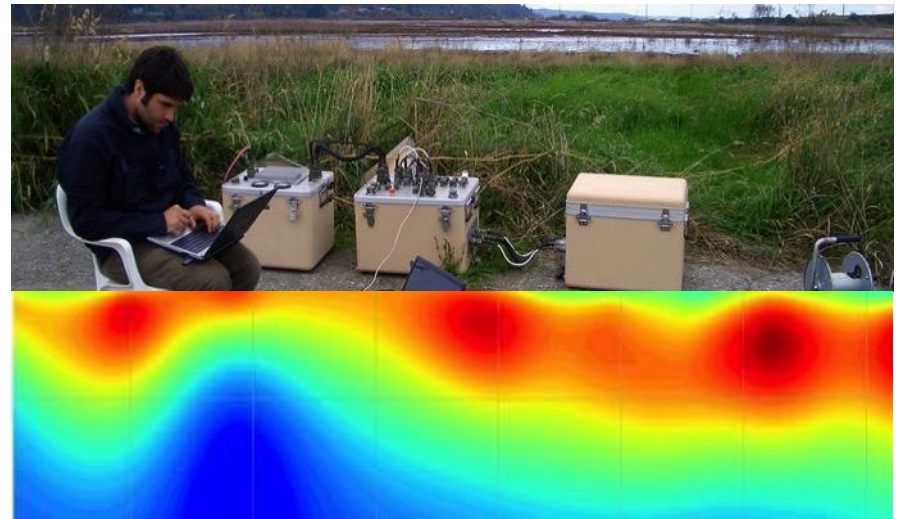




# EOSC 350 : Environmental, Geotechnical and Exploration Geophysics I

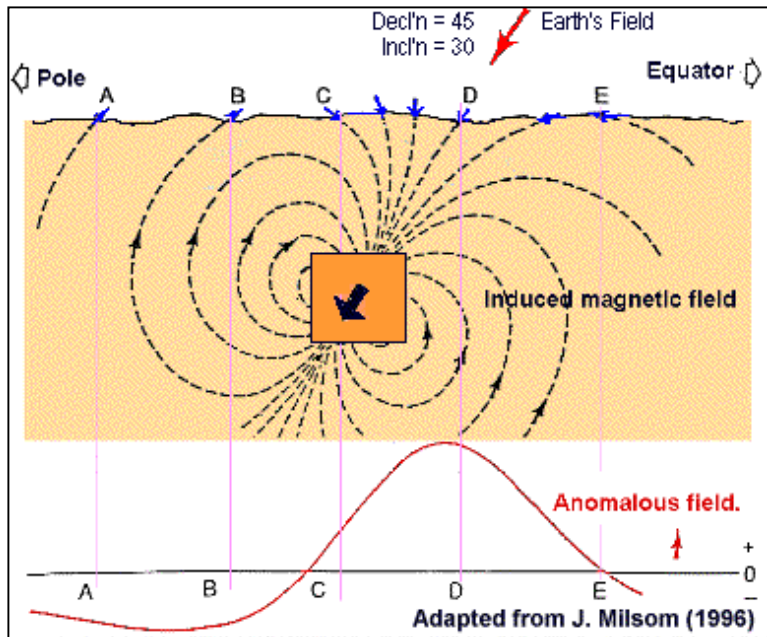
## EM Introduction



September – December, 2017

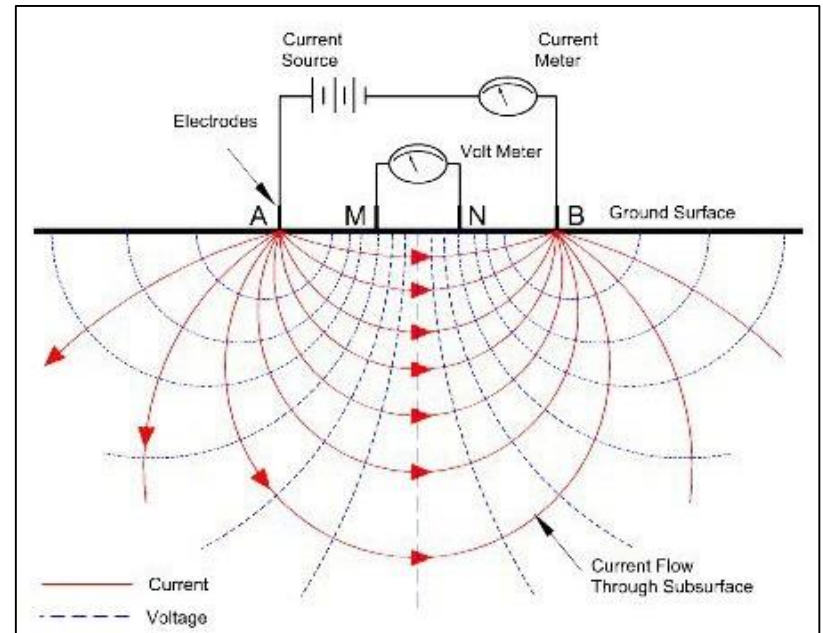
$$EM =$$

