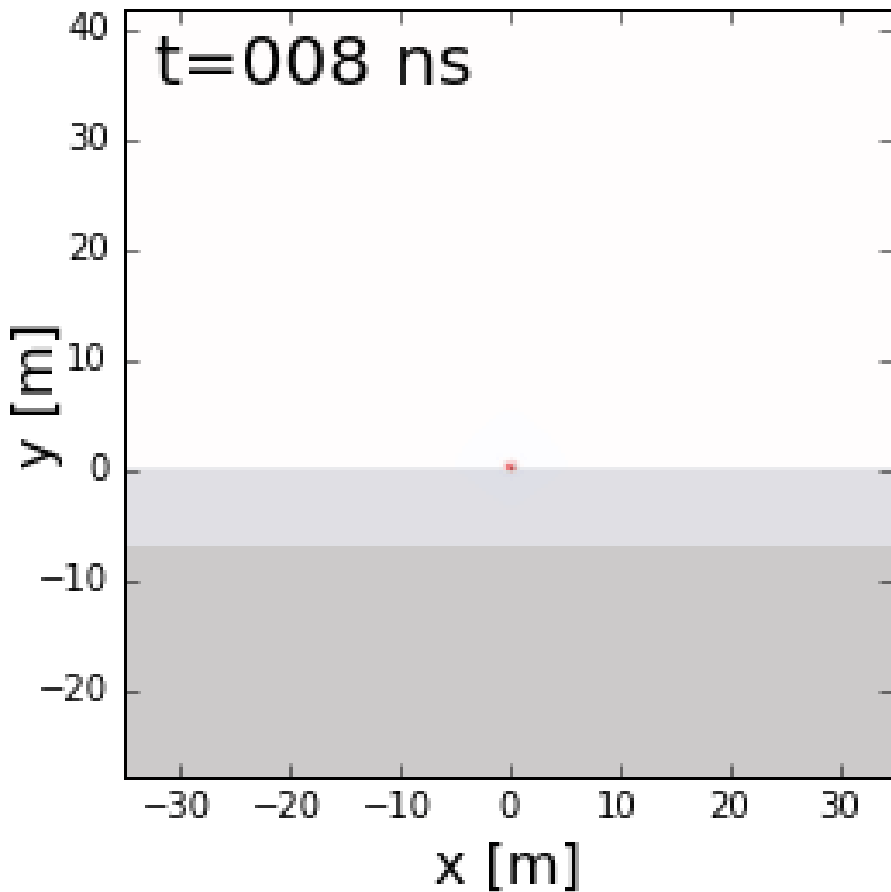


## 4) Refracted Wave

Travel Time: 
$$t_c = \frac{x}{c} + \text{Constant}$$

$$V_1 < V_0$$

# Identifying Ray Paths



# Recap Questions

**Q:** What is the difference between a wavefront and a ray path?

**Q:** Can a wave be critically refracted at the surface?

# Unit Activities

- **Labs (GPR)**
  - Monday, October 21<sup>st</sup>
  - Tuesday, October 22<sup>nd</sup>
- **TBL:**
  - Friday, October 18<sup>th</sup>
- **Quiz:**
  - Wednesday, October 23<sup>rd</sup>