

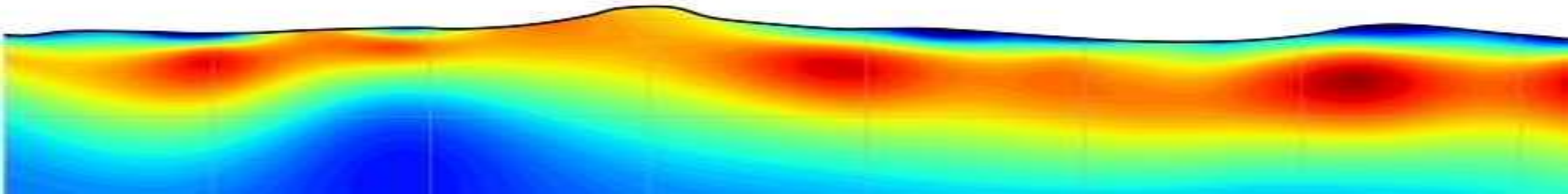
# ESS302 Applied Geophysics II

Gravity, Magnetic, Electrical, Electromagnetic and Well Logging

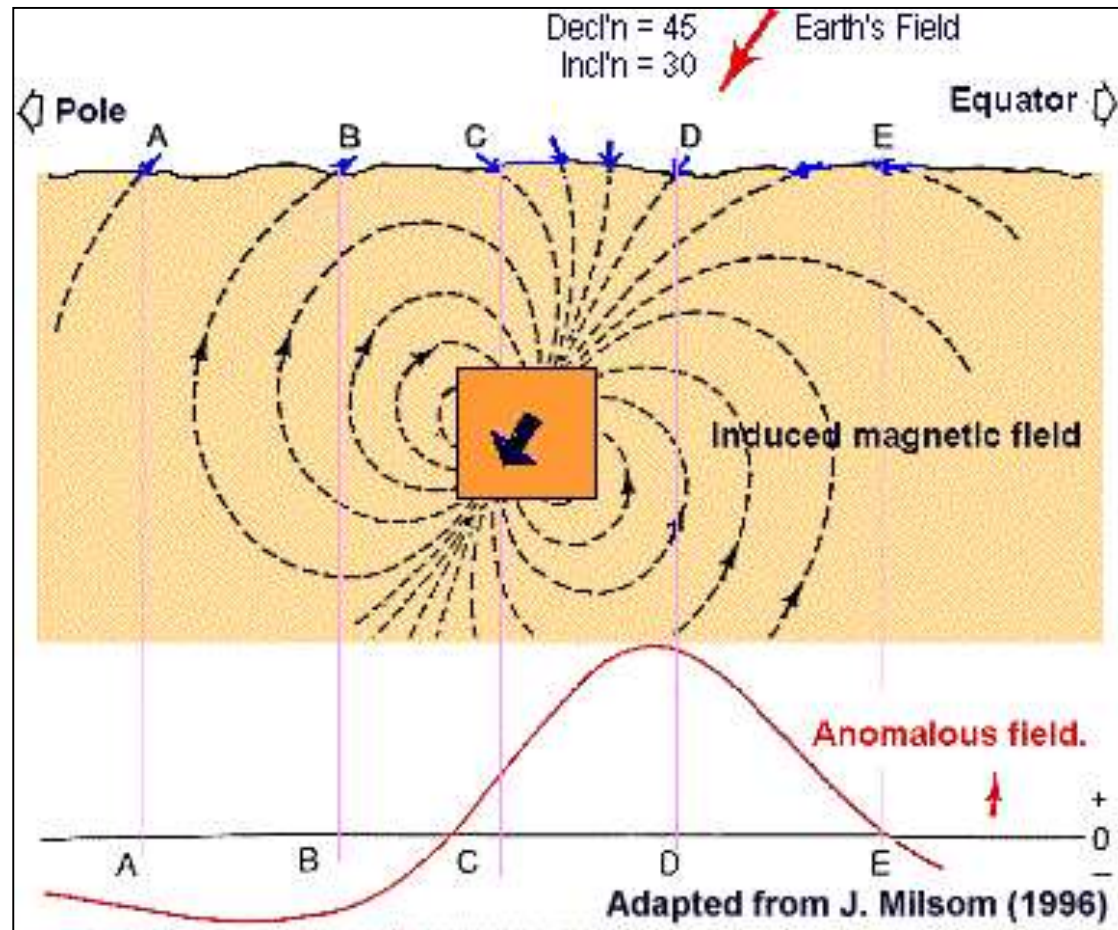
## Magnetic 3: Applications

Instructor: Dikun Yang

Feb – May, 2019



# Quiz



Draw a diagram similar to the figure on the left but with different inclinations

Option 1:  $\text{inc} = 80^\circ$

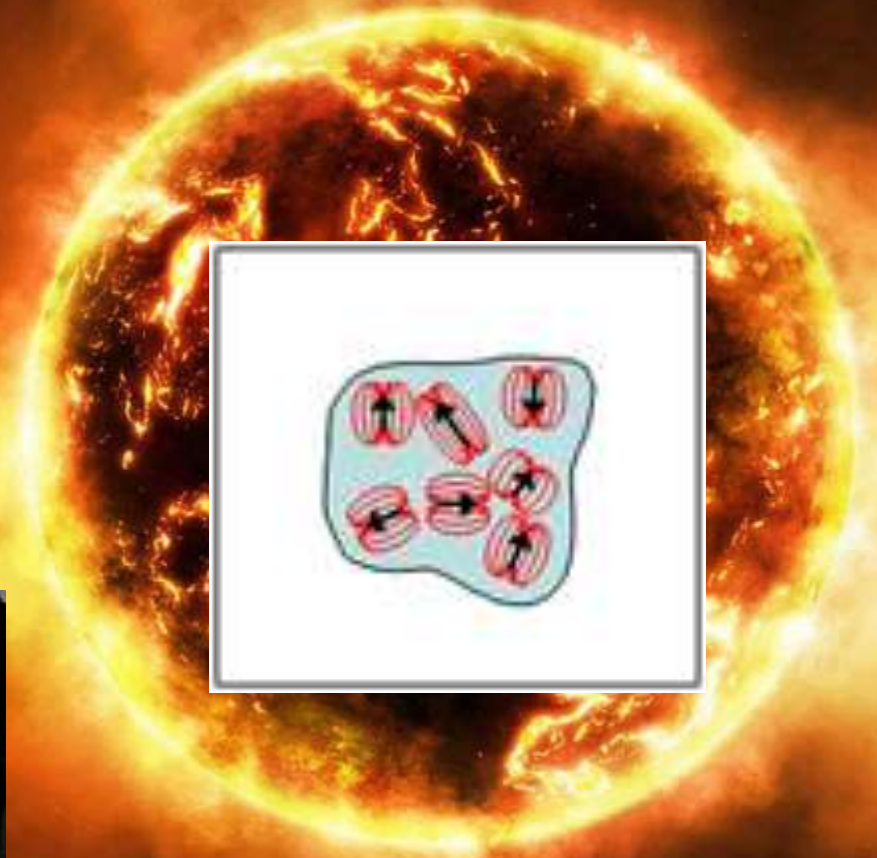
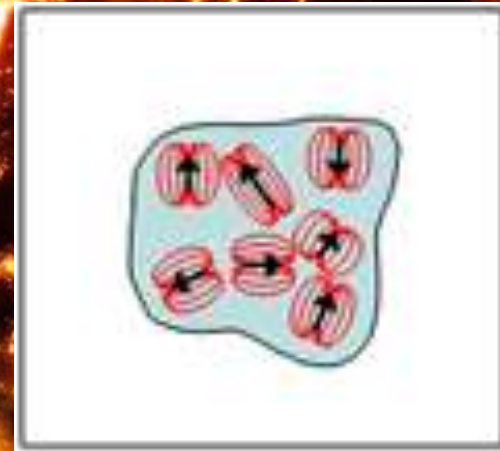
Option 2:  $\text{inc} = 0^\circ$

Option 3:  $\text{inc} = -70^\circ$

Option 4:  $\text{inc} = -90^\circ$

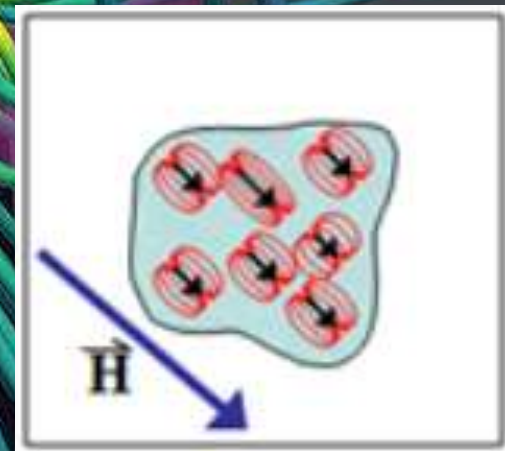
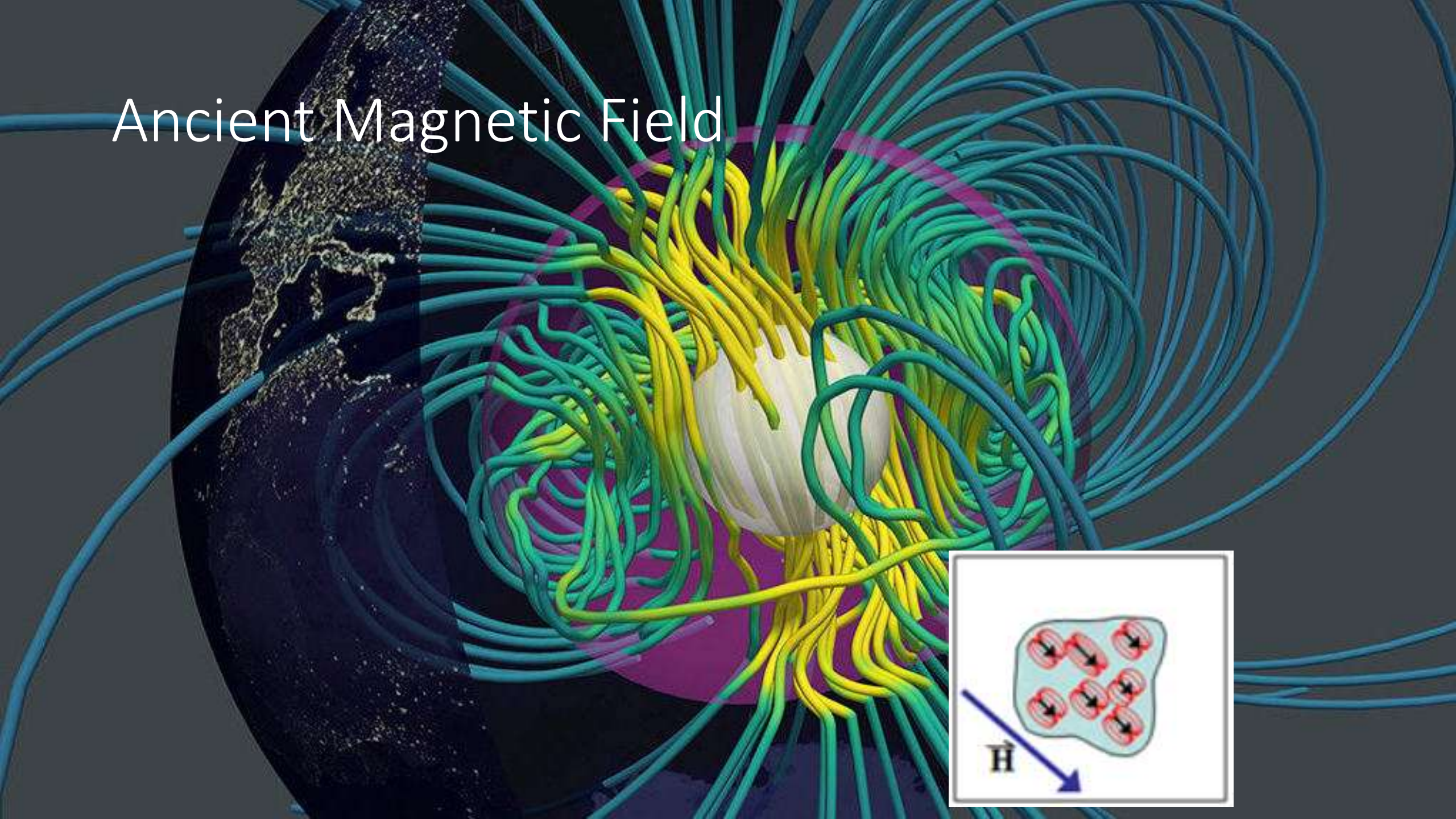


