Audition CNRS - Concours 06/02

Complexity-Theoretic Foundations of Cryptography

Willy Quach

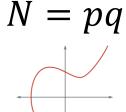
Area of research: Theory of cryptography

- > September 2023 : Postdoctoral Fellow at the Weizmann Institute of Science. Host: Zvika Brakerski
- September 2017 August 2023: PhD student at Northeastern University. Advisor: Daniel Wichs
- > September 2013 August 2017: École Normale Supérieure de Lyon

What makes modern cryptography reliable?



VS



"Ancient" cryptography

Modern cryptography

What makes modern cryptography reliable?



VS

$$N = pq$$

"Ancient" cryptography

Modern cryptography

We have abstractions to reason about security and paradigms to achieve them.

Formalize and quantify security (!)

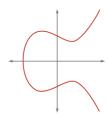
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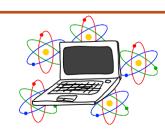
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What is there left to do?



Address new threats

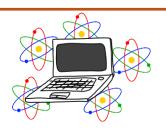
Devastating effects of **quantum attacks**, **side-channel attacks**





Address new threats

Devastating effects of quantum attacks, side-channel attacks



Security against quantum computers

How to argue security? [TCC '22, Invited to the Journal of Cryptology]
Alternate "quantum-secure" constructions [PKC '18, CRYPTO '19, TCC '21]



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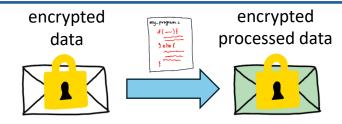
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Provide stronger functionalities

Private data used in **computation**, not just transit





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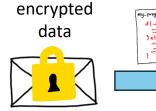
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encrypted processed data



Tools to compute blindly over encrypted data

Introducing new cryptographic tools [FOCS '18]
Advanced encryption [CRYPTO '19], program obfuscation [TCC '21]

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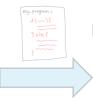
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Firmer foundations of cryptography

Foundations are still poorly understood



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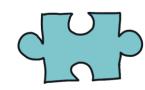
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Refine ties with complexity theory

Cryptographic proof systems [EUROCRYPT '19, CRYPTO '19, '21, '23] Alternate models of security [EUROCRYPT '22, '23, TCC '23]

Cryptographic security is proven under computational assumptions

Most cryptography can be broken in $NP \Longrightarrow$ need to assume algorithmic hardness / that $P \ne NP$

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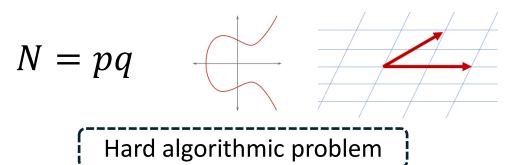
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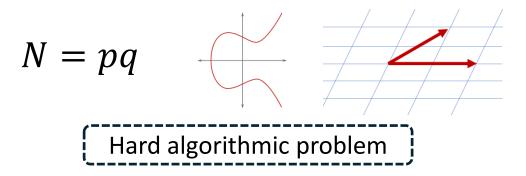
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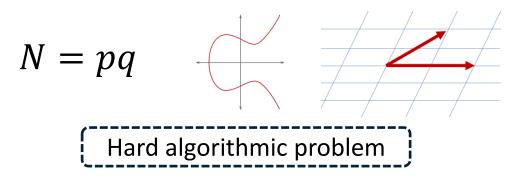
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2 Strong functionalities

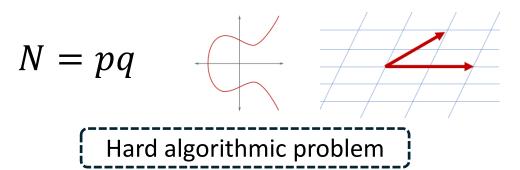




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Exploitable algebraic structure

(3) Foundations of cryptography



Strength of assumption

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Focus for today:

How (not) to argue security against quantum attacks [LMQW, TCC '22, Invited to the Journal of Cryptology]

lot!

Lara algorithmic propiciti

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Strength of assumption

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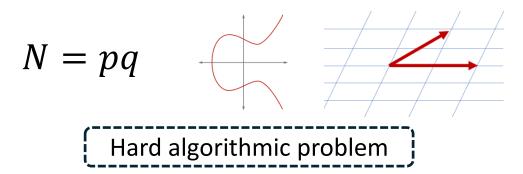
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How do we ensure security against quantum attacks?

