

# What do we know so far?

- Geophysical surveys measure the Earth's response to physical input(s)
- Geophysics is viable if there is sufficient contrast in one or more physical properties
- For each physical property contrast there is one or more geophysical methods
- We have a 7-step framework for using geophysics to answer geoscientific questions

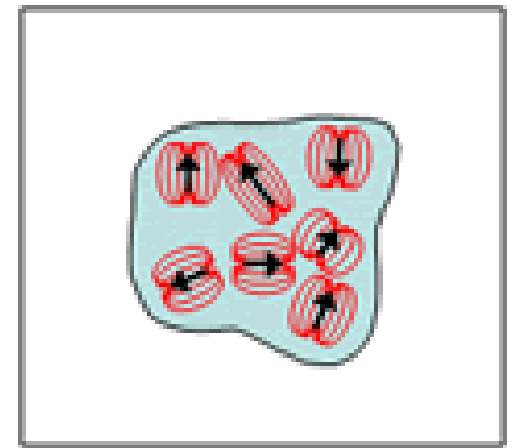
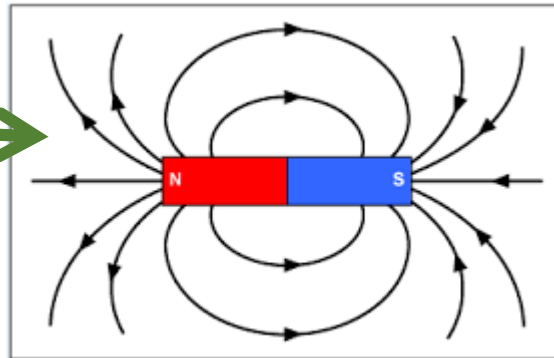
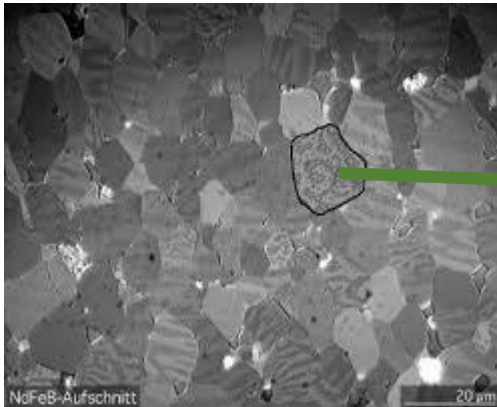
# Today's topics

- Magnetism fundamentals
- Physical properties
- Magnetic fields and fluxes
- Remanent magnetization
- Magnetic methods (basic idea)
- Examples of applications

# Magnetism Fundamentals

# Magnetic materials and magnetization

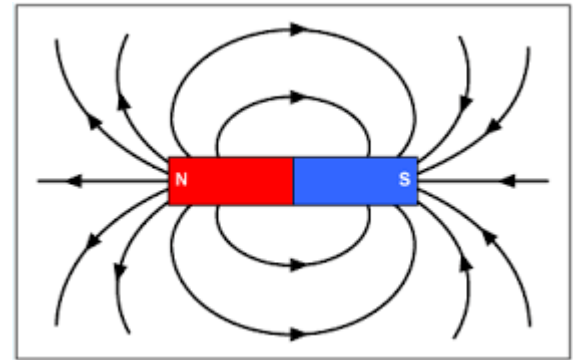
- Mineral grains contain **magnetic domains** that behave like small bar magnets
- Bar magnets have a North and a South pole  
→ **magnetic dipole**
- Each magnetic domain (dipole) contributes towards the overall magnetization of a material



# Magnetization and magnetic fields

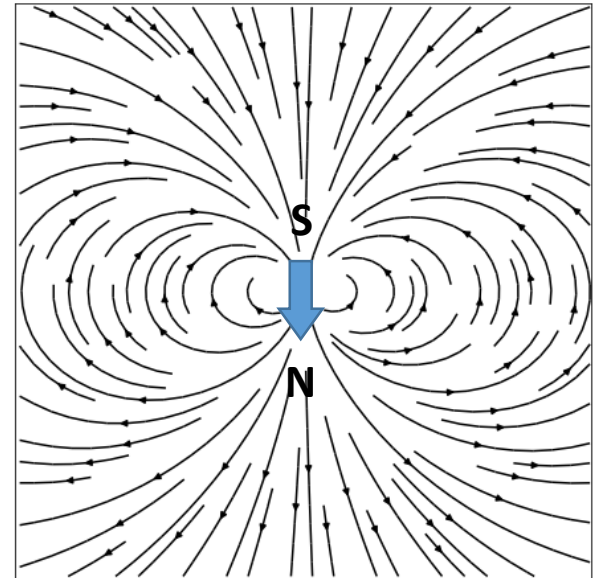
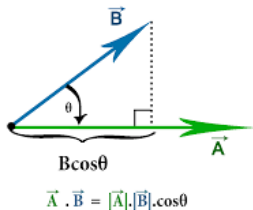
- Magnetization produces a magnetic field

- Magnetic field lines extend from North pole to South pole



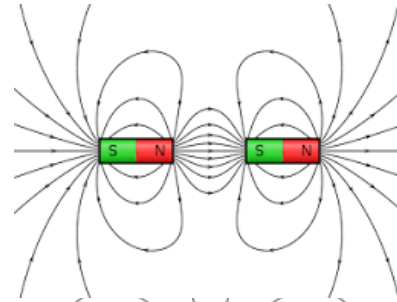
- Field due to a single dipole →

$$\vec{B} = \frac{\mu_0}{4\pi} \left( \frac{3\vec{r}(\vec{m} \cdot \vec{r})}{r^5} - \frac{\vec{m}}{r^3} \right)$$

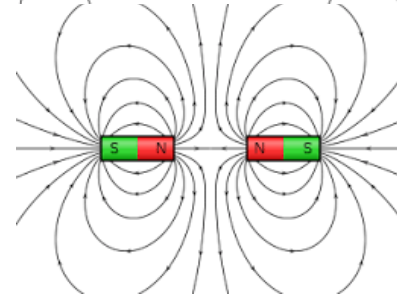


# How do bar magnets (dipoles) interact?

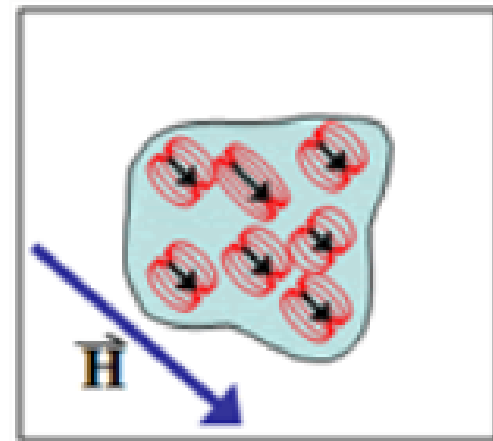
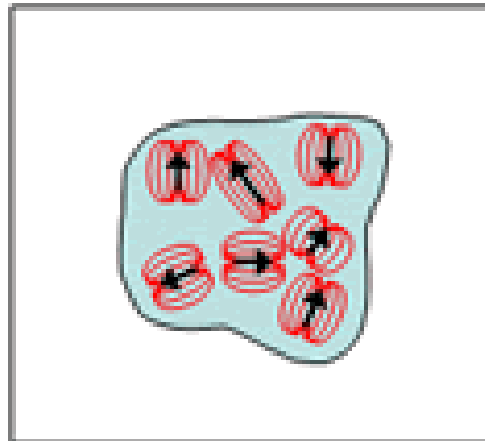
- Opposite poles attract