# Heat and Disorientation



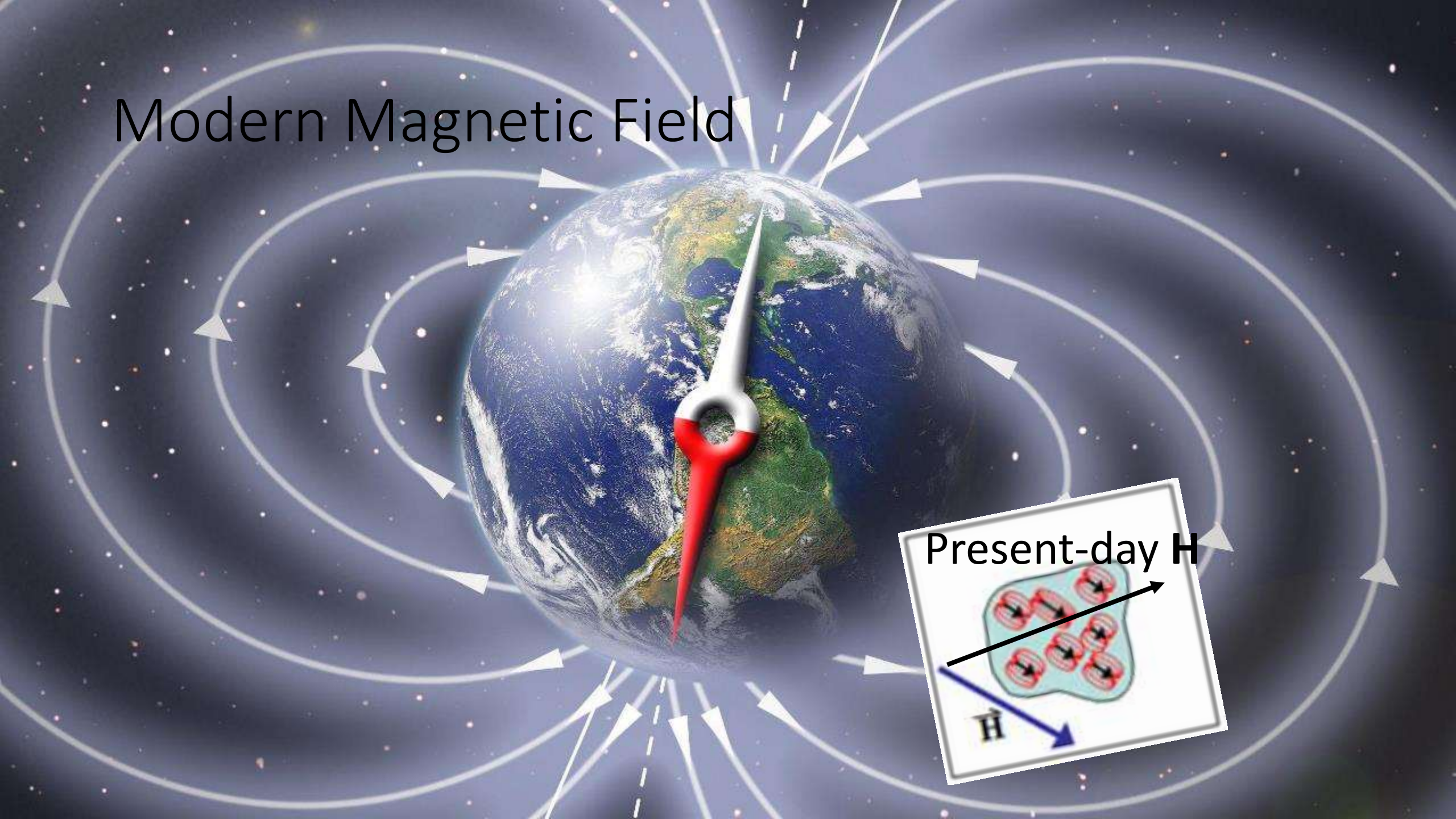


# Ancient Magnetic Field

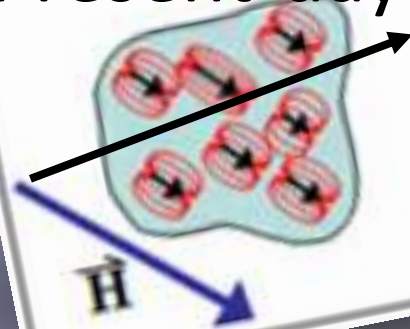




# Modern Magnetic Field

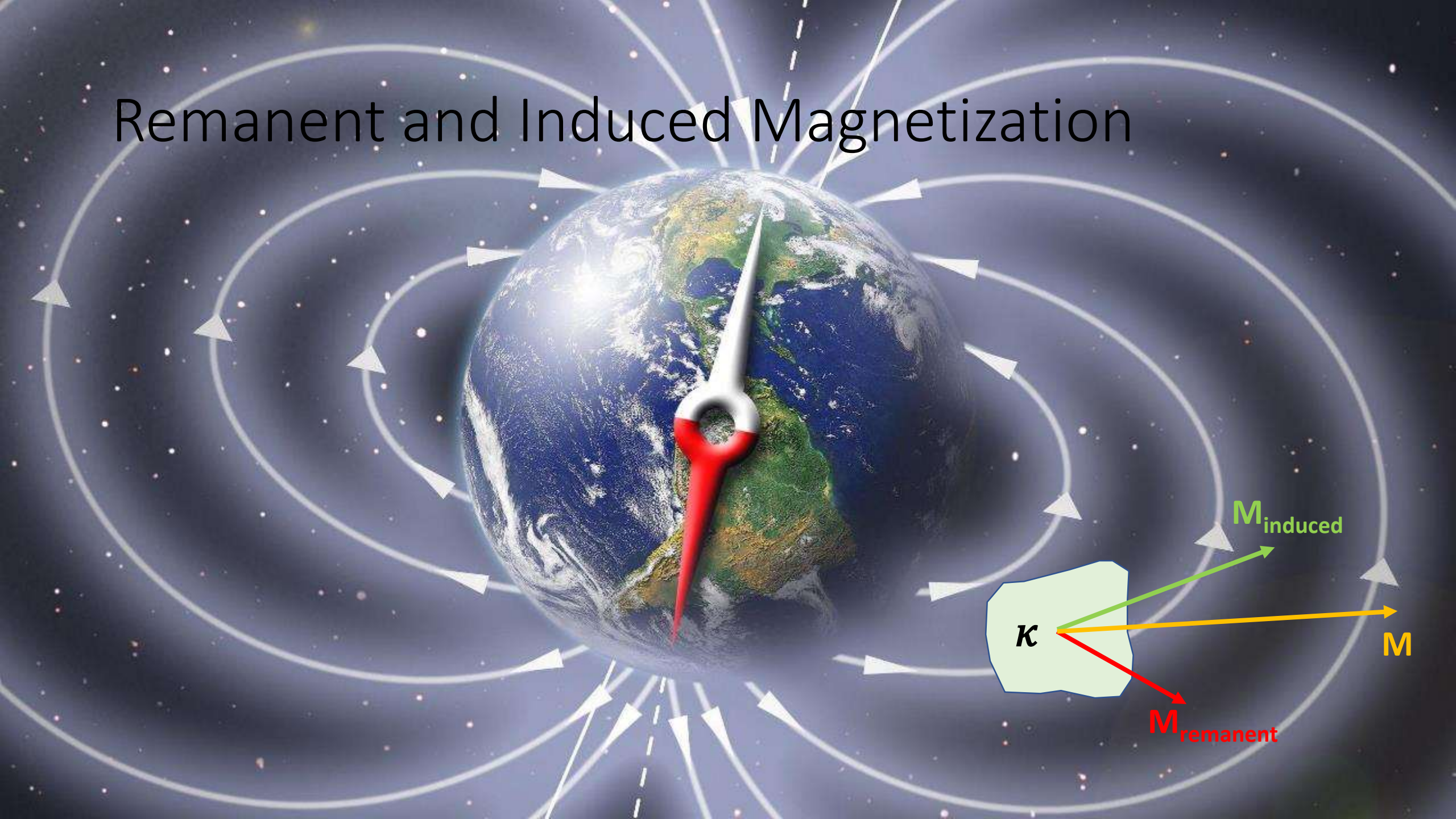


Present-day  $H$

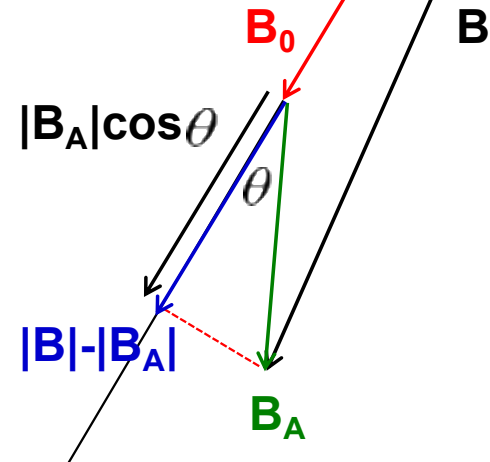
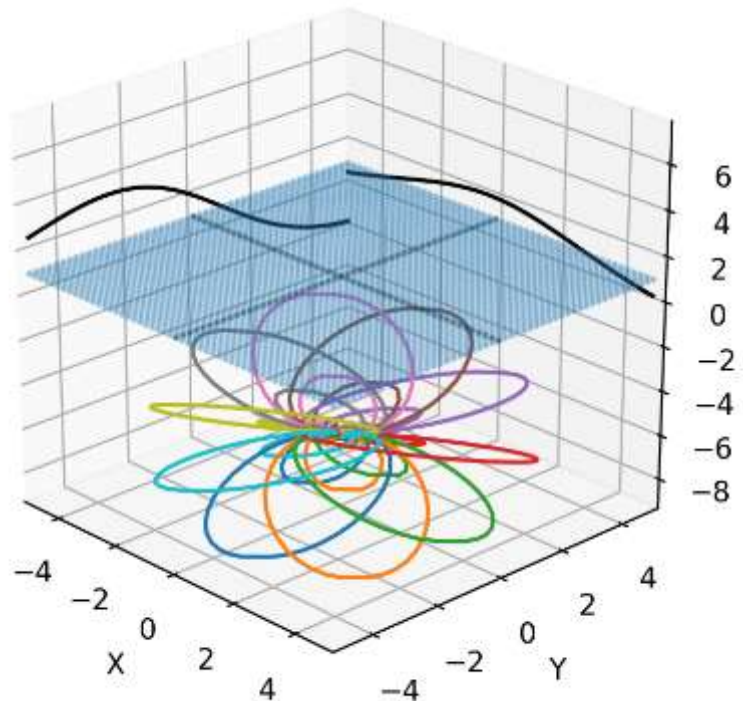
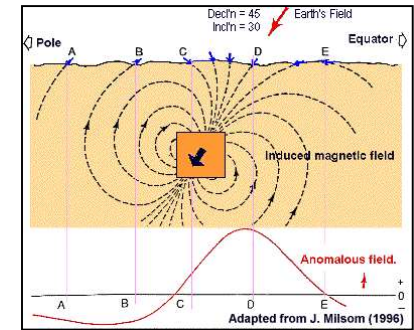
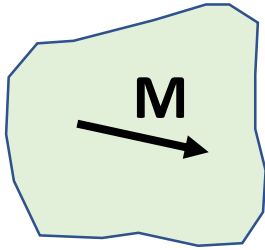




