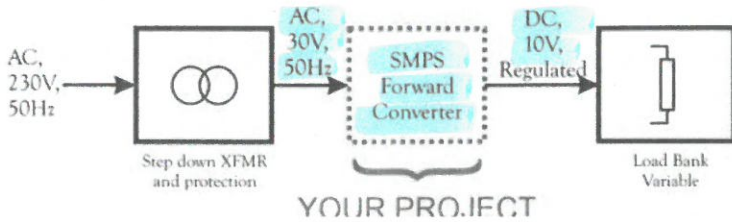


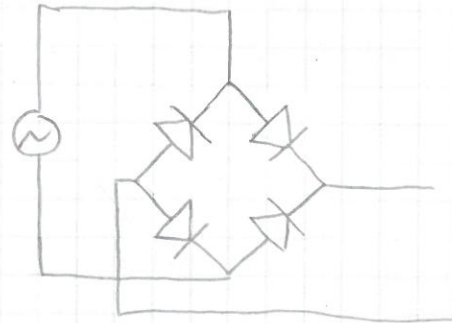
Energy project week 1

project aim : to design and build a practical SMPS (Switch Mode Power Supply) based on two-switch forward converter



20V AC (50Hz) → 100V

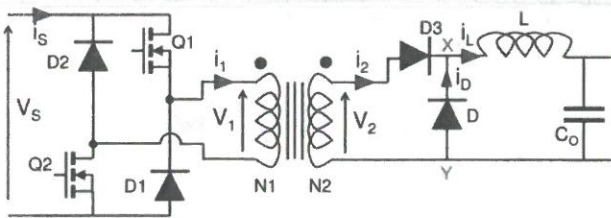
We can use full-bridge circuit to get a simple AC-DC converter



To avoid the saturation of the transformer. duty cycle for isolated forward converter is limited to 50%. ✓

Switching frequency : 75kHz - 150kHz

100kHz ✓



AC voltage : 20V RMS value : $20\sqrt{2}$

$$V_s = 20\sqrt{2} = 42.43V$$

DC voltage : 10V

mean voltage = dV_s

$$\text{If } d = 0.5 \quad \text{mean voltage} = 21.22$$

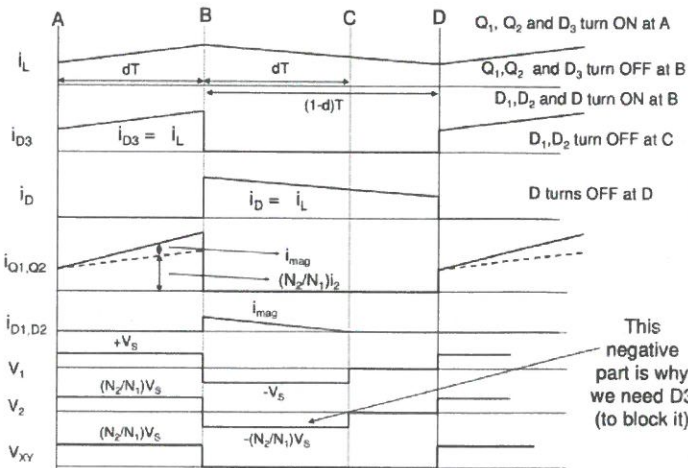
$$\text{If } d = 0.33 \quad \text{mean voltage} = 0.33 \cdot 42.43$$

For safety, set the duty cycle as 0.33

$$V_o = \left(\frac{N_2}{N_1}\right) dV_s$$

$$\frac{N_2}{N_1} = \frac{V_o}{dV_s} = \frac{10}{0.33 \cdot 42.43} = \frac{10}{14}$$

$$V_2 = \frac{N_2}{N_1} V_s = \frac{10}{14} \cdot 42.43 = 30.31V$$



This negative part is why we need D3 (to block it)

SMPS: an electronic circuit that converts power using switching devices that are turned on and off at high frequency. Storage components (inductors, capacitors) to supply power when the switching is in its non-conduction state. 4 major categories: AC-DC, DC-DC, DC-AC, AC-AC.

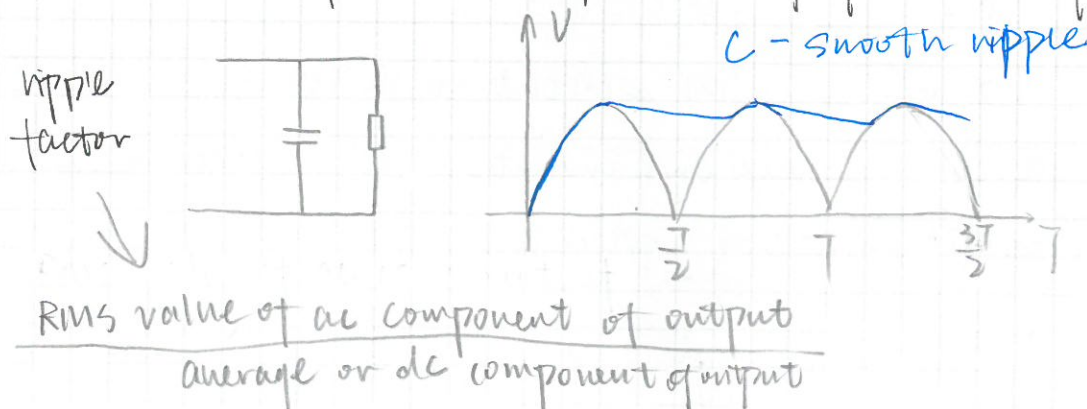
Why linear power supply transformer is much bigger than SMPS and what is different?

