/home/nicole/Jupyter/JG3/Data/0.5/M/10

https://cuda3.ansci.iastate.edu:9999/notebooks/Jupyter/JG3/J-SSBRnoJ-C-M.ipynb

```
In [4]:
        ;ls
        Correlation.G5.M.J.txt
        Correlation.G5.M.JC.txt
        G0.Genotype.ID
        G0.ID
        G0.noGenotype.ID
        G1.Genotype.ID
        G1.ID
        G1.noGenotype.ID
        G2.Genotype.ID
        G2.ID
        G2.noGenotype.ID
        G3.Genotype.ID
        G3.ID
        G3.noGenotype.ID
        G4.Genotype.ID
        G4.ID
        G4.noGenotype.ID
        G5.Genotype.ID
        G5.ID
        G5.noGenotype.ID
        MarNF.txt
        PedAll.txt
        Phe.txt
        PheAll.txt
        Regression.G5.M.J.txt
        Regression.G5.M.JC.txt
        all.ID
        alphaEstimatesJ
        alphaEstimatesJC
        epsiEstimatesJ
        epsiEstimatesJC
        genotype.ID
        meanOfSNPMAll
        meanOfSNPMG0
        meanOfSNPMG1
        meanOfSNPMG2
        meanOfSNPMG3
        meanOfSNPMG4
        meanOfSNPMG5
        noGenotype.ID
        sim.bv
        sim.phenotype
In [5]: | ;awk '{print $1}' PedAll.txt | sort -b > all.ID
In [6]: ;awk '{print $1}' MarNF.txt | sort -b > genotype.ID
In [7]:
        ;join -v1 all.ID genotype.ID > noGenotype.ID
In [8]: ;awk '{print $1,$2}' Phe.txt > sim.phenotype
        ;awk '{print $1,$3}' PheAll.txt > sim.bv
In [9]:
```

```
In [10]: ; awk 'NR >=1 && NR <=8000 {print $1}' PedAll.txt | sort -b > G0.ID
In [11]: ; awk 'NR >=8001 && NR <=16000 {print $1}' PedAll.txt | sort -b > G1.ID
         ; awk 'NR >=16001 && NR <=24000 {print $1}' PedAll.txt | sort -b > G2.ID
In [12]:
         ; awk 'NR >=24001 && NR <=32000 {print $1}' PedAll.txt | sort -b > G3.ID
         ; awk 'NR >=32001 && NR <=40000 {print $1}' PedAll.txt | sort -b > G4.ID
In [15]:
         ; awk 'NR >=40001 && NR <=48000 {print $1}' PedAll.txt | sort -b > G5.ID
         ; join G0.ID genotype.ID > G0.Genotype.ID
In [16]:
In [17]:
         ; join G1.ID genotype.ID > G1.Genotype.ID
In [18]:
         ; join G2.ID genotype.ID > G2.Genotype.ID
In [19]:
         ;join G3.ID genotype.ID > G3.Genotype.ID
In [20]:
         ; join G4.ID genotype.ID > G4.Genotype.ID
         ; join G5.ID genotype.ID > G5.Genotype.ID
In [21]:
In [22]:
         ; join -v1 G0.ID genotype.ID > G0.noGenotype.ID
In [23]:
         ;join -v1 G1.ID genotype.ID > G1.noGenotype.ID
In [24]:
         ; join -v1 G2.ID genotype.ID > G2.noGenotype.ID
         ;join -v1 G3.ID genotype.ID > G3.noGenotype.ID
In [26]:
         ; join -v1 G4.ID genotype.ID > G4.noGenotype.ID
In [27]:
         ; join -v1 G5.ID genotype.ID > G5.noGenotype.ID
In [28]:
         ;wc G0.Genotype.ID;wc G1.Genotype.ID;wc G2.Genotype.ID;wc G3.Genotype.ID;wc (
          200
               200 1200 GO.Genotype.ID
          200
               200 1200 G1.Genotype.ID
               200 1200 G2.Genotype.ID
          200
              200 1200 G3.Genotype.ID
               200 1200 G4.Genotype.ID
          200
          8000 8000 48000 G5.Genotype.ID
```

```
;wc G0.noGenotype.ID;wc G1.noGenotype.ID;wc G2.noGenotype.ID;wc G3.noGenotype
In [29]:
                7800 46800 G0.noGenotype.ID
          7800
                7800 46800 Gl.noGenotype.ID
          7800
                7800 46800 G2.noGenotype.ID