# Remanent and Induced Magnetization



# Magnetic Anomaly – Magnetized Objects

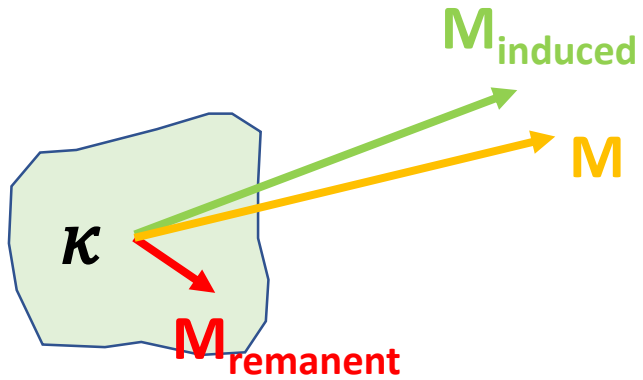


Total-field anomaly

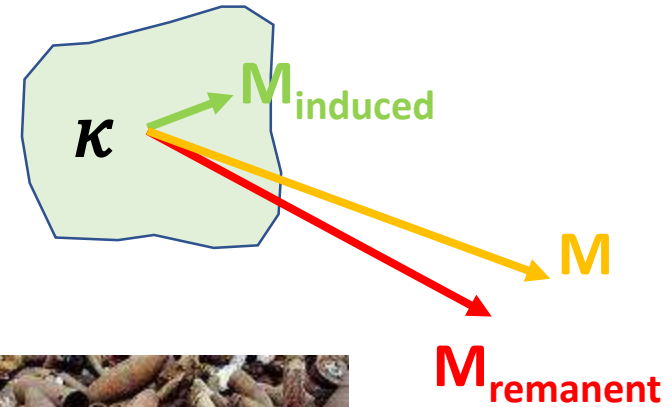
$$\begin{aligned}
 |\Delta \vec{B}| &= |\vec{B}_0 + \vec{B}_A| - |\vec{B}_0| \\
 &\simeq \vec{B}_A \cdot \hat{B}_0 \\
 &= |\vec{B}_A| \cos \theta
 \end{aligned}$$



# Sources of Magnetization



Susceptibility (magnetite)



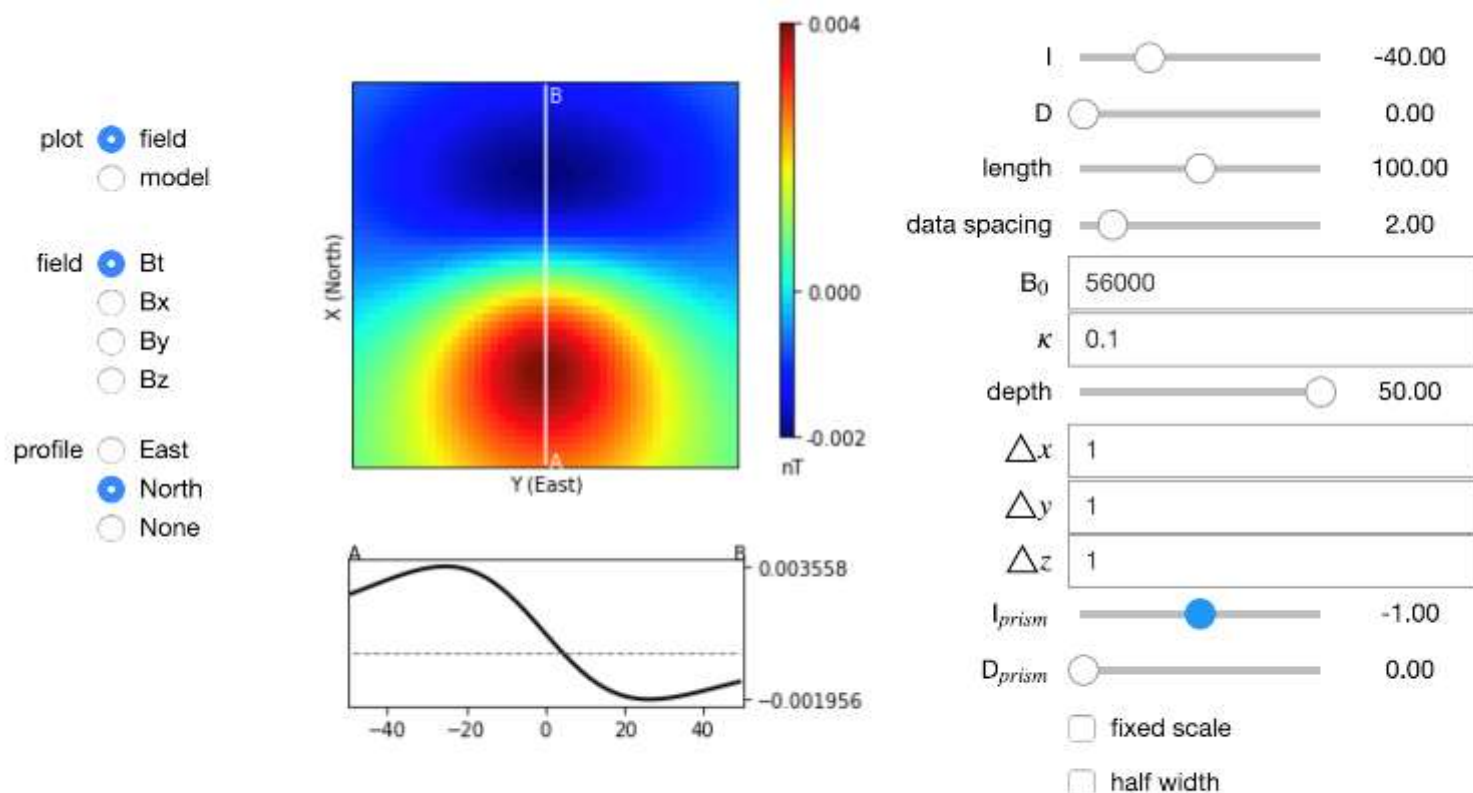
UXO





- $\Delta z$ : length in depth ( $z$  direction) (m) below the receiver
- depth: top boundary of the prism (meter)
- $I_{prism}$ : inclination of the prism (reference is north direction)
- $D_{prism}$ : declination of the prism (reference is north direction)

```
In [2]: mag = MagneticDipoleApp()
mag.interact_plot_model_prism()
```

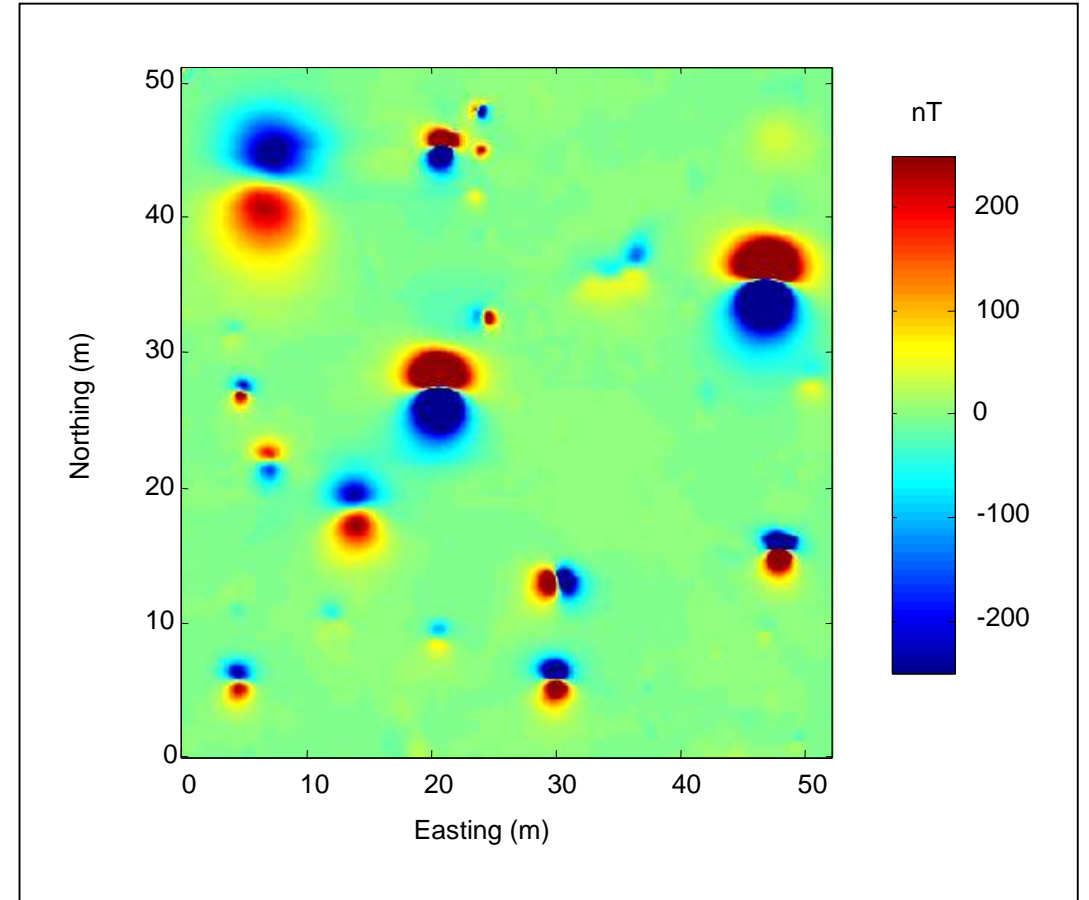


# UXO (Unexploded Ordnance)





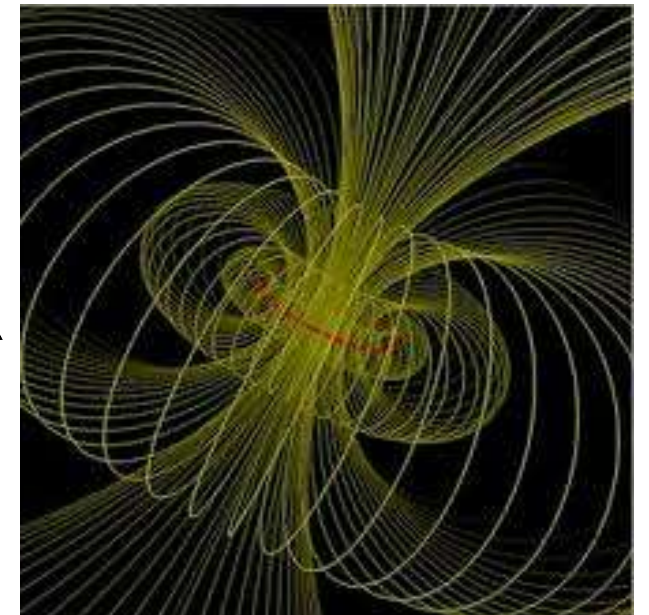
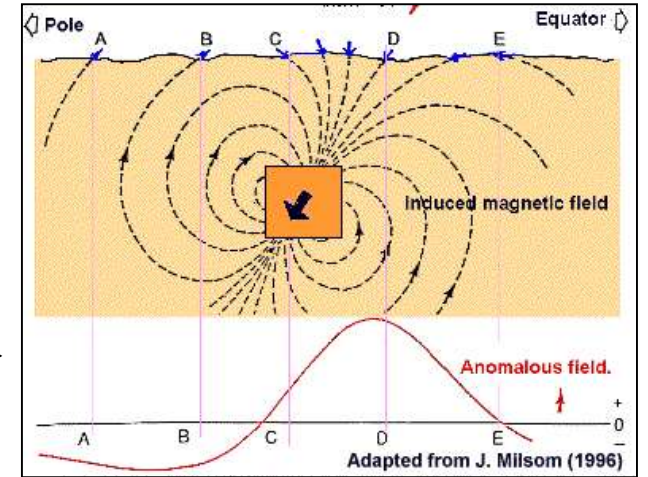
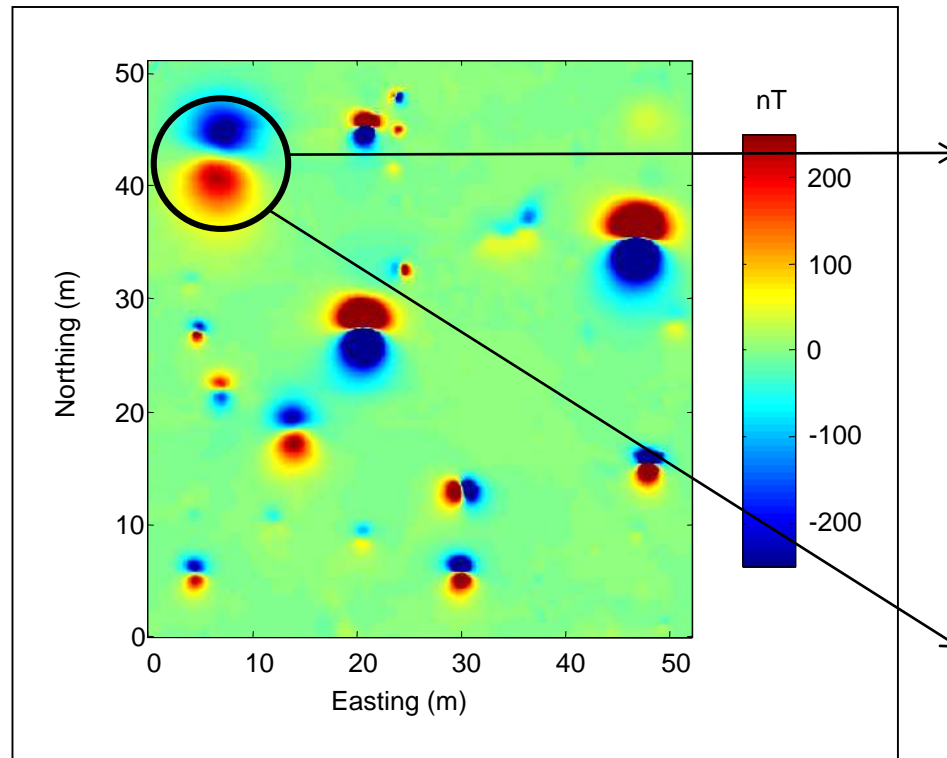
# Magnetic Survey



# Induced or Remanent?

A UXO anomaly map:

- Dipole field on the surface
- Induced or remanent?
- How can we tell it's a UXO?