- Like poles repel



- Small magnets align with fields from stronger magnets

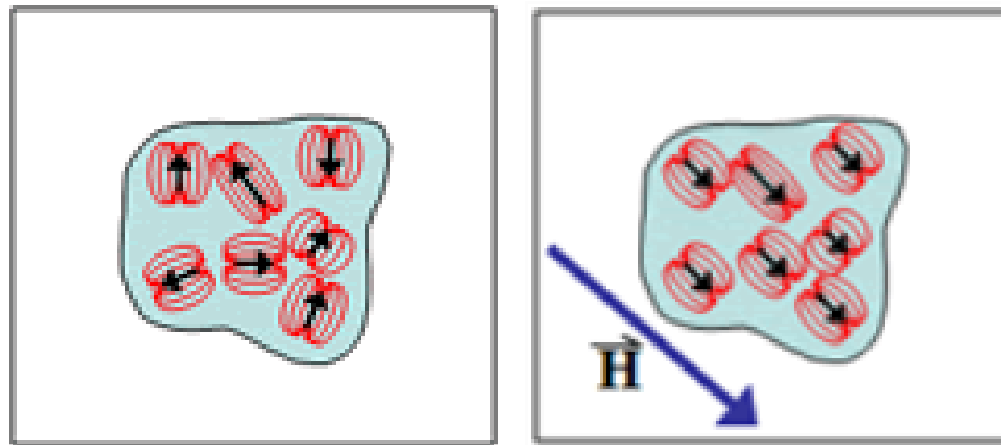


# Dipole moment and magnetization

- **Magnetic dipole moment**  $m_i$  defines the strength and orientation of a magnetization (domain or rock)
- **Magnetization** is average magnetic moment per unit volume

$$\vec{M} = \frac{\sum \vec{m}_i}{Volume}$$

- **Units:** dipole moment per unit volume Ampere/meter (A/m)



# More on dipole moments

- **Magnetic dipole moment**  $m_i$  defines the strength and orientation of a magnetization
- **Magnetization** is average magnetic moment per unit volume

$$\vec{M} = \frac{\Sigma \vec{m}_i}{Volume}$$

- Integrate magnetism to get dipole moment for a whole sample

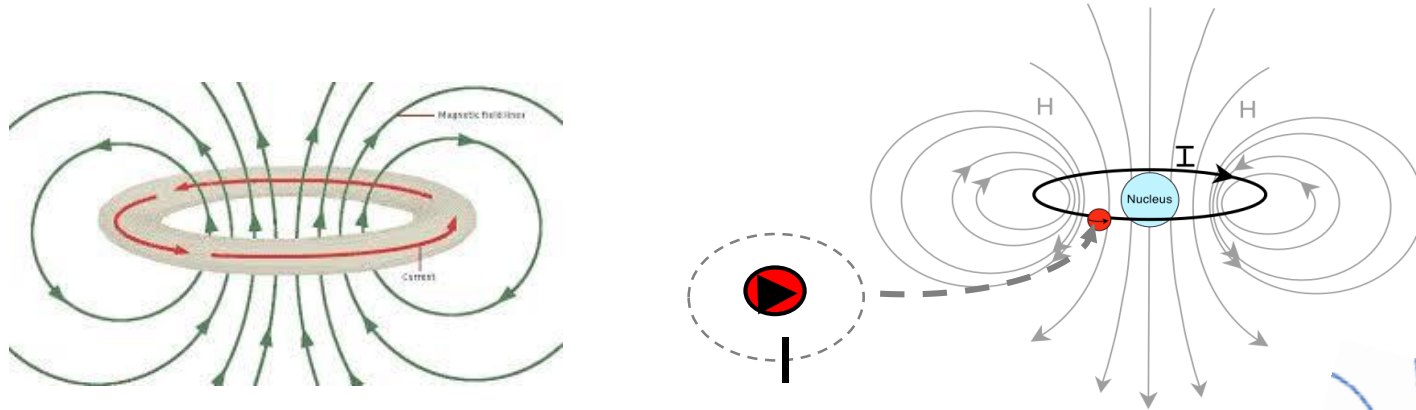
$$m = \int M dV$$

- Dipole moment has units Ampere-m<sup>2</sup>

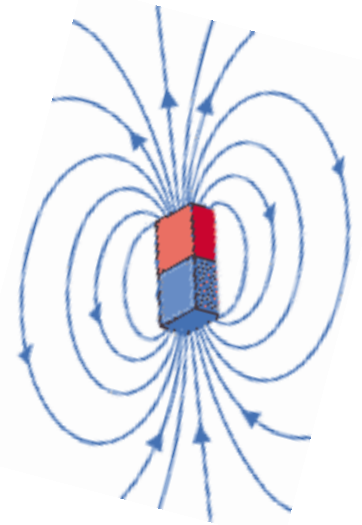


# Sources of magnetism

Magnetism results from movement of electric charges



- A current loop produces magnetic fields
- Atoms can have a dipole moment and produce fields:
  - Electrons and protons spin on their axis
  - Electron circulate around the atomic nucleus.
- A magnetic domain is a region of uniform atomic spins



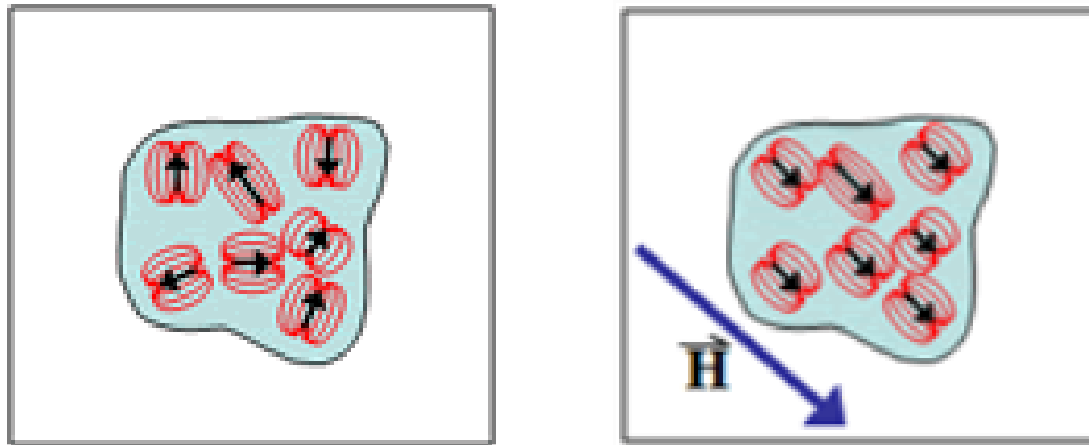
# Physical Properties

Reading on the GPG:

[https://gpg.geosci.xyz/content/physical\\_properties/magnetics\\_susceptibility\\_duplicate.html#susceptibility](https://gpg.geosci.xyz/content/physical_properties/magnetics_susceptibility_duplicate.html#susceptibility)

# What we learned

- The magnetization changes when a magnetic field is applied
- **Induced magnetization** lies along direction of the applied field



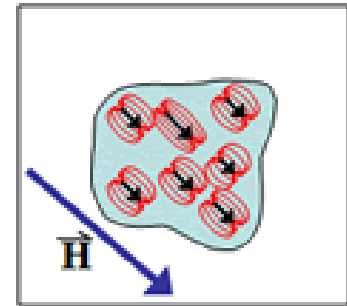
- How do we define the **induced magnetization** due to an applied magnetic field?

# Magnetic Susceptibility: $\kappa$

- Defines strength of magnetization due to an external field

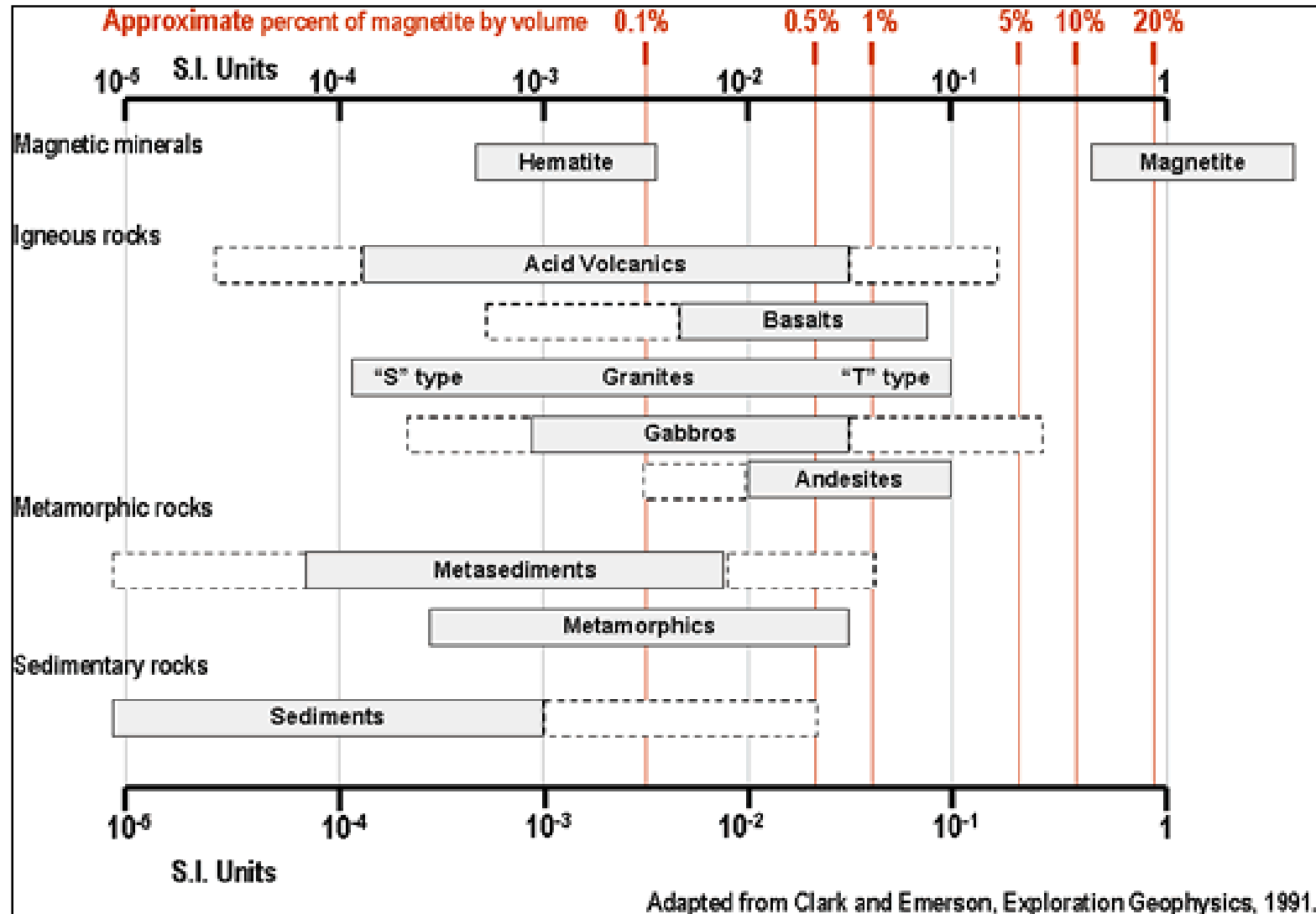
$$\vec{M} = \frac{\sum \vec{m}_i}{Volume}$$

$$\vec{M} = \kappa \vec{H}$$



- Magnetization parallel to inducing field
- Susceptibility units: dimensionless

# Magnetic Susceptibility of Rocks



# Different mechanisms for induced magnetization

$$\vec{M} = \kappa \vec{H}$$

- Ferromagnetic Materials:  $\kappa \sim +1 \rightarrow +10$
- Ferrimagnetic Materials:  $\kappa \sim +1 \rightarrow +10$
- Antiferromagnetic Materials:  $\kappa \sim +10^{-4} \rightarrow +10^{-3}$
- Paramagnetic Materials:  $\kappa \sim +10^{-5} \rightarrow +10^{-2}$
- Diamagnetic Materials:  $\kappa \sim -10^{-5}$ .