## Magnetics



- Magnetic dipole
- Magnetic flux (B)

## Electric Resistivity

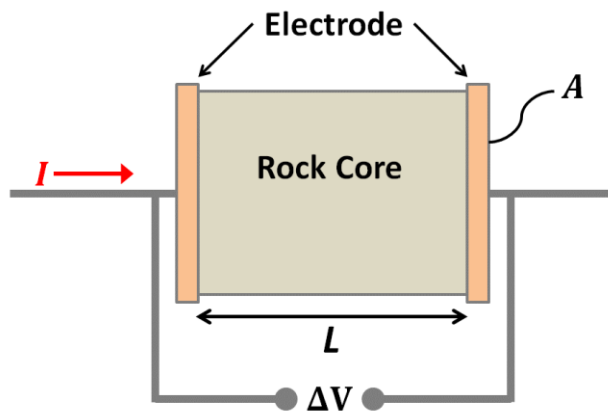


- Electric dipole
- Electric current (J)

# Electrical energy transmission

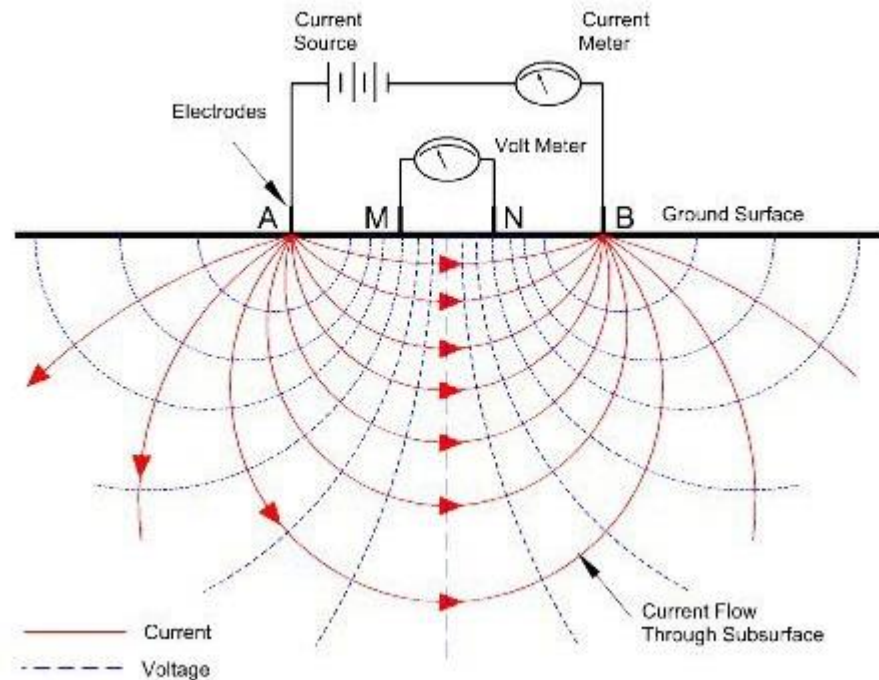
- Galvanic (electric current)

