

# Electromagnetic Methods

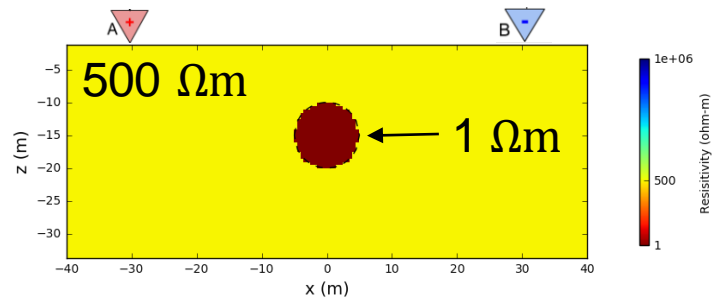
Reading on the GPG:

<https://gpg.geosci.xyz/content/electromagnetics/index.html>

# Today's Topics

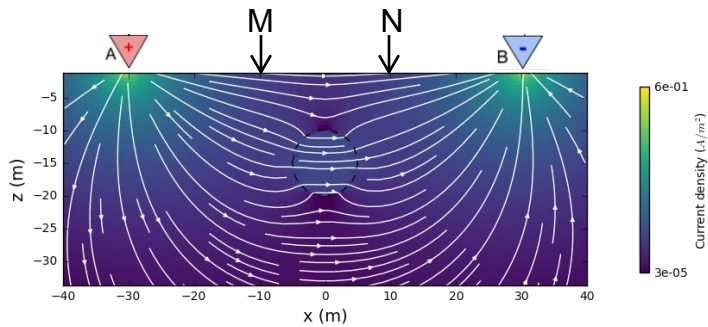
- The Problem with DC Resistivity
- Basic EM Experiment
- Physical Properties
- Basic Principles
  - Ampere's Law
  - Faraday's Law
  - Ohm's Law
  - Basic EM Experiment Revisited

# The Problem with DCR



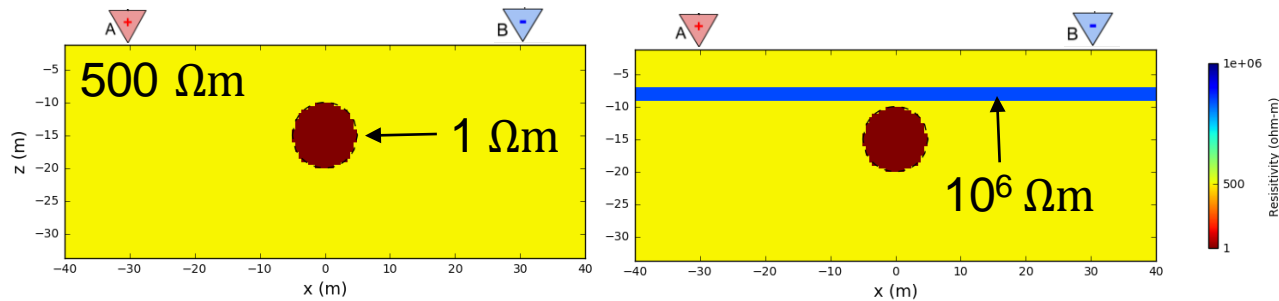
## Currents and measured data at MN

$$\rho_a = 430 \, \Omega\text{m}$$



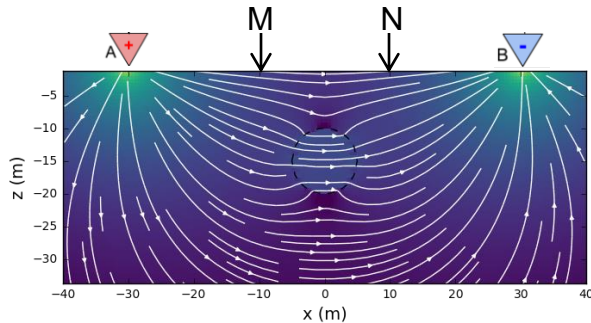
# The Problem with DCR

## Resistivity models (thin resistive layer)

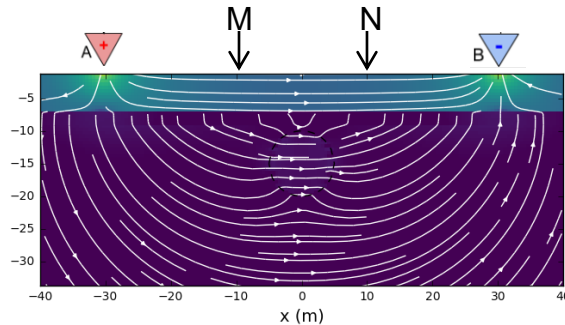


## Currents and measured data at MN

$$\rho_a = 430 \Omega\text{m}$$

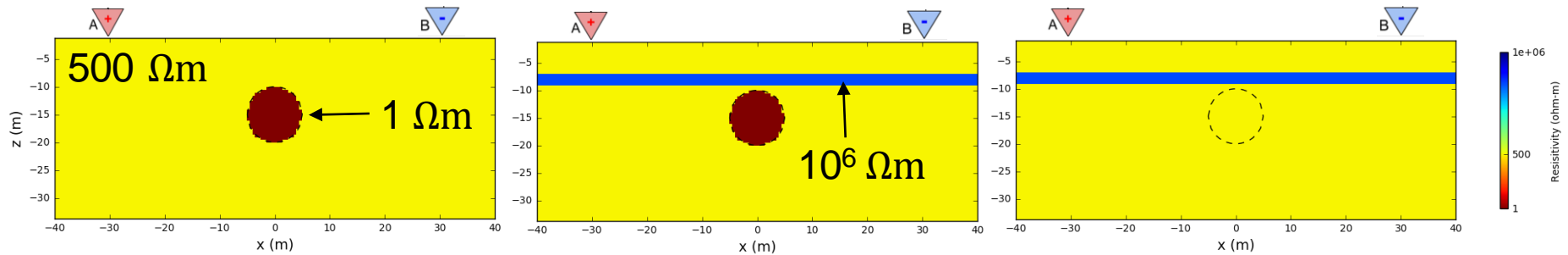


$$\rho_a = 1652 \Omega\text{m}$$

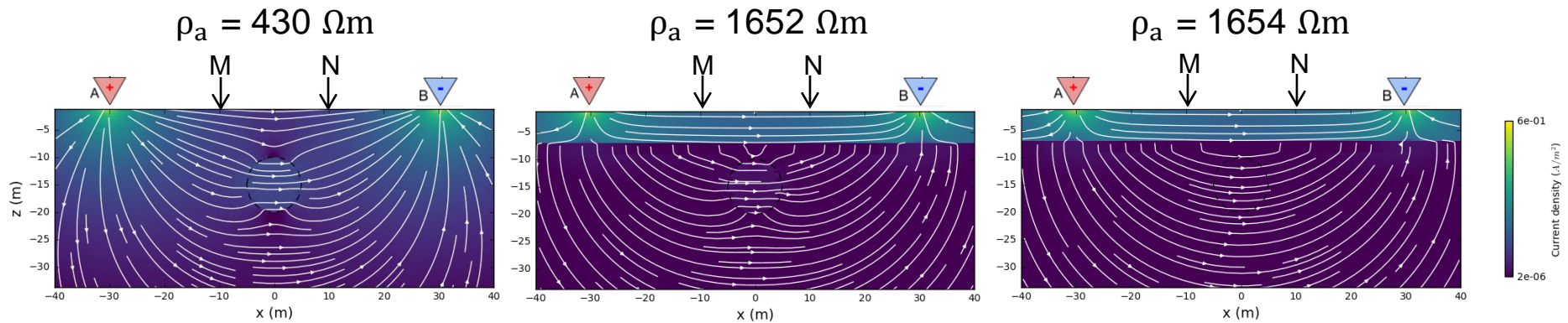


# The Problem with DCR

## Resistivity models (thin resistive layer)

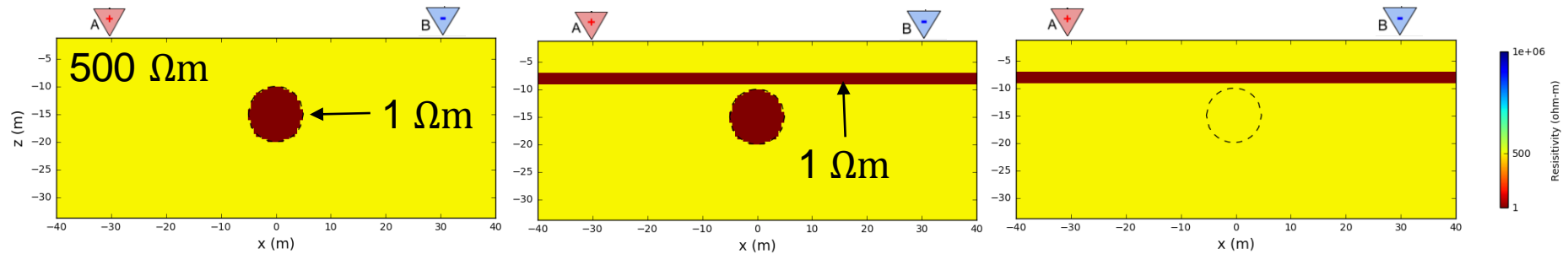


## Currents and measured data at MN

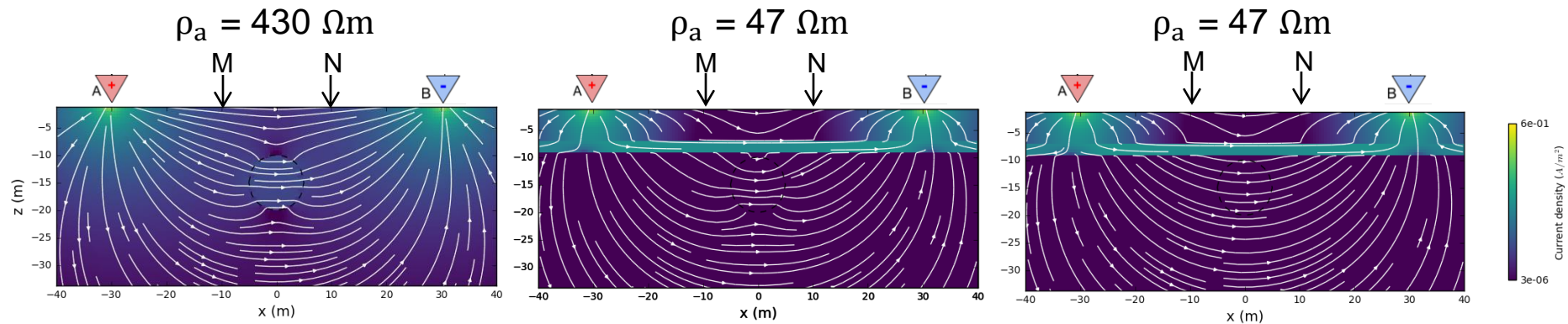


# The Problem with DCR

## Resistivity models (thin conductive layer)



## Currents and measured data at MN



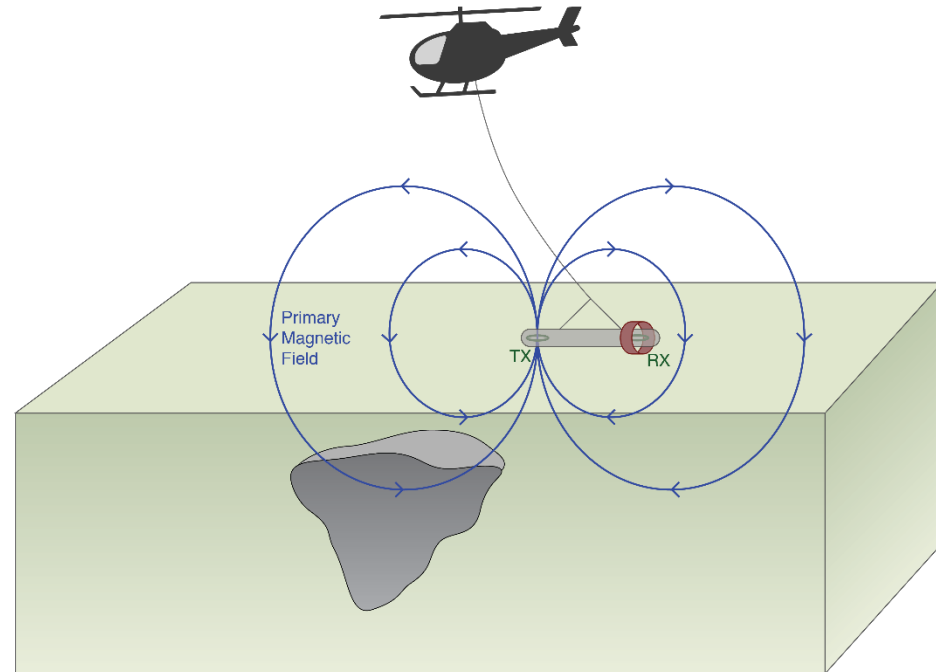
# Basic EM Experiment

Reading on the GPG:

[https://gpg.geosci.xyz/content/electromagnetics/electromagnetic\\_introduction.html](https://gpg.geosci.xyz/content/electromagnetics/electromagnetic_introduction.html)

# Basic Experiment

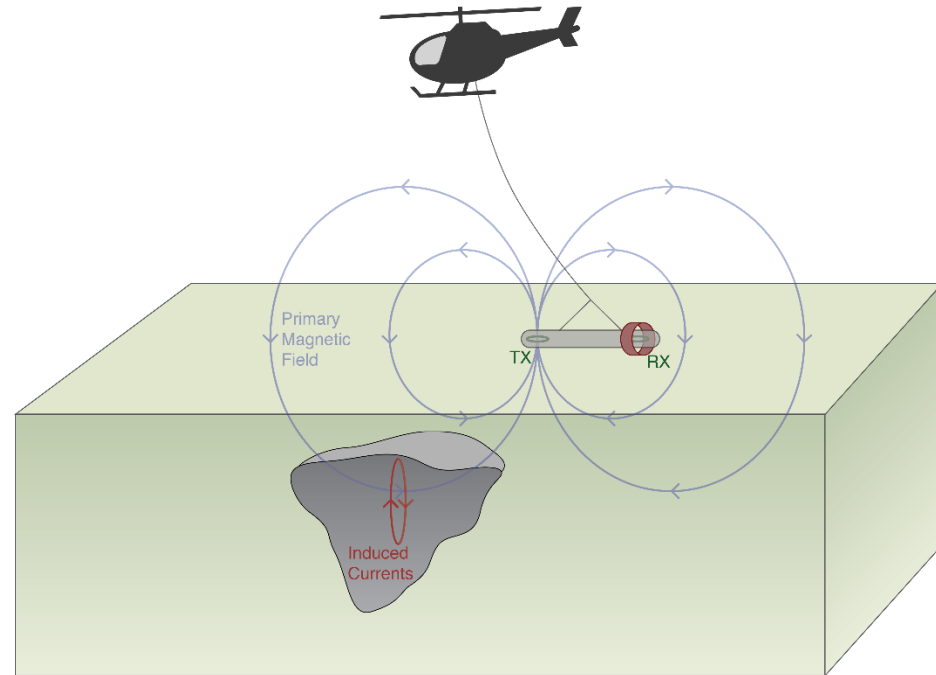
- **Source (Tx):**  
Current loop makes primary magnetic field





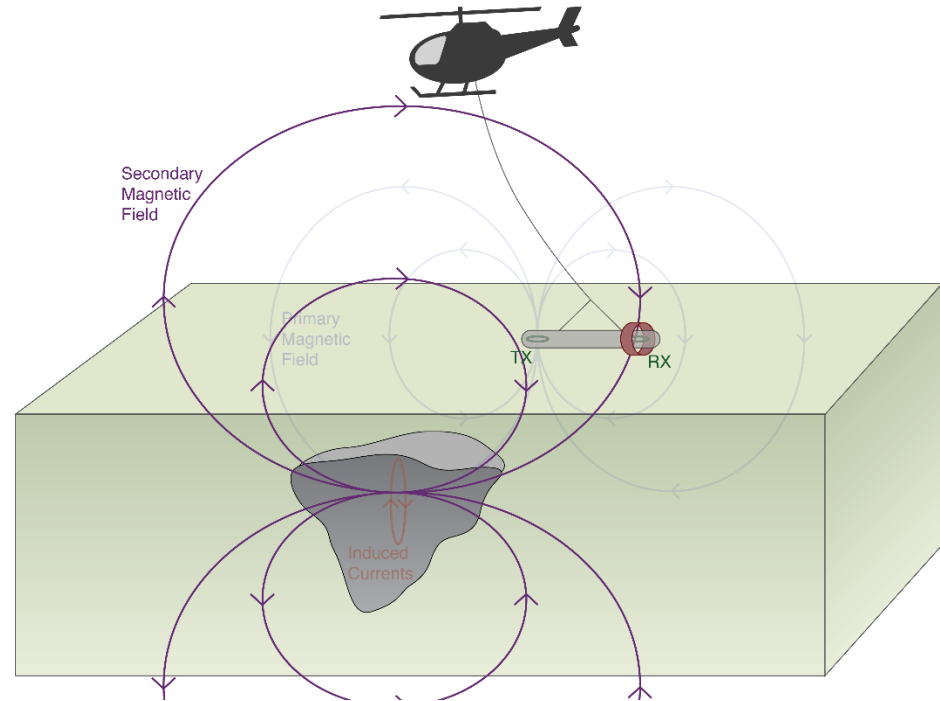
# Basic Experiment

- **Source (Tx):**  
Current loop makes primary magnetic field
- **Induction:**  
Time-varying magnetic fields induce electric fields everywhere  
  
→ Large induced currents in conductors

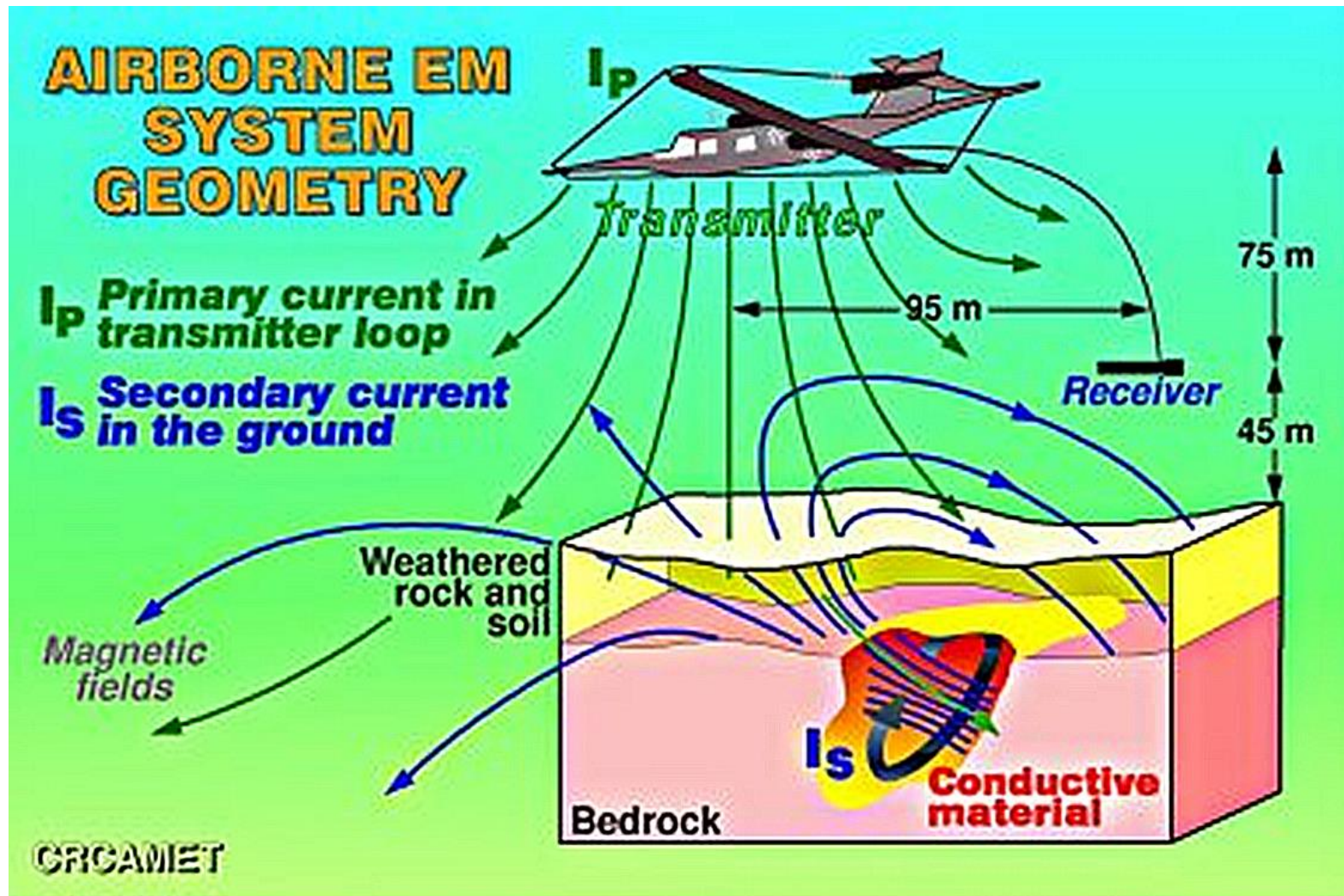


# Basic Experiment

- **Source (Tx):**  
Current loop makes primary magnetic field
- **Induction:**  
Time-varying magnetic fields induce electric fields everywhere  
  
→ Large induced currents in conductors
- **Secondary Fields:**  
Induced currents in conductors produce secondary magnetic fields
- **Receiver (Rx):**  
Measures magnetic fields