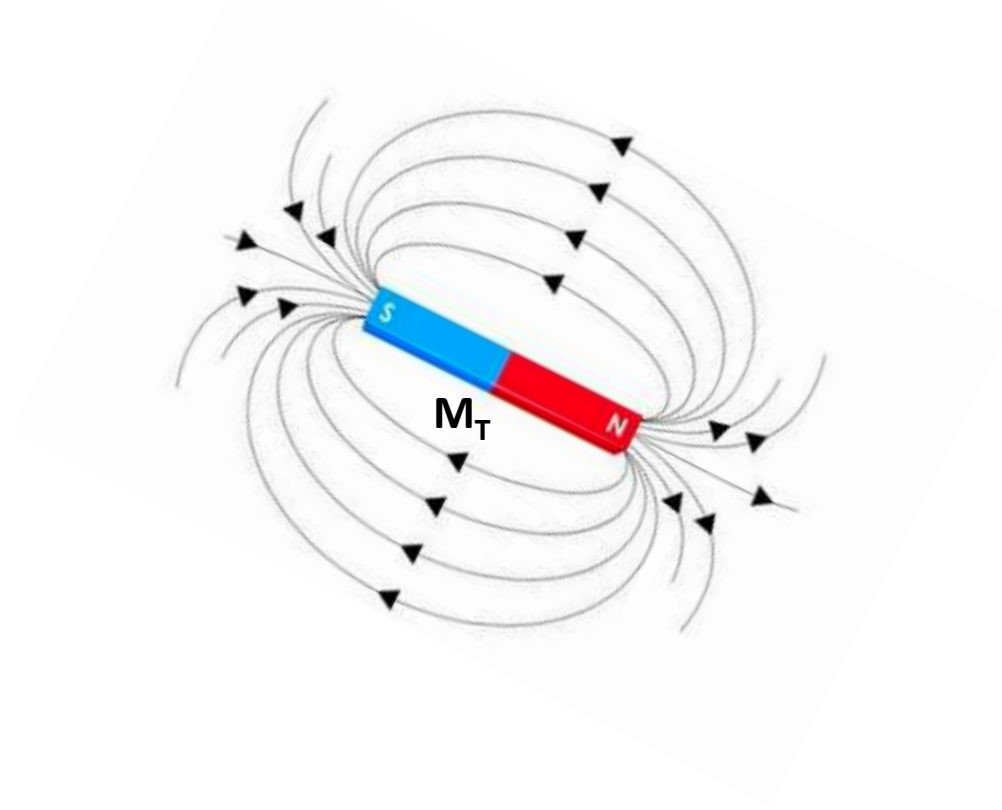
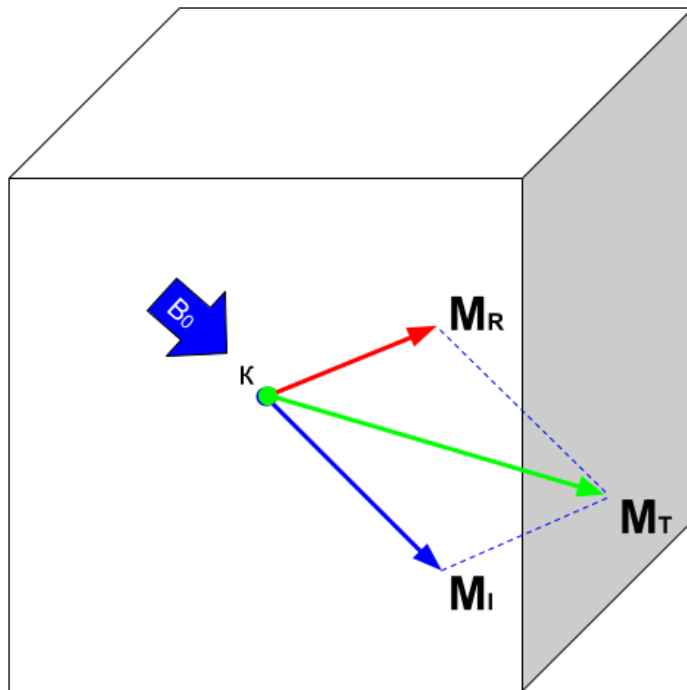




# Parameterization

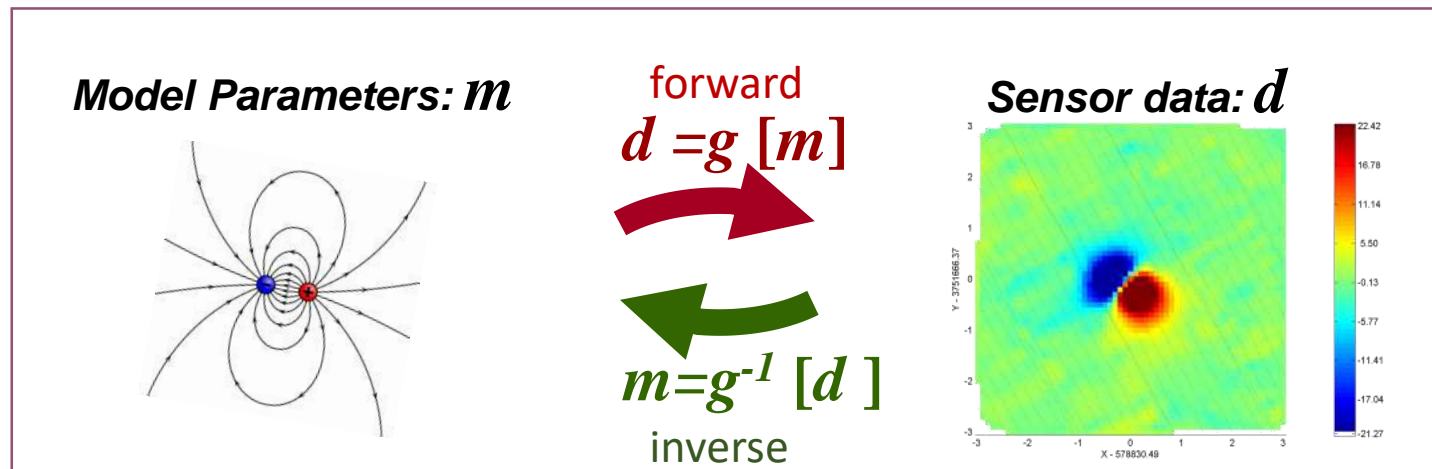
Following parameters uniquely define a dipole:

- Position (X, Y, Z)
- Total dipole moment vector ( $M_T$ ) from induced and remanent ( $M_x, M_y, M_z$ )

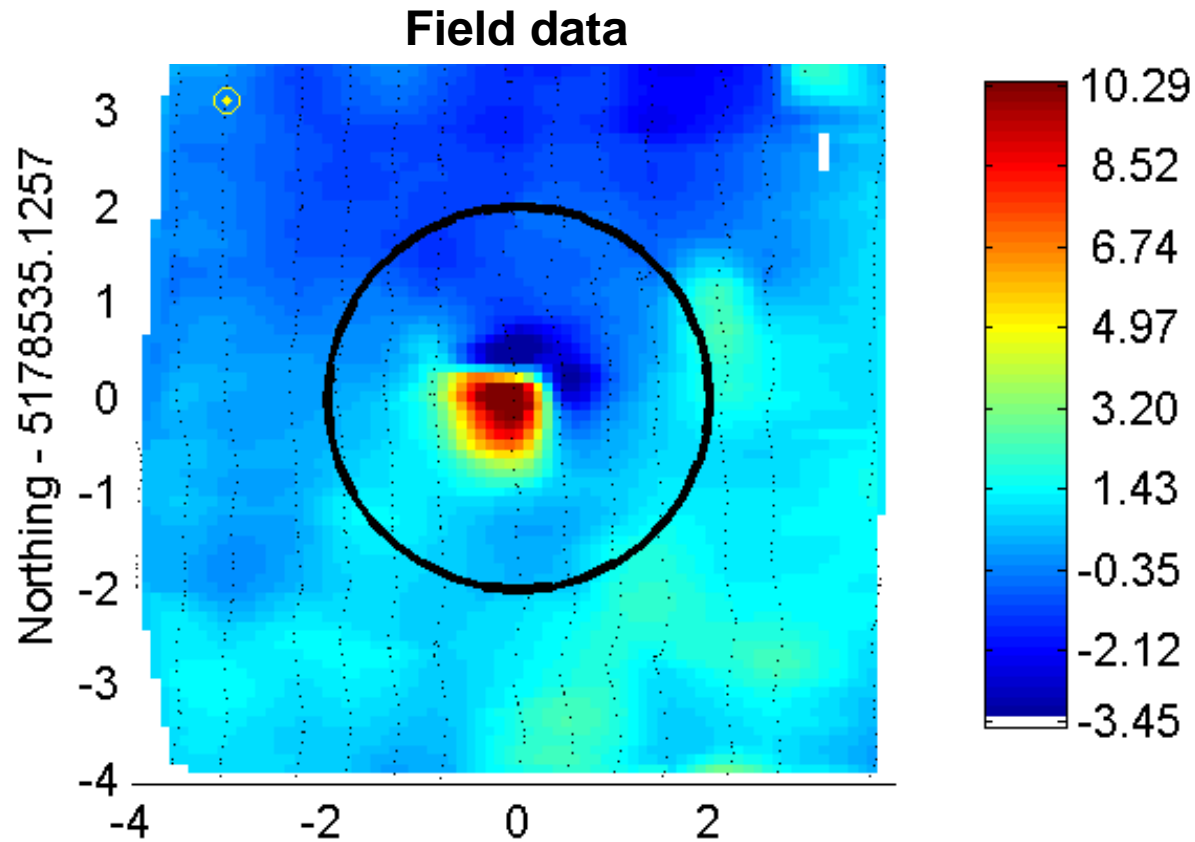


# Dipole Model Inversion

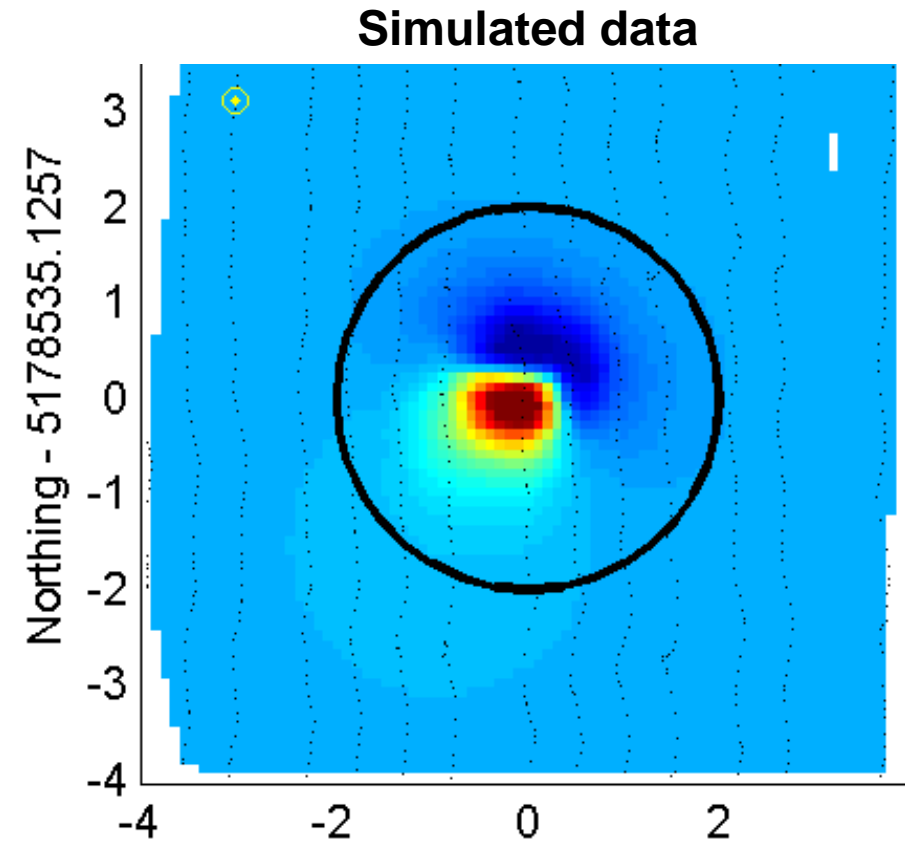
- Six parameters  $m = [X, Y, Z, M_x, M_y, M_z]$
- Data inversion: search the parameter space to find a particular combination of  $[X, Y, Z, M_x, M_y, M_z]$  that reproduces the dipole pattern on the map
- Automatic search or manual data fitting