Ohm's law



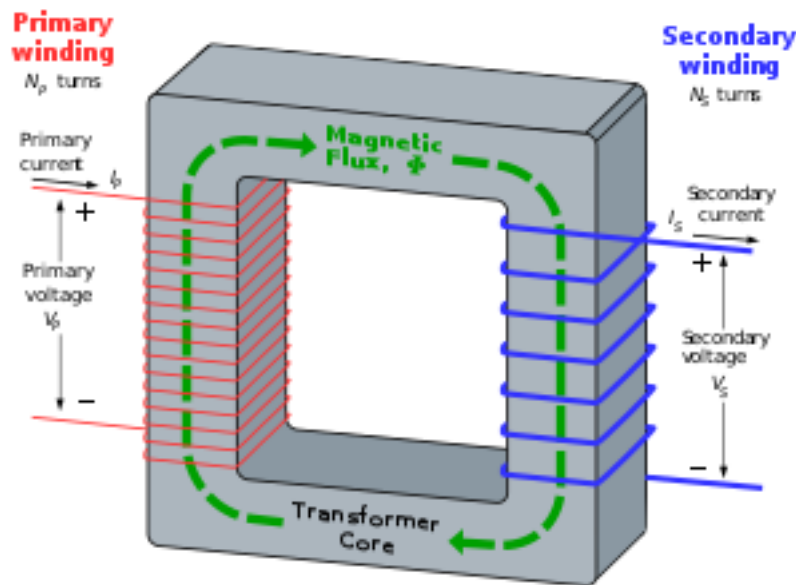
$$R = \frac{\Delta V}{I}$$

DC resistivity  
(electric resistivity tomography)



# Electrical energy transmission

- Inductive (magnetic flux  $B$ )



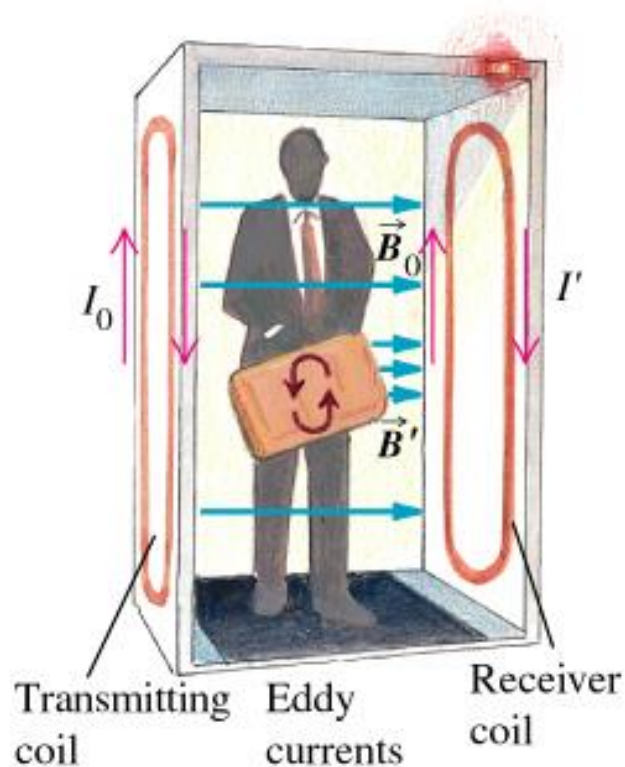
1. Change of current in the primary
2. Change of magnetic flux in the core
3. Induced current in the secondary

A transformer:

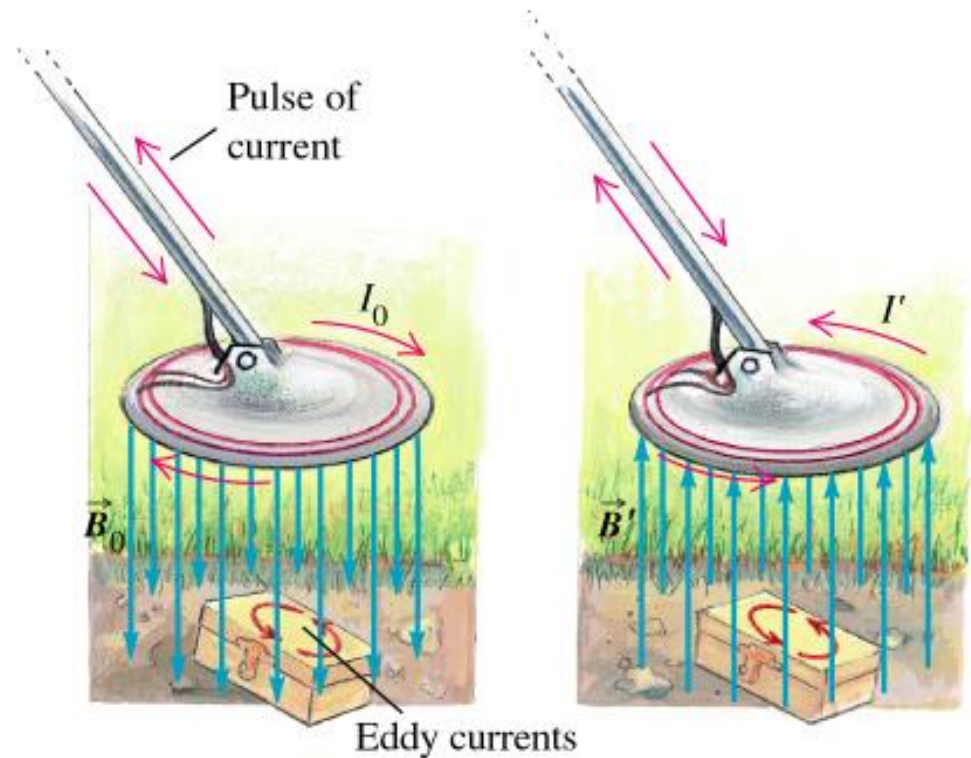
- No direct connection between primary and secondary windings
- Energy goes through in the forms of electric, magnetic then electric
- Magnetic flux linkage only in AC (requires non-stationary current)