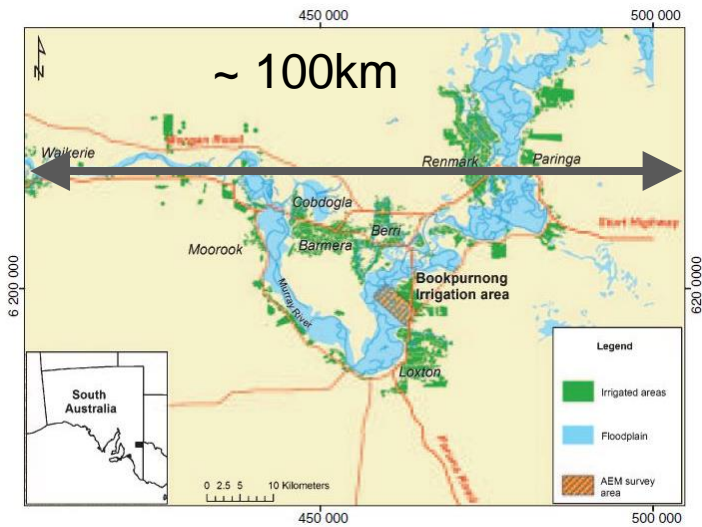


# All Together

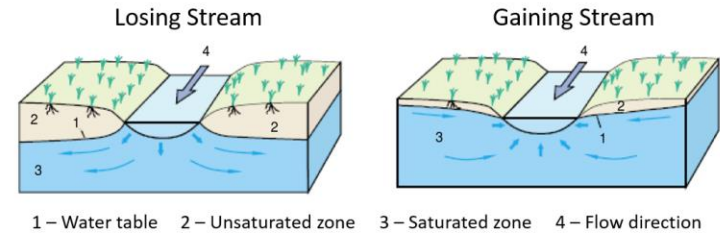


# Motivation for Airborne EM

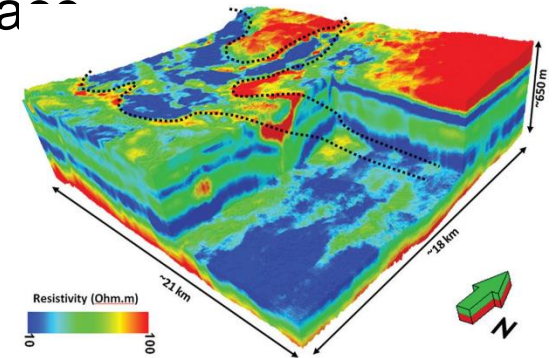
Large areas to be covered



Groundwater



High resolution near surface



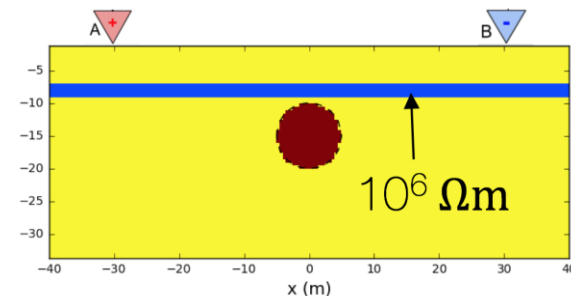
Rugged terrain



Minerals



Shielding problem





# Many applications

Electromagnetics can be used for ...



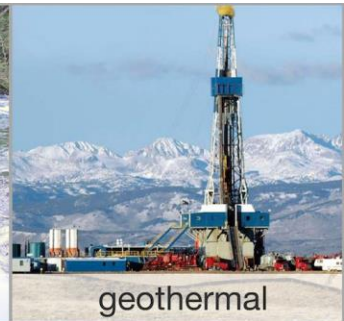
minerals



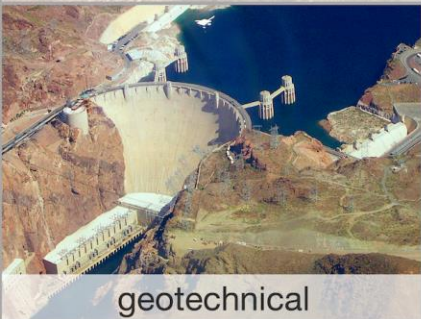
contaminants



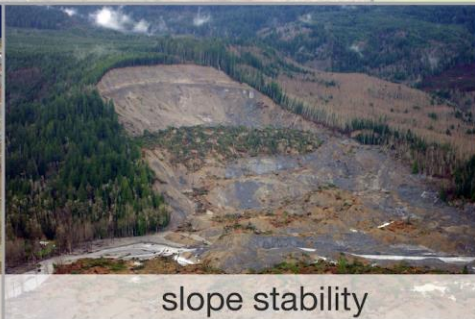
water



geothermal



geotechnical



slope stability



hydrocarbons



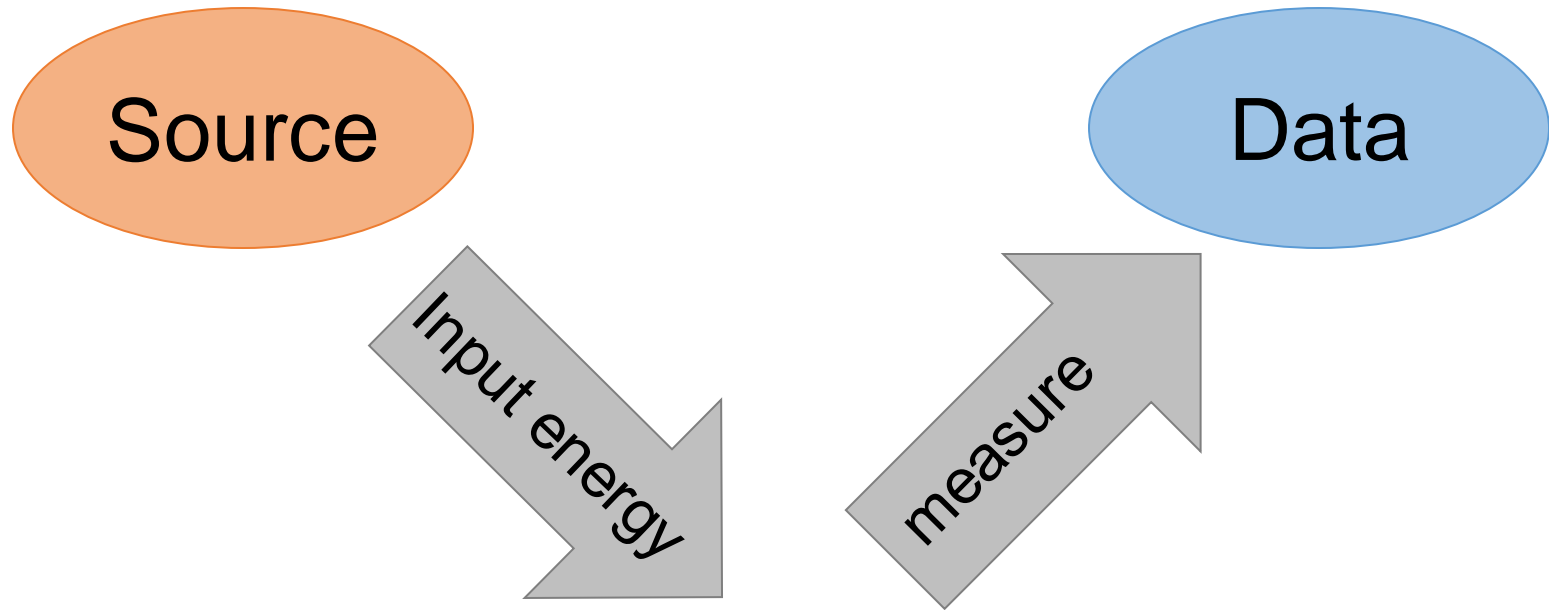
unexploded ordnance

# Physical properties

Reading on the GPG:

[https://gpg.geosci.xyz/content/electromagnetics/electromagnetic\\_physical\\_properties.html](https://gpg.geosci.xyz/content/electromagnetics/electromagnetic_physical_properties.html)

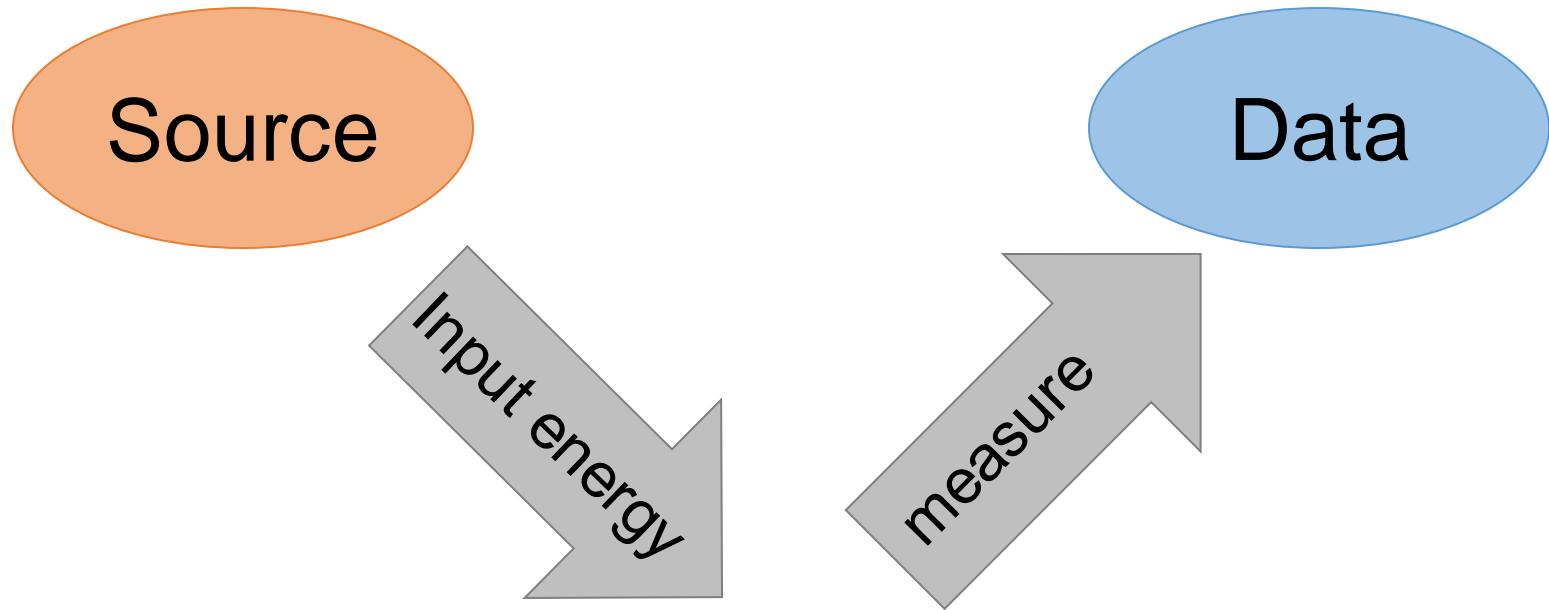
# EM Survey & Physical Properties



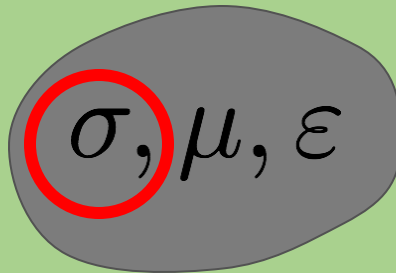
Physical  
Properties

$\sigma, \mu, \epsilon$

# EM Survey & Physical Properties



Physical  
Properties





# Electrical conductivity

$\sigma$ : Conductivity [S/m]