$$\vec{M} = \kappa \vec{H}$$

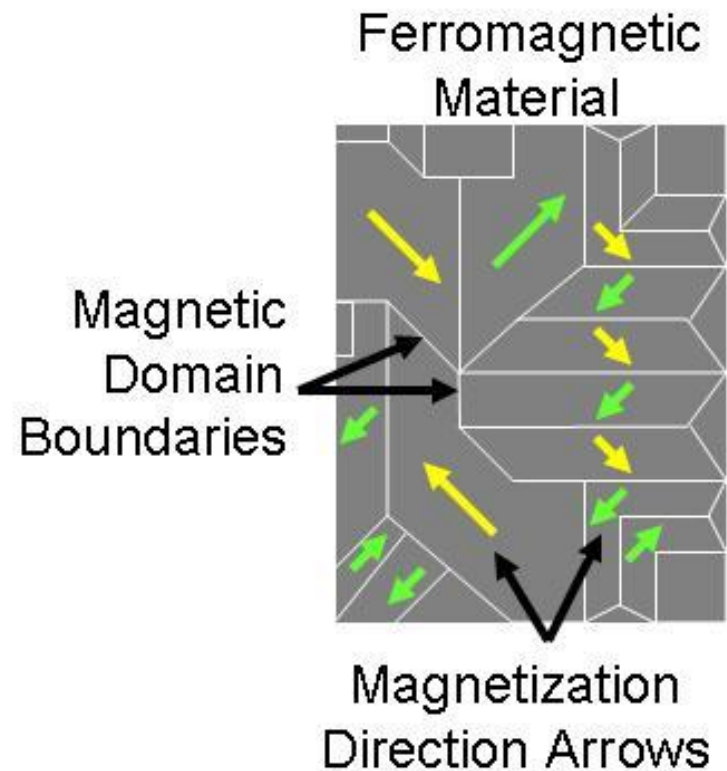
Ferromagnetic Materials:

$\kappa \sim +1 \rightarrow +10$

(induced field can be 10× inducing field). Magnetization is organized in domains of many atoms.

Iron, cobalt and nickel are ferromagnetic.

We place iron cores inside solenoids to make their magnetic fields stronger.



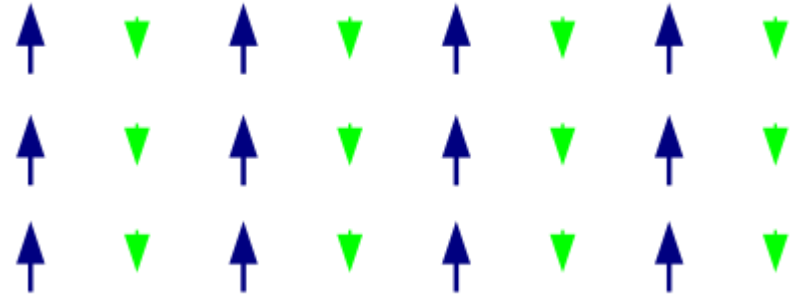
Anthropogenic features made of iron like pipes, rebar and drums are magnetized by Earth's field and show up well on magnetic surveys.

$$\vec{M} = \kappa \vec{H}$$

Ferrimagnetic Materials:  
 $\kappa \sim +1 \rightarrow +10$

are like ferromagnetics, but atoms in different positions in the crystal lattice have opposite and unequal magnetic moments.

Magnetite, ilmenite, titanomagnetite and pyrrhotite are examples



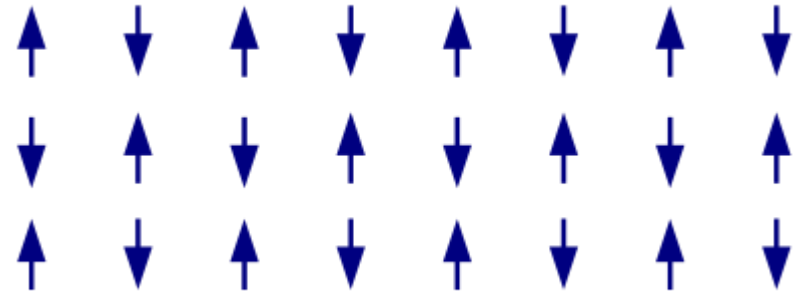
These minerals are responsible for most of the geological anomalies on magnetic surveys.



# Antiferromagnetic Materials

$$\kappa \sim +10^{-4} \rightarrow +10^{-3}$$

Neighbouring atoms have opposite and nearly equal magnetic moments leading to relatively small susceptibility.

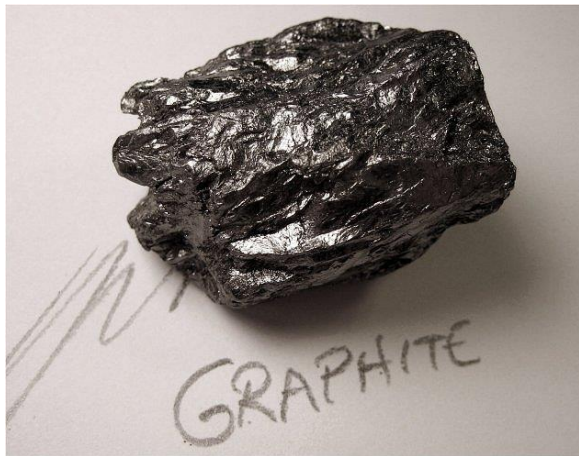


Hematite ( $\text{Fe}_2\text{O}_3$ ) is the most common example.



Diamagnetic Materials: negative  $\kappa$  approximately  $-10^{-5}$  (induced and inducing fields are in opposite directions).

- Oppose the applied magnetic field because that field changes the magnetic moments of electrons in their orbitals in a systematic way
- All materials are technically diamagnetic, but other forms of magnetization (if present) are much stronger
- Halite, graphite, calcite and quartz are common diamagnetic minerals



## Paramagnetic Materials: positive $\kappa$ in range $10^{-5}$ to $10^{-2}$

- Have unpaired electrons which align in a magnetic field to create an induced magnetic field
- Many metals are paramagnetic.



<http://periodictable.com/Elements/074/index.html>

# Magnetic Fields and Fluxes

# Magnetic fields, fluxes and permeability

$\vec{B}$ : Magnetic Flux Density ( $Wb/m^2 = \text{Tesla}$ )

$\vec{H}$ : Magnetic Field ( $A/m$ )

$$\vec{B} = \mu \vec{H}$$

$\mu$  = magnetic permeability

$$\mu = \mu_0(1 + \kappa)$$

Magnetic permeability of free space:

$$\mu_0 = 4\pi \times 10^{-7}$$

# Magnetic fields, fluxes and permeability

$\vec{B}$ : Magnetic Flux Density ( $Wb/m^2 = \text{Tesla}$ )

