

# Program Structures & Algorithms

## Spring 2021 Assignment No. 2

### Task:

Determine the relationship between the number of objects( $n$ ) and the number of pairs( $m$ ) generated to accomplish this(i.e. to reduce the number of components from  $n$  to 1).

### Output:

- Data points
  - `/INF06205/Python/src/union_find/stats.csv`

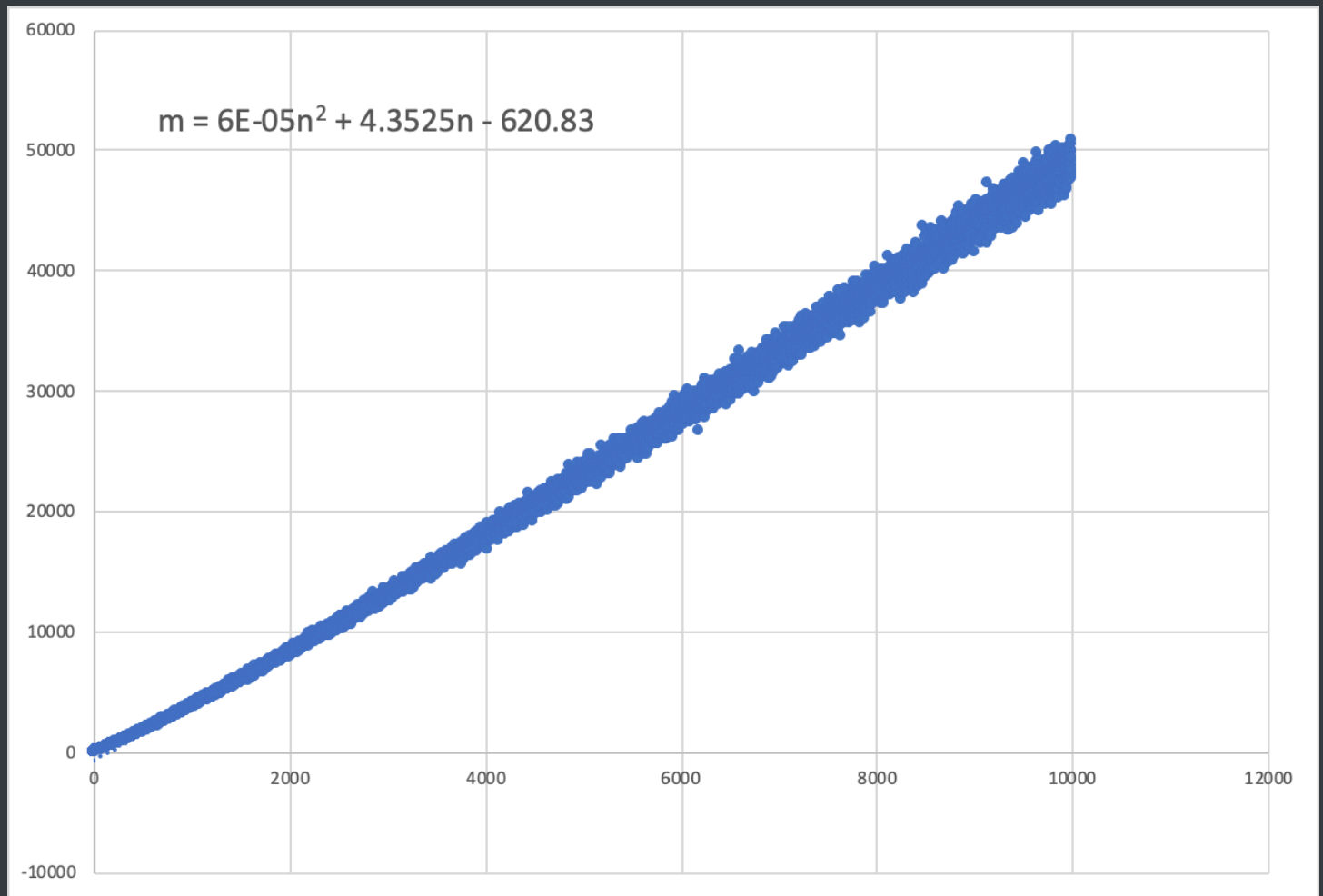
### Relationship Conclusion:

When the number of objects( $n$ ) gets larger, the number of pairs( $m$ ) gets larger. In general, the relationship between the number of objects( $n$ ) and the number of pairs( $m$ ) is roughly like  **$m = 6E-05n^2 + 4.3525n - 620.83$**

### Evidence to support the conclusion:

According to the output, if we just calculate the number of pairs which are getting connected through union,  **$m=n-1$** . If we count all the list of pairs generated, when  $n = 10000$ ,  **$m \approx 4.3525n$** . It is a linear relationship.

## Graphical representation:



## Unit tests result:

INFO6205 Python test test\_union\_find test\_uf\_hwqupc.py

Unittests for test\_uf\_hwqupc.Test\_UF\_HWQUPC

```
1 import unittest
2
3 from union_find.uf_hwqupc import UF_HWQUPC
4
5
6 class Test_UF_HWQUPC(unittest.TestCase):
7     def test_to_str(self):
8         h = UF_HWQUPC(2)
9         self.assertEqual("UF_HWQUPC:\n" +
10                          "  count: 2\n" +
11                          "  path compression? True\n" +
12                          "  parents: [0, 1]\n" +
13                          "  heights: [1, 1]", str(h))
14
15     def test_is_connected_01(self):
16         h = UF_HWQUPC(2)
17         self.assertFalse(h.is_connected(0, 1))
18
19     def test_is_connected_02(self):
20         h = UF_HWQUPC(1)
21         self.assertRaises(ValueError, h.is_connected, 0, 1)
22
23     def test_is_connected_03(self):
24         h = UF_HWQUPC(2)
25         self.assertIsNone(h.update_parent(0, 1))
26         self.assertTrue(h.is_connected(0, 1))
27
```

Run: uf\_main x Unittests for test\_uf\_hwqupc.Test\_UF\_HWQUPC x

Tests passed: 13 of 13 tests - 2 ms

Test Results 2 ms

Testing started at 10:11 上午 ...

Ran 13 tests in 0.008s

OK

Launching unittests with arguments python -m unittest test\_uf\_hwqupc.Test\_UF\_HWQUPC in /Users/mac/Documents/GitHub/INF06205/Python/1

Tests passed: 13 (moments ago)

3:22 Python 3.9 master