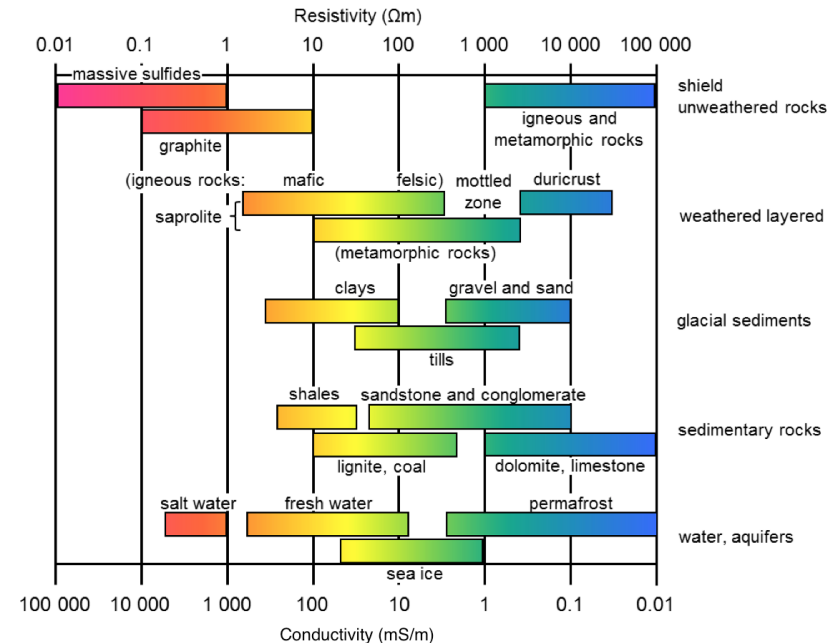
$\rho$ : Resistivity [ $\Omega\text{m}$ ]

$$\sigma = 1/\rho$$

- Varies over many orders of magnitude

- Depends on many factors:

- Rock type
- Porosity
- Connectivity of pores
- Nature of the fluid
- Metallic content of the solid matrix



# Basic Principles: Ampere's Law

Reading on the GPG:

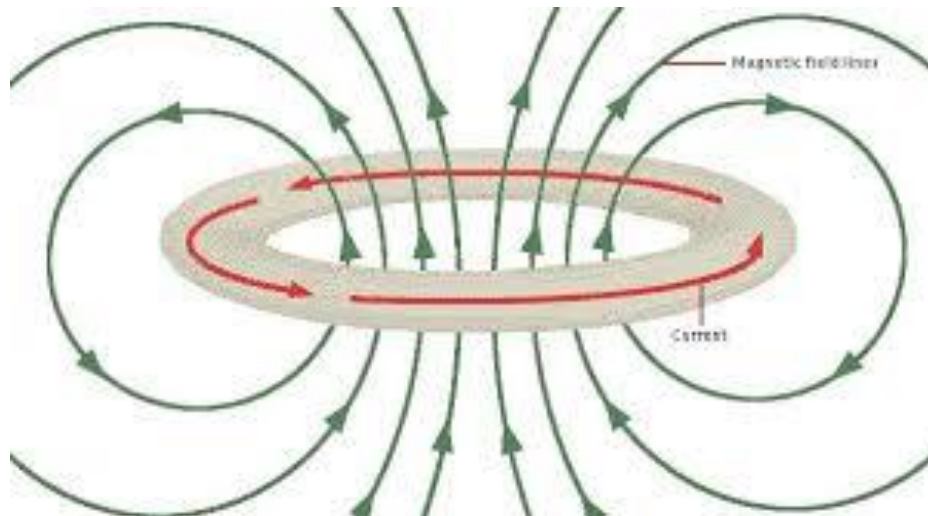
[https://gpg.geosci.xyz/content/electromagnetics/electromagnetic\\_basic\\_principles.html](https://gpg.geosci.xyz/content/electromagnetics/electromagnetic_basic_principles.html)

# Ampere's Law

$$\nabla \times \mathbf{H} = \mathbf{J}$$

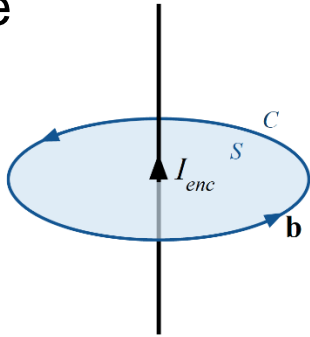
- Relationship between density of electric currents ( $\mathbf{J}$ ) and magnetic fields ( $\mathbf{H}$ )

→ Electric current produces magnetic fields



# Ampere's Law

Wire



$$\mathbf{B} = \frac{\mu_0 I_{enc}}{2\pi r} \hat{\phi}$$

Right hand rule

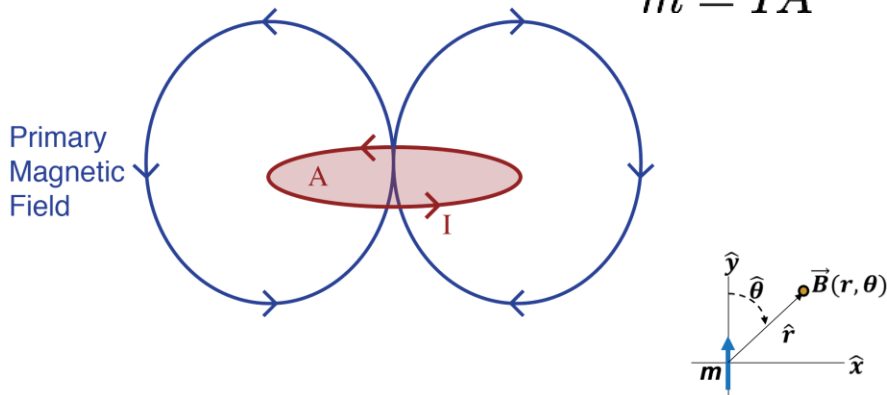
Wire:

- Right-hand rule
- Magnetic field proportional to:
  - Current
  - $1/r$

Current loop

$$\mathbf{B} = \frac{\mu_0 m}{4\pi r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

$$m = IA$$



Loop:

- Right-hand rule
- Magnetic field proportional to
  - Current X Area
  - $1/r^3$  far enough away (dipole field)

# Ampere's Law: Dipolar Field

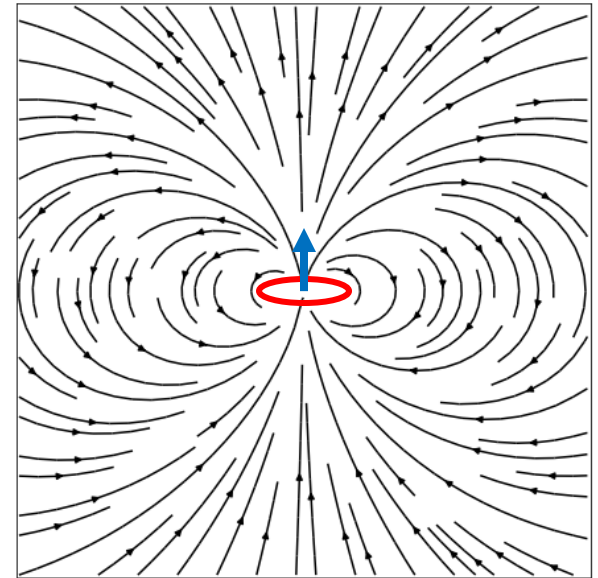
- Dipole moment:

$$m = IA$$

- Field due to a single dipole

$$\vec{B} = \frac{\mu_0}{4\pi} \left( \frac{3\vec{r}(\vec{m} \cdot \vec{r})}{r^5} - \frac{\vec{m}}{r^3} \right)$$

- Here current is CCW so by right-hand rule dipole moment is up



# Basic Principles: Faraday's Law

Reading on the GPG:


[https://gpg.geosci.xyz/content/electromagnetics/electromagnetic\\_basic\\_principles.html](https://gpg.geosci.xyz/content/electromagnetics/electromagnetic_basic_principles.html)

# Faraday's Law: Differential Form

- Time-dependent (or frequency-dependent) magnetic fields produce electric fields

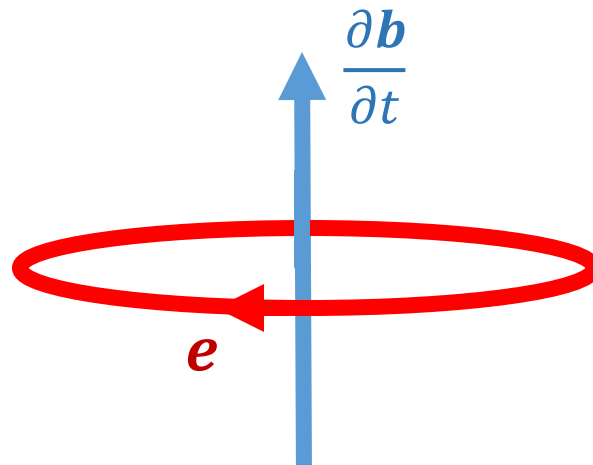
$$\nabla \times \mathbf{e} = - \frac{\partial \mathbf{b}}{\partial t}$$

Lenz'  
Law



$$\nabla \times \mathbf{E} = -i\omega \mathbf{B}$$

- Use “left-hand rule”



# Faraday's Law: Integral Form

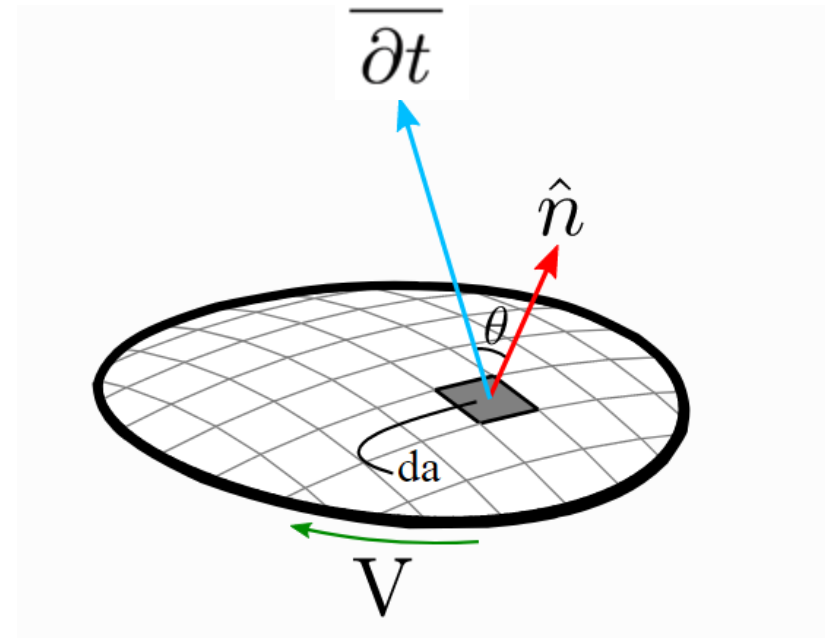
- Time varying magnetic flux induces voltage (EMF) in a current loop

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt}$$

- Magnetic flux is given by:

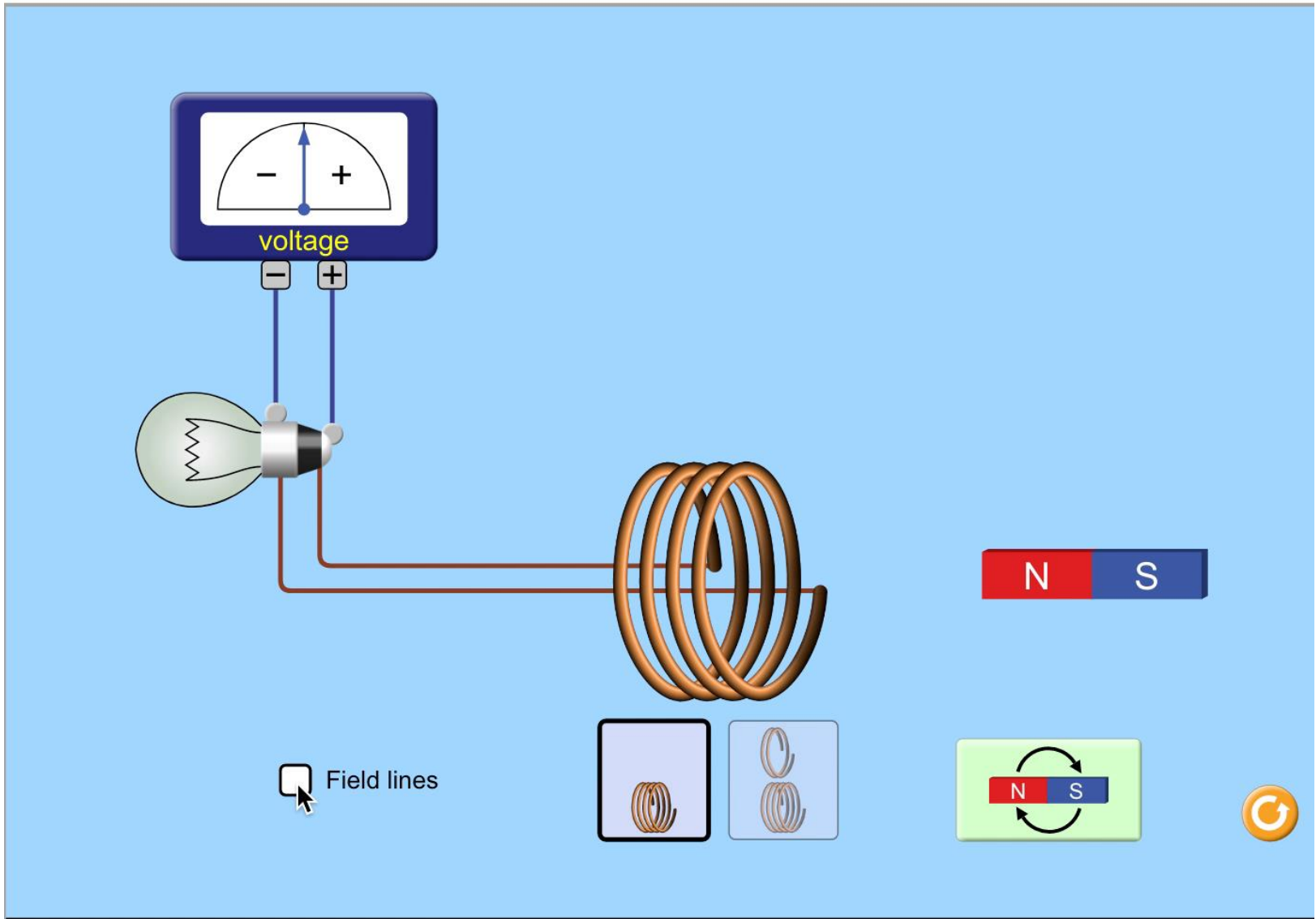
$$\phi_{\mathbf{b}} = \int_A \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

- Use left-hand rule





# Faraday's Law: Flux from magnet



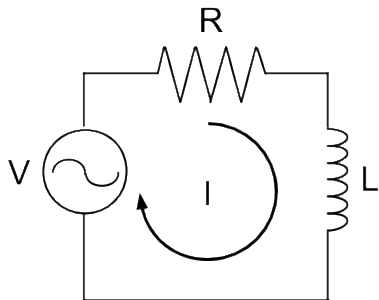
# Faraday's Law: Flux from magnet

Magnetic Flux

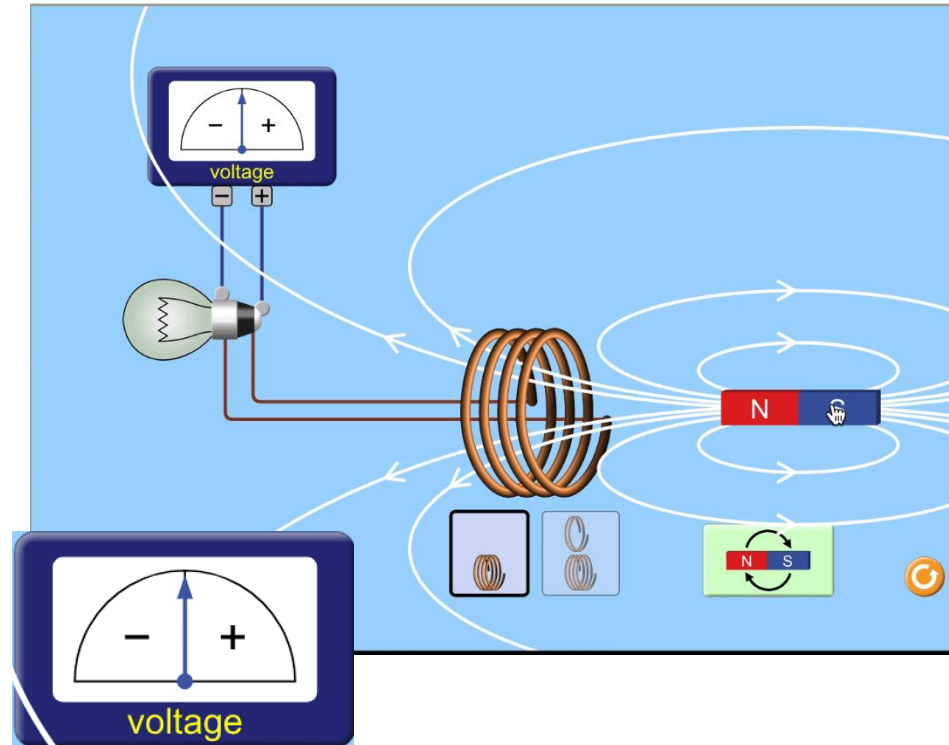
$$\phi_{\mathbf{b}} = \int_A \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

Induced EMF

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt} = \mathbf{0}$$



$\phi_b$  : constant



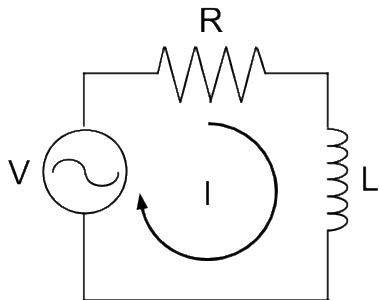
# Faraday's Law: Flux from magnet

Magnetic Flux

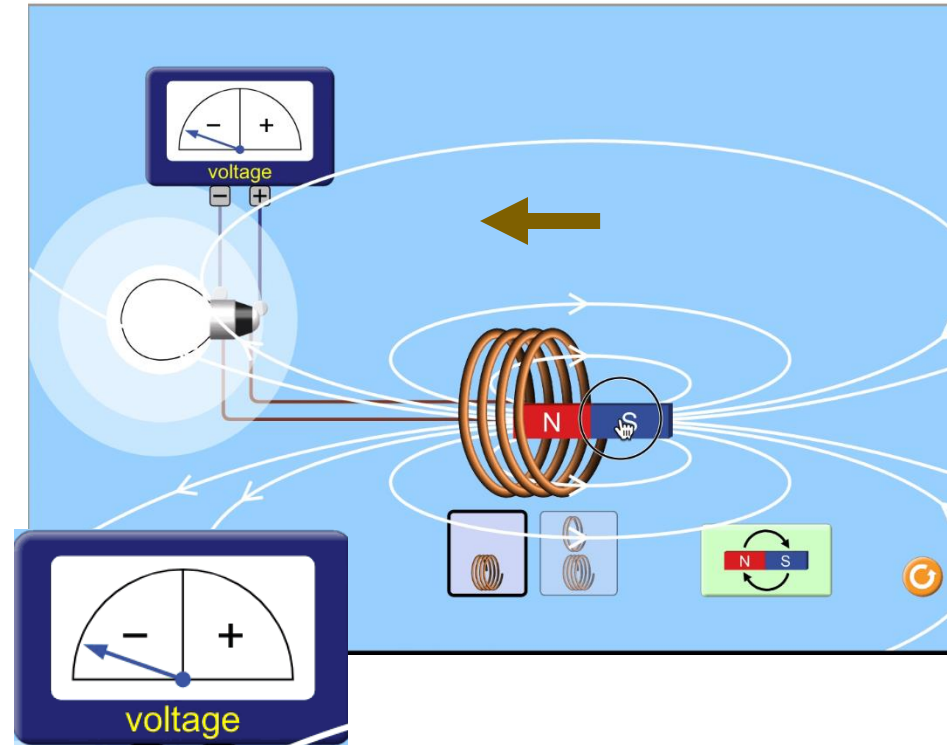
$$\phi_{\mathbf{b}} = \int_A \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

Induced EMF

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt} < 0$$



$\phi_b$  : 



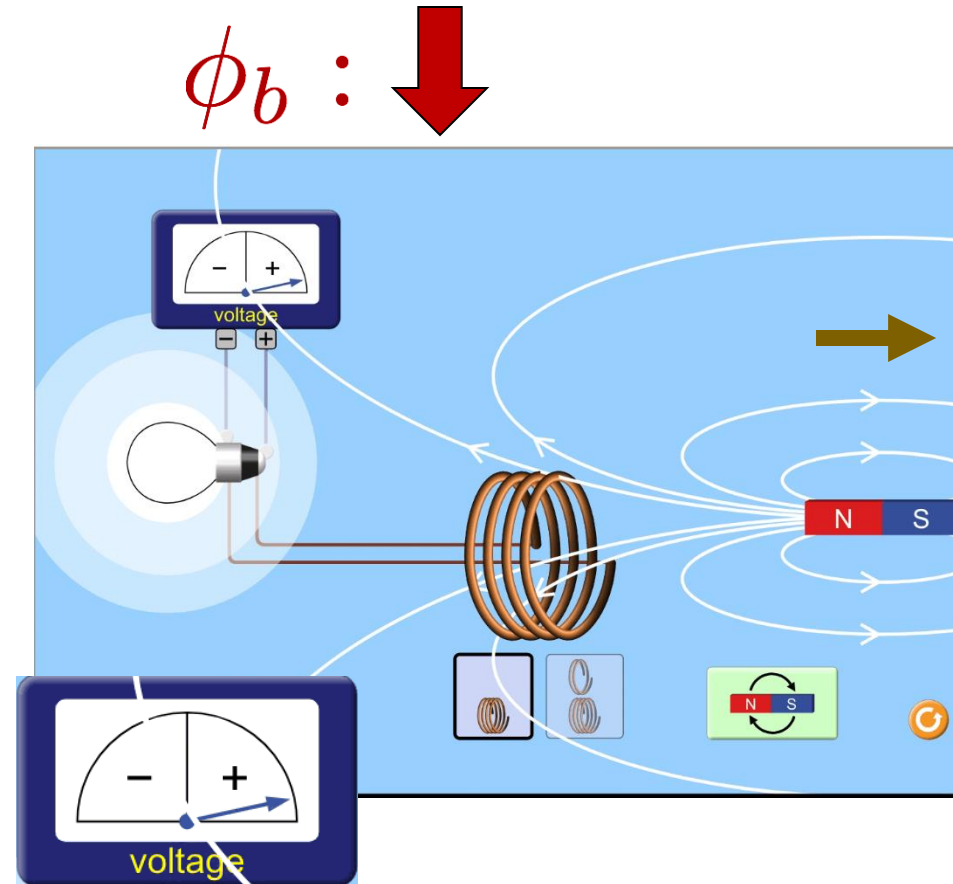
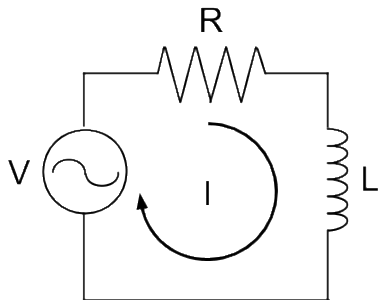
# Faraday's Law: Flux from magnet