Surprisingly little attention given to this general question

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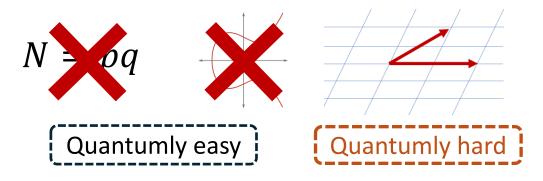
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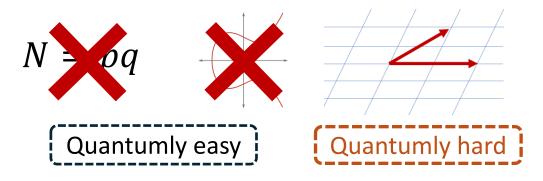
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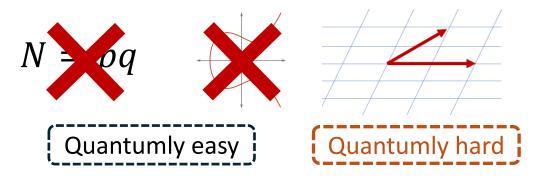
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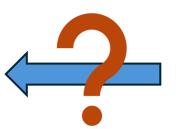
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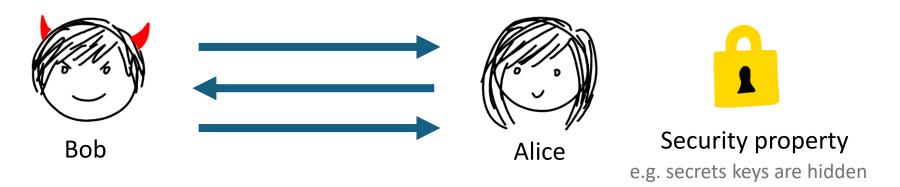
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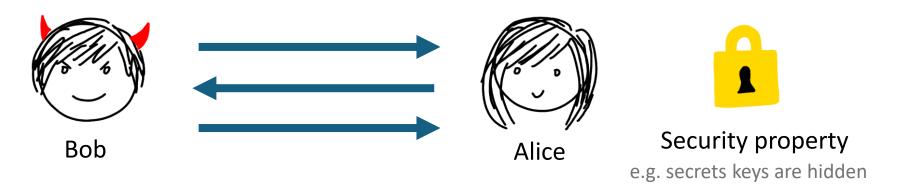
Post-quantum assumptions **are not** sufficient for post-quantum security

The folklore understanding is wrong!

What Goes Wrong?

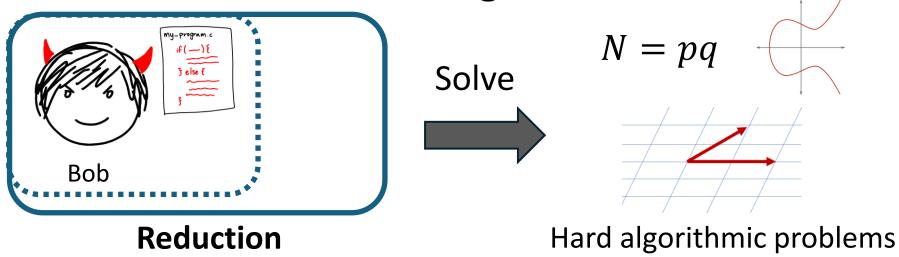


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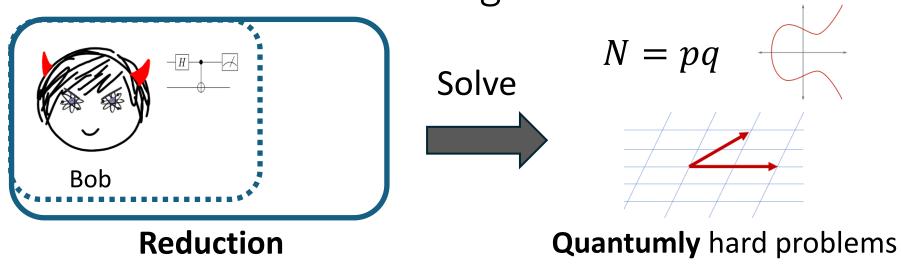
Successful attacks against implicitly solve a hard problem