$\vec{H}$ : Magnetic Field ( $A/m$ )

$$\vec{B} = \mu \vec{H} = \mu_0(1 + \kappa) \vec{H} = \mu_0(\vec{H} + \vec{M})$$

$\mu$  = magnetic permeability

$$\mu = \mu_0(1 + \kappa)$$

↑  
Inducing  
field

↑  
induced

Magnetic permeability of free space:

$$\mu_0 = 4\pi \times 10^{-7}$$

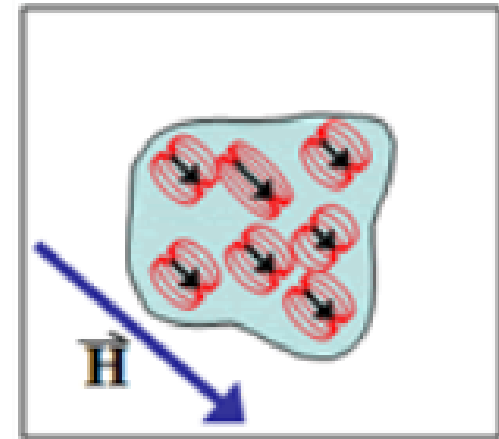
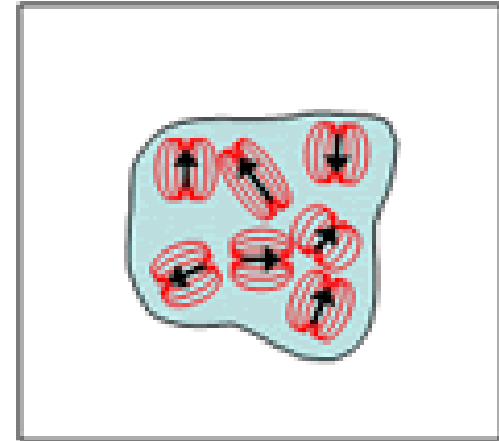
# Recap

- Earth materials contain magnetic domains that behave like magnetic dipoles
- Magnetization is the total dipole moment per unit volume

$$\vec{M} = \frac{\sum \vec{m}_i}{Volume}$$

- Magnetic dipoles will re-orient along the direction of an inducing field
- The strength of induced magnetization is defined by the magnetic susceptibility

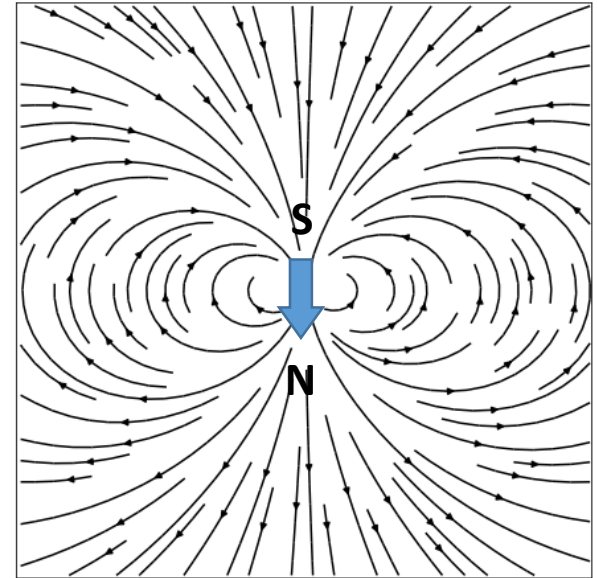
$$\vec{M} = \kappa \vec{H}$$



# Recap

- Magnetization produces a magnetic field

- Field lines got from North to South pole



- Magnetic fields and fluxes are related by the magnetic permeability

$$\vec{B} = \mu \vec{H} = \mu_0(1 + \kappa) \vec{H} = \mu_0(\vec{H} + \vec{M})$$

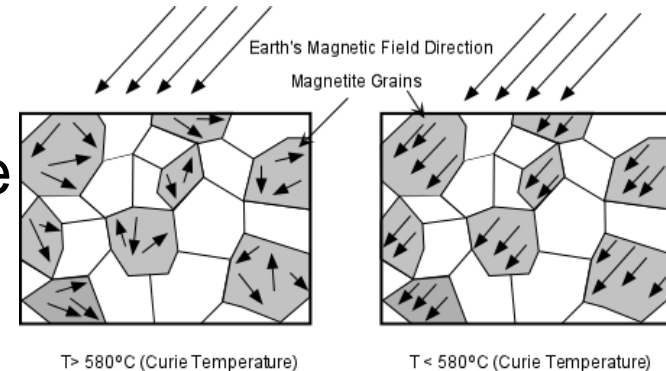
↑ inducing    ↑ induced



# Remanent Magnetization

# Remanent magnetization

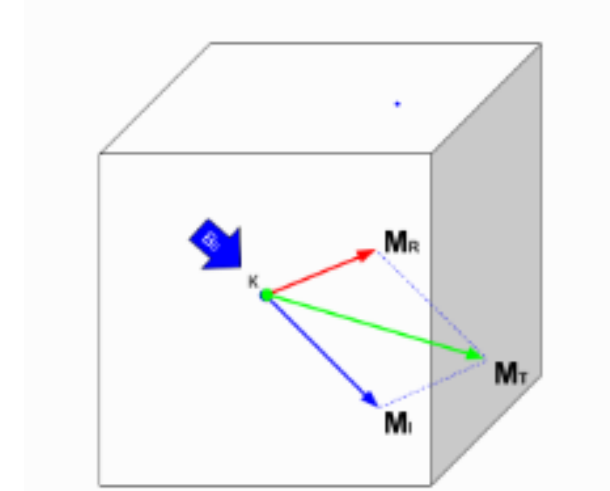
- A permanent magnetization contribution which is **not** supported by an external field
- Magma cools below Curie temperature  
→ Magnetic dipoles align along Earth's field and leave permanent imprint