SMPS transformer: the frequency go up, the core size go down.

For PCB design, consider the non-ideal situation, set a resistor connect to the capacitor. (because there may be an inner resistance in capacitor) set the resistance: 0.01Ω

Attention: Input capacitor is to be limited to a maximum of $2000\mu F$.

Changing the capacitance changes the ripple at the output of rectifier and changes all design parameters. (small capacitor \downarrow)



minimum load

$$50W \cdot 25\% = 12.5W$$

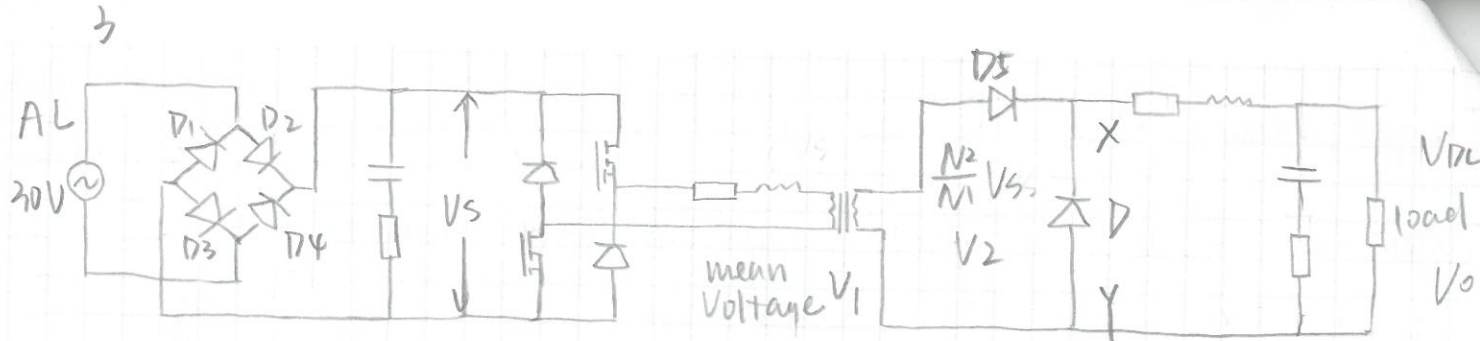
$$\frac{12.5W}{10V} = 1.25A \leftarrow \text{output current.}$$

$$R = \frac{10}{1.25} = 8\Omega.$$

maximum load

$$\frac{50W}{10V} = 5A \leftarrow \text{output current}$$

$$R = \frac{10}{5} = 2\Omega.$$



AC 30V
 $V_s = \sqrt{2} \cdot 30 = 42.43V$
 $V_1 = 42.43V$
 $\frac{N_2}{N_1} = \frac{10}{14}$
 $V_2 = \left(\frac{N_2}{N_1}\right) V_s = \frac{10}{14} \cdot 42.43 = 30.31V$
 $V_{XY} = \left(\frac{N_2}{N_1}\right) d V_s$
 DC $\left(\frac{N_2}{N_1}\right) d V_s \leftarrow 10V$