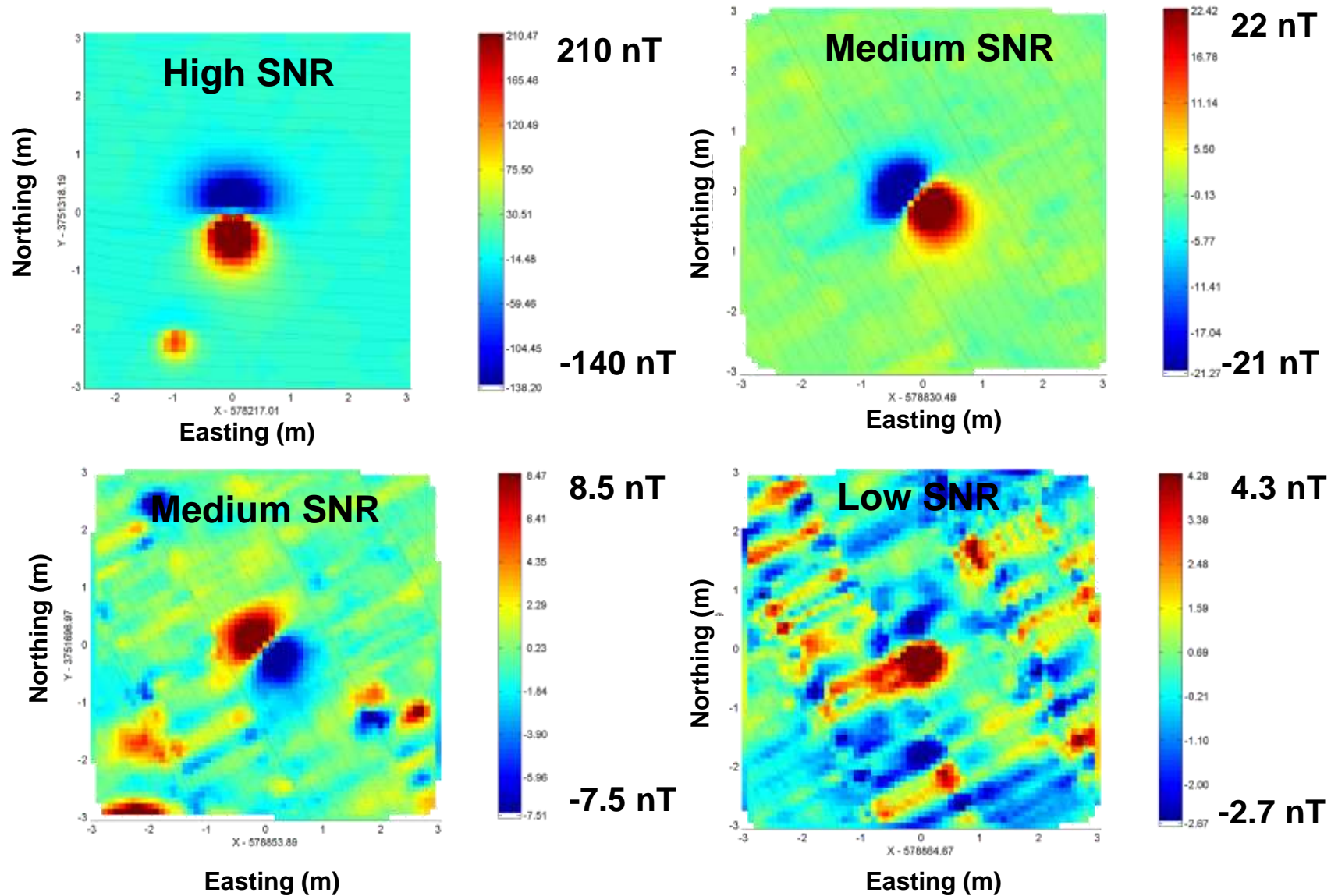


Easting = -0.13 m; Northing = 0.16 m  
Depth = 0.26 m; Moment = 0.0226 Am<sup>2</sup>  
Azimuth = 37°; Dip = 28.8°  
Fit quality = 0.95



Use the recovered dipole  
parameters to identify UXO

# Practical Issues





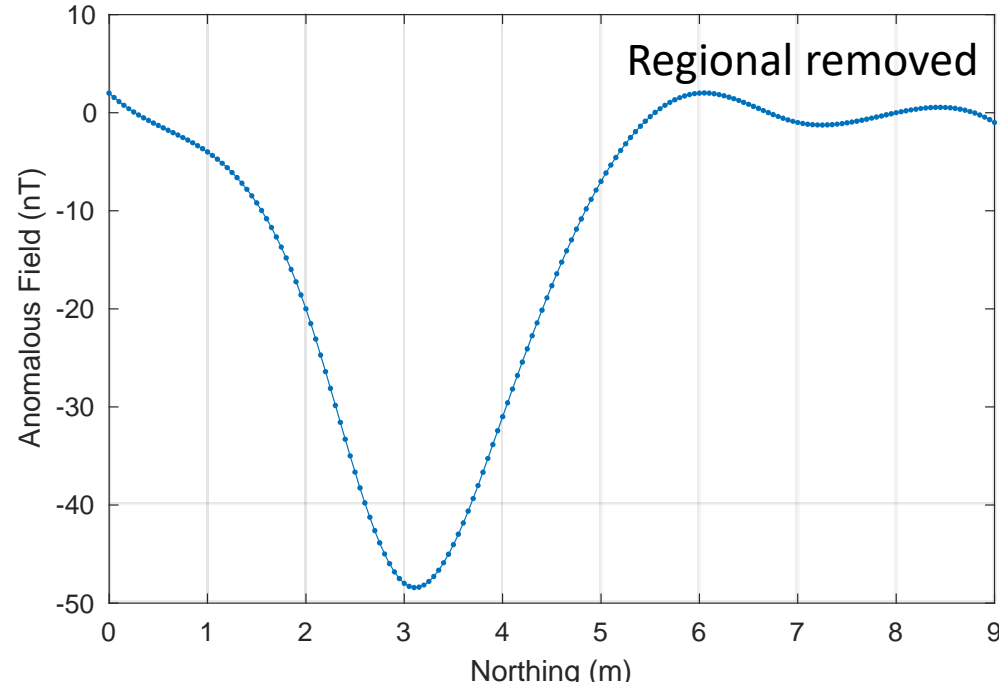
# The Lost Re-bar

A long re-bar was buried somewhere on a beach in Canada. It was hazardous so students need to locate it.

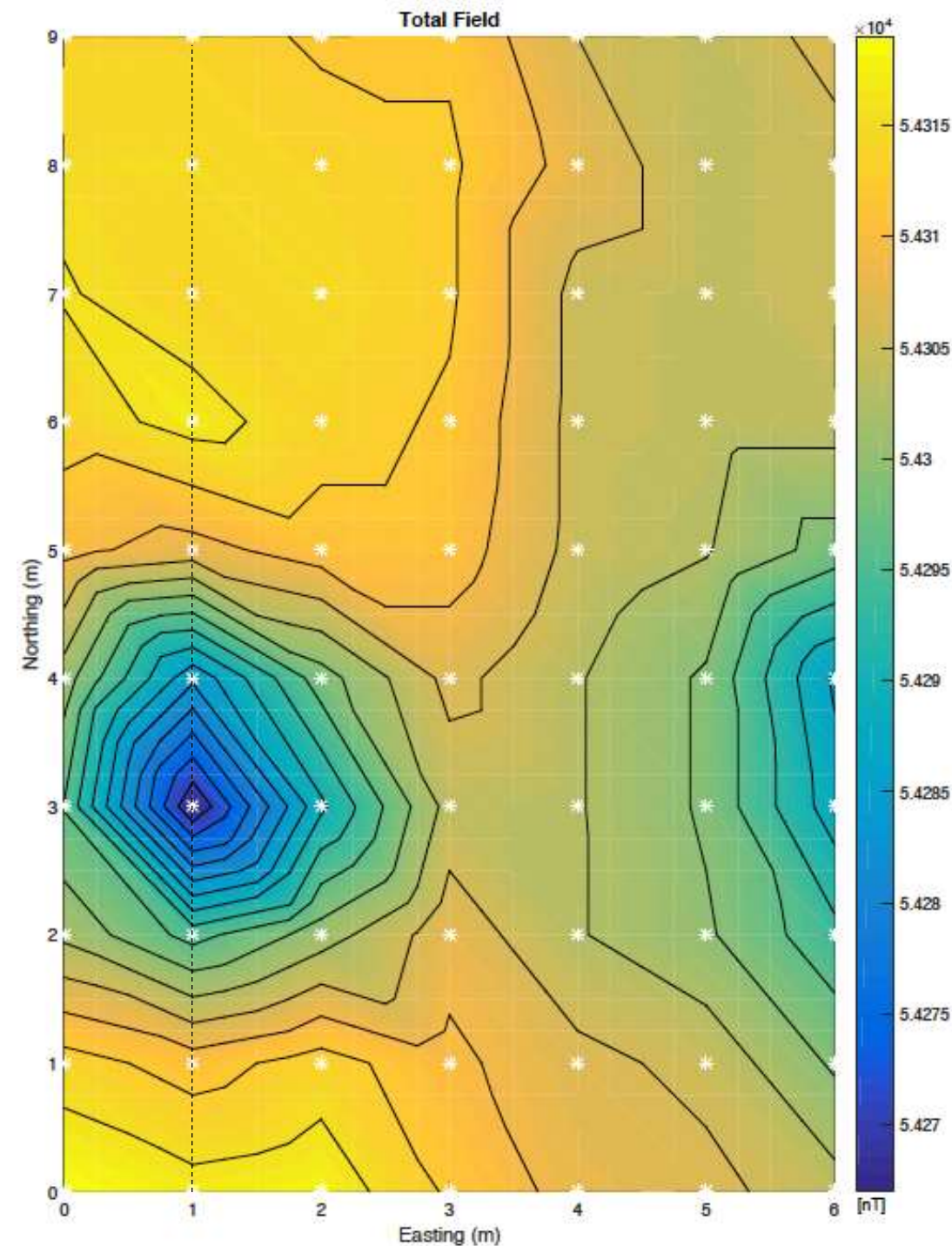


Digging in sand is exhausting...