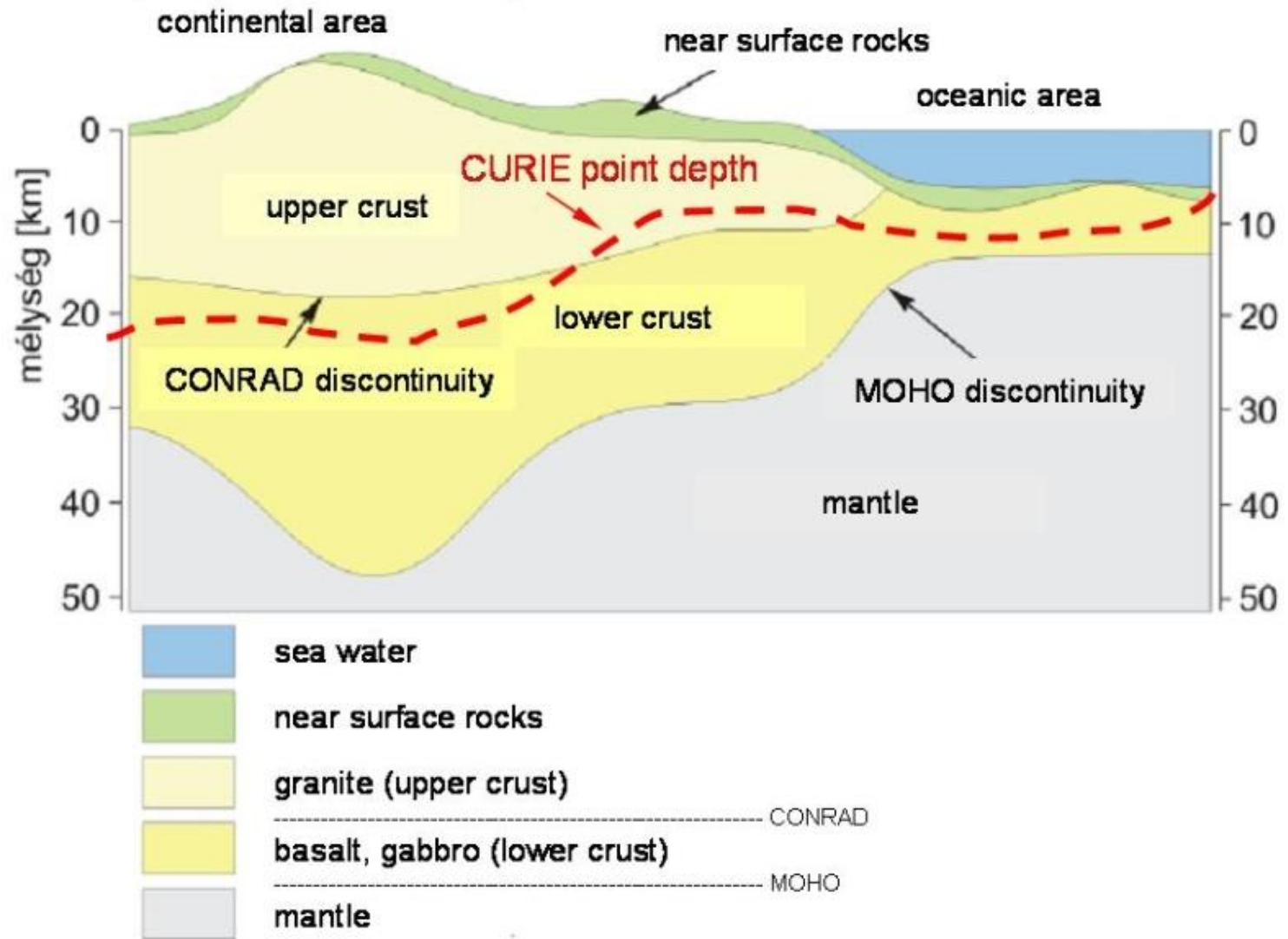


- Total magnetization is vector sum:

$$\vec{M}_T = \vec{M}_I + \vec{M}_R$$

- Only significant in ferromagnetic materials!!! (magnetite, steel etc...)





Geotherms ensure magnetization is restricted mostly to the upper crust. The mantle and core are too hot.

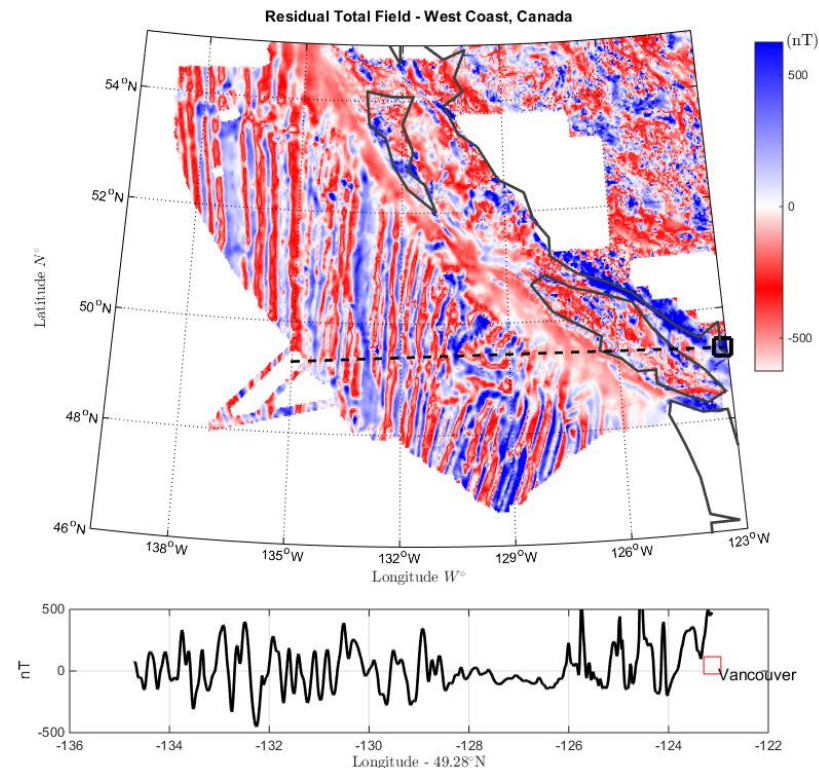
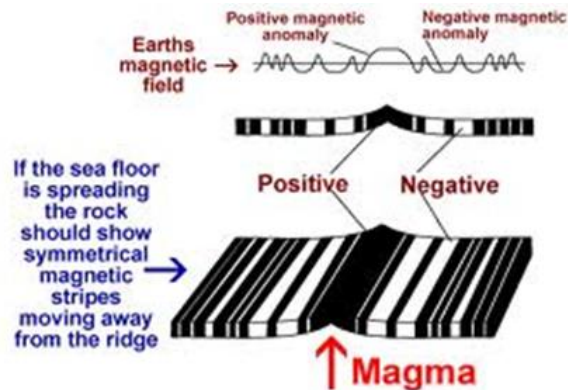
# Remanent Magnetism at different scales

- Small scale: UXO, rebar, drums



- Large scale: geologic units.

Sea floor spreading



# All Together Now!!!

$\vec{B}$ : Magnetic Flux Density ( $Wb/m^2 = \text{Tesla}$ )

$\vec{H}$ : Magnetic Field ( $A/m$ )

$\kappa$ : Magnetic susceptibility (*Unitless*)

$\mu$ : Magnetic permeability  $\mu = \mu_0(1 + \kappa)$

Inducing field      Induced magnetization      Remanent magnetization

$$\begin{aligned}\vec{B} &= \mu_0(\vec{H} + \vec{M}) \\ &= \mu_0(\vec{H} + \vec{M}_I + \vec{M}_R) \\ &= \mu_0(1 + \kappa)\vec{H} + \mu_0\vec{M}_R \\ &= \mu\vec{H} + \mu_0\vec{M}_R\end{aligned}$$

Inside susceptible material

Inducing field      Anomalous field (due to magnetization)

$$\begin{aligned}\vec{B} &= \mu_0(\vec{H} + \vec{H}_A) \\ &= \vec{B}_0 + \vec{B}_A\end{aligned}$$