          7800 7800 46800 G3.noGenotype.ID
          7800 7800 46800 G4.noGenotype.ID
         0 0 0 G5.noGenotype.ID
         ped,A Mats,numSSBayes = calc Ai("PedAll.txt", "genotype.ID", calculateInbreedia
In [30]:
         nothing
         df
                = read_genotypes("MarNF.txt",numSSBayes)
         M Mats = make MMats(df, A Mats, ped, center=true);
                                                                                  # with
         y_Vecs = make_yVecs("sim.phenotype",ped,numSSBayes);
         Z_Mats = make_ZMats(ped,y_Vecs,numSSBayes)
         X Mats, W Mats = make XWMats(Z Mats, M Mats, numSSBayes)
                                                                                  # no
         nothing
In [31]: | vRes
                = 0.583
                = 0.583
         vG
         nIter = 50000
         @time aHat1,alphaHat,betaHat,epsiHat =
         ssGibbs(M_Mats,y_Vecs,Z_Mats,X_Mats,W_Mats,A_Mats, numSSBayes,vRes,vG,nIter,
         nothing
         This is iteration 5000
         This is iteration 10000
         This is iteration 15000
         This is iteration 20000
         This is iteration 25000
         This is iteration 30000
         This is iteration 35000
         This is iteration 40000
         This is iteration 45000
         This is iteration 50000
         2844.795100 seconds (23.04 G allocations: 723.763 GB, 7.43% gc time)
In [32]: betaHat
Out[32]: 1-element Array{Float64,1}:
```

9.66796

```
alphaHat
In [33]:
Out[33]: 150-element Array{Float64,1}:
            0.0319097
          -0.0693461
           0.209577
          -0.0217318
            0.199291
          -0.0280865
           0.00203055
           0.0507779
            0.0250513
           0.0535578
           0.0893467
          -0.0256326
          -0.0775642
          -0.236386
           0.122775
           0.0524742
          -0.00510436
           0.0577151
           0.0164112
          -0.0239208
          -0.148441
           0.185294
            0.0540718
          -0.00286981
            0.0342075
In [34]: writedlm("alphaEstimatesC",alphaHat)
```

```
In [35]: epsiHat
Out[35]: 45932-element Array{Float64,1}:
           0.0156136
           0.574366
           0.115858
          -0.00885838
           0.366237
          -0.0148336
          -1.11095
           0.00923433
           0.0455988
           0.178113
           0.283974
           0.227646
          -0.120868
          -0.258542
           0.557841
          -0.272919
           0.0275498
          -0.475944
          -0.952313
          -0.578285
          -0.0509856
           1.05492
          -0.0804832
           0.0224183
           0.820476
In [36]: writedlm("epsiEstimatesC",epsiHat)
In [37]: using DataFrames
In [38]: df = readtable("sim.bv", eltypes =[UTF8String, Float64], separator = ' ',head
         a = Array(Float64, numSSBayes.num ped)
         for (i,ID) in enumerate(df[:,1])
              j = ped.idMap[ID].seqID
             a[j] = df[i,2]
         end
In [39]: IDs = readtable("all.ID", eltypes =[UTF8String], separator = ' ',header=false
         posAi = getPos(ped,IDs)
         cor1 = cor(a[posAi],aHat1[posAi])[1,1]
