

Parallel Self-Assembly under Uniform Control Inputs

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Abstract—We present fundamental progress on parallel self-assembly using large swarms of micro-scale particles in complex environments, controlled not by individual navigation, but by a uniform global, external force with the same effect on each particle. Consider a 2D grid world, in which all obstacles and particles are unit squares, and for each actuation, robots move maximally until they collide with an obstacle or another robot. We present algorithms that, given an arbitrary 2D structure, designs an obstacle layout. When actuated, this layout generates copies of the input 2D structure. We analyze the spatial and time complexity of the factory layouts. We present hardware results on a micro-scale, magnetically-actuated system.

I. INTRODUCTION

One of the exciting new directions of robotics is the design and development of micro- and nanorobot systems, with the goal of letting a massive swarm of robots perform complex operations in a complicated environment. Due to scaling issues, individual control of the involved robots becomes physically impossible: while energy storage capacity drops with the third power of robot length, medium resistance decreases much slower. As a consequence, current micro- and nanorobot systems with many robots are steered and directed by an external force that acts as a common control signal [1]–[7]. These common control signals include global magnetic or electric fields, chemical gradients, and turning a light source on and off.

A. Selective Control with Global Inputs

Having only one global signal that uniformly affects all robots at once limits the swarm’s ability to perform complex operations. This control symmetry can be broken using interactions between the robot swarm and obstacles in the environment. This paper builds on the techniques for controlling many simple particles with uniform control inputs presented in [8]–[10], where we demonstrated how such a system could implement digital computation.

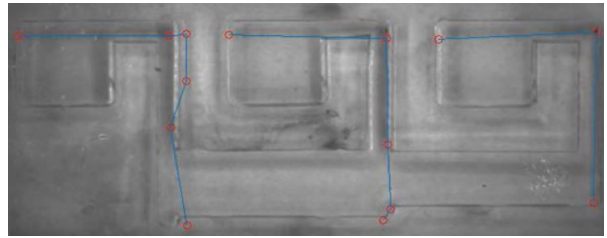
B. Model

Assume the following rules:

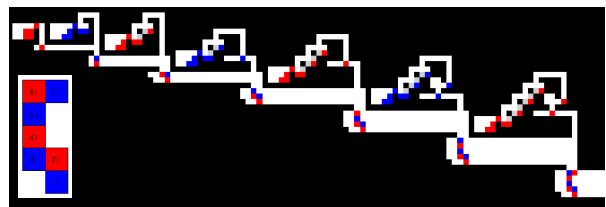
- 1) A planar grid *workspace* W is filled with a number of unit-square robots (each occupying one cell of the grid) and some fixed unit-square blocks. Each unit square in the workspace is either *free*, which a particle may

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(a)



(b)

Fig. 1. (a) A micro-scale magnetic based prototype. (b) A seven tile factory. Each particle is actuated simultaneously by the same global field. The factory is designed so each clockwise control input assembles another component.

occupy or *obstacle* which a robot may not occupy. Each square in the grid can be referenced by its Cartesian coordinates $\mathbf{x} = (x, y)$.

- 2) All particles are commanded in unison: the valid commands are “Go Up” (u), “Go Right” (r), “Go Down” (d), or “Go Left” (l).
- 3) Particles all move until they
 - a) hit an obstacle
 - b) hit a stationary particle.
 - c) share an edge with a compatible particle

If a particle shares an edge with a compatible robot the two robots bond and from then on move as a unit. A *move sequence* \mathbf{m} consists of an ordered sequence of moves m_k , where each $m_k \in \{u, d, r, l\}$. A representative move sequence is $\langle u, r, d, l, d, r, u, \dots \rangle$. We assume the area of W is finite and issue each command long enough for the robots to reach their maximum extent.

II. RELATED WORK

A. Microscale Biomanufacturing

Naturally derived biomaterials as building blocks for functional materials and devices are increasingly desired because they are environmentally and biologically safer than purely synthetic materials. One such class of materials, polysaccharide based hydrogels, are intriguing because they can reversibly encapsulate a variety of smaller components.