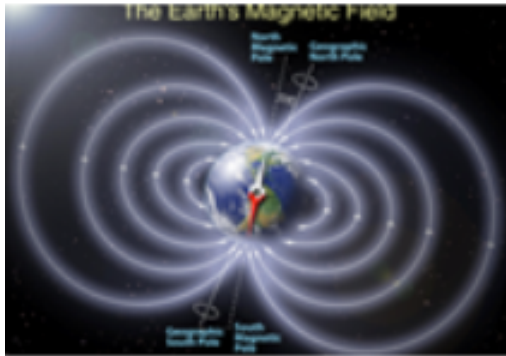
Outside susceptible material

# Magnetic methods (basic idea)

# Magnetic methods (basic idea)

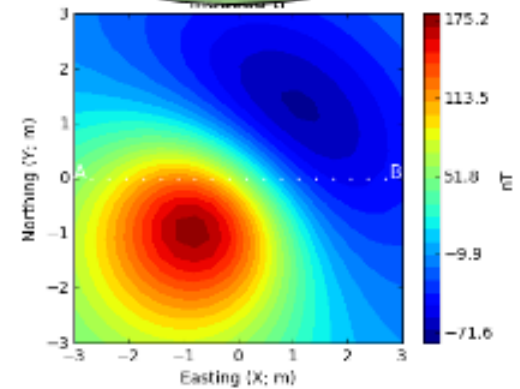
Source

Data



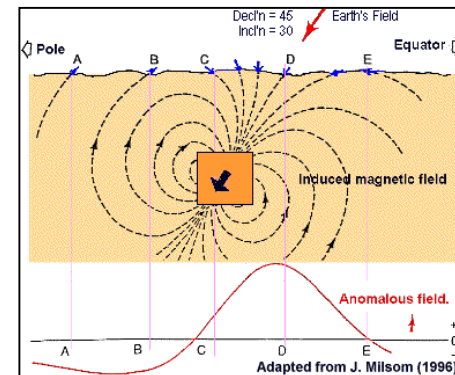
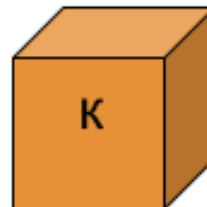
Input energy

Measured response

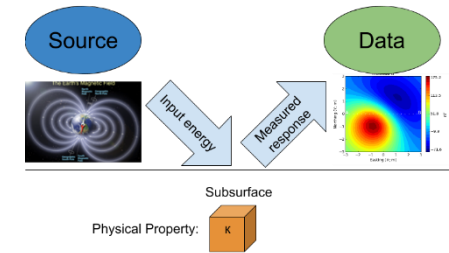


Physical Property:  
Magnetic susceptibility

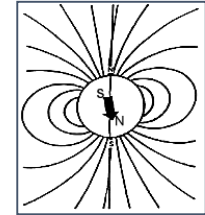
Subsurface



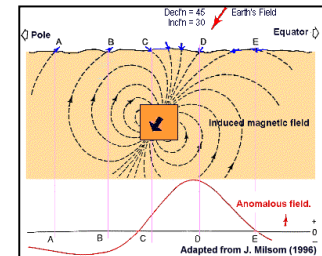
# Magnetic surveying



- Earth's magnetic field,  $B_0$ , is the source:

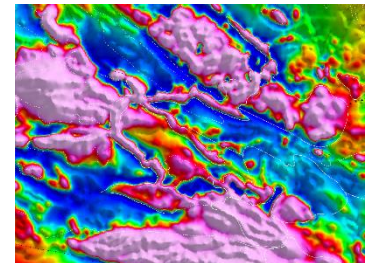


- Induces magnetization (may also have remanence):  
→ Creates anomalous field  $B_A$