         reg1 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - all.ID : correlation = %6.3f\n", cor1 ) # with 
         @printf("SSBRJC from Gibbs - all.ID : regression of TBV on GEBV = %6.3f\n",
         JCAll = cor1
         SSBRJC from Gibbs - all.ID : correlation = 0.906
         SSBRJC from Gibbs - all.ID : regression of TBV on GEBV = 0.998
Out[39]: 0.905564006610534
```

```
In [40]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[40]: 0.13653971324845515
In [41]: IDs = readtable("genotype.ID", eltypes =[UTF8String], separator = ' ',header:
         posAi = getPos(ped,IDs)
         cor2 = cor(a[posAi],aHat1[posAi])[1,1]
         reg2 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - genotype.ID : correlation = %6.3f\n", cor2 ) # |
         @printf("SSBRJC from Gibbs - genotype.ID : regression of TBV on GEBV = %6.3:
         JCAll = cor2
         SSBRJC from Gibbs - genotype.ID : correlation = 0.851
         SSBRJC from Gibbs - genotype.ID : regression of TBV on GEBV = 1.020
Out[41]: 0.8513154452011127
In [42]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[42]: 1.2465442681009715
In [43]: IDs = readtable("noGenotype.ID", eltypes =[UTF8String], separator = ' ',heade
         posAi = getPos(ped,IDs)
         cor3 = cor(a[posAi],aHat1[posAi])[1,1]
         reg3 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - noGenotype.ID : correlation = %6.3f\n", cor3 );
         @printf("SSBRJC from Gibbs - noGenotype.ID : regression of TBV on GEBV = %6
         JCAll = cor3
         SSBRJC from Gibbs - noGenotype.ID : correlation = 0.874
         SSBRJC from Gibbs - noGenotype.ID : regression of TBV on GEBV = 0.968
Out[43]: 0.8740794023374491
In [44]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[44]: -0.11961518402520256
In [45]: IDs = readtable("G0.ID", eltypes =[UTF8String], separator = ' ',header=false
         posAi = getPos(ped,IDs)
         cor4 = cor(a[posAi],aHat1[posAi])[1,1]
         reg4 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G0.ID : correlation = %6.3f\n", cor4 ) # with ep
         @printf("SSBRJC from Gibbs - G0.ID : regression of TBV on GEBV = %6.3f\n", re
         JCAll = cor4
         SSBRJC from Gibbs - G0.ID : correlation = 0.677
         SSBRJC from Gibbs - G0.ID: regression of TBV on GEBV = 0.799
Out[45]: 0.6771309082407354
```

```
In [46]: GEBV = aHat1[posAi]
         G1GEBV=mean(GEBV)
Out[46]: -1.21553556234854
In [47]: IDs = readtable("G1.ID", eltypes =[UTF8String], separator = ' ',header=false
         posAi = getPos(ped,IDs)
         cor4 = cor(a[posAi],aHat1[posAi])[1,1]
         reg4 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G1.ID : correlation = %6.3f\n", cor4 ) # with e;
         @printf("SSBRJC from Gibbs - G1.ID : regression of TBV on GEBV = %6.3f\n", re
         JCAll = cor4
         SSBRJC from Gibbs - G1.ID : correlation =
         SSBRJC from Gibbs - G1.ID: regression of TBV on GEBV = 0.956
Out[47]: 0.7611715483468551
In [48]: GEBV = aHat1[posAi]
         G1GEBV=mean(GEBV)
Out[48]: -0.5742613136281993
In [49]: IDs = readtable("G2.ID", eltypes =[UTF8String], separator = ' ', header=false
         posAi = getPos(ped,IDs)
         cor5 = cor(a[posAi],aHat1[posAi])[1,1]
         req5 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G2.ID : correlation = %6.3f\n", cor5 ) # with ei