$V_L = V_2 - V_o = 30.31 - 10 = 20.31V$
 $dV_L = d \cdot 20.31 = 6.70V$

Power 50W min $= 50 \times \frac{1}{5} = 10W$

$R = \frac{V^2}{P} = \frac{100}{10} = 10\Omega$

$I = \frac{V}{R} = \frac{10}{10} = 1A$

OL 2A

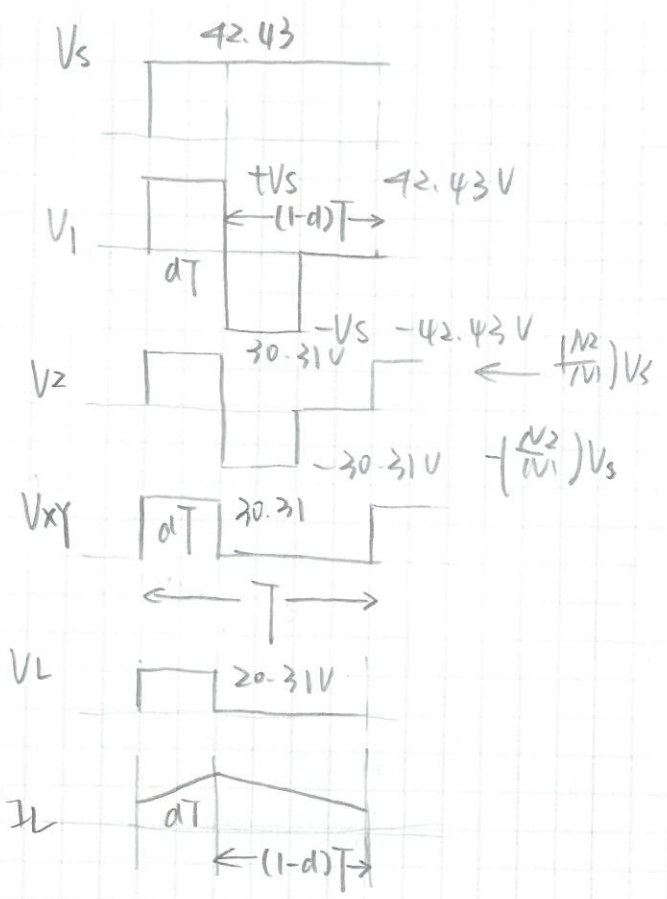
$L = \frac{dV_L T}{\Delta I} = \frac{6.7 \cdot 10^{-5}}{2} = 3.35 \cdot 10^{-5}H$

OV 0.1V \leftarrow ripple should less than 0.2V

$C = \frac{I T \Delta}{\Delta V} = \frac{1 \cdot 10^{-5} \cdot \frac{1}{2}}{0.1} = 2.5 \cdot 10^{-5}F$ so set as 0.1V

$\Delta I_L = \frac{(V_s - V_o) d T}{L}$


capacitor: ΔV_C



$f = 100k$
 $T = \frac{1}{f}$

4

AC: amplitude 42.43V
 frequency 20.50 rad/s
 phase 0

diode of the bridge 
 VS-KBP1
 forward voltage 1.1V

use an isolator to protect the element, translate the information
 \Rightarrow use an LED.

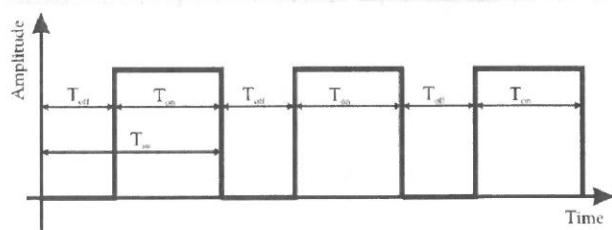
MOSFET: on-resistance 0.11
 initial conductivity 0 RF1530N/PBF

Diode: forward voltage 1.4
 On-resistance 0 BY620

Triode forward voltage 0.44 MBRB3030CT/LH

pwm circuit generation

In real world, we need to realize a circuit to switch on the MOSFET.
 MOSFET needs quite some voltage and current to be switched on, so it's
 not possible to connect directly to logic circuit.