# Electrical energy transmission

- Inductive (magnetic flux  $B$ )



Security scan



Metal detector



# Ampere's law

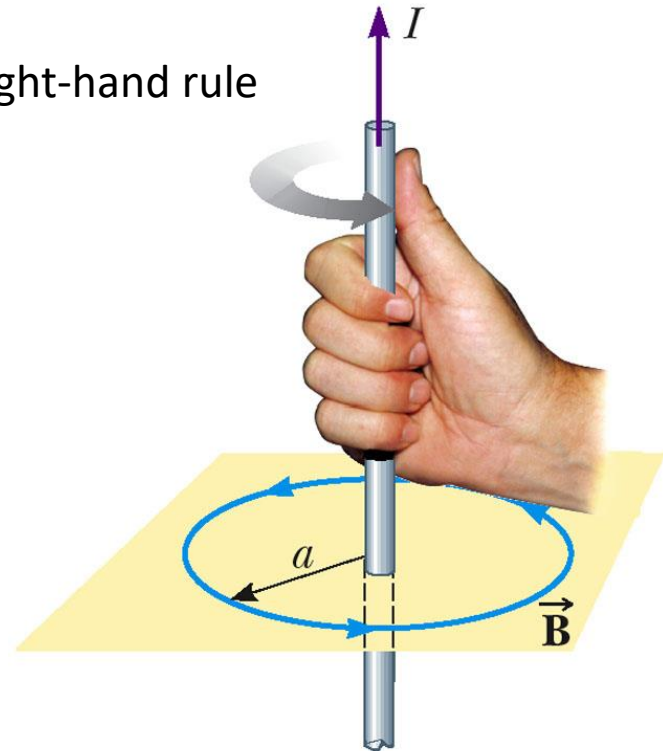
J generates B

$$\nabla \times \mu^{-1} \mathbf{B} = \mathbf{J} = \sigma \mathbf{E}$$



Current in wire causes a magnetic field to surround it (iron filings).

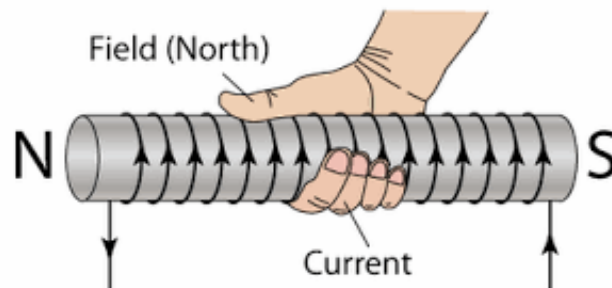
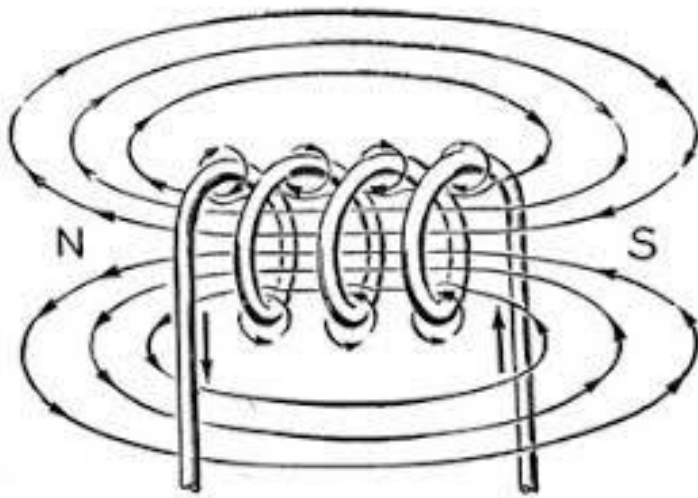
Right-hand rule