         @printf("SSBRJC from Gibbs - G2.ID : regression of TBV on GEBV = %6.3f\n", re
         JCAll = cor5
         SSBRJC from Gibbs - G2.ID : correlation = 0.755
         SSBRJC from Gibbs - G2.ID : regression of TBV on GEBV = 1.014
Out[49]: 0.755260705770557
In [50]: GEBV = aHat1[posAi]
         G2GEBV=mean(GEBV)
Out[50]: -0.011812617942626823
In [51]: IDs = readtable("G3.ID", eltypes =[UTF8String], separator = ' ',header=false
         posAi = getPos(ped,IDs)
         cor6 = cor(a[posAi],aHat1[posAi])[1,1]
         reg6 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G3.ID : correlation = %6.3f\n", cor6 ) # with ei
         @printf("SSBRJC from Gibbs - G3.ID : regression of TBV on GEBV = %6.3f\n", re
         JCAll = cor6
         SSBRJC from Gibbs - G3.ID : correlation = 0.769
         SSBRJC from Gibbs - G3.ID: regression of TBV on GEBV = 1.078
Out[51]: 0.7689592054577262
```

```
In [52]: | GEBV = aHat1[posAi]
         G3GEBV=mean(GEBV)
Out[52]: 0.45804441658468914
In [53]: IDs = readtable("G4.ID", eltypes =[UTF8String], separator = ' ',header=false
         posAi = getPos(ped,IDs)
         cor7 = cor(a[posAi],aHat1[posAi])[1,1]
         reg7 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G4.ID : correlation = %6.3f\n", cor7 ) # with e;
         @printf("SSBRJC from Gibbs - G4.ID : regression of TBV on GEBV = %6.3f\n", re
         JCAll = cor7
         SSBRJC from Gibbs - G4.ID : correlation =
         SSBRJC from Gibbs - G4.ID : regression of TBV on GEBV = 1.084
Out[53]: 0.7681660156282842
In [54]: GEBV = aHat1[posAi]
         G4GEBV=mean(GEBV)
Out[54]: 0.8755634261423658
In [55]: IDs = readtable("G5.ID", eltypes =[UTF8String], separator = ' ',header=false
         posAi = getPos(ped,IDs)
         cor8 = cor(a[posAi],aHat1[posAi])[1,1]
         reg8 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G5.ID : correlation = %6.3f\n", cor8 ) # with ep
         @printf("SSBRJC from Gibbs - G5.ID : regression of TBV on GEBV = %6.3f\n", re
         JCAll = cor8
         SSBRJC from Gibbs - G5.ID : correlation = 0.831
         SSBRJC from Gibbs - G5.ID: regression of TBV on GEBV = 0.986
Out[55]: 0.8308232189738398
In [56]: GEBV = aHat1[posAi]
         G5GEBV=mean(GEBV)
Out[56]: 1.2872399306830415
In [57]: GEBVG5G1=G5GEBV-G1GEBV
Out[57]: 1.8615012443112409
In [58]: GEBVG1G5=[G1GEBV;G2GEBV;G3GEBV;G4GEBV;G5GEBV]
Out[58]: 5-element Array{Float64,1}:
          -0.574261
          -0.0118126
           0.458044
           0.875563
           1.28724
```

```
In [59]: reg8 = linreg(aHat1[posAi], a[posAi])
Out[59]: 2-element Array{Float64,1}:
          9.78287
          0.98629
In [60]: VarGEBV=var(aHat1[posAi])
Out[60]: 0.32807139203518837
In [61]: VarTBV=var(a[posAi])
Out[61]: 0.4623390829223029
In [62]: Cov=cov(aHat1[posAi], a[posAi])
Out[62]: 0.3235736214115439
In [63]: b=Cov/VarGEBV
Out[63]: 0.9862902687255277
In [64]: IDs = readtable("G0.Genotype.ID", eltypes =[UTF8String], separator = ' ',head
         posAi = getPos(ped,IDs)
         cor9 = cor(a[posAi],aHat1[posAi])[1,1]
         reg9 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G0.Genotype.ID : correlation = %6.3f\n", cor9 )