Many groups have termed these loaded-alginate particles *artificial cells*, because they mimic the basic structure of living cells (membrane, cytoplasm, organelles, etc.) [11]–[13]. Construction with these micron-sized gels has numerous applications in industry, including cell manipulation, tissue engineering, and micro-particle assembly [14]–[18], but requires fundamental research in biology, medicine, and colloidal science. While there are several methods to efficiently fabricate these particulate systems, it is still challenging to construct larger composite materials out of these units [19]. Traditional methods of assembling larger macroscale systems are unemployable due to the change of dominant forces at small length scales. In particular, forces due to electromagnetic interactions dominate gravitational forces at the microscale resulting in strong adhesion and sudden shifts in the position of microparts under atmospheric conditions. To form constructs out of microgels, groups have traditionally turned to non-robotic microfluidic systems that utilize a variety of actuation methods, including mechanical, optical, dielectrophoretic, acoustophoretic, and thermophoretic [20]–[24]. While each of these methods has proven to be capable of manipulating biological cells, each method has significant drawbacks that limit their widespread application. For example, microscale mechanical, acoustophoretic, and thermophoretic manipulation methods use stimuli that can be potentially lethal to live cells [25]. Furthermore, most, if not all, of these techniques require expensive equipment and lack control schemes necessary to precisely manipulate large numbers of cells autonomously.

B. Control Microrobotic Swarms Using Only Global Signals

Today an exciting frontier in robotics is the development of micro- and nanorobotic systems, with potential impacts in the fields of manufacturing and medicine. Chemists, biologists, and roboticists have shown the ability to produce very large populations (10^3 – 10^{14}) of small scale (10^{-9} – 10^{-6} m) robots using a diverse array of materials and techniques [26]–[28]. Untethered swarms of these tiny robots may be ideal for on-site construction of high-resolution macroscale materials and devices. While these new types of large-population, small-sized, robotic systems have many advantages over their larger-scale counterparts, they also present a set of unique challenges in terms of their control. Due to current limitations in fabrication, micro- and nanorobots have little-to-no onboard computation, along with limited computation and communication ability [28]–[30]. These limitations make controlling swarms of these robots individually impractical. Thus, these robotic systems are often controlled by a uniform global external signal (e.g. chemical gradients, electric and magnetic fields), which makes motion planning for large robotic populations in tortuous environments difficult. We recently demonstrated that obstacles present in the workspace can break the symmetry of approximately identical robotic swarms, enabling positional configuration of robots [31]. Given a large-enough free space, a single obstacle is sufficient for positional control over N particles. This method can be used to form complex assemblies out of large swarms



Fig. 2. Any polyomino can be constructed with two compatible robot species.

of mobile microrobotic building blocks, using only a single global input signal.

C. Microrobot Based Microassembly

The ability to create microrobots, and control algorithms capable of autonomous manipulation and assembly of small scale components into functional materials is currently a major manufacturing challenge [11]. To address this challenge, teams of microrobotic systems must work together intelligently to coordinate manipulation tasks in novel environments. While several microrobots capable of performing simple manipulation and assembly tasks have been reported [12]–[17], few have shown the ability to pattern intricate designs or assemble complex multi-component parts. Recently, some groups have begun to develop cell-safe magnetically actuated microrobotic systems for cell patterning, yet their method is limited in that these systems are manually controlled, not automated, and suffer from low spatial resolution [32], [33]. In this paper, we seek to combine the use of microscale hybrid organic/inorganic actuators along with novel swarm control algorithms for mask free programmable patterning and micro-assembly. Specifically, this paper applies swarm control and particle logic computations to magnetically actuate artificial cells, to use them as micro-scale robotic swarms that create complex, high resolution, 2D patterns and assemblies.

III. THEORY

This section explains how to design factories that build arbitrary-shaped 2D polyominoes. We first assign species to individual tiles of the polyomino, second discover a build path, and finally build an assembly line of factory components that each add one tile to partially assembled polyomino and pass the polyomino to the next component.