Magnetic Flux

$$\phi_{\mathbf{b}} = \int_A \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

Induced EMF

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt} > 0$$



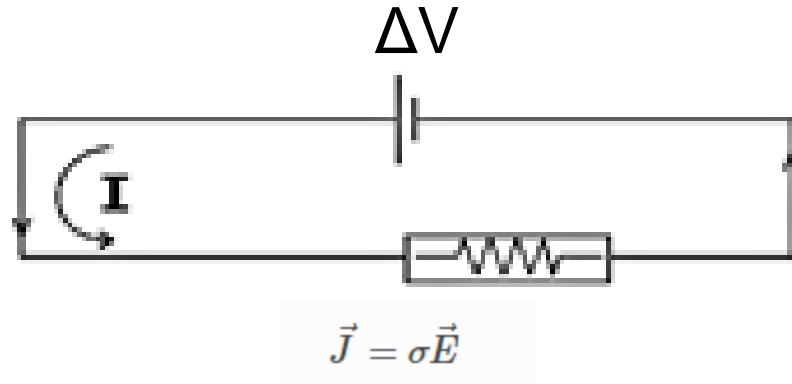
# Basic Principles: Ohm's Law

Reading on the GPG:

[https://gpg.geosci.xyz/content/electromagnetics/electromagnetic\\_basic\\_principles.html](https://gpg.geosci.xyz/content/electromagnetics/electromagnetic_basic_principles.html)

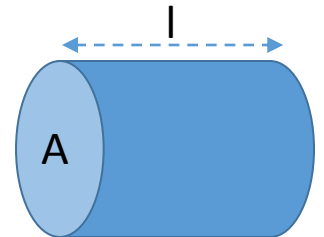
# DC resistivity and Ohm's Law

- Electric circuit:



- Ohm's Law:  $\Delta V = IR$

- Resistivity:  $\rho = R \frac{A}{l}$



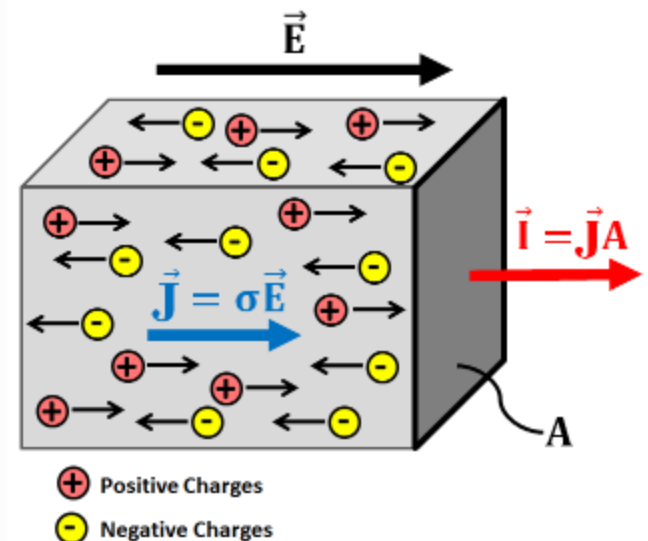
# General Ohm's Law

- Relates the electric field to density of electric current in a material
- Electric field and current in same direction
- Electric fields in conductive materials will produce stronger currents
- Electric fields in resistive materials produce very weak currents

$$\vec{J} = \sigma \vec{E}$$

$$\rho = \frac{1}{\sigma}$$

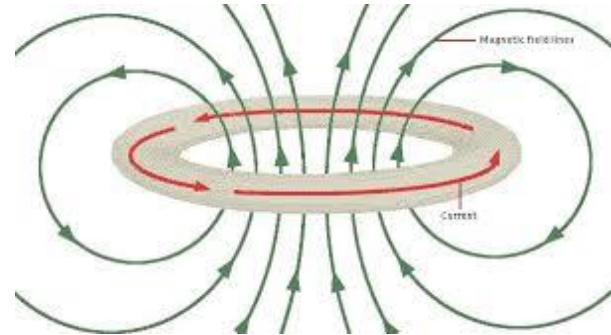
Conductivity in Materials



# Recap

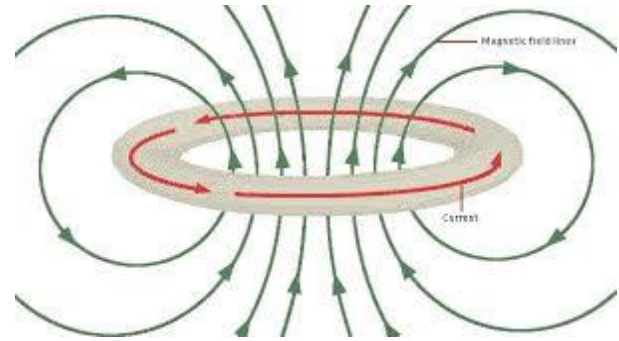
**Ampere's Law:**  $\nabla \times \mathbf{H} = \mathbf{J}$

- Currents produce magnetic fields
- Right-hand rule





# Recap

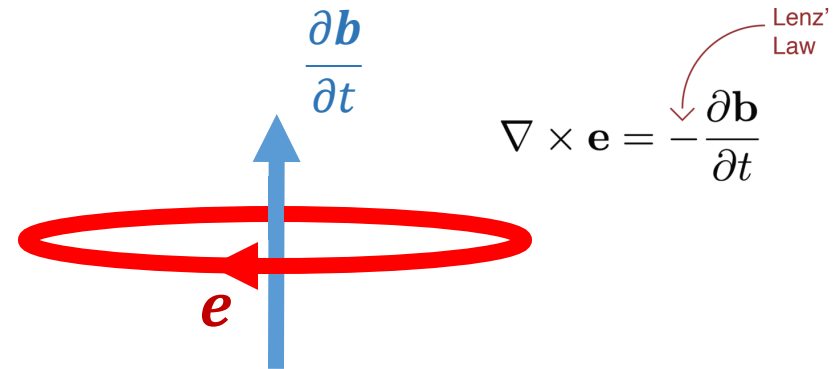


**Ampere's Law:**  $\nabla \times \mathbf{H} = \mathbf{J}$

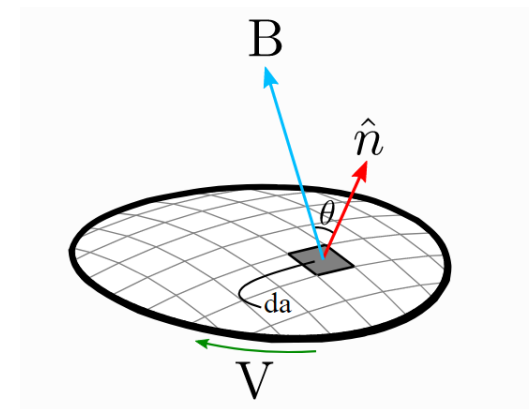
- Currents produce magnetic fields
- Right-hand rule

**Faraday's Law**

- Time/frequency varying magnetic fields produce electric fields
- Time/frequency varying magnetic flux generates voltage in wire loops
- Left-hand rule



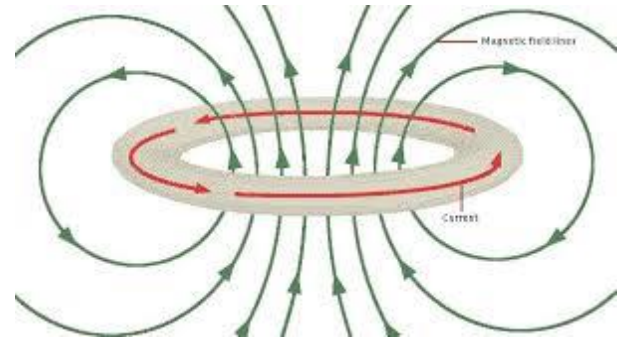
$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt}$$



# Recap

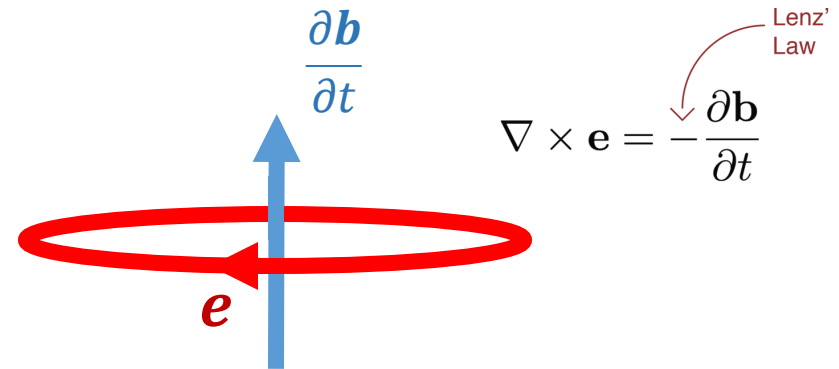
## Ampere's Law: $\nabla \times \mathbf{H} = \mathbf{J}$

- Currents produce magnetic fields
- Right-hand rule



## Faraday's Law

- Time/frequency varying magnetic fields produce electric fields
- Time/frequency varying magnetic flux generates voltage in wire loops
- Left-hand rule