# Magnetic Anomaly

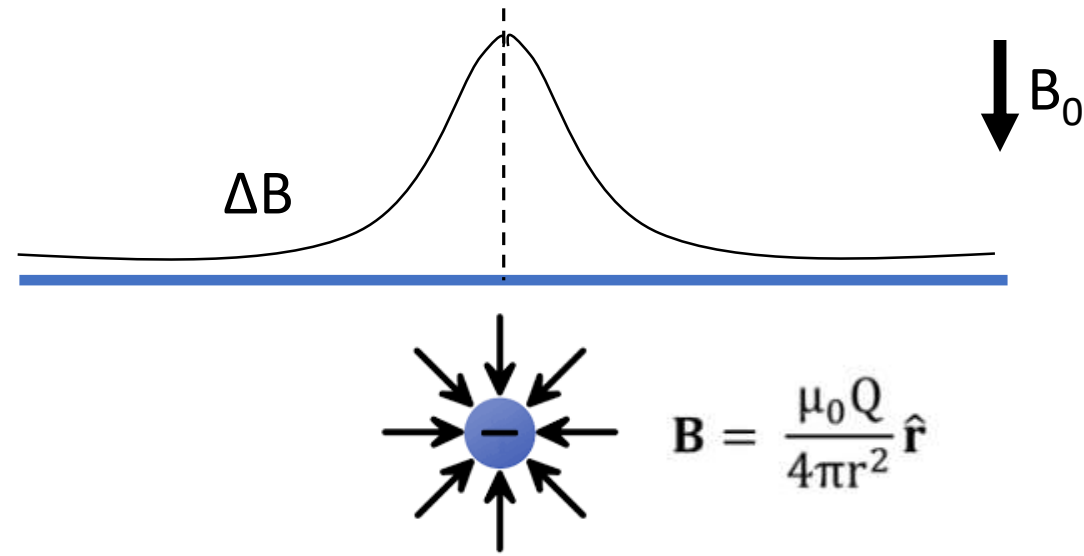
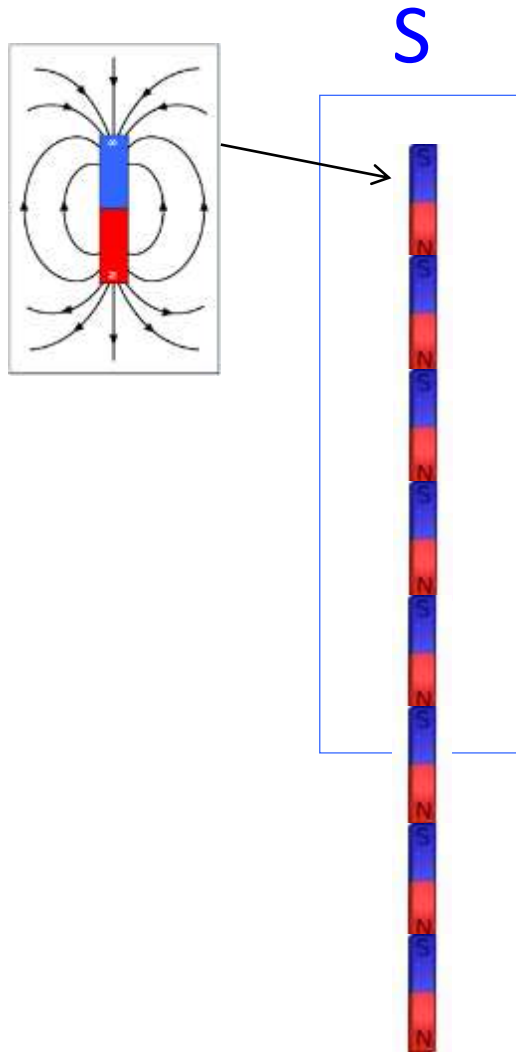


- **Digging:** 4+ hours, 60 (sweating) people, failed!
- **Magnetic:** 1 hour, 2 people, recovered the lost re-bar!
- Why single peak without sign changes?



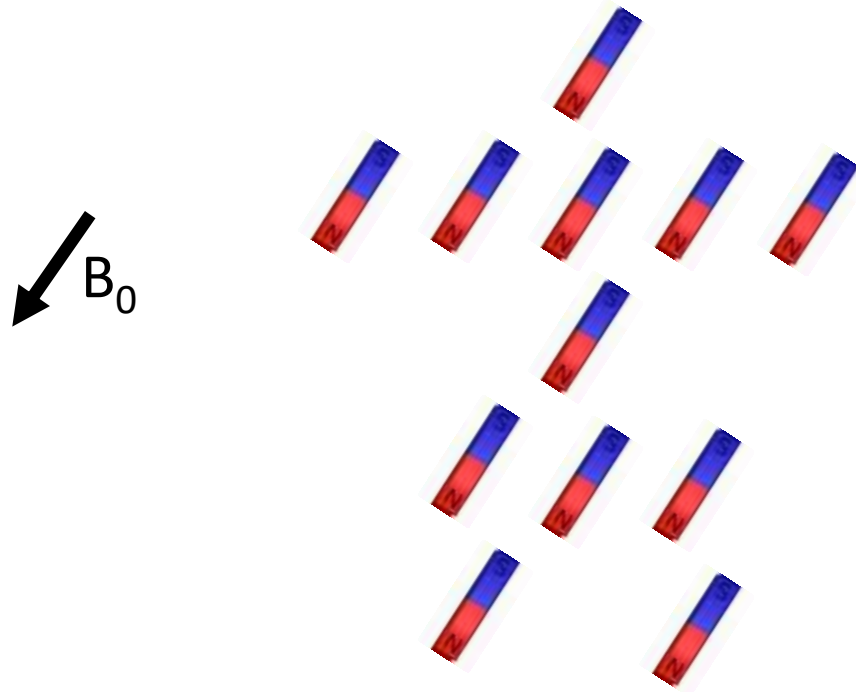


# Build a Long Rod using Dipoles



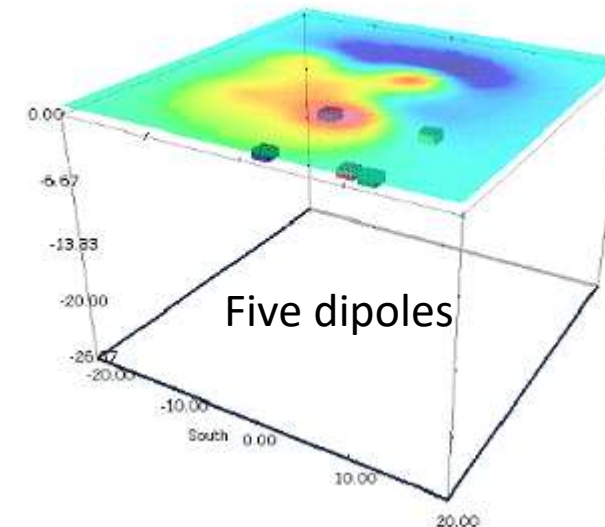
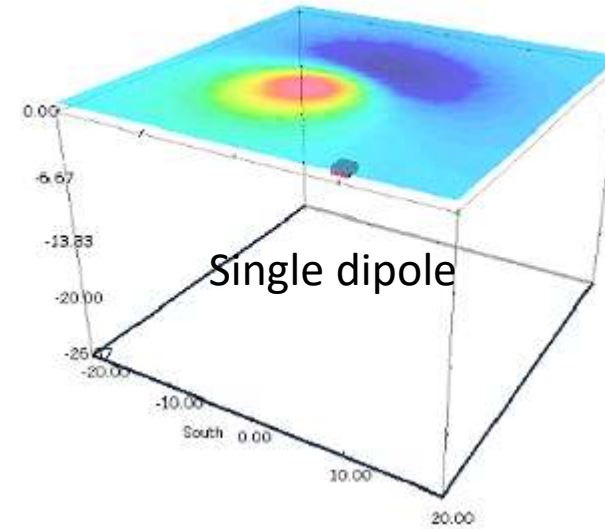
- N and S inside the rod cancel out
- Net negative and positive charge at two ends
- Only “see” one charge if the rod is vertical and long
- A **monopole** anomaly (field lines determined by a single magnetic charge)
- What if the remanence makes the magnetization not uniform inside the pipe?

# Build a Complex Body



Superposition: Sum up contribution from each dipole

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} \left( \frac{3\mathbf{r}(\mathbf{m} \cdot \mathbf{r})}{r^5} - \frac{\mathbf{m}}{r^3} \right)$$





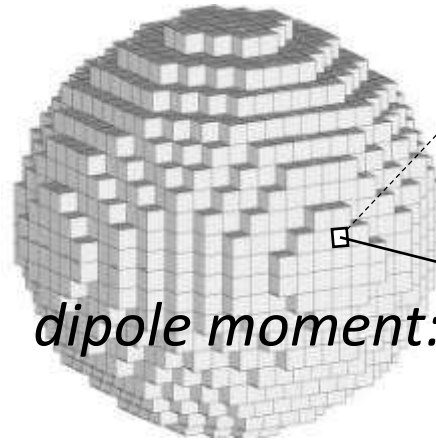
# Arbitrarily Shaped Objects

Superposition  $\sum_i B_i$

P

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} \left( \frac{3\mathbf{r}(\mathbf{m} \cdot \mathbf{r})}{r^5} - \frac{\mathbf{m}}{r^3} \right)$$

$r_i$



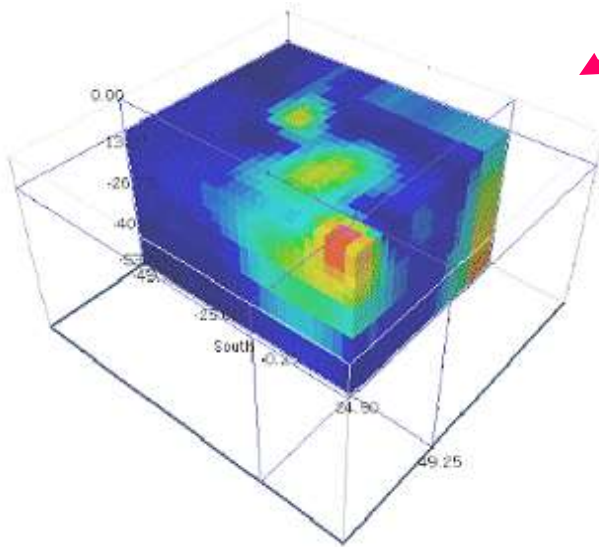
*dipole moment:  $m_i = \Delta V_i M_i$*

(Recall gravity)

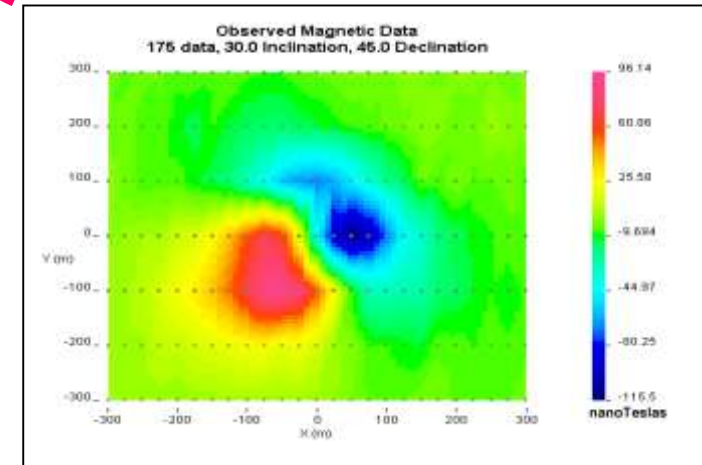
Can you think of any potential problem with this integration approach?

# Arbitrary Magnetic Dipole Applet

A complicated earth model of  $\kappa$   
(Induced magnetization)