         @printf("SSBRJC from Gibbs - G0.Genotype.ID : regression of TBV on GEBV = %6
         JCAll = cor9
         SSBRJC from Gibbs - G0.Genotype.ID : correlation = 0.832
         SSBRJC from Gibbs - G0.Genotype.ID : regression of TBV on GEBV = 0.895
Out[64]: 0.8316035823998392
In [65]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[65]: 0.13319226820843183
In [66]: IDs = readtable("G1.Genotype.ID", eltypes =[UTF8String], separator = ' ', head
         posAi = getPos(ped,IDs)
         cor9 = cor(a[posAi],aHat1[posAi])[1,1]
         reg9 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G1.Genotype.ID : correlation = %6.3f\n", cor9 )
         @printf("SSBRJC from Gibbs - G1.Genotype.ID : regression of TBV on GEBV = %6
         JCAll = cor9
         SSBRJC from Gibbs - G1.Genotype.ID : correlation =
                                                              0.795
         SSBRJC from Gibbs - G1.Genotype.ID : regression of TBV on GEBV = 0.856
Out[66]: 0.795286270931245
```

```
In [67]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[67]: 0.6154010411928796
In [68]: IDs = readtable("G2.Genotype.ID", eltypes =[UTF8String], separator = ' ',head
         posAi = getPos(ped,IDs)
         cor10 = cor(a[posAi],aHat1[posAi])[1,1]
         reg10 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G2.Genotype.ID : correlation = %6.3f\n", cor10
         @printf("SSBRJC from Gibbs - G2.Genotype.ID : regression of TBV on GEBV = %6
         JCAll = cor10
         SSBRJC from Gibbs - G2.Genotype.ID : correlation =
         SSBRJC from Gibbs - G2.Genotype.ID: regression of TBV on GEBV = 1.019
Out[68]: 0.8582451518412377
In [69]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[69]: 0.951620622311199
In [70]: IDs = readtable("G3.Genotype.ID", eltypes =[UTF8String], separator = ' ',head
         posAi = getPos(ped,IDs)
         cor11 = cor(a[posAi],aHat1[posAi])[1,1]
         reg11 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G3.Genotype.ID : correlation = %6.3f\n", cor11
         @printf("SSBRJC from Gibbs - G3.Genotype.ID : regression of TBV on GEBV = %6
         JCAll = cor11
         SSBRJC from Gibbs - G3.Genotype.ID : correlation = 0.829
         SSBRJC from Gibbs - G3.Genotype.ID : regression of TBV on GEBV = 0.949
Out[70]: 0.8290519210515696
In [71]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[71]: 1.2540490264255666
In [72]: IDs = readtable("G4.Genotype.ID", eltypes =[UTF8String], separator = ' ', head
         posAi = getPos(ped,IDs)
         cor12 = cor(a[posAi],aHat1[posAi])[1,1]
         reg12 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G4.Genotype.ID : correlation = %6.3f\n", cor12
         @printf("SSBRJC from Gibbs - G4.Genotype.ID : regression of TBV on GEBV = %6
         JCAll = cor12
         SSBRJC from Gibbs - G4.Genotype.ID : correlation = 0.731
         SSBRJC from Gibbs - G4.Genotype.ID: regression of TBV on GEBV = 0.745
Out[72]: 0.7311202360952556
```

```
In [73]: | GEBV = aHat1[posAi]
         mean(GEBV)
Out[73]: 1.6506318790839873
In [74]: IDs = readtable("G5.Genotype.ID", eltypes =[UTF8String], separator = ' ',heac
         posAi = getPos(ped,IDs)
         cor13 = cor(a[posAi],aHat1[posAi])[1,1]