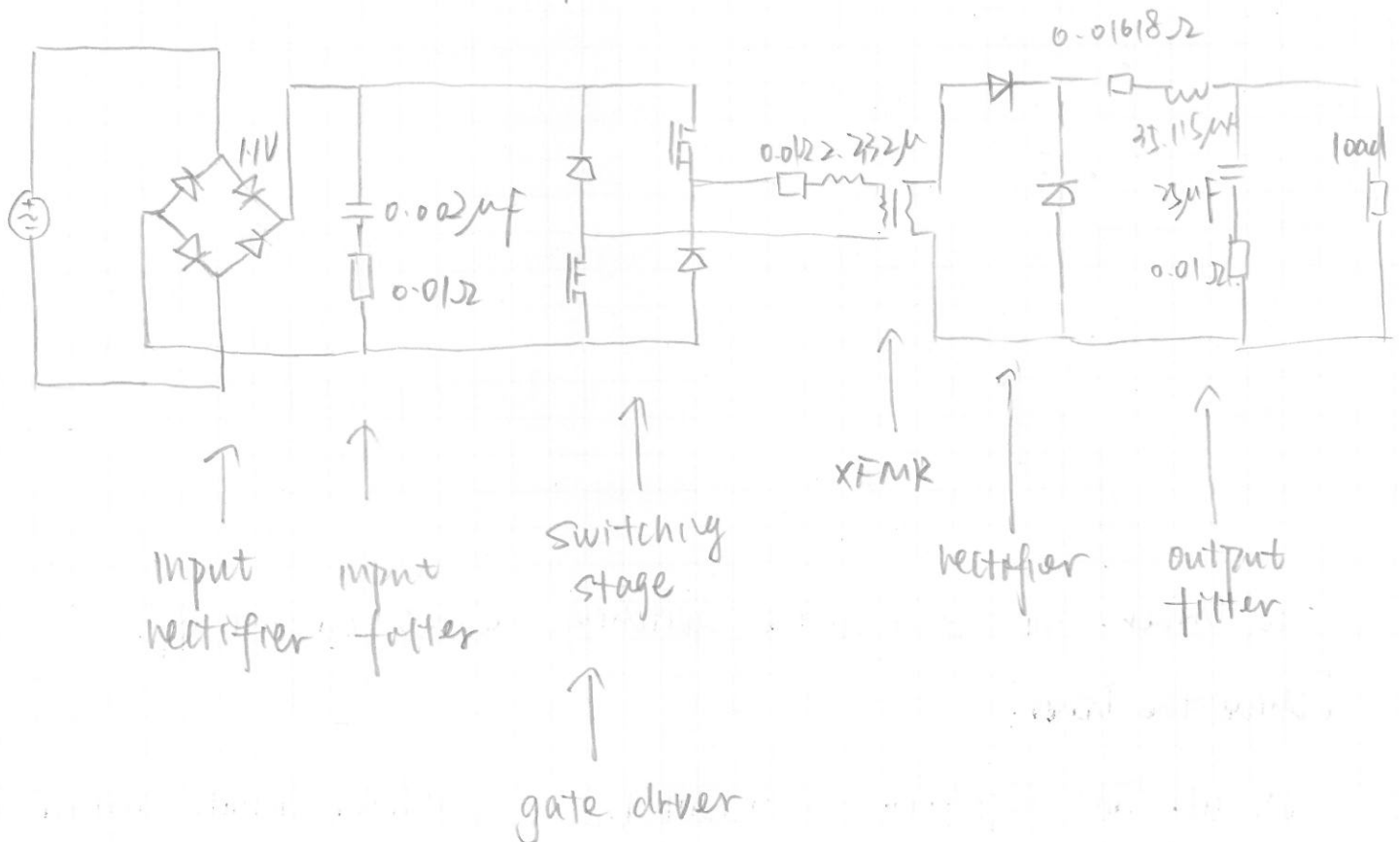


duty cycle $d = \frac{T_{on}}{T_{sw}}$

A UC3524 IC can be used as an open loop
 pwm generator with a variable duty cycle

5 Suggestion

1. Input capacitor maximum $2000\mu F$ smaller is better
2. Feedback control will compensate for the low frequency ripple at output voltage. (We can have a big ripple at output of rectifier)
3. Don't use RC rectifier (R dissipate power)
4. Use capacitor to filter the switch ripple.
5. Supply transformer and its impedance $\Rightarrow 1 - \frac{2}{3} - 2mH$.
because the load will influence converter input voltage.



Pulse generator \rightarrow gate driver.

1. 3 legs with case \rightarrow MOSFET.

UC3524AN PWM generator

max duty cycle 45%.

TL495 power amplifier.

MC6222 x 2

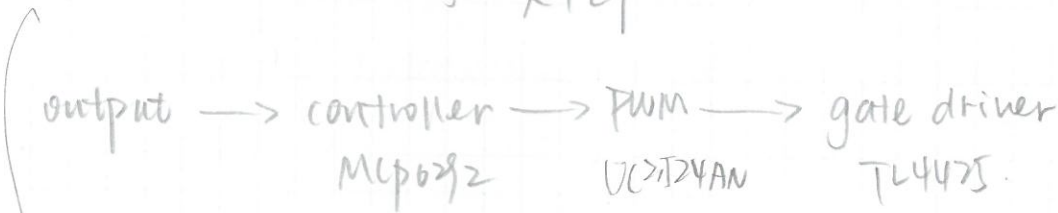
TL495 x 1

UC3524AN x 1

UC3524AN

$$f = \frac{1.18}{RTCT}$$

120Hz \sim 500kHz.



Timing Resistor R_T 1.8k - 100k

Timing Capacitor R_C 0.001 μ F - 0.1 μ F.