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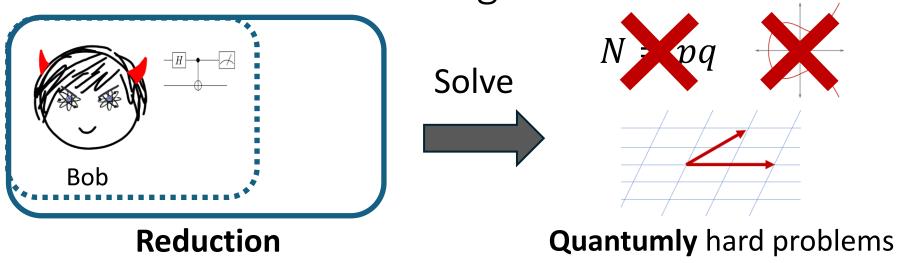
Reduction turns successful attacks into efficient algorithms

a.k.a proof of security



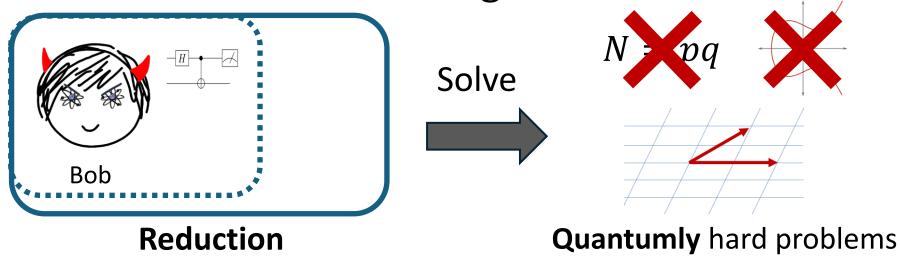
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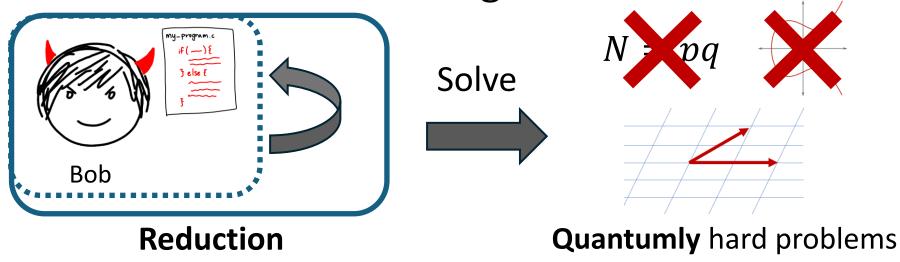
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Main issue: proofs of security are not proofs of post-quantum security Quantum attacks behave very differently from classical attacks

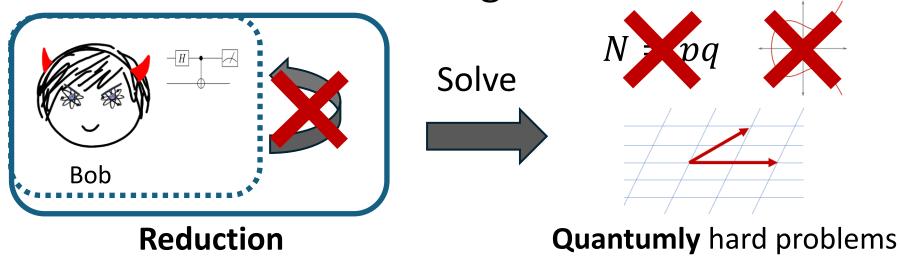


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Reduction turns successful quantum attacks into efficient quantum algorithms

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Main issue: proofs of security are not proofs of post-quantum security Quantum attacks behave very differently from classical attacks

- > Stateful classical algorithms can be run several times (rewinding)
- > Stateful quantum algorithms *cannot* be run several times (measurements are destructive)

Main Theorem [LMQW TCC'22]: Explicit counter-examples:

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- Quantumly broken

Includes symmetric-key encryption, digital signatures...