A. Arbitrary 2D shapes require two particle species

A *polyomino* is a 2D geometric figure formed by joining one or more equal squares edge to edge. Polyominoes have four-point connectivity.

Lemma 1: Any polyomino can be constructed using just two species

Proof: Label a grid with an alternating pattern like a checkerboard. Any desired polyomino can be constructed on this checkerboard, and all joints are between dissimilar species. An example shape is shown in Fig. 2. ■

The sufficiency of two species to construct any shape gives many options for implementation. The two species could correspond to any gendered connection, including electric charge, ionic charge, magnetic polarity, or hook-and-loop type fasteners.



Fig. 3. Polyomino parts. Difficulty increases from left to right. Parts 4 and 5 cannot be built by additive construction.

B. Complexity Handled in This Paper

Different 2D part geometries are more difficult to construct than others. Fig. 3 shows parts with increasing complexity.

Label the first particle in the assembly process the *seed particle*. Part 1 is shaped as a '#' symbol. Though it has an interior hole, any of the 16 particles could serve as the seed particle, and the shape could be constructed around it. The second shape is a spiral, and must be constructed from the inside-out. If the outer spiral was completed first, there would be no path to add particles to finish the interior because added particles would have to slide past compatible particles. Increasing the number of species would not solve this problem, because there is a narrow passage through the spiral that forces incoming parts to slide past the edges of all the bonded particles. The third shape is contains a loop, and the interior must be finished before the loop is closed. Shape 4 is the combination of a left-handed and a right-handed spiral. This part cannot be assembled by adding one particle at a time, because each spiral must be constructed from the inside-out. Instead, this part must be divided into sub-assemblies that are each constructed, and then combined. Shape 5 contains compound overhangs, and may be impossible to construct with additive manufacturing. The algorithms in this paper detect if the desired shape can be constructed one particle at a time. If so, a build order is provided, and a factory layout is designed.

C. Discovering a Build Path

Given a polyomino, Alg. 1 determines if the polyomino can be built by adding one component at a time. The problem of determining a build order is difficult because there are $O(n!)$ possible build orders, and many of them may violate the constraints given in Section I-B. Each new tile must have a straight-line path to its goal position in the polyomino that does not collide with any other particle, does not slide past an opposite species of tile, and terminates in a mating configuration with an opposite species tile. However, as in many robotics problem, the inverse problem of deconstruction is easier than the forward problem of construction.

Alg. 1 first assigns each tile in the polynomial a color, then calls the recursive function DECOMPOSE, which returns either a build order of polyomino coordinates and the directions to build, or an empty list if the part cannot be constructed. DECOMPOSE starts by calls the function ERODE. ERODE first counts the number of components in the 8-connected freespace. If there is more than one connected component, the polynomial contains loops. ERODE maintains

Algorithm 1 FINDBUILDPATH(\mathbf{P})

\mathbf{P} is the x, y coordinates of a 4-connected polyomino. Returns \mathbf{C} , \mathbf{c} and \mathbf{m} where \mathbf{C} contains sequence of polyomino coordinates, \mathbf{c} is a vector of color labels, and \mathbf{m} is a vector of directions for assembly.

- 1: $\mathbf{c} \leftarrow \text{LABELCOLOR}(\mathbf{P})$
 - 2: $\{\mathbf{C}, \mathbf{m}\} = \text{DECOMPOSE}(\mathbf{P}, \mathbf{c})$
 - 3: **return** $\{\mathbf{C}, \mathbf{c}, \mathbf{m}\}$
-



Fig. 4. Deconstruction order matters if loops are present. Loops occur when the 8-connected freespace has more than one connected component. In the top row, the green tile is removed first, resulting in a polyomino that cannot be decomposed. However, if the bottom right tile is removed first, deconstruction is possible.

an array of the remaining tiles in the polyomino \mathbf{R} . In the inner for loop at line 8, a temporary array \mathbf{T} is generated that contains all but the j th tile in \mathbf{R} . This for loop simply checks (1) if the j th tile can be removed along a straight-line path without colliding with any other particle or sliding past an opposite species of tile in line 9, (2) that its removal does not fragment the remaining polyomino into more than one piece in line 10, and (3) that its removal does not break a loop in line 11. If no loops are present, this algorithm requires at most $1/2n(1+n)$ iterations, because there are n particles to remove, and each iteration considers one less particle than the previous iteration.