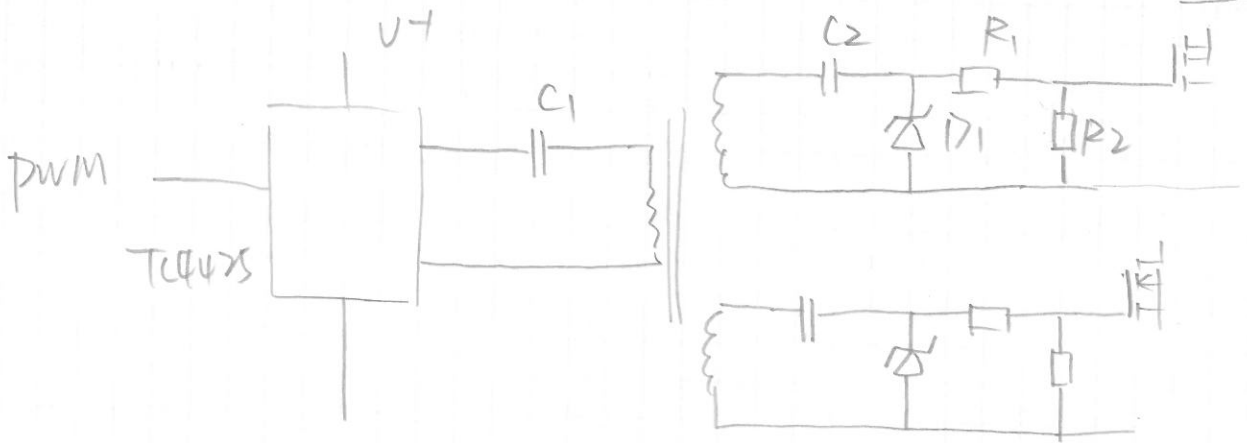
In our design. set PWM duty cycle to 45%.

frequency to 100kHz.

Gate Driver. how to turn the switching devices on and off.
(Drive the Devices).

acts like an amplifier which controlled by low level signals and increase the voltage and current output to a level capable of driving the power devices

0.5



- C1 not be too large $< 1000\text{ nF}$.
lead to constant saturation of the transformer.
- C2. maintain $V_{gs} > V_{th}$ during positive half cycle.
- D1. protect the gate from over voltage spikes.
- R1 determine the current flow in the gate.
- R2. pull down resistor. } discharge the gate.
stop the gate floating if gate driver fails.

Step

1. Select an airgap for an initial design 1mm
2. Calculate the number of turns required. 15 ~~24~~ 12
3. Check the peak flux density
4. Calculate the area of copper required for each turn of the winding.

5. Selecting the wire diameter. $A = \frac{\pi d^2}{4}$ (C)

skin depth $\delta = \sqrt{\frac{\rho}{\pi f \mu}}$ frequency $\rightarrow 100\text{kHz}$

$$f = 100\text{K}$$

$$\mu = 0.999 \Rightarrow \delta = 2.06 \times 10^{-4}$$

$$\rho = 1.678$$

$$A_{\text{Fea}} = \pi R^2 = 0.133\text{mm}^2$$

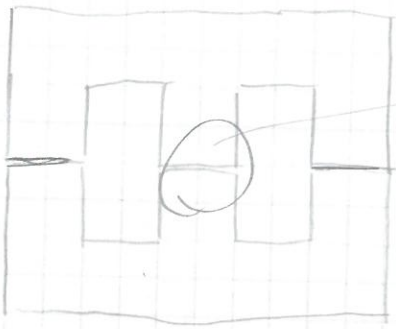
6. Calculating the power losses.

Design an Inductor

This inductor is used for secondary circuit of Forward Converter

Ferrite material

Ferrite is used because $\left\{ \begin{array}{l} \text{the frequency is too high to use steel.} \\ \text{the power losses in the core would be too high} \end{array} \right.$



$$36.8 \times 10^{-6} \text{ H}$$

air gap

flux must pass

air gap \downarrow

Inductor can store a significant amount of energy.
 Shorted.

wire	Cross section	Ohm	Typical current
20	0.9189	33.9	\geq
21	0.4116	42.7	1.6
23	0.2588	48.1	1.002
26	0.1281	143	0.506
28	0.0804	227	0.318
30	0.0507	361	0.2
32	0.0316	583	0.128

$$A = \frac{I_{rms}}{J} = \frac{\sqrt{\frac{24+36+24}{3}}}{J} = \frac{5.03}{J}$$

$$\text{Energy stored: } \frac{1}{2} \frac{B^2}{\mu}$$

$$\frac{5.03}{4}$$

□ difference between a transformer and inductor
Inductor: air gap

transformer: no air gap.

material 1V87 Ferrite.

shape of the core ETD (Economical transformer Design)

size ETD34 (longest dimension 34mm)

cores 0.05 1mm

Airgap 1mm N15 or 16. Attch 28.

$$N=15$$

$$N=16$$

$$R_{al} = 0.0124 \Omega$$

$$R = 0.0133 \Omega$$

$$\text{total flux } \phi(t) = \frac{N i(t)}{R}$$

$$L = \frac{N \phi(t)}{i(t)}$$

$$L = \frac{N^2}{R}$$

$$R = \frac{1}{A} \left[\frac{l_{core}}{\mu_r \mu_0} + \frac{g}{\mu_0} \right]$$

μ_0 permeability of free space

μ_r ferrite

A air of magnetic path

l_{core} length of the flux

g air gap length.