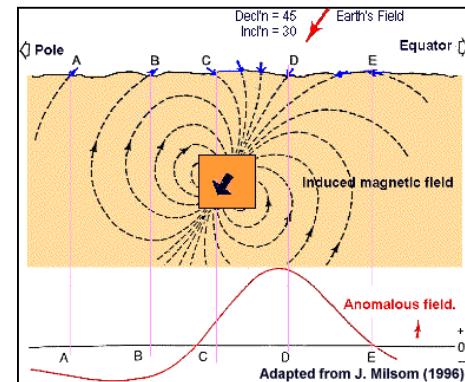
# Ampere's law

$\mathbf{J}$  generates  $\mathbf{B}$

$$\nabla \times \mu^{-1} \mathbf{B} = \mathbf{J} = \sigma \mathbf{E}$$



A small solenoid generates a magnetic field that can be approximated by a magnetic dipole (or a small bar magnet)

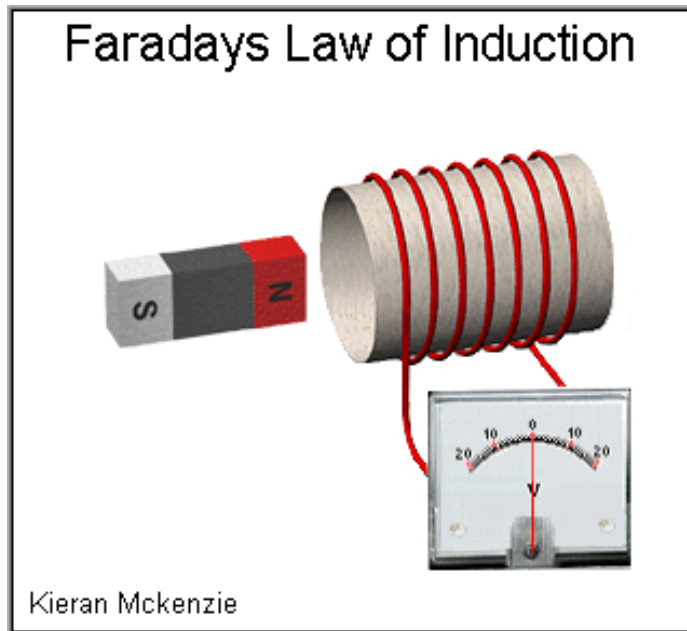


Still remember the magnetic dipole?

# Faraday's law

Change of B generates J

$$\nabla \times \sigma^{-1} \mathbf{J} = \nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$



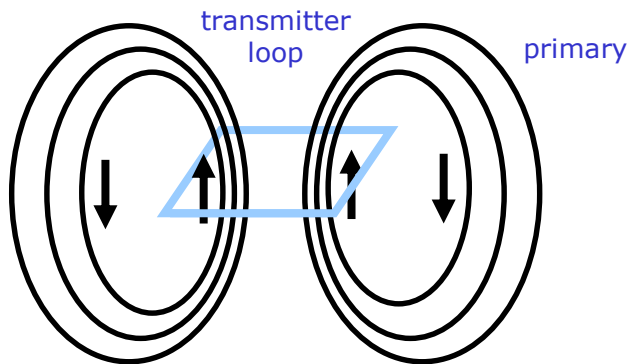
**Induced current depends on**

- How fast B changes
- How many B-field lines go through
- How conductive the object is



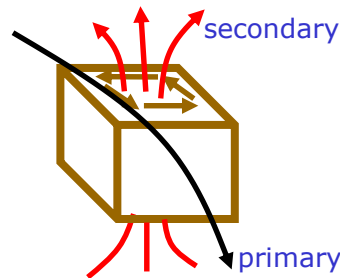
# Communicate with the earth

## Transmitter loop



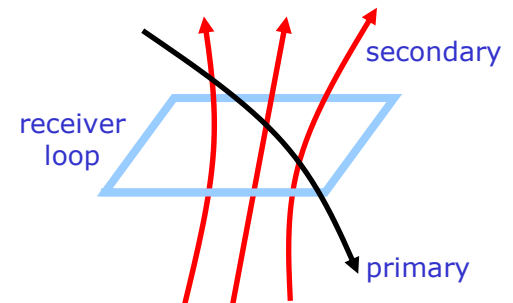
**Ampere:** time-varying current and changing primary magnetic field