- Measure total magnetic field

$$B = B_0 + B_A$$

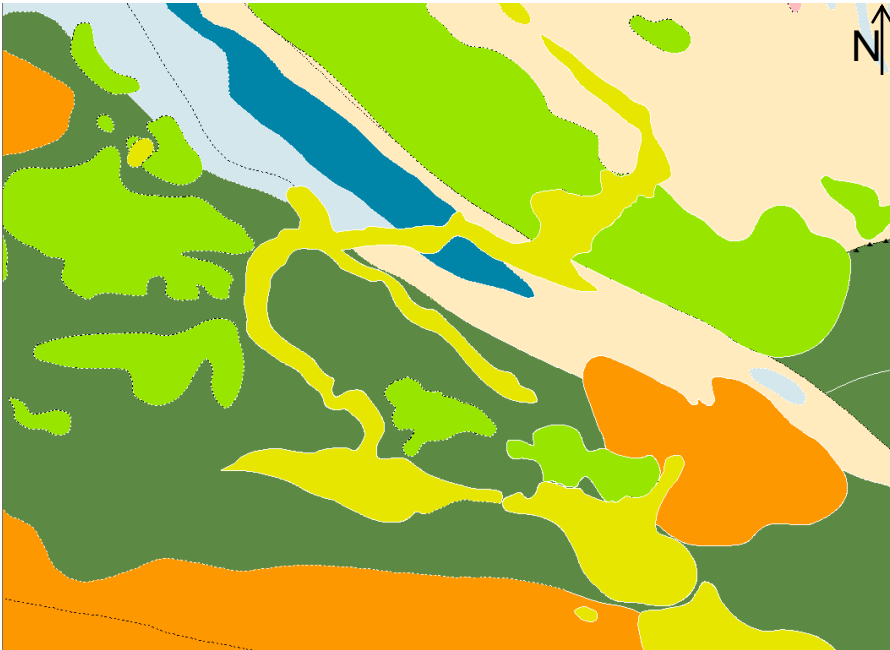




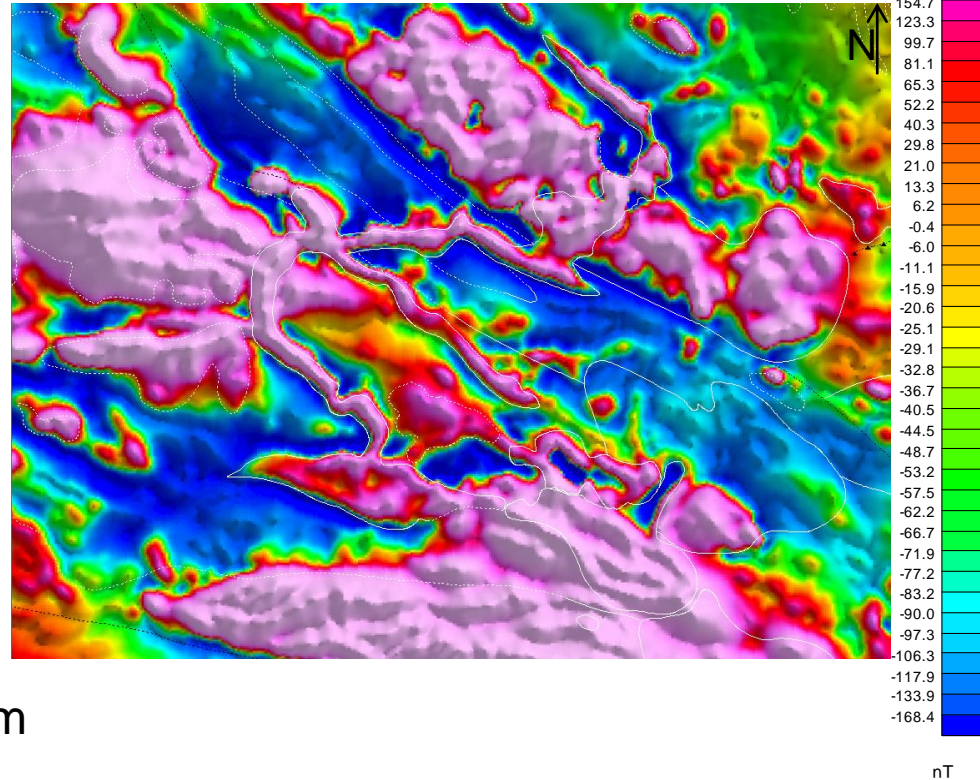
# Example Applications

# Geologic mapping

Geology map



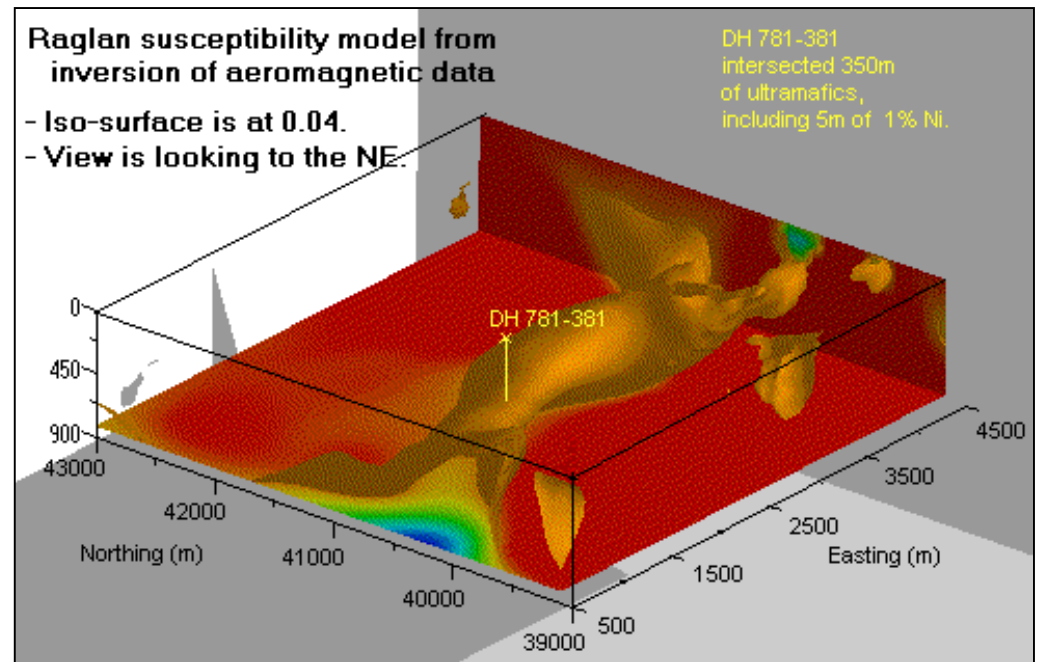
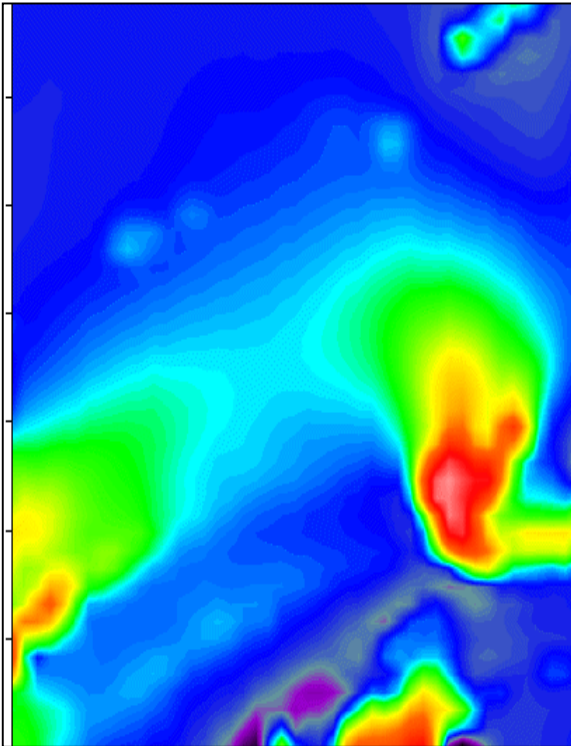
Magnetic map



30 km

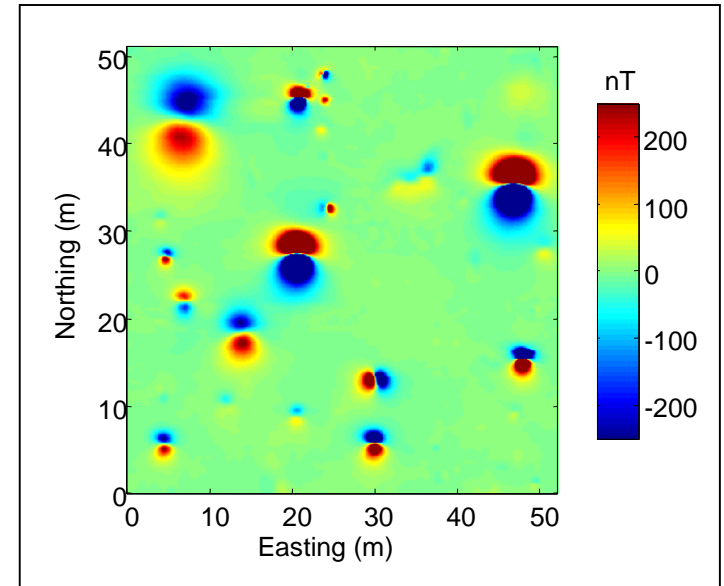
Geology contacts can be inferred from mag maps.

# Mineral exploration



Ore-bearing minerals may be significantly more susceptible than host

# Environmental Contaminants: UXO



UXOs are very susceptible compared to host

# Unit Activities

- **Labs: (Magnetics I)**
  - Monday, September 16<sup>th</sup>
  - Tuesday, September 17<sup>th</sup>
- **Labs: (Magnetics II)**
  - Monday, September 23<sup>rd</sup>
  - Tuesday, September 24<sup>th</sup>
- **TBL:**
  - Monday, September 23<sup>rd</sup>
- **Quiz:**
  - Monday, September 23<sup>rd</sup>