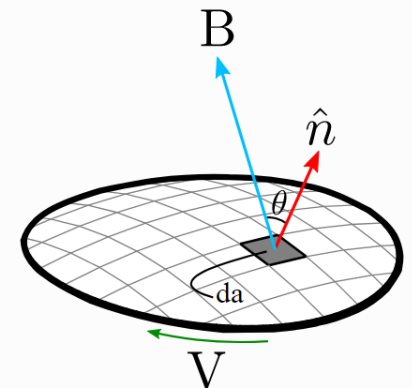


## Ohm's Law

- Current resulting from electric fields depends on conductivity/resistivity

$$\vec{J} = \sigma \vec{E}$$

$$V = EMF = -\frac{d\phi_{\mathbf{b}}}{dt}$$



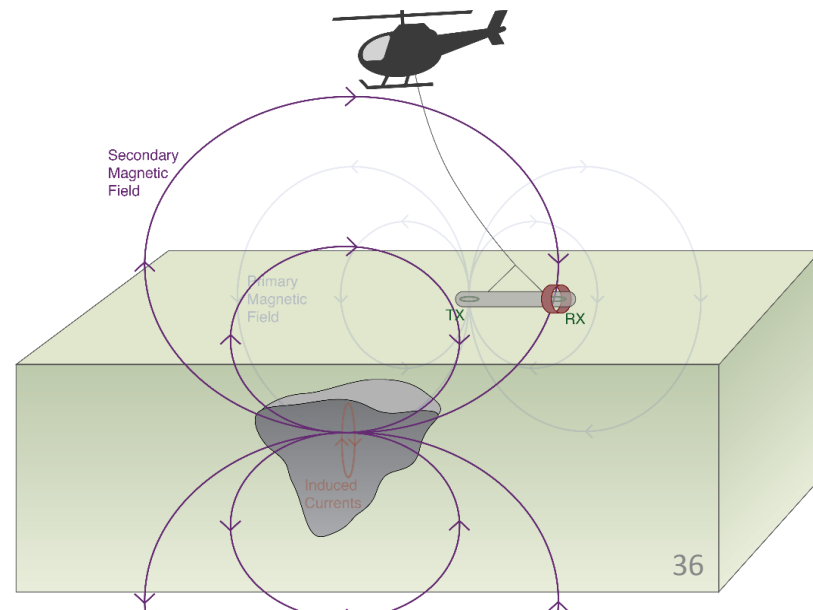
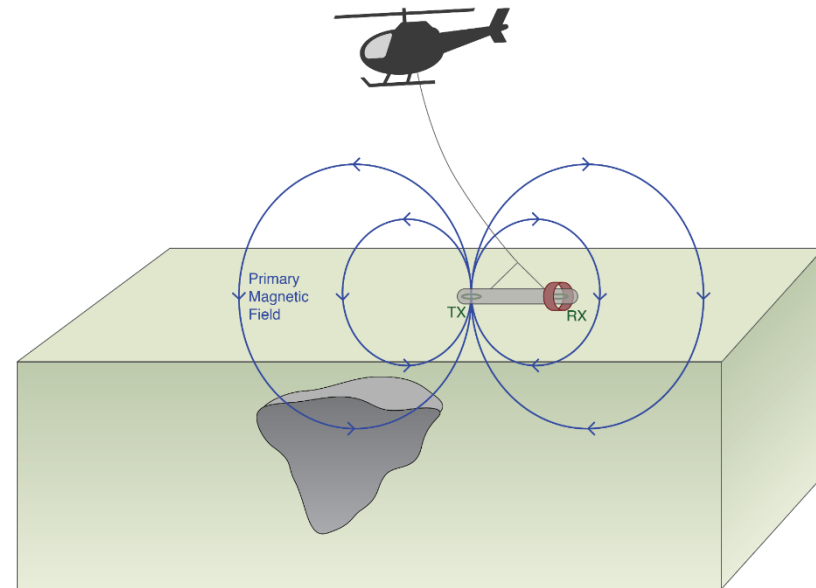
# Basic Principles: EM Experiment Revisited

Reading on the GPG:

[https://gpg.geosci.xyz/content/electromagnetics/electromagnetic\\_basic\\_principles.html](https://gpg.geosci.xyz/content/electromagnetics/electromagnetic_basic_principles.html)

# Basic Experiment

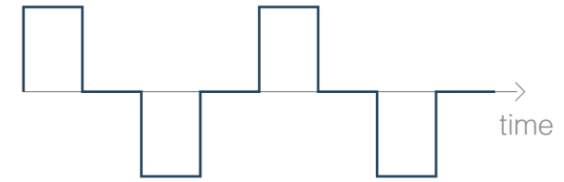
- **Source (Tx):**  
Current loop makes primary magnetic field
- **Induction:**  
Time-varying magnetic fields induce electric fields everywhere  
  
→ Large induced currents in conductors
- **Secondary Fields:**  
Induced currents in conductors produce secondary magnetic fields
- **Receiver (Rx):**  
Measures magnetic fields



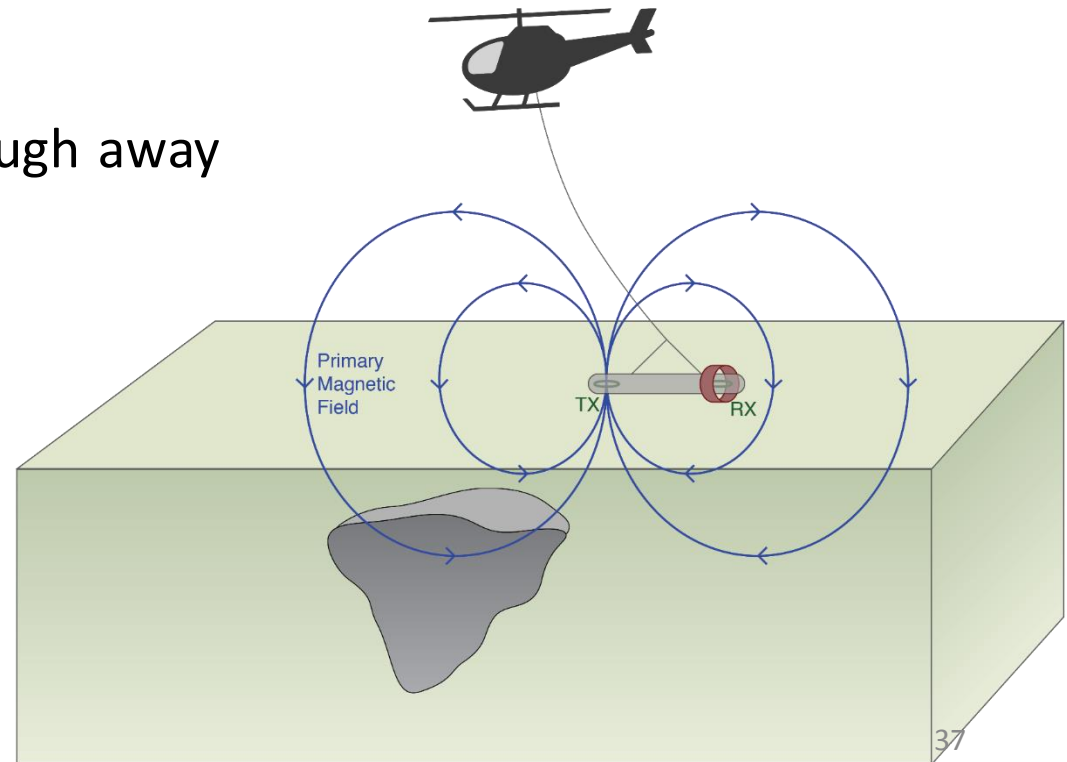
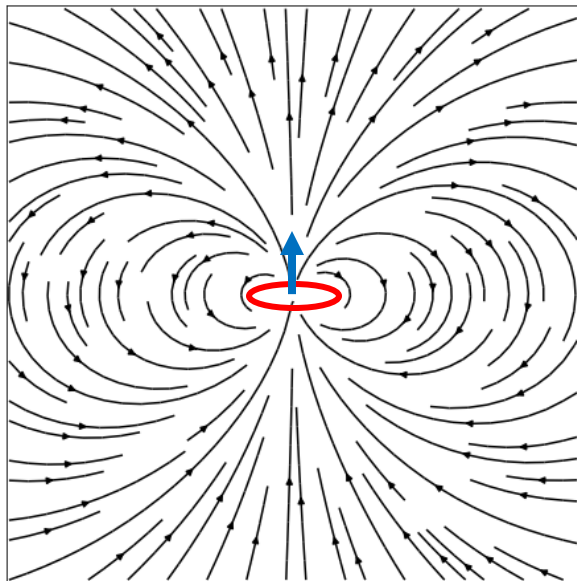
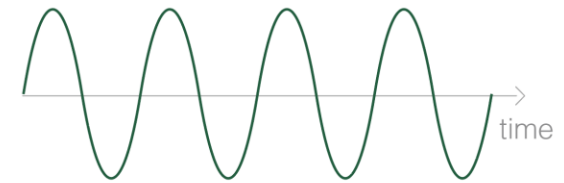
# Transmitter

- Transmitter is a current loop
- Currents produce primary magnetic field (Ampere)
- Current and primary field direction related by right hand rule
- Primary field dipolar far enough away

waveform

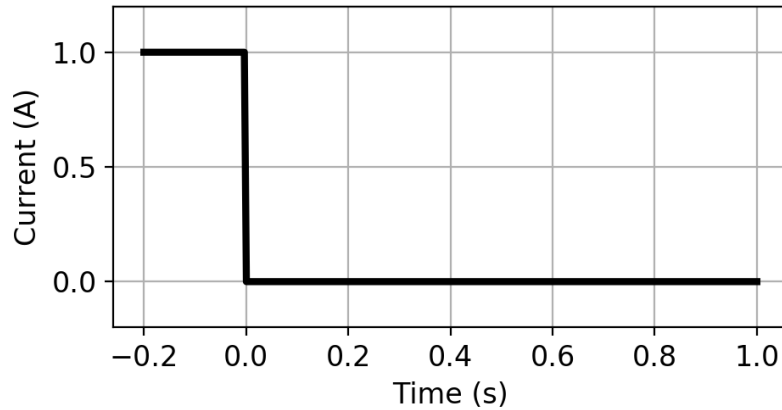


or

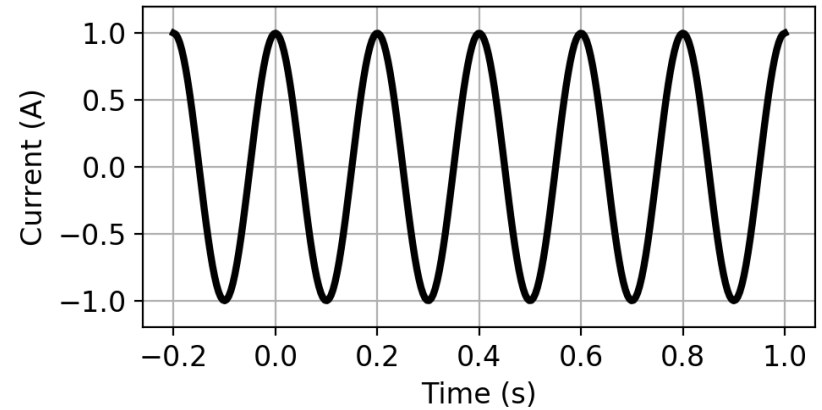


# Transmitter Waveforms

**Time Domain: Transient Pulse**



**Frequency Domain: Harmonic**

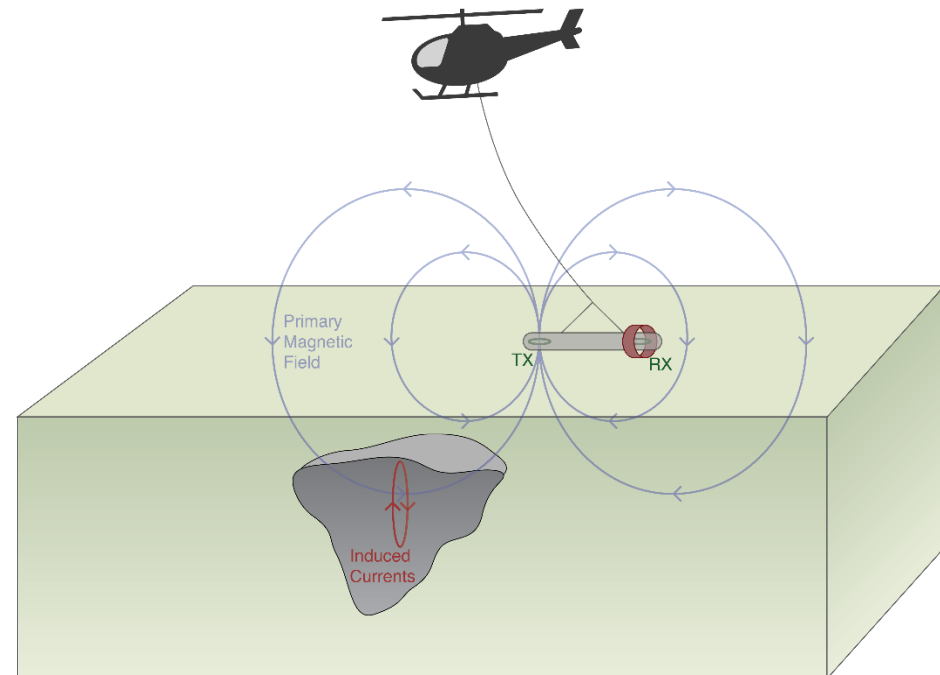


# Induction and Induced Currents

- Time-varying/harmonic magnetic fields induce electric fields (Faraday)
- Change in magnetic field and electric field direction related by left-hand rule