Polynomials with loops require care, because decomposing them in the wrong order can make disassembly impossible, as shown in Fig. 4. If loops exist then ERODE may return only a partial decomposition, so DECOMPOSE must then try every possible break point and recursively call DECOMPOSE until either a solution is found, or all possible decomposition orders have been tested. The worst-case number of function calls of DECOMPOSE are proportional to the factorial of the number of loops, $O(|8\text{-CONNCOMP}(\neg\mathbf{P})|!)$. Though large, this is much less than $O(n!)$.

D. Assembling Tiles

1) *Hopper Construction*: Two-part adhesives react when the components mix. Placing the components in separate containers prevents mixing. Similarly, storing many particles of a single species in separate containers allows controlled mixing.

We can design *part hoppers*, containers that store similarly labelled particles. These particles will not bond with each

Algorithm 2 ERODE(\mathbf{P}, \mathbf{c})

\mathbf{P} is the x, y coordinates of a 4-connected polyomino and \mathbf{c} is a vector of color labels. Returns \mathbf{R} , \mathbf{C} , \mathbf{m} , and ℓ where \mathbf{R} is a list of coordinates of the remaining polyomino, \mathbf{C} contains sequence of tile coordinates that were removed, \mathbf{m} is a vector of directions for assembly, and ℓ if loops were encountered.

```
1:  $\mathbf{C} \leftarrow \{\}, \mathbf{m} \leftarrow \{\}, \ell \leftarrow \text{FALSE}$ 
2:  $\mathbf{d} \leftarrow \{u, d, l, r\}, \mathbf{R} \leftarrow \mathbf{P}$ 
3:  $w \leftarrow |\text{8-CONNCOMP}(\neg \mathbf{R})|$ 
4: for  $i \leftarrow 1, i < |\mathbf{P}|$  do
5:    $\text{successRemove} \leftarrow \text{FALSE}$ 
6:   for  $j \leftarrow 1, j \leq |\mathbf{R}|$  do
7:      $\mathbf{p} \leftarrow \mathbf{R}_j, \mathbf{T} \leftarrow \mathbf{R} \setminus \mathbf{R}_j$ 
8:     for  $k \leftarrow 1, k \leq 4$  do
9:       if  $\text{CHECKPATHTILE}(\mathbf{T}, \mathbf{p}, \mathbf{d}_k, \mathbf{c})$  and
10:         $1 = |\text{4-CONNCOMP}(\mathbf{T})|$  then
11:        if  $w = |\text{8-CONNCOMP}(\neg \mathbf{T})|$  then
12:           $\mathbf{R} \leftarrow \mathbf{T}, \text{successRemove} \leftarrow \text{TRUE}$ 
13:           $\mathbf{C}_{1+|\mathbf{R}|} \leftarrow \mathbf{p}, \mathbf{m}_{|\mathbf{R}|} \leftarrow \mathbf{d}_k$ 
14:        else  $\ell \leftarrow \text{TRUE}$ 
15:        break
16:   if  $\text{successRemove} = \text{FALSE}$  then
17:      $\mathbf{C} \leftarrow \{\}, \mathbf{m} \leftarrow \{\}$ 
18:     break
19: if  $|\mathbf{R}| = 1$  then
20:    $\mathbf{C}_1 \leftarrow \mathbf{R}_1$ 
21: return  $\{\mathbf{R}, \mathbf{C}, \mathbf{m}, \ell\}$ 
```

Algorithm 3 DECOMPOSE(\mathbf{P}, \mathbf{c})