         reg13 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G5.Genotype.ID : correlation = %6.3f\n", cor13
         @printf("SSBRJC from Gibbs - G5.Genotype.ID : regression of TBV on GEBV = %6
         JCAll = cor13
         SSBRJC from Gibbs - G5.Genotype.ID : correlation =
         SSBRJC from Gibbs - G5.Genotype.ID: regression of TBV on GEBV = 0.986
Out[74]: 0.8308232189738398
In [75]: | writedlm("Correlation.G5.M.C.txt",cor13)
In [76]: | writedlm("Regression.G5.M.C.txt",reg13)
In [77]: GEBVG5Gall = aHat1[posAi]
         GEBVG5G=mean(GEBVG5Gall)
Out[77]: 1.2872399306830415
In [78]: IDs = readtable("G0.noGenotype.ID", eltypes =[UTF8String], separator = ' ',he
         posAi = getPos(ped,IDs)
         cor14 = cor(a[posAi],aHat1[posAi])[1,1]
         reg14 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G0.noGenotype.ID : correlation = %6.3f\n", corl
         @printf("SSBRJC from Gibbs - G0.noGenotype.ID : regression of TBV on GEBV = '
         JCAll = cor14
         SSBRJC from Gibbs - G0.noGenotype.ID : correlation = 0.656
         SSBRJC from Gibbs - G0.noGenotype.ID: regression of TBV on GEBV = 0.804
Out[78]: 0.6557751944809082
In [79]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[79]: -1.2501183272346164
```

```
In [80]: IDs = readtable("G1.noGenotype.ID", eltypes =[UTF8String], separator = ' ',he
         posAi = getPos(ped,IDs)
         cor14 = cor(a[posAi],aHat1[posAi])[1,1]
         reg14 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G1.noGenotype.ID : correlation = %6.3f\n", corl
         @printf("SSBRJC from Gibbs - G1.noGenotype.ID : regression of TBV on GEBV = '
         JCAll = cor14
         SSBRJC from Gibbs - G1.noGenotype.ID : correlation = 0.742
         SSBRJC from Gibbs - G1.noGenotype.ID: regression of TBV on GEBV = 0.959
Out[80]: 0.741856654651308
In [81]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[81]: -0.6047654765723295
In [82]: IDs = readtable("G2.noGenotype.ID", eltypes =[UTF8String], separator = ' ',he
         posAi = getPos(ped,IDs)
         cor15 = cor(a[posAi],aHat1[posAi])[1,1]
         reg15 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G2.noGenotype.ID : correlation = %6.3f\n", cor1!
         @printf("SSBRJC from Gibbs - G2.noGenotype.ID : regression of TBV on GEBV = '
         JCAll = cor15
         SSBRJC from Gibbs - G2.noGenotype.ID : correlation = 0.738
         SSBRJC from Gibbs - G2.noGenotype.ID : regression of TBV on GEBV = 1.014
Out[82]: 0.7382214143554697
In [83]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[83]: -0.036516034359391575
In [84]: IDs = readtable("G3.noGenotype.ID", eltypes =[UTF8String], separator = ' ',he
         posAi = getPos(ped,IDs)
         cor16 = cor(a[posAi],aHat1[posAi])[1,1]
         reg16 = linreg(aHat1[posAi], a[posAi])[2,1]
         @printf("SSBRJC from Gibbs - G3.noGenotype.ID : correlation = %6.3f\n", cor1
         @printf("SSBRJC from Gibbs - G3.noGenotype.ID : regression of TBV on GEBV = '
         JCAll = cor16
         SSBRJC from Gibbs - G3.noGenotype.ID : correlation = 0.756
         SSBRJC from Gibbs - G3.noGenotype.ID : regression of TBV on GEBV = 1.073
Out[84]: 0.7559243457491109
In [85]: GEBV = aHat1[posAi]
         mean(GEBV)
Out[85]: 0.4376340419733846
```