$$\nabla \times \mathbf{e} = -\frac{\partial \mathbf{b}}{\partial t}$$

Lenz' Law



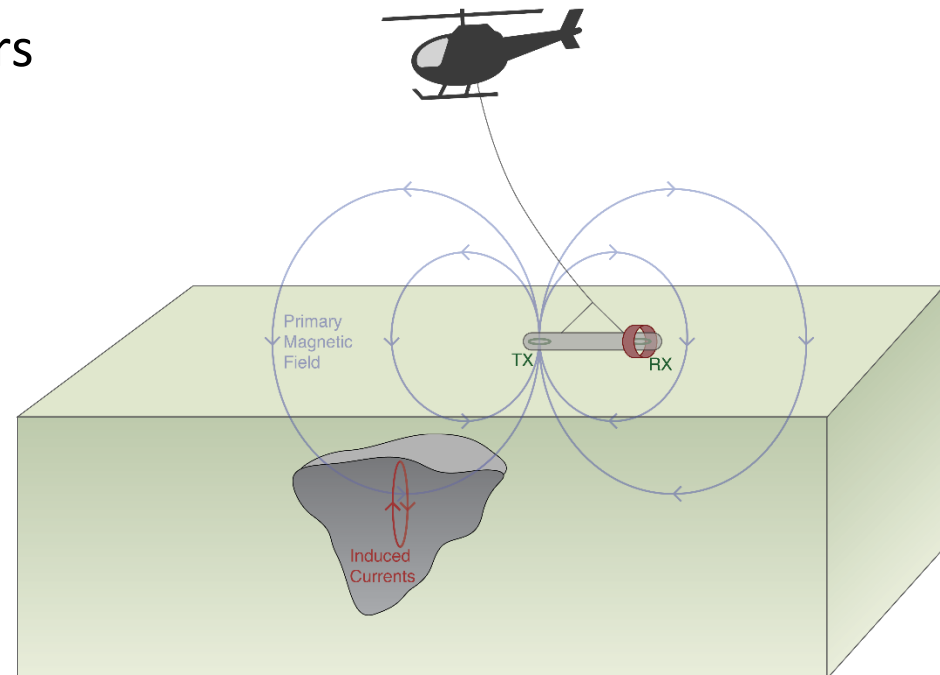
# Induction and Induced Currents

- Time-varying/harmonic magnetic fields induce electric fields (Faraday)
- Change in magnetic field and electric field direction related by left-hand rule
- Induced electric fields (Ohm's law)
  - Large induced currents in conductors
  - Weak induced currents in resistors

$$\vec{J} = \sigma \vec{E}$$

$$\nabla \times \mathbf{e} = - \frac{\partial \mathbf{b}}{\partial t}$$

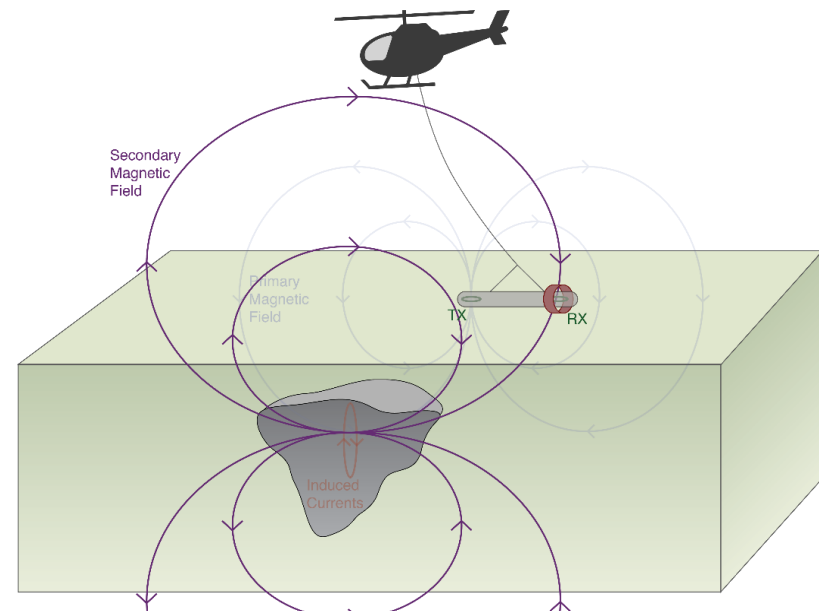
Lenz' Law





# Secondary Fields

- Induced current produce secondary magnetic field (Ampere)
  - Strong secondary fields from conductors
  - Weak secondary fields from resistors
- Current and secondary field direction related by right hand rule

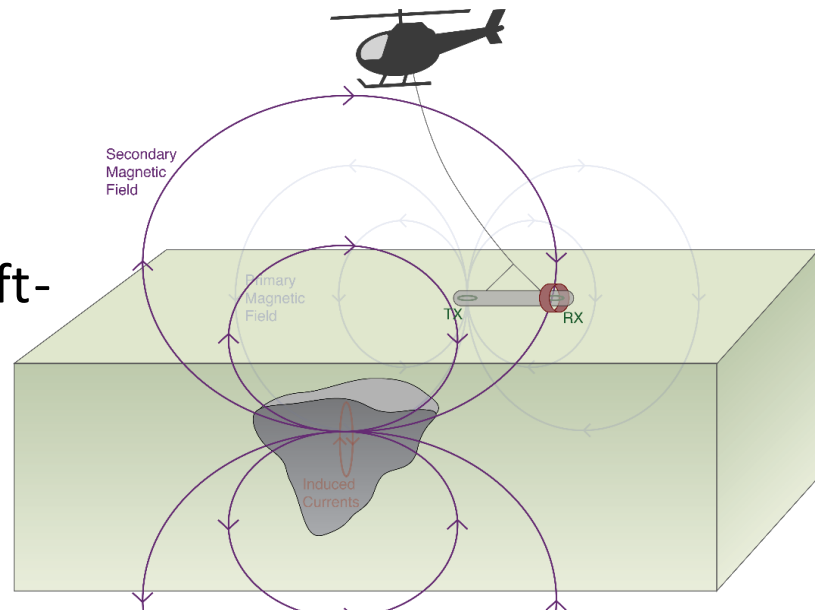


# Receivers

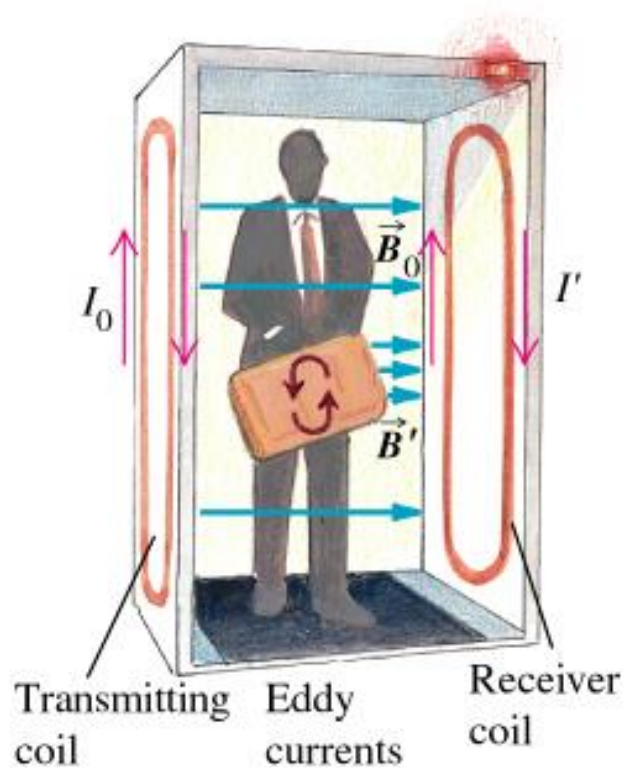
- Secondary fields (and primary fields) are time-varying/harmonic
  - Change in magnetic flux through receiver loop
  - Induces voltage in receiver loop (Faraday)
- Only measures component of the field normal to the receiver loop
- Voltage and change in flux related by left-hand rule

$$\phi_{\mathbf{b}} = \int_A \mathbf{b} \cdot \hat{\mathbf{n}} \, da$$

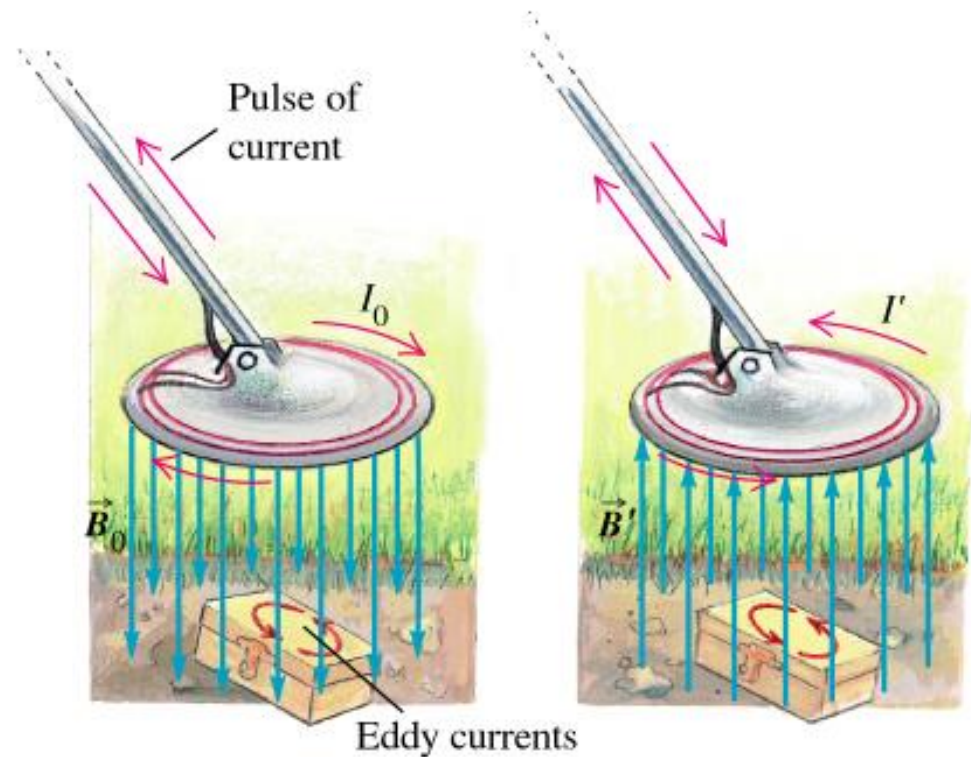
$$V = EMF = - \frac{d\phi_{\mathbf{b}}}{dt}$$



# Other EM Applications



Security scan



Metal detector

# Unit Activities

- **Labs: (EM I)**
  - Monday, November 4<sup>th</sup>
  - Tuesday, November 5<sup>th</sup>
- **Labs: (EM II)**
  - Monday, November 18<sup>th</sup>
  - Tuesday, November 19<sup>th</sup>
- **TBL:**
  - Friday, November 15<sup>th</sup>
- **Quiz:**
  - Wednesday, November 20<sup>th</sup>