\mathbf{P} is the x, y coordinates of a 4-connected polyomino and \mathbf{c} is a vector of color labels. Returns \mathbf{C} and \mathbf{m} where \mathbf{C} contains sequence of polyomino coordinates and \mathbf{m} is a vector of directions for assembly.

```
1:  $\{\mathbf{R}, \mathbf{C}, \mathbf{m}, \ell\} \leftarrow \text{ERODE}(\mathbf{P}, \mathbf{c})$ 
2: if  $|\mathbf{R}| = 0$  or  $\neg \ell$  then
3:   return  $\{\mathbf{C}, \mathbf{m}\}$ 
4:  $\mathbf{d} \leftarrow \{u, d, l, r\}, \mathbf{R} \leftarrow \mathbf{P}$ 
5: for  $j \leftarrow 1, j \leq |\mathbf{R}|$  do
6:    $\mathbf{p} \leftarrow \mathbf{R}_j, \mathbf{T} \leftarrow \mathbf{R} \setminus \mathbf{R}_j$ 
7:   for  $k \leftarrow 1, k \leq 4$  do
8:     if  $(\text{CHECKPATHTILE}(\mathbf{T}, \mathbf{p}, \mathbf{d}_k, \mathbf{c}) \text{ and}$ 
9:        $1 = |\text{4-CONNCOMP}(\mathbf{T})|)$  then
10:       $\{\mathbf{C}_2, \mathbf{m}_2\} \leftarrow \text{DECOMPOSE}(\mathbf{T}, \mathbf{c})$ 
11:      if  $\mathbf{C}_2 \neq \{\}$  then
12:         $\mathbf{C}_{1:|\mathbf{C}_2|+1} \leftarrow \{\mathbf{C}_2, \mathbf{p}\}$ 
13:         $\mathbf{m}_{1:|\mathbf{m}_2|+1} \leftarrow \{\mathbf{m}_2, \mathbf{d}_k\}$ 
14:        return  $\{\mathbf{C}, \mathbf{m}\}$ 
15:     break
16:  $\mathbf{C} \leftarrow \{\}, \mathbf{m} \leftarrow \{\}$ 
17: return  $\{\mathbf{C}, \mathbf{m}\}$ 
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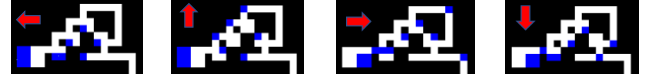


Fig. 5. Hopper with delays. The hopper is filled with similarly-labelled robots that will not combine. Every clockwise command sequence $\langle u, r, d, l \rangle$ releases one robot from the hopper.



Fig. 6. A twenty-four tile factory (full resolution – zoom in for details).

other. The hopper shown in Fig. 5 releases one particle every cycle. Delay blocks are used to ensure the n th part hopper does not start releasing particles until cycle n .

E. Part Assembly Jigs

Assembly is an iterative procedure. A factory layout is generated by $\text{BUILDFACTORY}(\mathbf{P}, n_c)$, described in Alg. 4. This function takes a 2D polyomino \mathbf{P} and, if \mathbf{P} has a valid build path, designs an obstacle layout to generate n_c copies of the polyomino. A polyomino is composed of $|\mathbf{P}| = n$ tiles.

For each tile, the function $\text{FACTORYADDTILE}(n_c, \mathbf{b}, \mathbf{m}, \mathbf{C}, \mathbf{c}, w)$ described in Alg. 5 is called to generate an obstacle configuration \mathbf{A} . \mathbf{A} forms a hopper that releases a particle each iteration and a chamber that temporarily holds the partially-assembled polyomino \mathbf{b} and guides the new particle \mathbf{C} to the correct mating position. A 24-tile factory is shown in Fig. 6.

Algorithm 4 BUILDFACTORY(\mathbf{P}, n_c)

\mathbf{P} is the x, y coordinates of a 4-connected polyomino. n_c is the number of parts desired. Returns a two dimensional array \mathbf{F} containing the factory obstacles and filled hoppers.