**Inversion**

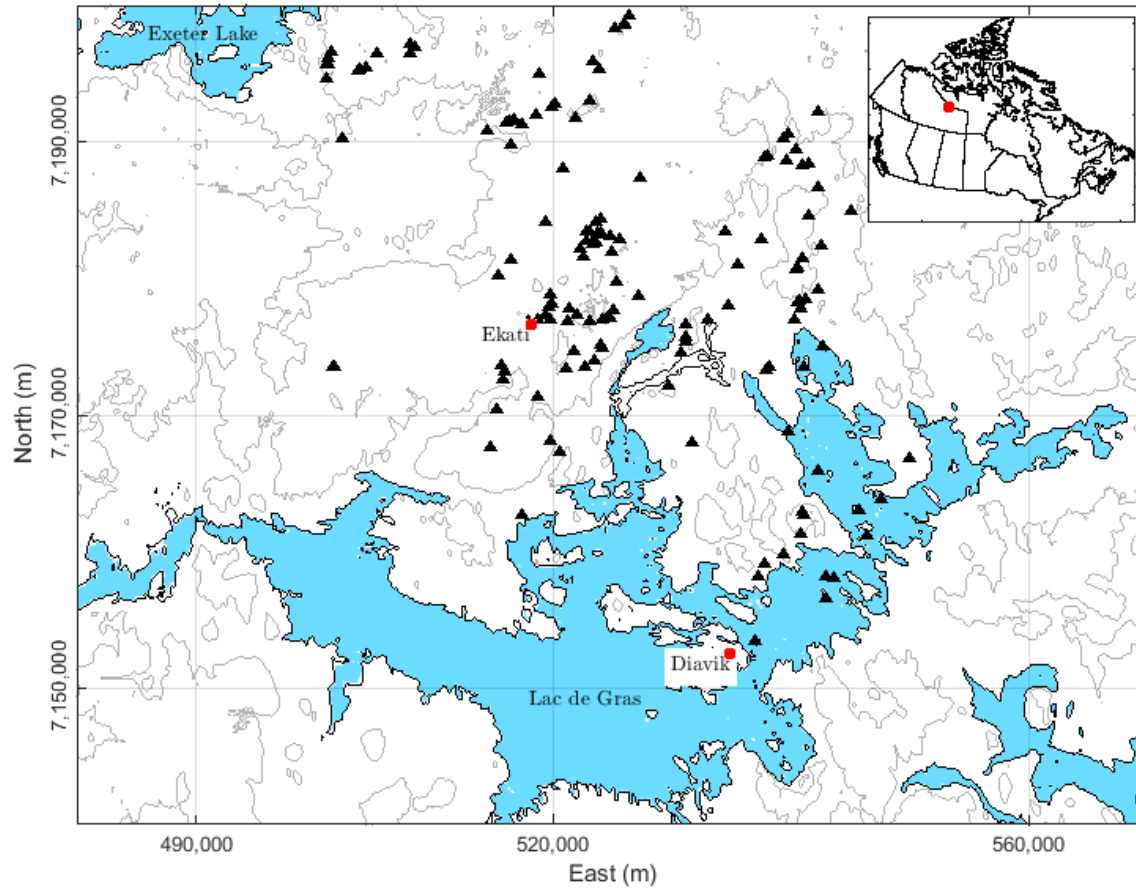


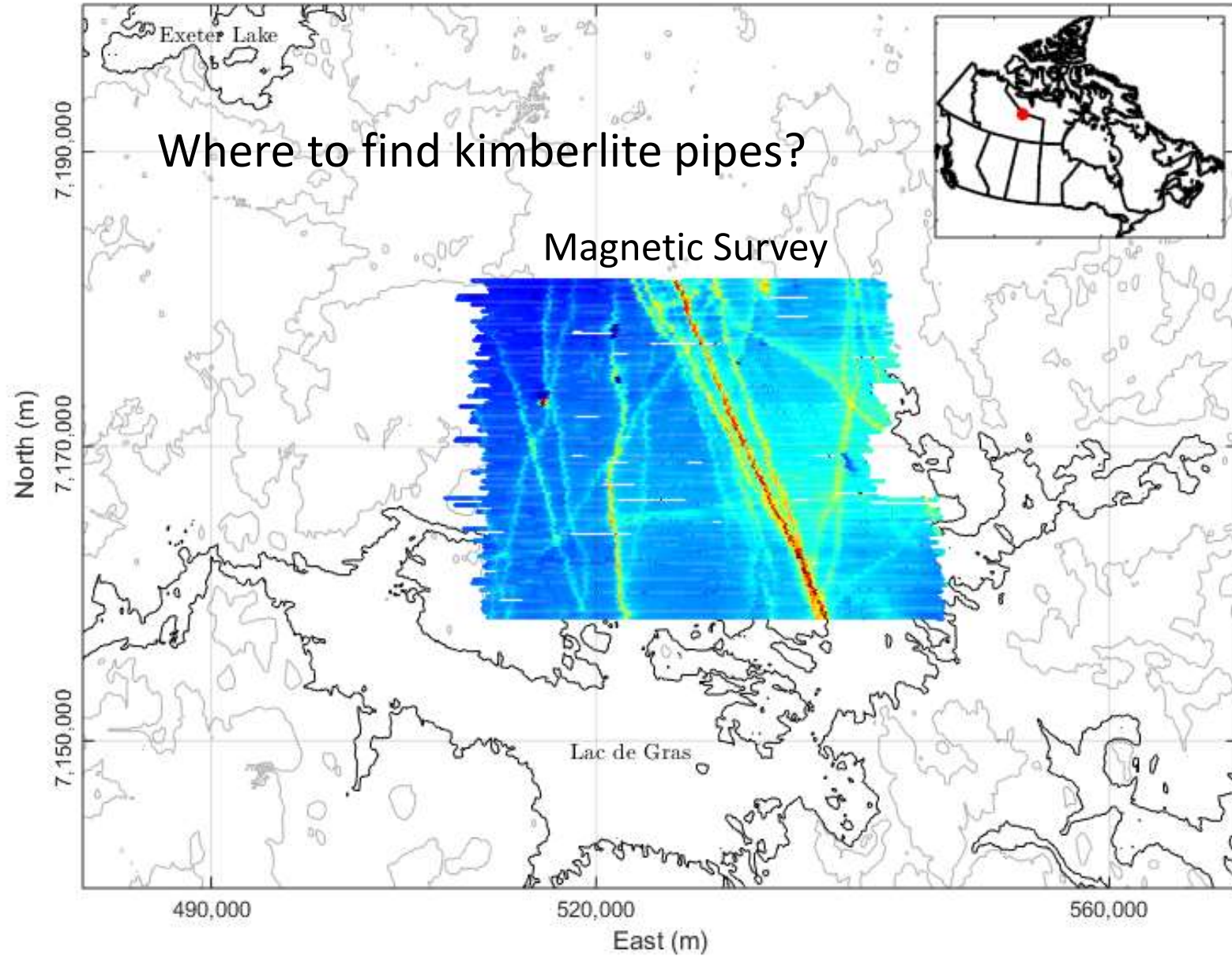
Divide the earth into many cells that contribute to the data on surface

- Each cell has a constant but unknown susceptibility (induced magnetization only)
- Each cell has an unknown magnetization vector (induced and/or remanent magnetization)



# Ekati Diamond Property, Northwest Territories

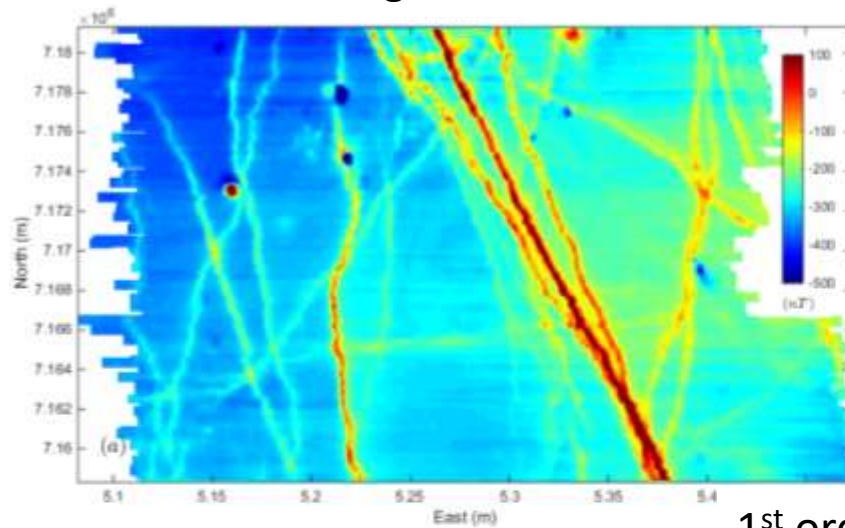




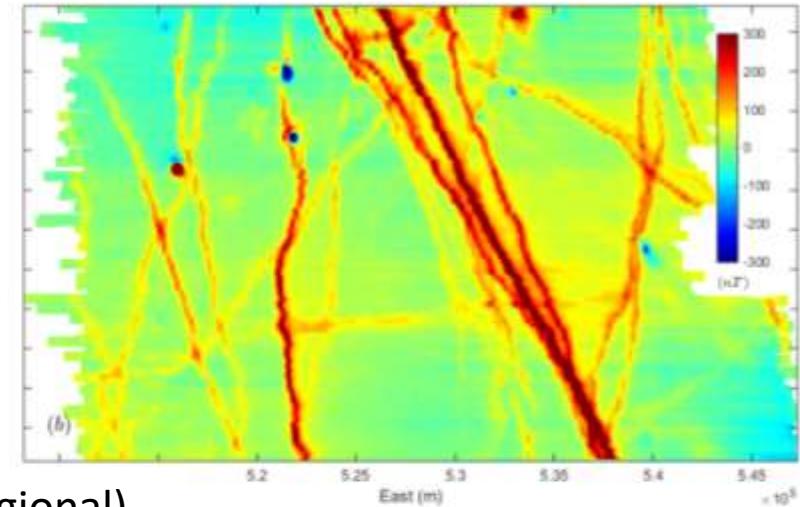


# Data Processing: Regional Removal

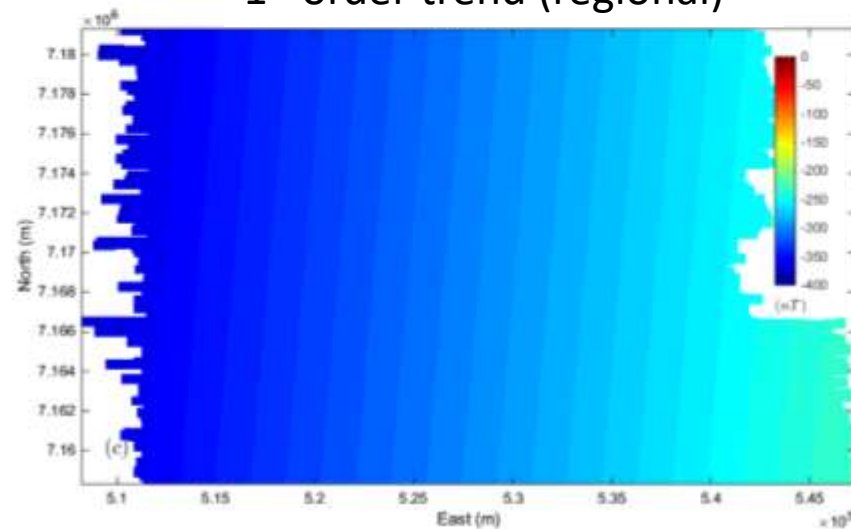
Original data



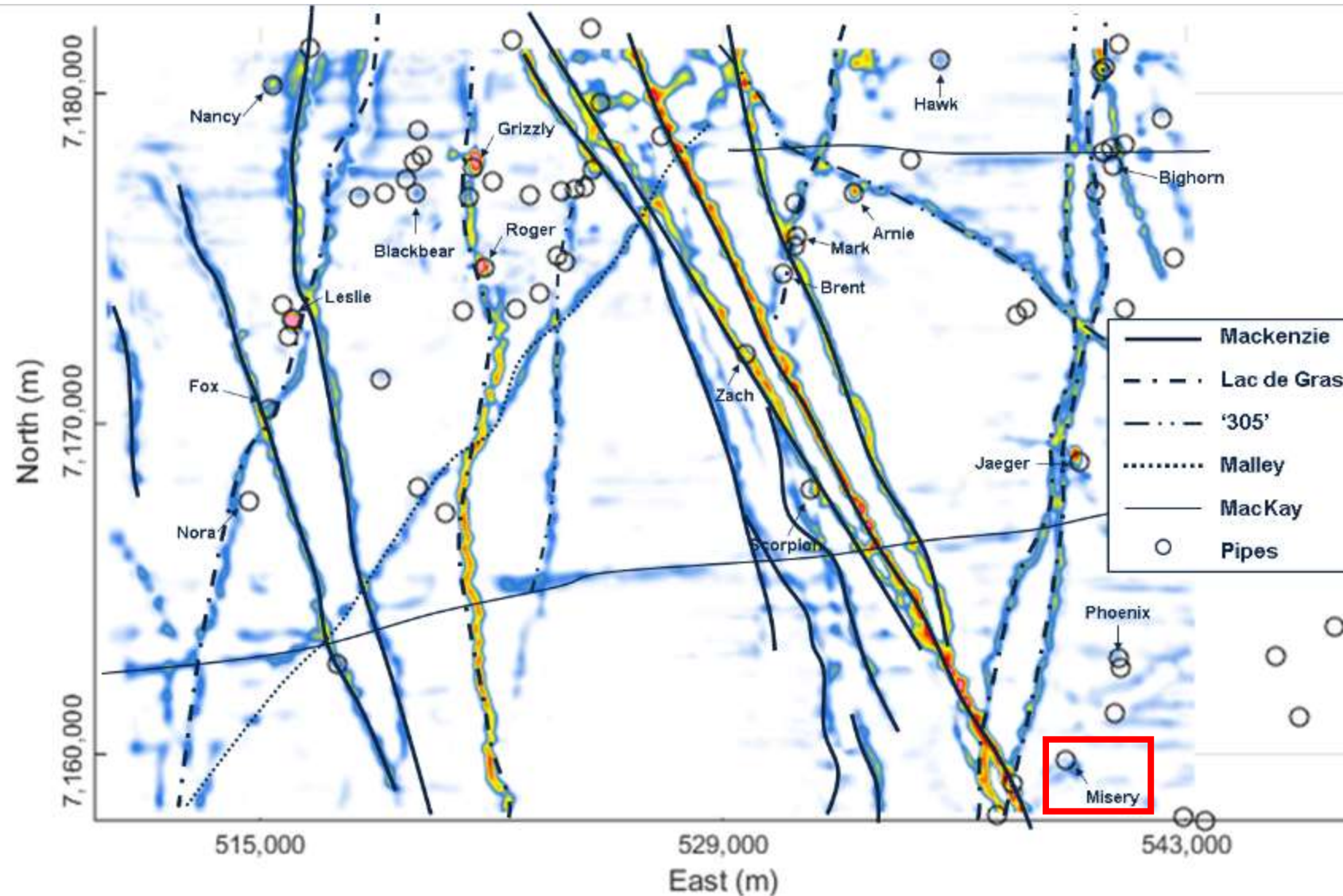
After regional removal



1<sup>st</sup> order trend (regional)