## Target



**Faraday:** current induced by the changing primary field;  
**Ampere:** induced current generates a secondary magnetic field

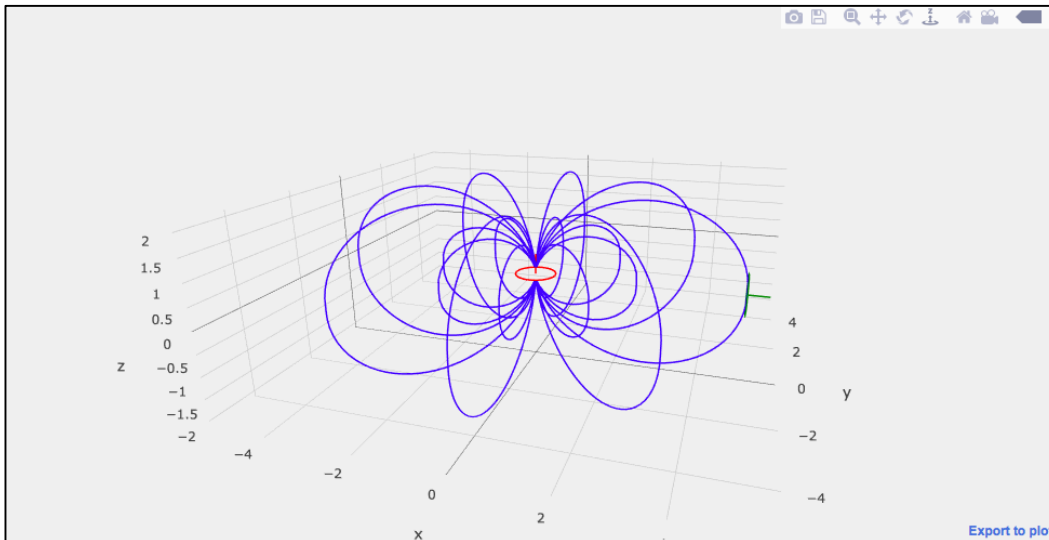
## Receiver loop



**Faraday:** measurable current induced in the loop by the changing secondary field

# Notebook: Loop, dipole and field lines

- Hands-on practice in TBL teams
- “MagDipoleLoops3D.ipynb”
- Clone or download from <https://github.com/yangdikun/magLab.git>
- Finish the following tasks in teams



## Tips:

The buttons on the top-right corner of the figure area can help you zoom, pan and rotate.

# Task 1: Loop by default

- “Run All” to get the default result
- Shown is a loop wire carrying an 1A current. The equivalent dipole moment is calculated as the product of loop area and current. Your estimate of the dipole moment is \_\_\_\_\_.
- The straight line perpendicular to the loop surface indicates the direction of the dipole moment. The plot you see represents a ***horizontal*** or ***vertical*** loop with a ***horizontal*** or ***vertical*** dipole moment. (circle one of the two choices)

# Task 2: Reorient loop

- Adjust the declination and inclination of Loop 1, so the dipole moment points to the +x direction. Now the loop represents a ***horizontal*** or ***vertical*** dipole. (circle one of the two choices)
- Take a screenshot of the figure and paste it below. Remember to include the axis labels.

# Task 3: Loop-loop coupling

- Check “Show Loop 2” to turn on the second loop.
- Keep the orientation of Loop 2 unchanged and adjust the location of Loop 2 to a point where it has the best geometric coupling with Loop 1 through the magnetic flux linkage (tangential direction of field lines is parallel to the dipole moment direction of a loop). Take a screenshot and paste it below. Remember to include the axis labels.



# Task 4: Loop-loop coupling

- Change the orientation of Loop 2, so the dipole moment points to the +x direction.
- Move Loop 2 around to find two locations where (1) Loop 1 and 2 are fully coupled and (2) Loop 1 and Loop 2 are null coupled. Paste the TWO screenshots below. Remember to include the axis labels.

# Submission

- If you have Microsoft PowerPoint, you can directly work in em\_intro\_tasks.pptx (download from the course website)
- You can also choose to copy the contents in the pptx file to your preferred word processing software and work in it
- Or send an email including your answers in plain text and pictures as attachment
- Each team needs to send a document or an email to [yangdikun@gmail.com](mailto:yangdikun@gmail.com)
- Submissions will be reviewed next week