```
1:  $\mathbf{F} \leftarrow \{\}$  ▷ the factory obstacle array
2:  $\mathbf{b} \leftarrow \{\}$  ▷ the part being built
3:  $\{\mathbf{C}, \mathbf{c}, \mathbf{m}\} \leftarrow \text{FINDBUILDPATH}(\mathbf{P})$ 
4: if  $\{\} = \mathbf{m}$  then
5:   return  $\mathbf{F}$ 
6:  $\{\mathbf{A}, \mathbf{b}\} \leftarrow \text{FACTORYFIRSTTILE}(n_c, \mathbf{c}_i, w)$ 
7: for  $i \leftarrow 2, i \leq |\mathbf{c}|$  do
8:    $\{\mathbf{A}, \mathbf{b}\} \leftarrow \text{FACTORYADDTILE}(n_c, \mathbf{b}, \mathbf{m}_{i-1}, \mathbf{C}_i, \mathbf{c}_i, w)$ 
9:    $\mathbf{F} \leftarrow \text{CONCATFACTORIES}(\mathbf{F}, \mathbf{A})$ 
10: return  $\mathbf{F}$ 
```

IV. ANALYSIS

This section analyzes the time and space required for a factory and gives simulation results.


```

1: {hopper}  $\leftarrow$  HOPPER( $c, n_c, w$ )
2: if  $m = d$  and ( $C_x \leq \max \mathbf{b}_x$  or  $C_y < \min \mathbf{b}_y$ ) then
3:   {A, b}  $\leftarrow$  DOWNDIR(hopper, b, C)
4: else if  $m = l$  and ( $C_y \leq \max \mathbf{b}_y$  or  $C_x > \max \mathbf{b}_x$ ) then
5:   {A, b}  $\leftarrow$  LEFTDIR(hopper, b, C)
6: else if  $m = l$  and ( $C_x \geq \max \mathbf{b}_x$  or  $C_y > \max \mathbf{b}_y$ ) then
7:   {A, b}  $\leftarrow$  UPDIR(hopper, b, C)
8: else if  $m = r$  and ( $C_y \geq \min \mathbf{b}_y$  or  $C_x < \min \mathbf{b}_x$ ) then
9:   {A, b}  $\leftarrow$  RIGHTDIR(hopper, b, C)
10: return {A, b}

```

Running a factory simulation has three phases, ramp up, production, and wind down. During the $n-1$ *ramp up* cycles, the first polyomino is being constructed one tile at a time and no polyominoes are produced. Clever design of delays in the part hoppers ensures no unconnected tiles are released. During *production* cycles, one polyomino is finished each cycle. Once the first part hopper empties, the $n-1$ *wind down* cycles each produce a complete polyomino as each successive hopper empties. This section analyzes running time, defined as the time required for each commanded move until all tiles are stopped. We assume all tiles move unit distance in unit time. There are two results, the *construction time*, the time required to assemble a single polyomino from scratch, and the *cycle time*, the time required during production cycles to advance all partial assemblies one cycle. Since a polyomino contains n tiles, the *construction time* during production cycles is $n \cdot \text{cycle time}$.

B. Space Required

The space required by a factory is a function of the size of individual sub-assemblies.

$$height(i) = \begin{cases} \lceil \frac{n_c}{w} \rceil + 2(\lceil \frac{i}{2} \rceil + 1) + (\mathbf{b}_y + 1)), \\ \text{for } m = l \text{ or } d, i \geq 2 \\ \lceil \frac{n_c}{w} \rceil + (2(\lceil \frac{i}{2} \rceil + 1) + \mathbf{b}_y) + 5), \\ \text{for } m = u \text{ or } r, i \geq 2 \end{cases} \quad (1)$$