$$N = \sqrt{\frac{g L}{\mu_0 A}}$$



$$\mu_0 = 4\pi \cdot 10^{-7}$$

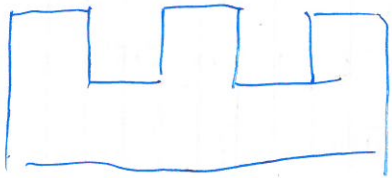
$$B = \frac{\phi}{A} = \sqrt{\frac{\mu_0 L}{g A}} i$$

size

ETD 34 in N87

transformer

shape



no airgap.

connections

4

(inductor, 1000 turns)

turn ratio

11:10

material

Ferrite

the value of N_1 determines the peak flux in the core and the peak magnetic current

$$V_1 = N_1 \frac{d\phi}{dt}$$

$$\hat{\phi} = \frac{V_{sdT}}{N_1}$$

$$I_{mag} = \frac{V_{sdT}}{Z_{mag}}$$

inductor factor
↓
 $N^2 A_L$

$$\hat{\phi} = \frac{39.44877}{12} \sqrt{\frac{0.3 \times 0.05}{100 \times 10^3}} \rightarrow 2 \times 10^{-6}$$

$$B_{sat} = 0.45 T$$

windy transformer

reduce leakage inductance

leakage inductance : ringing in the voltage.

non-interleaved

Snubbers across the diode.

Transformer for gate driver

Type

ferrite (used for high frequency)

saturation flux density 0.4-0.5T.

3C90 ferrite.

Size

TN 13/7.5/5

TN 14/9/5

Winds

1:2

ratio

1:1:1

$$V = N \frac{d\phi}{dt}$$

$$N \int V dt = \phi_1 - \phi_0$$

$$\frac{VTA}{NA_{core}} = \Delta B$$



magnetic inductance

$$L_{mag} = \frac{N^2}{R}$$

$$R = \frac{l}{A_{core} \left(\frac{\mu_{core}}{\mu_r \mu_0} \right)}$$

$\mu_0 = 4\pi \cdot 10^{-7}$

$$L_{mag} = AN^2 = 2.6 \cdot 10^{-4} H$$

Size of wire.

Cross sectional area A_{cu} .

Losses.

core losses

hysteresis losses

1. close loop control (week 8)



$$\frac{C(s)}{R(s)} = \frac{G(s)}{1 + G(s)H(s)}$$

2. Bode Plot using MATLAB (week 9)

X-axis: $\log_{10}(\text{frequency})$
 Y-axis: $20 \log_{10}(\text{magnitude})$

X-axis: $\log_{10}(\text{frequency})$
 Y-axis: $20 \log_{10}(\text{magnitude})$

★ method.

example: $G_p(s) = \frac{s^2 + 6s + 5}{s^2 + 5s}$

$U(s) \rightarrow [G_p(s)] \rightarrow C(s)$

numerator: 1, 6, 5 denominator: 1, 5, 0

input transfer function: $G_p = \text{tf}([1 \ 6 \ 5], [1 \ 5 \ 0])$

plot bode plot: `bode(Gp)`

show the magnitude and phase: $(G_p \text{mag}, G_p \text{phase}) = \text{bode}(G_p, \omega_c)$

$$\omega_c = \frac{1}{\sqrt{LC}}$$

3. Transfer function (conclusion).

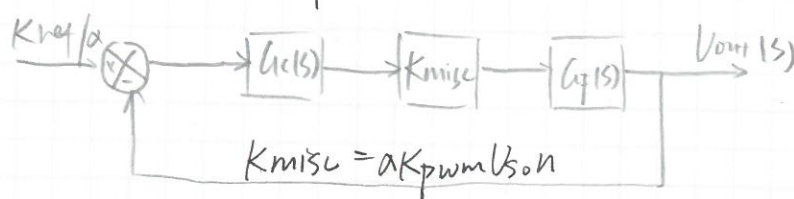
★ A simple controller (Type 1)

a simple integrator. $G_i(s) = \frac{A}{s}$ phase shift 90° (lagging)

how to define the gain of $G_i(s)$ $\Rightarrow G = |G_i(s)|_{\omega_c} = |G_i(j\omega_c)| = \frac{A}{\omega_c}$

use the method in (2). to find out bode plot

calculate the value of K_{misc}



calculate the gain of controller $G = \frac{1}{K_{misc} |G_f(j\omega_c)|}$

d: potential divider
 (change)