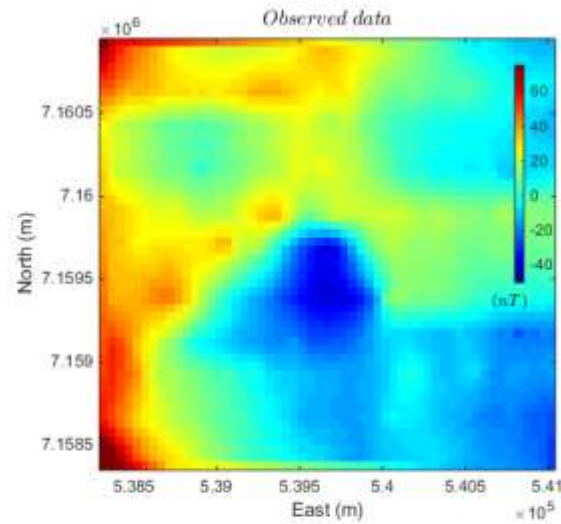


# Misery Pipe

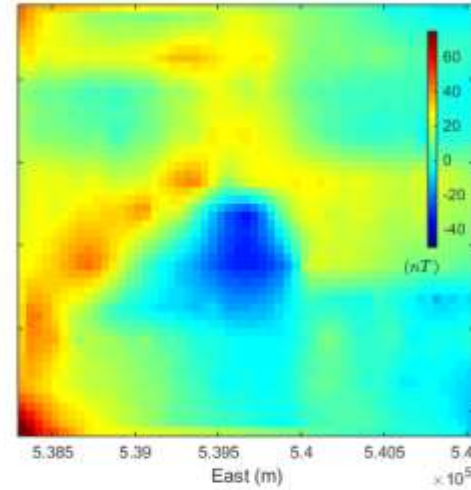


# Data Around Misery Pipe

Original



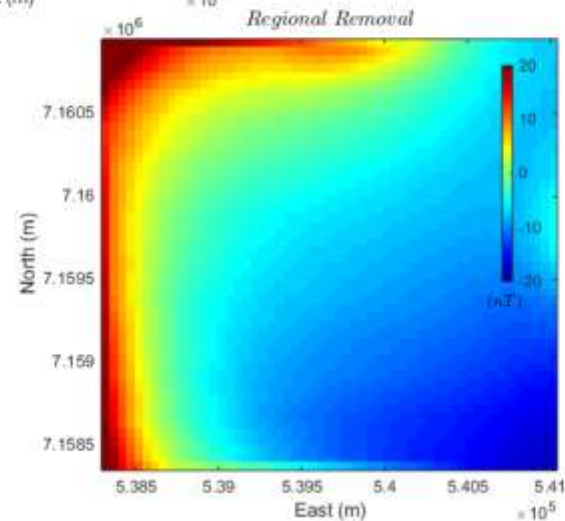
Levelled data



After regional removal

- Local anomaly showing reversely magnetized body (remanent)
- Removal of the regional field to enhance the target (ready for inversion)

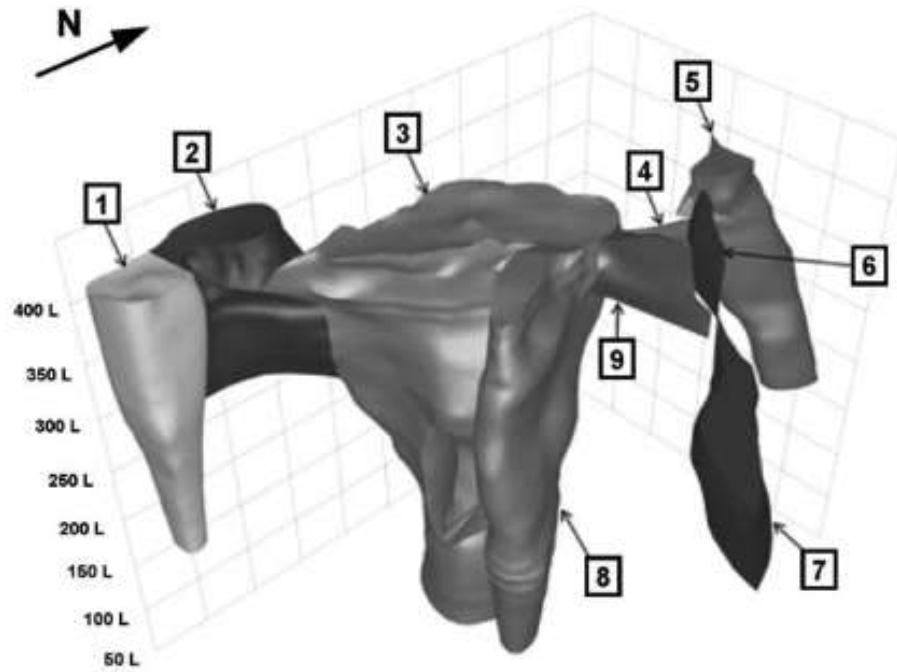
Regional



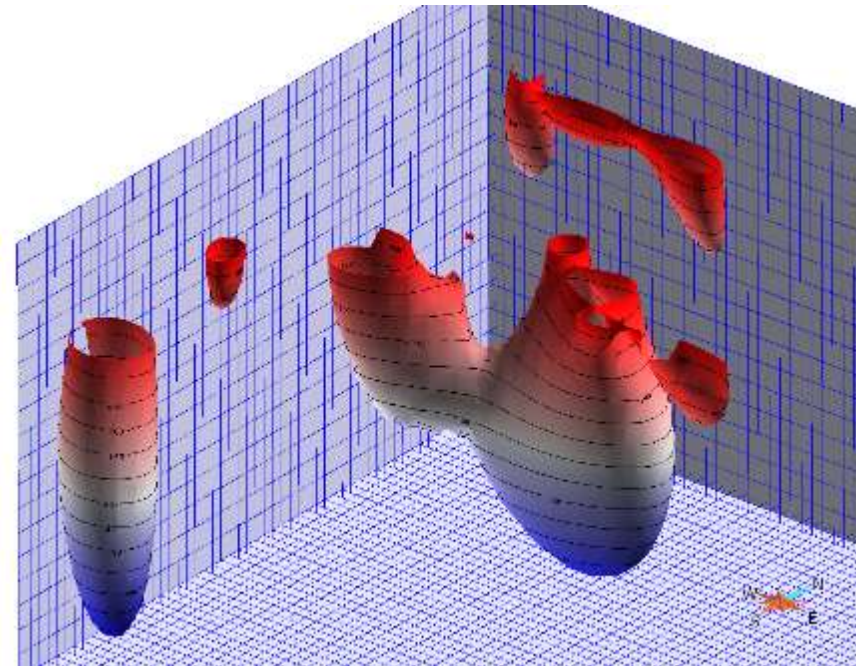


# Inversion Result

Geology from drilling



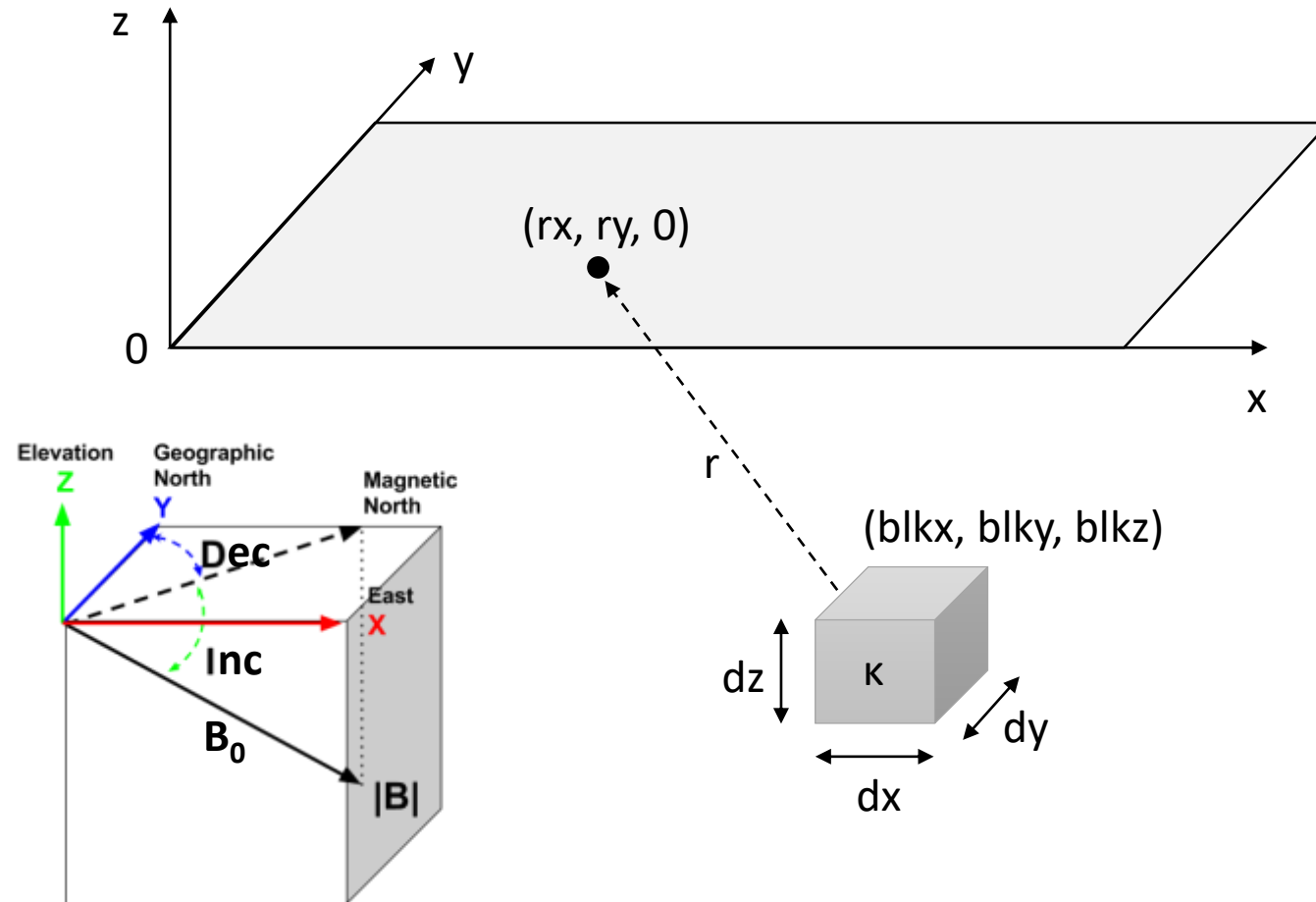
Inverted model



# Summary

- Two types of magnetization
- Dipole model builds everything
- UXO
- Re-bar
- Mineral (diamond) exploration

# Magnetic Assignment – Block



Magnetic anomaly from a susceptible block

$$\mathbf{M} = \kappa \mathbf{H}_0 = \kappa \mathbf{B}_0 / \mu_0$$

$$\mathbf{m} = \mathbf{M}V$$

$$\mathbf{B}(\mathbf{r}) = \frac{\mu_0}{4\pi} \left( \frac{3\mathbf{r}(\mathbf{m} \cdot \mathbf{r})}{r^5} - \frac{\mathbf{m}}{r^3} \right).$$