$$(hopper + delays)_{width} = w + (2 \lceil i/2 \rceil + 8), i \geq 2 \quad (2)$$

$$width(i) = \begin{cases} (hopper + delays)_{width} + (\mathbf{b}_x - column_{loc}), & \text{for } m = d \\ (hopper + delays)_{width}, & \text{for } m \neq d \end{cases} \quad (3)$$

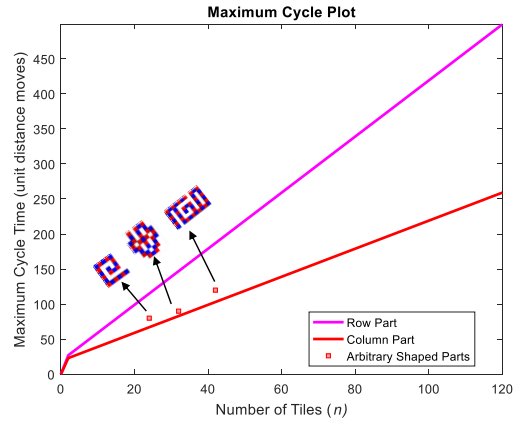


Fig. 7. Cycle time plotted against number of tiles n . The cycle time is the sum time to move during the r, d, l, u moves each cycle. Cycle time increases linearly and is upper bounded by row parts and lower bounded by column parts. Total construction time for a particle is $n \cdot$ cycle time.

The first sub-assembly is constructed separately and it does not have any delay. Beginning from the second sub-assembly, height can be computed as a function of number of copies n_c of the polyomino, width of the hopper w , position of the sub-assembly i , and the rows of the sub-assembled polyomino \mathbf{b}_y . If a tile is added before top row of \mathbf{b} , then an additional row is added to the height. The width of the sub-assembly can be calculated similarly. In a case where twice of \mathbf{b}_x is greater than $(hopper + delays)_{width}$ then additional columns are added to the left of sub-assembly. When a tile is added to \mathbf{b} using a down move, width also depends on the location of the column, $column_{loc}$ to which the tile is added.

Because a factory requires $O(n)$ rows and $O(n)$ columns, the total requires space is $O(n^2)$. As shown in Fig. 8, the required size is upper bounded by column-shaped polyominoes and lower bounded by row-shaped polyominoes, and is $O(n^2)$.

C. Simulation Results

Algorithms 1 through 5 were coded in MATLAB and are available at [34].

V. EXPERIMENT

To demonstrate the algorithm, we developed a magnetic control stage and alginate micro-particles.

a) *Experimental setup:* We designed a custom magnetic control stage to generate the global control inputs. This stage generates a magnetic drag force by moving a permanent magnet. This permanent magnet can translate in x and y -axes, actuated by stepper motors and moving on linear rails. The neodymium permanent magnet field strength is 433 mT and dimensions are 25.4×25.4 mm². The assembly workspace is laser cut into PDMS to a depth of XXXX mm and then filled with motility buffer. All microrobots used for these experiments are loaded alginate paramagnetic

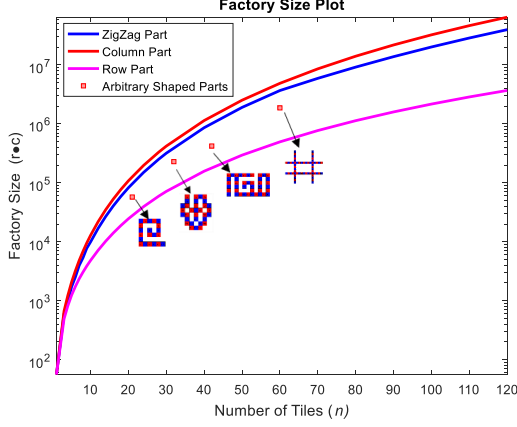


Fig. 8. Factory size grows quadratically with the number of tiles, and is upper bounded by column-shaped polyominos and lower bounded by row-shaped polyominos.

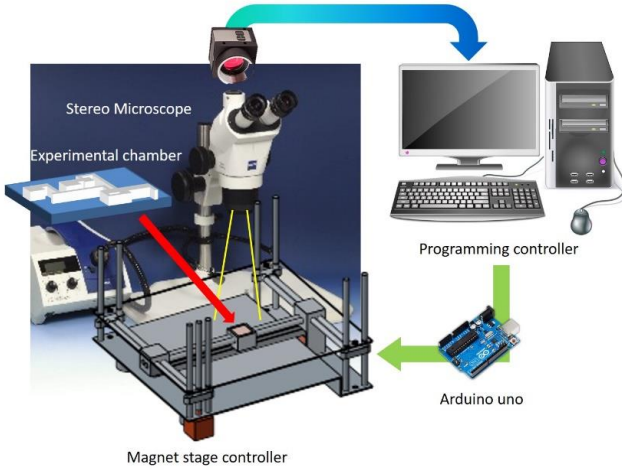


Fig. 9. Experimental platform.

hydrogels, otherwise known as artificial cells. The alginate microrobots were fabricated using a centrifugal method, as described in previous work [35]. The average microrobot size is $300 \mu\text{m}$, and were composed of a concentration of 5% (w/v) Alginate-Na and 5% (w/v) concentration of CaCl_2 , and then impregnated with nano-paramagnetic particles.