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Technique: constructions of "cryptographic proofs of quantumness" with stateless verifiers

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Conceptually: Proofs of quantumness \equiv Counter-examples

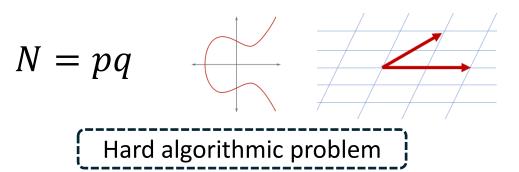
← breaking security "proves quantumness"

Takeaway: cannot simply plug-in post-quantum assumptions, need special-purpose proofs of post-quantum security

Research Project

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Property about the assumption:

(1) | Security against quantum attacks



Hardness against quantum computers

(2) | Strong functionalities



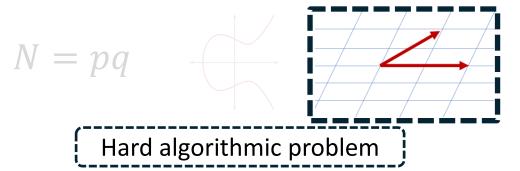


Exploitable algebraic structure

(3) Foundations of cryptography



Cryptographic security is proven under computational assumptions



Lattices are extremely convenient!

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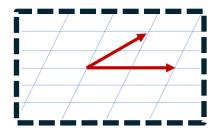
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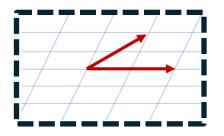
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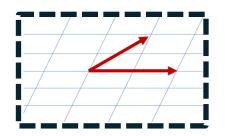
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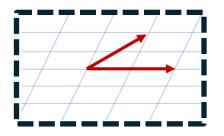


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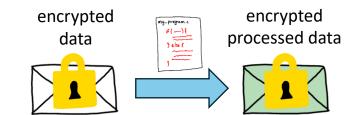
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My goal: Decouple cryptography from specific hardness assumptions

1

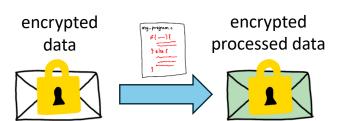
Strong functionalities from a wide range of assumptions



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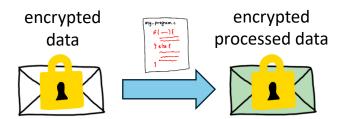
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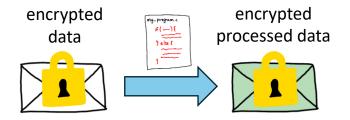


Long-term goal: develop new generic paradigms for cryptography

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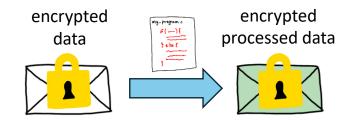
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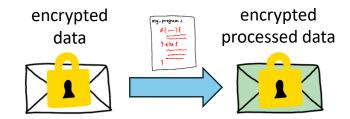
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Example: allowing a **single** computation, fixed in advance, on encrypted data suffices in applications, avoids complexity-theoretic barriers!



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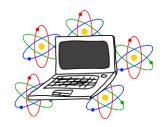
Develop techniques suited to other assumptions

New assumptions ignored by theory: lattice isomorphisms, isogenies, multivariate systems... But also old assumptions! (elliptic curves, coding theory...)

... or explain the absence of such techniques

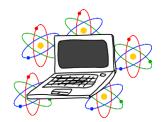


Quantum computation and cryptography





Quantum computation and cryptography



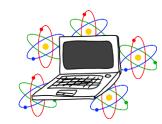
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Can we use quantum computing for **stronger cryptography**?

a.k.a *quantum cryptography*, where honest users use quantum computers



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Can we devise entirely new applications?



Quantum computation and cryptography



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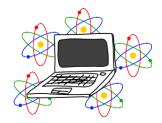
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Standard complexity theory studies problems with classical descriptions

e.g. find a Hamiltonian cycle in a graph, break a classical ciphertext...



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Need a new theory to reason about **inherently quantum problems** e.g. breaking security of a *quantum* ciphertext

Integration in Teams

DI-ENS, Paris, équipe CASCADE David Pointcheval (elliptic curves, functional encryption...) Phong Nguyen (lattices, quadratic forms...) Brice Minaud (searchable encryption...) Céline Chevalier (quantum uncloneable cryptography...)

LIP6, Paris, équipe ALMASTY
Damien Vergnaud (randomness in cryptography, leakage-resilience...)
Charles Bouillaguet (alternate assumptions...)
QI team (Alex B. Grilo...) (foundations of quantum cryptography...)

Highlights

- > Research area: theory of cryptography
 - Keywords: advanced forms of security and functionality, foundations
 - Research project: Diversifying sources of hardness in cryptography
- 17 publications ("A* conferences": CRYPTO x6, EUROCRYPT x3, FOCS)
- > 25 co-authors
- Program committees (PKC '23, CRYPTO '24, TCC'24)