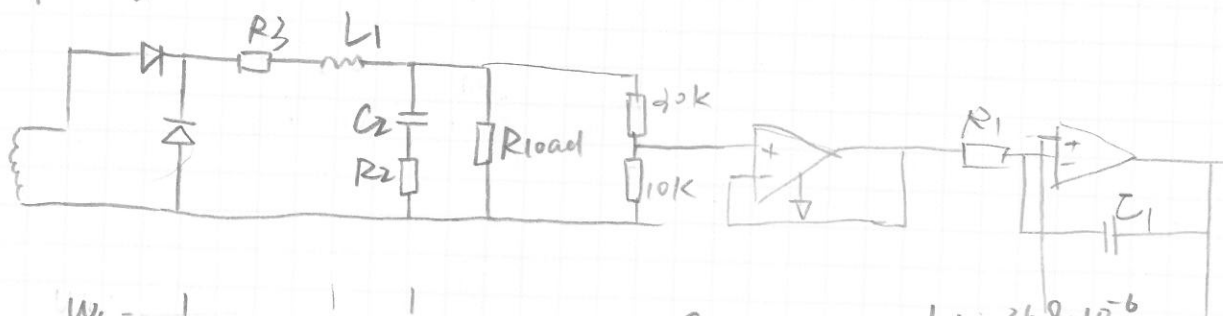
$$K_{pwm} = \frac{d}{V_B - V_A}$$

d: max 0-45

V_B, V_A : check datasheet

h: turn ratio: transformer
 (last semester) $\frac{11}{10}$

For type 1



$$\omega_c = \frac{1}{10\sqrt{LC}} = \frac{1}{10\sqrt{368 \cdot 10^{-6} \cdot 33 \cdot 10^{-6}}} = 2869.59$$

$$L1 = 368 \cdot 10^{-6}$$

$$C2 = 33 \cdot 10^{-6}$$

$$R2 = 0.01$$

$$R1 = 10k$$

$$C1 = 4.7 \cdot 10^{-8}$$

$$Gf(s) = \frac{1 + sR1C1}{s^2LC + s\left(\frac{L}{R} + LRC1\right) + 1}$$

$$= \frac{1 + 0.01 \cdot 33 \cdot 10^{-6}s}{s^2LC + s\left(\frac{L}{R} + LRC1\right) + 1}$$

$$= \frac{10^6 + 0.33s}{368 \cdot 10^{-6} \cdot 33 \cdot 10^{-6}s^2 + s\left(\frac{368 \cdot 10^{-6}}{2} + 33 \cdot 10^{-6} \cdot 0.01\right) + 1}$$

$$= \frac{10^6 + 0.33s}{1214.4 \cdot 10^{-6}s^2 + 18.73s + 10^0}$$

Appendix A. System Modeling.

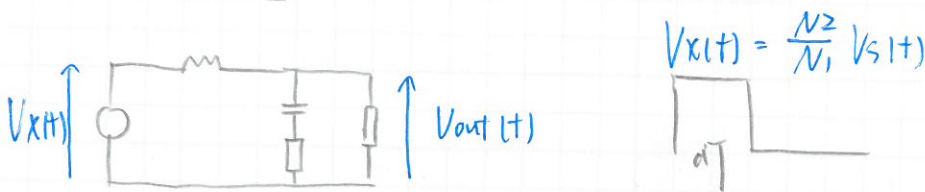
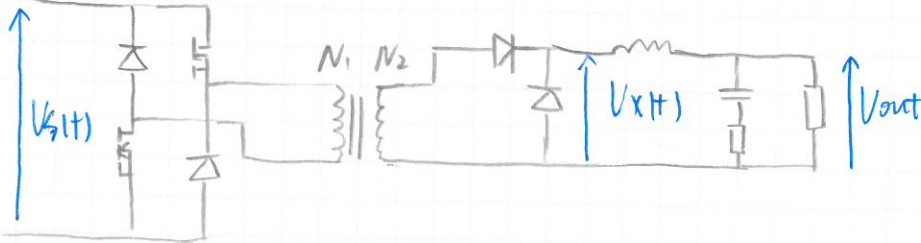
1. Power circuit modelling

ideal voltage source $V_s(t)$

$$V_s(t) = V_{s0} + V_{s1}(t)$$

$\left\{ \begin{array}{l} V_{s0} \text{ steady} \\ V_{s1}(t) \text{ ripple} \end{array} \right.$

use the forward converter circuit



In this case, the variations in $k(t)$, $d(t)$ at 100Hz . Switch frequency $\approx 100\text{Hz}$.

$$f = 100\text{Hz} \quad T = \frac{1}{f} = 0.01\text{s}.$$

$$V_x(t) = \frac{N_2}{N_1} V_s(t) d(t).$$

$$d(t) = D_0 + \Delta d(t)$$

$$= \frac{N_2}{N_1} (V_{s0} + V_{s1}(t)) (D_0 + \Delta d(t))$$

$$= \frac{N_2}{N_1} (V_{s0} (D_0 + \Delta d(t)) + V_{s1}(t) (D_0 + \Delta d(t))).$$

$$= \frac{N_2}{N_1} (V_{s0} \Delta d(t) + D_0 V_{s1}(t)).$$

output voltage $V_{out}(s)$ $V_{out}(s) = G_f(s) V_x(s)$

$$= \left(\frac{N_2}{N_1} \right) (V_{s0} G_f(s) \Delta d(s) + D_0 G_f(s) V_{s1}(s)).$$

Appendix B - transfer function.