After the alginate microrobots were loaded at each hopper in the microfluidic factory layout, the experimental channel was placed at the center of the stage. Next, the magnet centered beneath the microfluidic factory layout. This position was saved as the home position for the permanent magnet. Stepper motors controlled the stage position. An Arduino UNO programmed in C++ commanded these stepper motors using a 2Hz control loop. After a command was

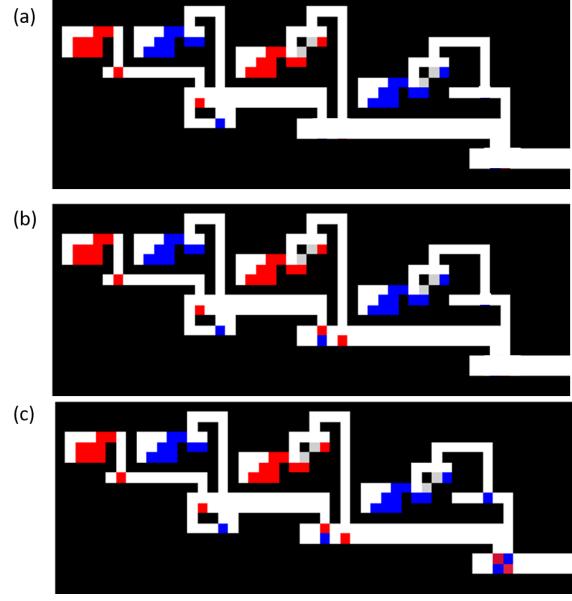


Fig. 10. Construction of a microrobotic polyomino from four alginate artificial cells. (a) Initial position of alginate microrobots in all chambers, (b) First assembly by two microrobots from two chambers, (c) Final result of construction. The scale bar represents $XXX \mu\text{m}$.

initiated, such as each direction in the $\langle u, r, d, l \rangle$ sequence, the permanent magnet was returned to the home position to better control the distribution of the magnetic gradient. The layout was observed through a stereomicroscope and the installed camera (Motion Pro X3) captured the procedure at 30 fps. Using ??? magnification in the stereomicroscope, the observed field of view is $23.6 \times 18.9 \text{ mm}^2$. A system schematic is shown in Fig. 9.

b) Experimental result: Using a factory layout generated by Alg. 4, we demonstrated micro-scale assembly using multiple alginate microrobots. The initial scene is shown in Fig. 10(a) and the first assembly operation was orchestrated by moving the magnet in a clockwise direction, following the $\langle u, r, d, l \rangle$ sequence as indicated in Fig. 10(b). Each input was applied sufficiently long to ensure all alginate microrobots moved until they touched a wall. The completed square polyomino is shown in the lower right corner in Fig. 10(c). In addition, other square polyominoes were manufactured simultaneously.

VI. CONCLUSION

This work introduces a new model for additive assembly that enables efficient parallel construction because it does not depend on individual control of each agent. Instead, the workspace is designed to direct particles. This enables a simple global control input to produce a complex output.

Interesting applications will aim at microfluidics work.

Future work could extend Algorithms 1–5 to three dimensions. Additional work could focus on reducing assembly time. To build a polyomino, our current algorithm requires

time that grows quadratically with the number of tiles in a polyomino. Parts could be decomposed into subassemblies, which would enable more complex parts to be created and enable construction in logarithmic time.

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