1. calculate filter transfer function.

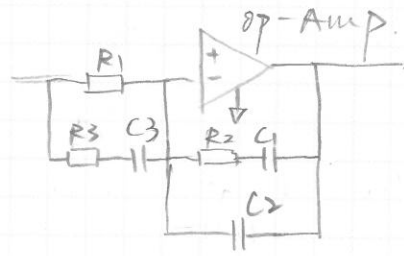
$$G_f(s) = \frac{V_{out}(s)}{V_x(s)} = \frac{1 + sR_L C}{s^2 L + s\left(-\frac{L}{R} + CR_L\right) + 1}$$

Amplifier transfer function

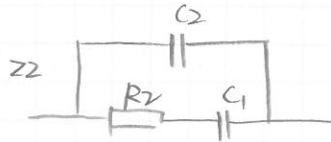
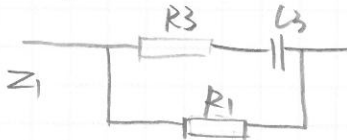
① Type 1

$$G(s) = \frac{A}{s}$$

$$A = \frac{1}{C_1 R_1}$$



② Type 3.



$$G(s) = \frac{A \left(1 + \frac{s}{\omega_{z1}}\right) \left(1 + \frac{s}{\omega_{z2}}\right)}{s \left(1 + \frac{s}{\omega_{p1}}\right) \left(1 + \frac{s}{\omega_{p2}}\right)}$$

$$A = \frac{1}{(C_1 + C_2) R_1}$$

$$\omega_{z1} = \frac{1}{C_1 R_2}$$

$$\omega_{p1} = \frac{(C_1 + C_2)}{C_2 C_1 R_2}$$

$$\omega_{z2} = \frac{1}{C_2 (R_1 + R_3)}$$

$$\omega_{p2} = \frac{1}{C_3 R_3}$$

$$R_1 = 10K \quad R_3 = 330 \quad R_2 = 20K \quad C_3 = 4.7 \cdot 10^{-9} \quad C_1 = 2.2 \cdot 10^{-9} \quad C_2 = 0.1 \cdot 10^{-9}$$

$$A = \frac{1}{(C_1 + C_2) R_1} = \frac{1}{2.3 \cdot 10^{-9} \cdot 10 \cdot 10^3} = 43478.26$$

$$\omega_{z1} = \frac{1}{C_1 R_2} = \frac{1}{2.2 \cdot 10^{-9} \cdot 20 \cdot 10^3} = 22727.27$$

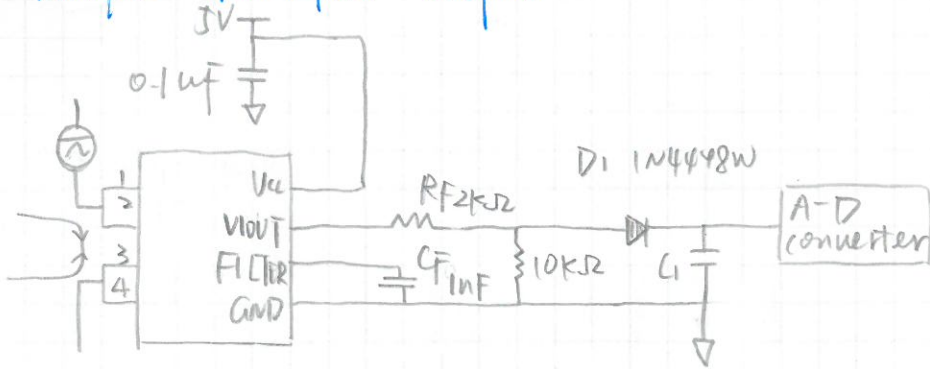
$$\omega_{p1} = \frac{C_1 + C_2}{C_1 C_2 R_2} = \frac{2.3 \cdot 10^{-9}}{2.2 \cdot 10^{-9} \cdot 0.1 \cdot 10^{-9} \cdot 20 \cdot 10^3} = 522727.27$$

$$\omega_{z2} = \frac{1}{C_2 (R_1 + R_3)} = \frac{1}{4.7 \cdot 10^{-9} (10 \cdot 10^3 + 330)} = 20590.90$$

$$\omega_{p2} = \frac{1}{C_3 R_3} = \frac{1}{330 \cdot 4.7 \cdot 10^{-9}} = 644745.33$$

$$G(s) = \frac{A}{s} \frac{\left(1 + \frac{s}{\omega_{z1}}\right) \left(1 + \frac{s}{\omega_{z2}}\right)}{\left(1 + \frac{s}{\omega_{p1}}\right) \left(1 + \frac{s}{\omega_{p2}}\right)}$$

ACS712 Rectified output



1nf 102
01uf 104

use multimeter to check "short circuit"

tips: ① turn to "Σ"

② Press yellow button at upper right corner